

PRACTICE EXAM

Difficulty: MEDIUM

Questions: 10

Algorithms & Data Structures Exam

Instructions: Please answer all questions to the best of your ability.

Section 1: Multiple Choice Questions (4 points each, 40 points total)

Instructions: Choose the best answer for each question.

Question 1: In the provided INSERTION-SORT algorithm, what is the purpose of the 'key' variable?

- A) It stores the index of the element being compared.
- B) It stores the value of the element being inserted into the sorted portion.
- C) It represents the size of the array.
- D) It stores the value of the element being compared.

Question 2: In the INSERTION-SORT algorithm, the 'while' loop condition is ' $i > 0$ and $A[i] > \text{key}$ '. What does ' $i > 0$ ' ensure?

- A) That the loop continues until the end of the array.
- B) That the loop iterates through all possible values of j .
- C) That the algorithm doesn't access an index outside of the array bounds.
- D) That the key is correctly assigned.

Question 3: Based on the provided recurrence relation $T(n) = 2T(n/2) + \Theta(n)$, what general type of algorithm design paradigm is likely being analyzed?

- A) Greedy algorithm
- B) Dynamic programming
- C) Divide and conquer
- D) Branch and bound

Question 4: In the merging of two sorted arrays example, what determines the order in which elements are placed into the final merged array?

- A) The order they appear in the first input array.
- B) The order they appear in the second input array.
- C) Comparing the current elements of both input arrays.
- D) Random assignment.

Section 2: Short Answer Questions (6 points each, 30 points total)

Instructions: Answer each question in 2-3 sentences.

Question 5: Explain the role of the inner `while` loop in the provided INSERTION-SORT algorithm.

Question 6: What is the significance of ' $\Theta(n)$ ' in the recurrence relation $T(n) = 2T(n/2) + \blacksquare(n)$?

Question 7: Briefly explain the high-level steps involved in merging two sorted arrays into a single sorted array.

Section 3: Problem-Solving Questions (10 points each, 30 points total)

Instructions: Show your work and provide a detailed explanation for each answer.

Question 8: Using the INSERTION-SORT algorithm provided, trace the execution of the algorithm on the following array: [5, 1, 4, 2, 8]. Show the state of the array after each iteration of the outer loop (the 'j' loop).

Question 9: Given the recurrence relation $T(n) = T(n-1) + \blacksquare(n)$ and the guess $T(n) \leq cn^2$, explain the steps involved in attempting to prove this upper bound using substitution method. Point out one challenge encountered when trying to prove the upper bound.

Question 10: Consider merging two sorted arrays $A = [2, 5, 8]$ and $B = [1, 3, 9]$. Show step by step how the two arrays are merged and write the final result.