

# PRACTICE EXAM

**Difficulty: MEDIUM**

**Questions: 10**

# Data Structures Exam

**Instructions: Please answer all questions to the best of your ability.**

## # Multiple Choice (4 points each, 40 points total)

Instructions: Choose the best answer for each question.

**Question 1:** What is the worst-case time complexity of Heap Sort?

- A)  $O(n)$
- B)  $O(n^2)$
- C)  $O(n \lg n)$
- D)  $O(\lg n)$

**Question 2:** In a heap data structure represented as an array, what is the index of the left child of the node at index  $*i$ ?

- A)  $*i/2$
- B)  $*i - 1$
- C)  $2*i + 1$
- D)  $2*i$

**Question 3:** Which of the following describes a Stack Overflow condition?

- A) Attempting to remove an element from an empty stack.
- B) Attempting to add an element to a full stack.
- C) Successfully adding an element to a stack.
- D) Attempting to remove an element from a full stack.

**Question 4:** In the context of sets, which operation finds the element with the smallest key value?

- A) Search( $S, k$ )
- B) Maximum( $S$ )
- C) Successor( $S, x$ )
- D) Minimum( $S$ )

## # Short Answer (6 points each, 30 points total)

Instructions: Answer each question in 2-3 sentences.

**Question 5:** Briefly explain the difference between a Queue Overflow and a Queue Underflow.

**Question 6:** Describe how a linked list differs from an array in terms of how elements are ordered.

**Question 7:** Explain the purpose of the `key` variable in the provided Insertion Sort pseudocode.

## **# Problem Solving (10 points each, 30 points total)**

Instructions: Provide detailed solutions, showing all steps.

**Question 8:** Trace the execution of the `ENQUEUE` operation on a queue `Q` with length 5, head = 1, and tail = 5, when adding the element `x`. Clearly show the updated values of `Q`, `head[Q]`, and `tail[Q]` after the operation.

**Question 9:** Given the initial unsorted array [9, 8, 2, 4, 9, 3, 6], demonstrate the steps of Insertion Sort to sort this array in ascending order. Show the state of the array after each iteration of the outer loop (for  $j = 2$  to  $n$ ).

**Question 10:** Describe the steps involved in building a Heap data structure and then performing a sorting operation using Heap Sort. Briefly explain the role of the `MAX` or `MIN HEAPIFY` procedure.