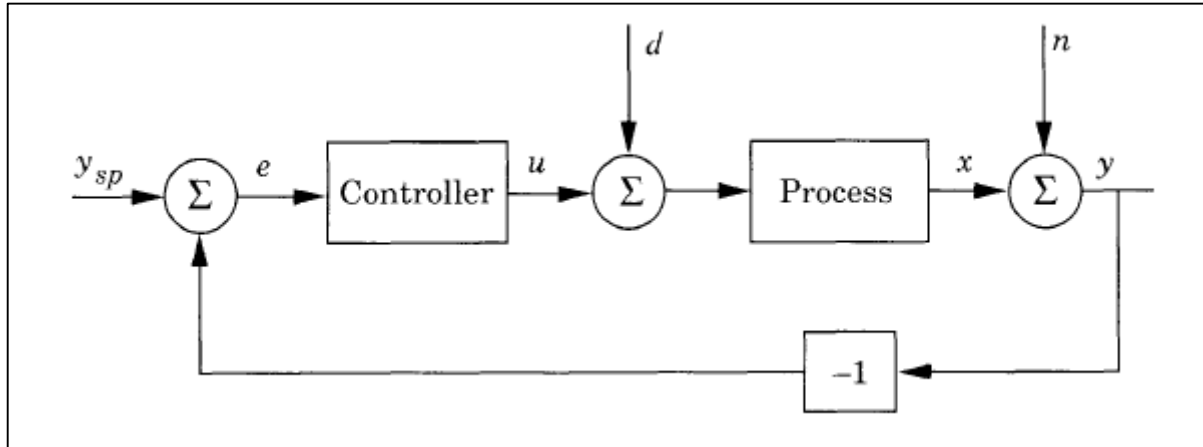


# MEE427 PID CONTROL ASSIGNMENT # 1

## 1) Time Response Simulation

Consider the simple feedback loop, as seen in Figure 1, with disturbance  $d$  and the noise  $n$  are zero.

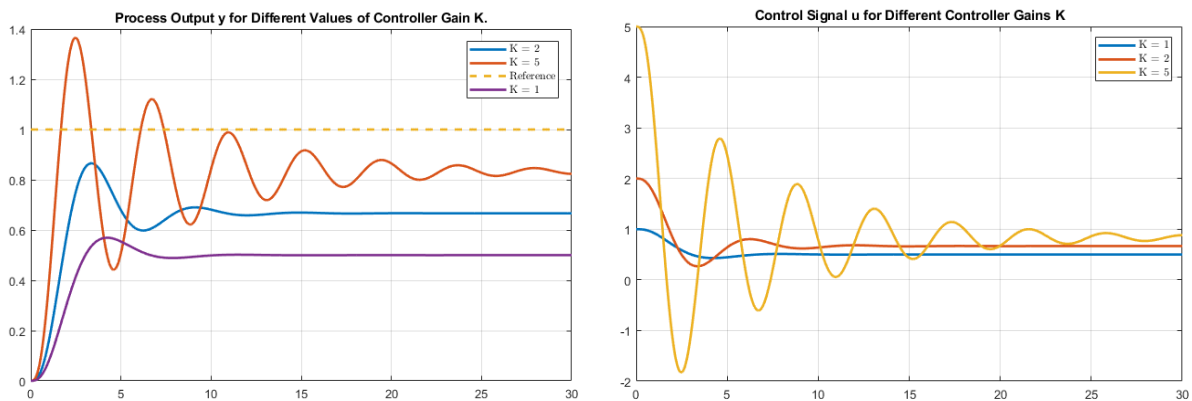


**Figure 1:** Simple feedback loop

The process block is given in Equation 1. The controller is considered as proportional action.

$$G(s) = \frac{1}{(s + 1)^3} \quad (1)$$

- Simulate the system with a unit step change in the set point ( $y_{sp}$ ) with different proportional gain  $K_p$  ( $K_p = 1$ ,  $K_p = 2$ ,  $K_p = 5$ ) by using any simulation program (Matlab/Simulink, Python etc.) and demonstrate the process output ( $y$ ) and control signal ( $u$ ) plots. Eventually, you should reach the responses in time domain as given in Figure 2a and 2b.



**Figure 2: a) Process output for different K gains b) Control signal for different K gains**

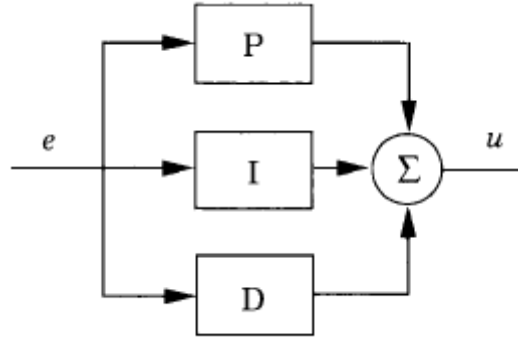
- For further works, the simulation to be compatible to PI controller implementation as well.
- Bring all the necessary codes, models and figures to laboratory course to investigate the process thoroughly.

## 2) Frequency Response Simulation

The controller transfer function can be represented as shown in Equation 2 using control parameters (proportional gain  $K_p$ , integral time  $T_i$  and derivative time  $T_d$ ).

$$C(s) = K_p \left( 1 + \frac{1}{sT_i} + sT_d \right) \quad (2)$$

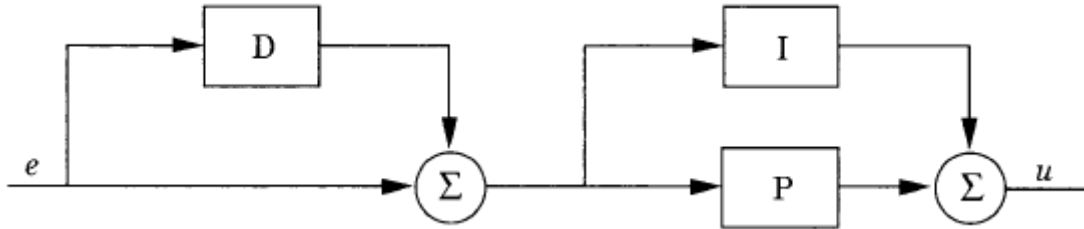
This kind of controller is called non-interacting form and its block expression is given in Figure 3.



**Figure 3:** Non-interacting form

The interacting form is represented as in Equation 3, where the derivative time  $T'_d$  influence the integral part and the block representation is given in Figure 4.

$$C'(s) = K'_p \left( 1 + \frac{1}{sT'_i} + sT'_d \right) \quad (3)$$



**Figure 4:** Interacting form

The interacting form controller ( $C'(s)$ ) can always be represented as a non-interacting form controller whose coefficients are given by

$$\begin{aligned} K_p &= K'_p \frac{T'_i + T'_d}{T'_i} \\ T_i &= T'_i + T'_d \\ T_d &= \frac{T'_i T'_d}{T'_i + T'_d} \end{aligned} \quad (4)$$

- Define a first order plant with a specific  $p$  value as in the transfer function given in Equation 5.

$$G(s) = \frac{K}{s + p} \quad (5)$$

- Draw the frequency response diagram of the specified plant by using any simulation program (Matlab/Simulink, Python etc.).
- Draw the frequency response of PID controller with the interacting by using parameters below.
- Draw the frequency response of controlled system (PID controller and given plant) so that simulation of the overall cascade system can be shown.
- Calculate the non-interacting PID controller parameters by using Equation 4, then draw the frequency response diagram by using the non-interacting form PID controller. Compare these two results.
- Bring all the necessary codes, models and figures to laboratory course to investigate the process thoroughly.

Parameters given;

$$p = 10$$

$$K = 1$$

$$K'_p = 6$$

$$T'_i = 4$$

$$T'_d = 1$$