### **MACHINE**

xOwl

### **DEFINITIONS**

 $END\_OF\_GENERATED\_DEFINITIONS\_FOR == xOwl;$ 

## **SETS**

XOWL;

AXIOM;

CLASSEXPRESSION;

ENTITY;

ANNOTATION;

OBJECTPROPERTYEXPRESSION

## ABSTRACT\_VARIABLES

XOwl,

Axiom,

ClassExpression,

Entity,

Annotation,

Object Property Expression,

Assertion,

Class,

Individual,

ClassAxiom,

Declaration,

 $Object Complement O\!f,$ 

ObjectOneOf,

 $Object Has \, Value,$ 

ObjectProperty,

ObjectSomeValuesFrom,

ObjectAllValuesFrom,

Datatype,

Class Assertion,

Equivalent Classes,

Disjoint Union,

Disjoint Classes,

SubClassOf,

axioms,

classOfClassExp,

 $A\_classExpression\_classAssertion,$ 

 $A\_individual\_classAssertion$ ,

axiomAnnotations,

 $A\_classExpressions\_equivalentClasses,$ 

 $A\_class\_disjointUnion,$ 

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A\_disjointClassExpressions\_disjointUnion,\\ disjointClassExp,
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 $sub\,ClassExp,$ 

superClassExp,

 $A\_entity\_declaration,$ 

 $A\_classExpression\_objectComplementOf,$ 

 $A\_individuals\_objectOneOf$ ,

 $A\_objectProperty\_objectPropertyExpression,$ 

 $A\_objectPropertyExpression\_objectHasValue,$ 

 $A\_individual\_objectHasValue$ ,

 $A\_objectPropertyExpression\_objectSomeValuesFrom,$ 

 $A\_classExpression\_objectSomeValuesFrom,$ 

 $A\_objectPropertyExpression\_objectAllValuesFrom,$ 

 $A\_classExpression\_objectAllValuesFrom,$ 

 $xOwl\_ontologyIRI$ ,

 $xOwl\_versionIRI$ ,

 $Entity\_name,$ 

 $Annotation\_annotation Value$ 

#### INVARIANT

```
XOwl \in \mathcal{F} (XOWL) \land
Axiom \in \mathcal{F} (AXIOM) \land
ClassExpression \in \mathcal{F} \ (CLASSEXPRESSION) \land
Entity \in \mathcal{F} (ENTITY) \land
Annotation \in \mathcal{F} (ANNOTATION) \land
ObjectPropertyExpression \in \mathcal{F} \ (OBJECTPROPERTYEXPRESSION) \land
Assertion \subseteq Axiom \land
Class \subseteq Entity \land
Individual \subseteq Entity \land
ClassAxiom \subseteq Axiom \land
Declaration \subseteq Axiom \land
ObjectComplementOf \subseteq ClassExpression \land
ObjectOneOf \subseteq ClassExpression \land
ObjectHasValue \subseteq ClassExpression \land
ObjectProperty \subseteq Entity \land
ObjectSomeValuesFrom \subseteq ClassExpression \land
ObjectAllValuesFrom \subseteq ClassExpression \land
Datatype \subseteq Entity \land
ClassAssertion \subseteq Assertion \land
EquivalentClasses \subseteq ClassAxiom \land
DisjointUnion \subseteq ClassAxiom \land
DisjointClasses \subseteq ClassAxiom \land
SubClassOf \subseteq ClassAxiom \land
axioms \in Axiom \rightarrow XOwl \land
classOfClassExp \in ClassExpression \rightarrow Class \land
A\_classExpression\_classAssertion \in ClassAssertion \mapsto ClassExpression \land
A\_individual\_classAssertion \in ClassAssertion \rightarrow Individual \land
axiomAnnotations \in Annotation \rightarrow ClassAxiom \land
```

```
A\_classExpressions\_equivalentClasses \in ClassExpression \Rightarrow EquivalentClasses \land
   A\_class\_disjointUnion \in DisjointUnion \rightarrow Class \land
   A\_disjointClassExpressions\_disjointUnion \in ClassExpression \Rightarrow DisjointUnion \land
   disjointClassExp \in ClassExpression \Rightarrow DisjointClasses \land
   subClassExp \in SubClassOf \rightarrow ClassExpression \land
   superClassExp \in SubClassOf \mapsto ClassExpression \land
   A\_entity\_declaration \in Declaration \implies Entity \land
   A\_classExpression\_objectComplementOf \in ObjectComplementOf \mapsto ClassExpression \land
   A\_individuals\_objectOneOf \in ObjectOneOf \leftrightarrow Individual \land
   A\_objectProperty\_objectPropertyExpression \in ObjectPropertyExpression \Rightarrow ObjectProperty \land
   A\_objectPropertyExpression\_objectHasValue \in ObjectHasValue \Rightarrow ObjectPropertyExpression
Λ
   A\_individual\_objectHasValue \in ObjectHasValue \Rightarrow Individual \land
   A\_objectPropertyExpression\_objectSomeValuesFrom \in ObjectSomeValuesFrom <math>\mapsto Object-
PropertyExpression \land
   A\_classExpression\_objectSomeValuesFrom \in ObjectSomeValuesFrom \mapsto ClassExpression \land
   A\_objectPropertyExpression\_objectAllValuesFrom \in ObjectAllValuesFrom \mapsto ObjectProperty-
Expression \land
   A\_classExpression\_objectAllValuesFrom \in ObjectAllValuesFrom \rightarrowtail ClassExpression \land \\
   xOwl\_ontologyIRI \in XOwl \rightarrow STRING \land
   xOwl\_versionIRI \in XOwl \rightarrow STRING \land
   Entity\_name \in Entity \rightarrow STRING \land
   Annotation\_annotationValue \in Annotation \rightarrow STRING \land
   Assertion \cap Declaration = \emptyset \land
   Assertion \cap ClassAxiom = \emptyset \land
   Declaration \cap ClassAxiom = \emptyset \land
   ObjectComplementOf \cap ObjectOneOf = \emptyset \land
   ObjectComplementOf \cap ObjectAllValuesFrom = \emptyset \land
   ObjectComplementOf \cap ObjectSomeValuesFrom = \emptyset \land
   ObjectComplementOf \cap ObjectHasValue = \emptyset \land
   ObjectOneOf \cap ObjectAllValuesFrom = \emptyset \land
   ObjectOneOf \cap ObjectSomeValuesFrom = \emptyset \land
   ObjectOneOf \cap ObjectHasValue = \emptyset \land
   ObjectAllValuesFrom \cap ObjectSomeValuesFrom = \emptyset \land
   ObjectAllValuesFrom \cap ObjectHasValue = \emptyset \land
   ObjectSomeValuesFrom \cap ObjectHasValue = \emptyset \land
   Class \cap Individual = \emptyset \land
   Class \cap ObjectProperty = \emptyset \land
   Class \cap Datatype = \emptyset \land
   Individual \cap ObjectProperty = \emptyset \land
   Individual \cap Datatype = \emptyset \land
   ObjectProperty \cap Datatype = \emptyset \land
   DisjointClasses \cap SubClassOf = \emptyset \land
   DisjointClasses \cap EquivalentClasses = \emptyset \land
   DisjointClasses \cap DisjointUnion = \emptyset \land
   SubClassOf \cap EquivalentClasses = \emptyset \land
   SubClassOf \cap DisjointUnion = \emptyset \land
   EquivalentClasses \cap DisjointUnion = \emptyset \land
    \forall \ aDisjointClasses.(\ aDisjointClasses \in \mathbf{ran}(disjointClassExp) \Rightarrow \mathbf{card}(disjointClassExp^{-1})
[\{aDisjointClasses\}] \geq 2
```

**INITIALISATION** 

 $XOwl := \emptyset \mid \mid$ 

```
Axiom := \emptyset \mid \mid
ClassExpression := \emptyset | |
Entity := \emptyset \parallel
Annotation := \emptyset \mid \mid
ObjectPropertyExpression := \emptyset | |
Assertion := \emptyset \mid \mid
Class := \emptyset \mid \mid
Individual := \emptyset | |
ClassAxiom := \emptyset | |
Declaration := \emptyset \mid \mid
ObjectComplementOf := \emptyset \mid \mid
ObjectOneOf := \emptyset \mid \mid
ObjectHasValue := \emptyset | |
ObjectProperty := \emptyset \parallel
ObjectSomeValuesFrom := \emptyset \parallel
ObjectAllValuesFrom := \emptyset \parallel
Datatype := \emptyset \mid \mid
ClassAssertion := \emptyset \mid \mid
EquivalentClasses := \emptyset \parallel
Disjoint Union := \emptyset \mid \mid
DisjointClasses := \emptyset \mid \mid
SubClassOf := \emptyset | |
axioms := \emptyset \mid \mid
classOfClassExp := \emptyset | |
A\_classExpression\_classAssertion := \emptyset | |
A\_individual\_classAssertion := \emptyset | |
axiomAnnotations := \emptyset | |
A\_classExpressions\_equivalentClasses := \emptyset | |
A\_class\_disjointUnion := \emptyset \parallel
A\_disjointClassExpressions\_disjointUnion := \emptyset | |
disjointClassExp := \emptyset \mid \mid
subClassExp := \emptyset \mid \mid
superClassExp := \emptyset \parallel
A\_entity\_declaration := \emptyset \parallel
A\_classExpression\_objectComplementOf := \emptyset | |
A\_individuals\_objectOneOf := \emptyset | |
A\_objectProperty\_objectPropertyExpression := \emptyset | |
A\_objectPropertyExpression\_objectHasValue := \emptyset \parallel
A\_individual\_objectHasValue := \emptyset \parallel
A\_objectPropertyExpression\_objectSomeValuesFrom := \emptyset | |
A\_classExpression\_objectSomeValuesFrom := \emptyset | |
A\_objectPropertyExpression\_objectAllValuesFrom := \emptyset | |
A\_classExpression\_objectAllValuesFrom := \emptyset | |
xOwl\_ontologyIRI := \emptyset \mid \mid
xOwl\_versionIRI := \emptyset \mid \mid
Entity\_name := \emptyset \mid \mid
Annotation\_annotationValue := \emptyset
```

# **OPERATIONS**

```
xOwl_NEW(aXOwl) =
\mathbf{PRE}
        aXOwl \in XOWL \land
   aXOwl \not\in XOwl
THEN
   XOwl := XOwl \cup \{aXOwl\}
END;
Axiom_NEW(aAxiom) =
PRE aAxiom \in AXIOM \land
   aAxiom \not\in Axiom
THEN
   Axiom := Axiom \cup \{aAxiom\}
END;
ClassExpression\_NEW(aClassExpression) =
        aClassExpression \in CLASSEXPRESSION \land
   aClassExpression \not\in ClassExpression
THEN
   ClassExpression := ClassExpression \cup \{aClassExpression\}
END;
Entity_NEW(aEntity) =
PRE aEntity \in ENTITY \land
   aEntity \not\in Entity
THEN
   Entity := Entity \cup \{aEntity\}
END;
Annotation\_NEW(\mathit{aAnnotation}) =
        aAnnotation \in ANNOTATION \land
   aAnnotation \not\in Annotation
THEN
   Annotation := Annotation \cup \{aAnnotation\}
END;
\mathbf{ObjectPropertyExpression\_NEW}(aObjectPropertyExpression) =
        aObjectPropertyExpression \in OBJECTPROPERTYEXPRESSION \land
   aObjectPropertyExpression \not\in ObjectPropertyExpression
THEN
   ObjectPropertyExpression := ObjectPropertyExpression \cup \{aObjectPropertyExpression\}
END;
Assertion_NEW(aAssertion) =
       aAssertion \in AXIOM \land
```

5

 $aAssertion \not\in Axiom$ 

```
Assertion := Assertion \cup \{aAssertion\} \mid |
   Axiom := Axiom \cup \{aAssertion\}
END;
Class_NEW(aClass) =
PRE aClass \in ENTITY \land
   aClass \not\in Entity
THEN
   Class := Class \cup \{aClass\} \mid \mid
   Entity := Entity \cup \{aClass\}
END;
Individual\_NEW(aIndividual) =
\mathbf{PRE}
        aIndividual \in ENTITY \land
   aIndividual \not\in Entity
THEN
   Individual := Individual \cup \{aIndividual\} \mid |
   Entity := Entity \cup \{aIndividual\}
\mathbf{END}:
ClassAxiom\_NEW(aClassAxiom) =
        aClassAxiom \in AXIOM \land
   aClassAxiom \not\in Axiom
THEN
   ClassAxiom := ClassAxiom \cup \{aClassAxiom\} \mid |
   Axiom := Axiom \cup \{aClassAxiom\}
END;
Declaration_NEW(aDeclaration) =
PRE aDeclaration \in AXIOM \land
   aDeclaration \not\in Axiom
THEN
   Declaration := Declaration \cup \{aDeclaration\} \mid |
   Axiom := Axiom \cup \{aDeclaration\}
END;
ObjectComplementOf_NEW(aObjectComplementOf) =
        aObjectComplementOf \in CLASSEXPRESSION \land
   aObjectComplementOf \not\in ClassExpression
THEN
   ObjectComplementOf := ObjectComplementOf \cup \{aObjectComplementOf\} \mid |
   ClassExpression := ClassExpression \cup \{aObjectComplementOf\}
END;
ObjectOneOf_NEW(aObjectOneOf) =
        aObjectOneOf \in CLASSEXPRESSION \land
   aObjectOneOf \not\in ClassExpression
```

```
ObjectOneOf := ObjectOneOf \cup \{aObjectOneOf\} \mid |
   ClassExpression := ClassExpression \cup \{aObjectOneOf\}
END;
ObjectHasValue\_NEW(aObjectHasValue) =
        aObjectHasValue \in CLASSEXPRESSION \land
   aObjectHasValue \not\in ClassExpression
THEN
   ObjectHasValue := ObjectHasValue \cup \{aObjectHasValue\} ||
   ClassExpression := ClassExpression \cup \{aObjectHasValue\}
END;
ObjectProperty\_NEW(aObjectProperty) =
        aObjectProperty \in ENTITY \land
   aObjectProperty \not\in Entity
THEN
   ObjectProperty := ObjectProperty \cup \{aObjectProperty\} \mid |
   Entity := Entity \cup \{aObjectProperty\}
END;
ObjectSomeValuesFrom_NEW(aObjectSomeValuesFrom) =
        aObjectSomeValuesFrom \in CLASSEXPRESSION \land
   aObjectSomeValuesFrom \not\in ClassExpression
THEN
   ObjectSomeValuesFrom := ObjectSomeValuesFrom \cup \{aObjectSomeValuesFrom\} | 
   ClassExpression := ClassExpression \cup \{aObjectSomeValuesFrom\}
END;
ObjectAllValuesFrom\_NEW(aObjectAllValuesFrom) =
        aObjectAllValuesFrom \in CLASSEXPRESSION \land
   aObjectAllValuesFrom \not\in ClassExpression
THEN
   ObjectAllValuesFrom := ObjectAllValuesFrom \cup \{aObjectAllValuesFrom\} \mid 
   ClassExpression := ClassExpression \cup \{aObjectAllValuesFrom\}
END;
\mathbf{Datatype}_{-}\mathbf{NEW}(aDatatype) =
        aDatatype \in ENTITY \land
   aDatatype \notin Entity
THEN
   Datatype := Datatype \cup \{aDatatype\} \mid \mid
   Entity := Entity \cup \{aDatatype\}
END;
ClassAssertion\_NEW(aClassAssertion) =
        aClassAssertion \in AXIOM \land
   aClassAssertion \not\in Axiom
```

```
ClassAssertion := ClassAssertion \cup \{aClassAssertion\} ||
   Assertion := Assertion \cup \{aClassAssertion\} \mid |
   Axiom := Axiom \cup \{aClassAssertion\}
END;
EquivalentClasses\_NEW(aEquivalentClasses) =
         aEquivalentClasses \in AXIOM \land
   aEquivalentClasses \not\in Axiom
THEN
   EquivalentClasses := EquivalentClasses \cup \{aEquivalentClasses\} \mid |
   ClassAxiom := ClassAxiom \cup \{aEquivalentClasses\} \mid 
   Axiom := Axiom \cup \{aEquivalentClasses\}
END;
{\bf Disjoint Union\_NEW}(\mathit{aDisjoint Union}) =
         aDisjointUnion \in AXIOM \land
   aDisjointUnion \not\in Axiom
THEN
   DisjointUnion := DisjointUnion \cup \{aDisjointUnion\} \mid 
   ClassAxiom := ClassAxiom \cup \{aDisjointUnion\} \mid |
   Axiom := Axiom \cup \{aDisjointUnion\}
END;
DisjointClasses\_NEW(aDisjointClasses, theClassExpressions) =
         aDisjointClasses \in AXIOM \land
PRE
   theClassExpressions \in \mathcal{F} \ (ClassExpression) \land
   aDisjointClasses \not\in Axiom \land
   \mathbf{card}(theClassExpressions) > 2 \land
    \forall \ added.(\ added \in theClassExpressions \Rightarrow disjointClassExp[\{added\}] = \emptyset)
THEN
   DisjointClasses := DisjointClasses \cup \{aDisjointClasses\} \mid |
   ClassAxiom := ClassAxiom \cup \{aDisjointClasses\} \mid |
   Axiom := Axiom \cup \{aDisjointClasses\} \parallel
   disjointClassExp := disjointClassExp \cup (theClassExpressions \times \{aDisjointClasses\})
END;
{f SubClassOf\_NEW}(aSubClassOf,aSubClassExpression,aSuperClassExpression) =
PRE
         aSubClassOf \in AXIOM \land
   aSubClassExpression \in ClassExpression \land
   aSuperClassExpression \in ClassExpression \land
   aSubClassOf \not\in Axiom \land
   subClassExp^{-1} [\{aSubClassExpression\}] = \emptyset \land
   superClassExp ^{-1} [\{aSuperClassExpression\}] = \emptyset
THEN
   SubClassOf := SubClassOf \cup \{aSubClassOf\} \mid |
   ClassAxiom := ClassAxiom \cup \{aSubClassOf\} \mid |
   Axiom := Axiom \cup \{aSubClassOf\} \mid \mid
   subClassExp := subClassExp \cup \{(aSubClassOf \mapsto aSubClassExpression)\} \mid\mid
   superClassExp := superClassExp \cup \{(aSubClassOf \mapsto aSuperClassExpression)\}
```

```
END;
   xOwl\_Free(aXOwl) =
   PRE
             aXOwl \in XOwl
   THEN
       XOwl := XOwl - \{aXOwl\} \mid \mid
       axioms := axioms \Rightarrow \{aXOwl\} ||
       xOwl\_ontologyIRI := \{aXOwl\} \triangleleft xOwl\_ontologyIRI \mid \}
       xOwl\_versionIRI := \{aXOwl\} \lessdot xOwl\_versionIRI
   END;
   Axiom\_Free(aAxiom) =
   PRE
             aAxiom \in Axiom \land
       aAxiom \not\in Assertion \land
       aAxiom \not\in Declaration \land
       aAxiom \not\in ClassAxiom
   THEN
       Axiom := Axiom - \{aAxiom\} ||
       axioms := \{aAxiom\} \lessdot axioms
   END;
   ClassExpression\_Free(aClassExpression) =
             aClassExpression \in ClassExpression \land
       aClassExpression \not\in ObjectComplementOf \land
       aClassExpression \not\in ObjectOneOf \land
       aClassExpression \not\in ObjectAllValuesFrom \land
       aClassExpression \not\in ObjectSomeValuesFrom \land
       aClassExpression \not\in ObjectHasValue \land
         \forall a Disjoint Classes. (a Disjoint Classes \in disjoint Class Exp[\{a Class Expression\}] \Rightarrow
\mathbf{card}(\mathit{disjointClassExp}^{-1} [\{\mathit{aDisjointClasses}\}]) \geq 3) \land
       subClassExp^{-1} [\{aClassExpression\}] = \emptyset \land
       superClassExp^{-1} [\{aClassExpression\}] = \emptyset
   THEN
       ClassExpression := ClassExpression - \{aClassExpression\} \parallel
       classOfClassExp := \{aClassExpression\} \triangleleft classOfClassExp \mid \}
       A\_classExpression\_classAssertion
                                                    :=
                                                              A\_classExpression\_classAssertion
                                                                                                            \triangleright
\{aClassExpression\} | |
       A\_classExpressions\_equivalentClasses
                                                                          \{aClassExpression\}
                                                            :=
                                                                                                            \triangleleft
A\_classExpressions\_equivalentClasses ||
       A\_disjointClassExpressions\_disjointUnion
                                                                            \{aClassExpression\}
                                                               :=
                                                                                                            ∢
A\_disjointClassExpressions\_disjointUnion ||
       disjointClassExp := \{aClassExpression\} \triangleleft disjointClassExp \mid |
       subClassExp := subClassExp \Rightarrow \{aClassExpression\} \mid |
       superClassExp := superClassExp \Rightarrow \{aClassExpression\} \mid \}
       A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf \Rightarrow
\{aClassExpression\} \mid |
       A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom
\Rightarrow \{aClassExpression\} \parallel
       A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom <math>\Rightarrow
\{aClassExpression\}
```

```
END;
          Entity\_Free(aEntity) =
          PRE
                                          aEntity \in Entity \land
                       aEntity \not\in Class \land
                       aEntity \not\in Individual \land
                       aEntity \not\in ObjectProperty \land
                       aEntity \not\in Datatype
          THEN
                       Entity := Entity - \{aEntity\} ||
                      A\_entity\_declaration := A\_entity\_declaration \Rightarrow \{aEntity\} \mid |
                       Entity\_name := \{aEntity\} \triangleleft Entity\_name
          END;
          Annotation\_Free(aAnnotation) =
          PRE
                                          aAnnotation \in Annotation
          THEN
                       Annotation := Annotation - \{aAnnotation\} \parallel
                       axiomAnnotations := \{aAnnotation\} \triangleleft axiomAnnotations ||
                       Annotation\_annotationValue := \{aAnnotation\} \prec Annotation\_annotationValue\}
          END;
           {f ObjectPropertyExpression\_Free}(aObjectPropertyExpression) =
                                          aObjectPropertyExpression \in ObjectPropertyExpression
          THEN
                       ObjectPropertyExpression := ObjectPropertyExpression - \{aObjectPropertyExpression\} ||
                       A\_objectProperty\_objectPropertyExpression
                                                                                                                                                                                           := \{aObjectPropertyExpression\}
A\_objectProperty\_objectPropertyExpression ||
                       A\_objectPropertyExpression\_objectHasValue := A\_objectPropertyExpression\_objectHasValue
\Rightarrow \{aObjectPropertyExpression\} | |
                       A\_objectPropertyExpression\_objectSomeValuesFrom := A\_objectPropertyExpression\_objectFrom := A\_objectPropertyExpression\_objectFrom := A\_objectPropertyExpression\_objectFrom := A\_objectFrom := A\_objectFro
\Rightarrow \{aObjectPropertyExpression\} | |
                       A\_objectPropertyExpression\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFr
\Rightarrow \{aObjectPropertyExpression\}
          END;
           Assertion\_Free(aAssertion) =
                                          aAssertion \in Assertion \land
                       aAssertion \not\in ClassAssertion
          THEN
                       Assertion := Assertion - \{aAssertion\} \mid \mid
                       Axiom := Axiom - \{aAssertion\} \mid \mid
                       axioms := \{aAssertion\} \triangleleft axioms
          END;
           Class\_Free(aClass) =
          PRE
                                          aClass \in Class
          THEN
```

 $Class := Class - \{aClass\} ||$ 

```
Entity := Entity - \{aClass\} ||
       classOfClassExp := classOfClassExp \Rightarrow \{aClass\} ||
       A\_class\_disjointUnion := A\_class\_disjointUnion \Rightarrow \{aClass\} ||
       A\_entity\_declaration := A\_entity\_declaration \Rightarrow \{aClass\} | |
       Entity\_name := \{aClass\} \triangleleft Entity\_name
   END;
   Individual\_Free(aIndividual) =
   PRE
             aIndividual \in Individual
   THEN
       Individual := Individual - \{aIndividual\} \parallel
       Entity := Entity - \{aIndividual\} \mid |
       A\_individual\_classAssertion := A\_individual\_classAssertion \Rightarrow \{aIndividual\} \mid |
       A\_entity\_declaration := A\_entity\_declaration \Rightarrow \{aIndividual\} ||
       A\_individuals\_objectOneOf := A\_individuals\_objectOneOf \Rightarrow \{aIndividual\} \mid |
       A\_individual\_objectHasValue := A\_individual\_objectHasValue \Rightarrow \{aIndividual\} ||
       Entity\_name := \{aIndividual\} \triangleleft Entity\_name
   END;
   ClassAxiom\_Free(aClassAxiom) =
             aClassAxiom \in ClassAxiom \land
       aClassAxiom \not\in DisjointClasses \land
       aClassAxiom \not\in SubClassOf \land
       aClassAxiom \not\in EquivalentClasses \land
       aClassAxiom \not\in DisjointUnion
   THEN
       ClassAxiom := ClassAxiom - \{aClassAxiom\} | |
       Axiom := Axiom - \{aClassAxiom\} \mid |
       axioms := \{aClassAxiom\} \triangleleft axioms \mid \mid
       axiomAnnotations := axiomAnnotations \Rightarrow \{aClassAxiom\}
   END;
   Declaration\_Free(aDeclaration) =
             aDeclaration \in Declaration
   THEN
       Declaration := Declaration - \{aDeclaration\} \mid |
       Axiom := Axiom - \{aDeclaration\} \mid |
       axioms := \{aDeclaration\} \triangleleft axioms \mid \mid
       A\_entity\_declaration := \{aDeclaration\} \prec A\_entity\_declaration
   END;
   ObjectComplementOf\_Free(aObjectComplementOf) =
             aObjectComplementOf \in ObjectComplementOf \land
        \forall \ aDisjointClasses.(\ aDisjointClasses \in disjointClassExp[\{aObjectComplementOf\}] \Rightarrow
\mathbf{card}(\mathit{disjointClassExp}^{-1} [\{\mathit{aDisjointClasses}\}]) \ge 3) \land
       subClassExp^{-1} [\{aObjectComplementOf\}] = \emptyset \land
       superClassExp^{-1}[\{aObjectComplementOf\}] = \emptyset
   THEN
       ObjectComplementOf := ObjectComplementOf - \{aObjectComplementOf\} |
```

```
ClassExpression := ClassExpression - \{aObjectComplementOf\} | |
       classOfClassExp := \{aObjectComplementOf\} \lhd classOfClassExp \mid \}
       A\_classExpression\_classAssertion
                                                   :=
                                                             A\_classExpression\_classAssertion
                                                                                                          ⊳
\{aObjectComplementOf\} ||
                                                                     \{aObjectComplementOf\}
       A\_classExpressions\_equivalentClasses
                                                                                                          \triangleleft
A\_classExpressions\_equivalentClasses ||
                                                                       \{aObjectComplementOf\}
       A\_disjointClassExpressions\_disjointUnion
                                                            :=
                                                                                                          ∢
A\_disjointClassExpressions\_disjointUnion | |
       disjointClassExp := \{aObjectComplementOf\} \bowtie disjointClassExp \mid \}
       subClassExp := subClassExp \Rightarrow \{aObjectComplementOf\} \mid 
       superClassExp := superClassExp \Rightarrow \{aObjectComplementOf\} \mid |
       A\_classExpression\_objectComplementOf
                                                                      { aObjectComplementOf}
                                                           :=
                                                                                                          \triangleleft
(A\_classExpression\_objectComplementOf \Rightarrow \{aObjectComplementOf\}) ||
       A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom
\Rightarrow \{aObjectComplementOf\} | |
       A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom <math>\Rightarrow
\{aObjectComplementOf\}
   END;
   ObjectOneOf\_Free(aObjectOneOf) =
             aObjectOneOf \in ObjectOneOf \land
              aDisjointClasses. ( aDisjointClasses \in disjointClassExp[{aObjectOneOf}]
\mathbf{card}(\mathit{disjointClassExp}^{-1} \ [\{\mathit{aDisjointClasses}\}]) \ge 3) \land 
       subClassExp^{-1}[\{aObjectOneOf\}] = \emptyset \land
       superClassExp^{-1}[\{aObjectOneOf\}] = \emptyset
   THEN
       ObjectOneOf := ObjectOneOf - \{aObjectOneOf\} \mid 
       ClassExpression := ClassExpression - \{aObjectOneOf\} | |
       classOfClassExp := \{aObjectOneOf\} \triangleleft classOfClassExp \mid |
       A\_classExpression\_classAssertion
                                                             A\_classExpression\_classAssertion
                                                   :=
\{aObjectOneOf\} \mid |
       A\_classExpressions\_equivalentClasses
                                                                           \{aObjectOneOf\}
                                                                                                          ∢
A\_classExpressions\_equivalentClasses | |
                                                                             \{aObjectOneOf\}
       A\_disjointClassExpressions\_disjointUnion
                                                               :=
                                                                                                          \triangleleft
A\_disjointClassExpressions\_disjointUnion | |
       disjointClassExp := \{aObjectOneOf\} \triangleleft disjointClassExp \mid \}
       subClassExp := subClassExp \Rightarrow \{aObjectOneOf\} \mid |
       superClassExp := superClassExp \Rightarrow \{aObjectOneOf\} \mid |
       A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf \Rightarrow
\{aObjectOneOf\} \mid |
       A\_individuals\_objectOneOf := \{aObjectOneOf\} \prec A\_individuals\_objectOneOf\}
       A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom
\Rightarrow \{aObjectOneOf\} ||
       A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom <math>\Rightarrow
\{aObjectOneOf\}
   END;
   ObjectHasValue\_Free(aObjectHasValue) =
   PRE
             aObjectHasValue \in ObjectHasValue \land
             aDisjointClasses.( aDisjointClasses \in disjointClassExp[\{aObjectHasValue\}] \Rightarrow
\operatorname{\mathbf{card}}(\operatorname{\mathit{disjointClassExp}}^{-1} [\{\operatorname{\mathit{aDisjointClasses}}\}]) \geq 3) \land
       subClassExp^{-1} [\{aObjectHasValue\}] = \emptyset \land
```

```
superClassExp^{-1} [\{aObjectHasValue\}] = \emptyset
   THEN
       ObjectHasValue := ObjectHasValue - \{aObjectHasValue\} | 
       ClassExpression := ClassExpression - \{aObjectHasValue\} | |
       classOfClassExp := \{aObjectHasValue\} \lhd classOfClassExp \mid |
       A\_classExpression\_classAssertion
                                                  :=
                                                            A\_classExpression\_classAssertion
                                                                                                         \Rightarrow
\{aObjectHasValue\} | |
                                                                        \{aObjectHasValue\}
       A\_classExpressions\_equivalentClasses
                                                                                                         \triangleleft
A\_classExpressions\_equivalentClasses ||
       A\_disjointClassExpressions\_disjointUnion
                                                                          \{aObjectHasValue\}
                                                              :=
                                                                                                         \triangleleft
A\_disjointClassExpressions\_disjointUnion | |
       disjointClassExp := \{aObjectHasValue\} \triangleleft disjointClassExp \mid |
       subClassExp := subClassExp \Rightarrow \{aObjectHasValue\} \mid |
       superClassExp := superClassExp \Rightarrow \{aObjectHasValue\} \mid \}
       A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf \Rightarrow
\{aObjectHasValue\} \mid |
       A\_objectPropertyExpression\_objectHasValue
                                                                           \{aObjectHasValue\}
                                                                :=
                                                                                                         \triangleleft
A\_objectPropertyExpression\_objectHasValue | |
       A\_individual\_objectHasValue := \{aObjectHasValue\} \neq A\_individual\_objectHasValue ||
       A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom
\Rightarrow \{aObjectHasValue\} \mid |
       A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom <math>\Rightarrow
\{aObjectHasValue\}
   END;
   ObjectProperty\_Free(aObjectProperty) =
   \mathbf{PRE}
             aObjectProperty \in ObjectProperty
   THEN
       ObjectProperty := ObjectProperty - \{aObjectProperty\} ||
       Entity := Entity - \{aObjectProperty\} \mid \mid
       A\_entity\_declaration := A\_entity\_declaration \Rightarrow \{aObjectProperty\} \mid |
       A\_objectProperty\_objectPropertyExpression := A\_objectProperty\_objectPropertyExpression
\Rightarrow \{aObjectProperty\} ||
       Entity\_name := \{aObjectProperty\} \triangleleft Entity\_name
   END;
   \mathbf{ObjectSomeValuesFrom\_Free}(\mathit{aObjectSomeValuesFrom}) =
             aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
       \forall \ aDisjointClasses.(\ aDisjointClasses \in disjointClassExp[\{aObjectSomeValuesFrom\}] \Rightarrow
\mathbf{card}(\mathit{disjointClassExp}^{-1} [\{a\mathit{DisjointClasses}\}]) \geq 3) \land
       subClassExp^{-1} [\{aObjectSomeValuesFrom\}] = \emptyset \land
       superClassExp^{-1} [\{aObjectSomeValuesFrom\}] = \emptyset
   THEN
       ObjectSome\ ValuesFrom := ObjectSome\ ValuesFrom - \{aObjectSome\ ValuesFrom\}\ ||
       ClassExpression := ClassExpression - \{aObjectSomeValuesFrom\} | 
       classOfClassExp := \{aObjectSomeValuesFrom\} \lessdot classOfClassExp \mid \}
                                                            A\_classExpression\_classAssertion
       A\_classExpression\_classAssertion
                                                   :=
```

:=

 $\{aObjectSomeValuesFrom\} \parallel$ 

 $A\_classExpressions\_equivalentClasses$ 

 $A\_classExpressions\_equivalentClasses ||$ 

₽

 $\triangleleft$ 

{ a Object Some Values From}

```
A\_disjointClassExpressions\_disjointUnion
                                                                    { aObjectSome ValuesFrom}
                                                           :=
                                                                                                        \triangleleft
A\_disjointClassExpressions\_disjointUnion ||
       disjointClassExp := \{aObjectSomeValuesFrom\} \triangleleft disjointClassExp \mid \}
       subClassExp := subClassExp \Rightarrow \{aObjectSomeValuesFrom\} \mid 
       superClassExp := superClassExp \Rightarrow \{aObjectSomeValuesFrom\} \mid |
       A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf \Rightarrow
\{aObjectSomeValuesFrom\} \parallel
       A\_objectPropertyExpression\_objectSomeValuesFrom := \{aObjectSomeValuesFrom\}
A\_objectPropertyExpression\_objectSomeValuesFrom | |
       A\_classExpression\_objectSomeValuesFrom
                                                                    { aObjectSome ValuesFrom}
                                                                                                        \triangleleft
(A\_classExpression\_objectSomeValuesFrom \Rightarrow \{aObjectSomeValuesFrom\}) ||
       A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom <math>\Rightarrow
\{aObjectSomeValuesFrom\}
   END;
   ObjectAllValuesFrom\_Free(aObjectAllValuesFrom) =
             aObjectAllValuesFrom \in ObjectAllValuesFrom \land
        \forall \ aDisjointClasses.(\ aDisjointClasses \in disjointClassExp[\{aObjectAllValuesFrom\}] \Rightarrow
\mathbf{card}(\mathit{disjointClassExp}^{-1} [\{a\mathit{DisjointClasses}\}]) \geq 3) \land
       subClassExp^{-1} [\{aObjectAllValuesFrom\}] = \emptyset \land
       superClassExp^{-1} [\{aObjectAllValuesFrom\}] = \emptyset
   THEN
       ObjectAllValuesFrom := ObjectAllValuesFrom - \{aObjectAllValuesFrom\} | 
       ClassExpression := ClassExpression - \{aObjectAllValuesFrom\} | |
       classOfClassExp := \{aObjectAllValuesFrom\} \lessdot classOfClassExp \mid |
       A\_classExpression\_classAssertion
                                                  :=
                                                            A\_classExpression\_classAssertion
                                                                                                        ₽
\{aObjectAllValuesFrom\} \mid |
       A\_classExpressions\_equivalentClasses
                                                                    \{aObjectAllValuesFrom\}
                                                                                                         ⋖
A\_classExpressions\_equivalentClasses ||
                                                                      \{aObjectAllValuesFrom\}
       A\_disjointClassExpressions\_disjointUnion
                                                            :=
                                                                                                        \triangleleft
A\_disjointClassExpressions\_disjointUnion | |
       disjointClassExp := \{aObjectAllValuesFrom\} \triangleleft disjointClassExp \mid \}
       subClassExp := subClassExp \Rightarrow \{aObjectAllValuesFrom\} \mid |
       superClassExp := superClassExp \Rightarrow \{aObjectAllValuesFrom\} \mid 
       A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf \Rightarrow
\{aObjectAllValuesFrom\} \parallel
       A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom
\Rightarrow \{aObjectAllValuesFrom\} \mid |
       A\_objectPropertyExpression\_objectAllValuesFrom
                                                                         { aObjectAllValuesFrom}
                                                                                                        \triangleleft
A\_objectPropertyExpression\_objectAllValuesFrom | |
                                                                     { aObjectAllValuesFrom}
       A\_classExpression\_objectAllValuesFrom
                                                                                                        \triangleleft
(A\_classExpression\_objectAllValuesFrom \Rightarrow \{aObjectAllValuesFrom\})
   END;
   Datatype\_Free(aDatatype) =
   \mathbf{PRE}
            aDatatype \in Datatype
   THEN
       Datatype := Datatype - \{aDatatype\} \mid \mid
       Entity := Entity - \{aDatatype\} | |
       A\_entity\_declaration := A\_entity\_declaration \Rightarrow \{aDatatype\} \mid |
       Entity\_name := \{aDatatype\} \triangleleft Entity\_name
```

```
END;
   ClassAssertion\_Free(aClassAssertion) =
   PRE
            aClassAssertion \in ClassAssertion
   THEN
      ClassAssertion := ClassAssertion - \{aClassAssertion\} | |
      Assertion := Assertion - \{aClassAssertion\} | |
      Axiom := Axiom - \{aClassAssertion\} \mid |
      axioms := \{aClassAssertion\} \triangleleft axioms \mid |
      A\_classExpression\_classAssertion
                                                                      \{aClassAssertion\}
                                                                                                       \triangleleft
A\_classExpression\_classAssertion ||
      A\_individual\_classAssertion := \{aClassAssertion\} \not= A\_individual\_classAssertion\}
   END;
   EquivalentClasses\_Free(aEquivalentClasses) =
   PRE
            aEquivalentClasses \in EquivalentClasses
   THEN
      EquivalentClasses := EquivalentClasses - \{aEquivalentClasses\} \parallel
      ClassAxiom := ClassAxiom - \{aEquivalentClasses\} | |
      Axiom := Axiom - \{aEquivalentClasses\} \mid \mid
      axioms := \{aEquivalentClasses\} \triangleleft axioms | |
      axiomAnnotations := axiomAnnotations \Rightarrow \{aEquivalentClasses\} \mid |
      A\_classExpressions\_equivalentClasses
                                                 :=
                                                         A\_classExpressions\_equivalentClasses
\{aEquivalentClasses\}
   END;
   DisjointUnion\_Free(aDisjointUnion) =
   \mathbf{PRE}
            aDisjointUnion \in DisjointUnion
   THEN
      Disjoint Union := Disjoint Union - \{aDisjoint Union\} \parallel
      ClassAxiom := ClassAxiom - \{aDisjointUnion\} | |
      Axiom := Axiom - \{aDisjointUnion\} \mid |
      axioms := \{aDisjointUnion\} \triangleleft axioms \mid \}
      axiomAnnotations := axiomAnnotations \Rightarrow \{aDisjointUnion\} \parallel
      A\_class\_disjointUnion := \{aDisjointUnion\} \bowtie A\_class\_disjointUnion | \}
      A\_disjointClassExpressions\_disjointUnion := A\_disjointClassExpressions\_disjointUnion
\Rightarrow \{\mathit{aDisjointUnion}\}
   END;
   DisjointClasses\_Free(aDisjointClasses) =
   \mathbf{PRE}
            aDisjointClasses \in DisjointClasses
   THEN
      DisjointClasses := DisjointClasses - \{aDisjointClasses\} ||
      ClassAxiom := ClassAxiom - \{aDisjointClasses\} | |
      Axiom := Axiom - \{aDisjointClasses\} | |
      axioms := \{aDisjointClasses\} \triangleleft axioms \mid \mid
      axiomAnnotations := axiomAnnotations \Rightarrow \{aDisjointClasses\} ||
      disjointClassExp := disjointClassExp \Rightarrow \{aDisjointClasses\}
```

```
END;
SubClassOf\_Free(aSubClassOf) =
PRE
         aSubClassOf \in SubClassOf
THEN
   SubClassOf := SubClassOf - \{aSubClassOf\} \mid |
   ClassAxiom := ClassAxiom - \{aSubClassOf\} ||
   Axiom := Axiom - \{aSubClassOf\} \mid |
   axioms := \{aSubClassOf\} \triangleleft axioms \mid \}
   axiomAnnotations := axiomAnnotations \Rightarrow \{aSubClassOf\} \mid |
   subClassExp := \{aSubClassOf\} \lessdot subClassExp \mid \}
   superClassExp := \{aSubClassOf\} \triangleleft superClassExp
END;
result \leftarrow \mathbf{xOwl\_GetAxioms}(aXOwl) =
         aXOwl \in XOwl \land
   aXOwl \in \mathbf{ran}(axioms)
THEN
   result := axioms^{-1} [\{aXOwl\}]
END;
result \leftarrow ClassAssertion\_GetClassExpression(aClassAssertion) =
         aClassAssertion \in ClassAssertion \land
   aClassAssertion \in \mathbf{dom}(A\_classExpression\_classAssertion)
THEN
   result := A\_classExpression\_classAssertion(aClassAssertion)
END;
result \leftarrow ClassAssertion\_GetIndividual(aClassAssertion) =
         aClassAssertion \in ClassAssertion \land
   aClassAssertion \in \mathbf{dom}(A\_individual\_classAssertion)
THEN
   result := A\_individual\_classAssertion(aClassAssertion)
END;
result \leftarrow ClassExpression\_GetClass(aClassExpression) =
         aClassExpression \in ClassExpression \land
   aClassExpression \in \mathbf{dom}(classOfClassExp)
   result := classOfClassExp(aClassExpression)
END;
result \leftarrow ClassAxiom\_GetAxiomAnnotations(aClassAxiom) =
         aClassAxiom \in ClassAxiom \land
   aClassAxiom \in \mathbf{ran}(axiomAnnotations)
THEN
   result := axiomAnnotations^{-1} [\{aClassAxiom\}]
```

```
END;
result \leftarrow \mathbf{EquivalentClasses\_GetClassExpressions}(aEquivalentClasses) =
         aEquivalentClasses \in EquivalentClasses \land
   aEquivalentClasses \in \mathbf{ran}(A\_classExpressions\_equivalentClasses)
THEN
   result := A\_classExpressions\_equivalentClasses ^{-1} [\{aEquivalentClasses\}]
END;
result \leftarrow \mathbf{DisjointUnion\_GetClass}(aDisjointUnion) =
         aDisjointUnion \in DisjointUnion \land
   aDisjointUnion \in \mathbf{dom}(A\_class\_disjointUnion)
THEN
   result := A\_class\_disjointUnion(aDisjointUnion)
END;
result \leftarrow \mathbf{DisjointUnion\_GetDisjointClassExpressions}(aDisjointUnion) =
         aDisjointUnion \in DisjointUnion \land
   aDisjointUnion \in \mathbf{ran}(A\_disjointClassExpressions\_disjointUnion)
THEN
   result := A\_disjointClassExpressions\_disjointUnion^{-1} [\{aDisjointUnion\}]
END;
result \leftarrow DisjointClasses\_GetClassExpressions(aDisjointClasses) =
         aDisjointClasses \in DisjointClasses \land
   aDisjointClasses \in \mathbf{ran}(disjointClassExp)
THEN
   result := disjointClassExp^{-1} [\{aDisjointClasses\}]
END;
result \leftarrow \mathbf{SubClassOf\_GetSubClassExpression}(aSubClassOf) =
         aSubClassOf \in SubClassOf \land
   aSubClassOf \in \mathbf{dom}(subClassExp)
THEN
   result := subClassExp(aSubClassOf)
END;
result \leftarrow \mathbf{SubClassOf\_GetSuperClassExpression}(aSubClassOf) =
         aSubClassOf \in SubClassOf \land
   aSubClassOf \in \mathbf{dom}(superClassExp)
THEN
   result := superClassExp(aSubClassOf)
END;
result \leftarrow \mathbf{Declaration\_GetEntity}(aDeclaration) =
         aDeclaration \in Declaration \land
   aDeclaration \in \mathbf{dom}(A\_entity\_declaration)
```

```
THEN
   result := A\_entity\_declaration(aDeclaration)
END;
result \leftarrow \mathbf{ObjectComplementOf\_GetClassExpression}(aObjectComplementOf) =
        aObjectComplementOf \in ObjectComplementOf \land
   aObjectComplementOf \in \mathbf{dom}(A\_classExpression\_objectComplementOf)
THEN
   result := A\_classExpression\_objectComplementOf(aObjectComplementOf)
END;
result \leftarrow \mathbf{ObjectOneOf\_GetIndividuals}(aObjectOneOf) =
         aObjectOneOf \in ObjectOneOf \land
   aObjectOneOf \in \mathbf{dom}(A\_individuals\_objectOneOf)
   result := A\_individuals\_objectOneOf[{aObjectOneOf}]
END;
result \leftarrow \mathbf{ObjectHasValue\_GetObjectPropertyExpression}(aObjectHasValue) =
         aObjectHasValue \in ObjectHasValue \land
   aObjectHasValue \in \mathbf{dom}(A\_objectPropertyExpression\_objectHasValue)
THEN
   result := A\_objectPropertyExpression\_objectHasValue(aObjectHasValue)
END;
result \leftarrow \mathbf{ObjectHasValue\_GetIndividual}(aObjectHasValue) =
         aObjectHasValue \in ObjectHasValue \land
   aObjectHasValue \in \mathbf{dom}(A\_individual\_objectHasValue)
THEN
   result := A\_individual\_objectHasValue(aObjectHasValue)
END;
result \leftarrow \mathbf{ObjectPropertyExpression\_GetObjectProperty}(aObjectPropertyExpression)
         aObjectPropertyExpression \in ObjectPropertyExpression \land
   aObjectPropertyExpression \in \mathbf{dom}(A\_objectProperty\_objectPropertyExpression)
THEN
   result := A\_objectProperty\_objectPropertyExpression(aObjectPropertyExpression)
END;
result \leftarrow \mathbf{ObjectSomeValuesFrom\_GetObjectPropertyExpression}(aObjectSomeValuesFrom)
PRE
         aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
   aObjectSomeValuesFrom \in \mathbf{dom}(A\_objectPropertyExpression\_objectSomeValuesFrom)
THEN
```

 $result := A\_objectPropertyExpression\_objectSomeValuesFrom(aObjectSomeValuesFrom)$ 

```
END;
   result \leftarrow \mathbf{ObjectSomeValuesFrom\_GetClassExpression}(\mathit{aObjectSomeValuesFrom}) = 0
            aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
      aObjectSomeValuesFrom \in \mathbf{dom}(A\_classExpression\_objectSomeValuesFrom)
   THEN
      result := A\_classExpression\_objectSomeValuesFrom(aObjectSomeValuesFrom)
   END;
   result \leftarrow \mathbf{ObjectAllValuesFrom\_GetObjectPropertyExpression}(aObjectAllValuesFrom)
  PRE
            aObjectAllValuesFrom \in ObjectAllValuesFrom \land
      aObjectAllValuesFrom \in \mathbf{dom}(A\_objectPropertyExpression\_objectAllValuesFrom)
  THEN
      result := A\_objectPropertyExpression\_objectAllValuesFrom(aObjectAllValuesFrom)
  END;
   result \leftarrow \mathbf{ObjectAllValuesFrom\_GetClassExpression}(aObjectAllValuesFrom) =
            aObjectAllValuesFrom \in ObjectAllValuesFrom \land
      aObjectAllValuesFrom \in \mathbf{dom}(A\_classExpression\_objectAllValuesFrom)
   THEN
      result := A\_classExpression\_objectAllValuesFrom(aObjectAllValuesFrom)
   \mathbf{END};
  xOwl\_SetAxioms(aXOwl, theAxioms) =
  \mathbf{PRE}
            aXOwl \in XOwl \land
      theAxioms \in \mathcal{F} (Axiom) \land
      (theAxioms \times \{aXOwl\}) \not\subseteq axioms \land
       \forall \ added.(\ added \in theAxioms \Rightarrow axioms[\{added\}] = \emptyset)
   THEN
      axioms := (axioms \Rightarrow \{aXOwl\}) \cup (theAxioms \times \{aXOwl\})
   END;
   ClassAssertion\_SetClassExpression(aClassAssertion, aClassExpression) =
   PRE
            aClassAssertion \in ClassAssertion \land
      aClassExpression \in ClassExpression \land
      \{(aClassAssertion \mapsto aClassExpression)\} \not\subseteq A\_classExpression\_classAssertion \land
      A\_classExpression\_classAssertion^{-1} [\{aClassExpression\}] = \emptyset
   THEN
      A\_classExpression\_classAssertion
                                                                    (\{aClassAssertion\})
                                                                                                     ∢
A\_classExpression\_classAssertion) \cup \{(aClassAssertion \mapsto aClassExpression)\}
   END;
   ClassAssertion\_SetIndividual(aClassAssertion, aIndividual) =
            aClassAssertion \in ClassAssertion \land
      aIndividual \in Individual \land
      \{(aClassAssertion \mapsto aIndividual)\} \not\subseteq A\_individual\_classAssertion
```

```
\{(aClassAssertion \mapsto aIndividual)\}
   END;
   ClassExpression\_SetClass(aClassExpression, aClass) =
            aClassExpression \in ClassExpression \land
      aClass \in Class \land
      \{(aClassExpression \mapsto aClass)\} \not\subseteq classOfClassExp
      aClass)
   END;
   ClassAxiom\_SetAxiomAnnotations(aClassAxiom, the AxiomAnnotations) =
            aClassAxiom \in ClassAxiom \land
      theAxiomAnnotations \in \mathcal{F} (Annotation) \land
      (theAxiomAnnotations \times \{aClassAxiom\}) \not\subseteq axiomAnnotations \land
      \forall \ added.(\ added \in theAxiomAnnotations \Rightarrow axiomAnnotations[\{added\}] = \emptyset)
   THEN
      axiomAnnotations := (axiomAnnotations \Rightarrow \{aClassAxiom\}) \cup (theAxiomAnnotations \times axiomAnnotations)
\{aClassAxiom\}
   END;
   Equivalent Classes\_Set Class Expressions (a Equivalent Classes, the Class Expressions) =
            aEquivalentClasses \in EquivalentClasses \ \land
   PRE
      theClassExpressions \in \mathcal{F} \ (ClassExpression) \land
      (the Class Expressions \times \{aEquivalent Classes\}) \not\subseteq A\_class Expressions\_equivalent Classes \land
       \forall \ added.(\ added \in theClassExpressions \Rightarrow A\_classExpressions\_equivalentClasses[\{added\}]
=\emptyset)
   THEN
      A\_classExpressions\_equivalentClasses :=
                                                      (A\_classExpressions\_equivalentClasses
\{aEquivalentClasses\}) \cup (theClassExpressions \times \{aEquivalentClasses\})
   END:
   DisjointUnion\_SetClass(aDisjointUnion, aClass) =
   \mathbf{PRE}
            aDisjointUnion \in DisjointUnion \land
      aClass \in Class \land
      \{(aDisjointUnion \mapsto aClass)\} \not\subseteq A\_class\_disjointUnion
   THEN
      A\_class\_disjointUnion
                                        (\{aDisjointUnion\})
                                                                     A\_class\_disjointUnion
                                                                                                  \bigcup
\{(aDisjointUnion \mapsto aClass)\}
  END;
   {\bf Disjoint Union\_Set Disjoint Class Expressions} (a Disjoint Union, the Disjoint Class Expressions)
            aDisjointUnion \in DisjointUnion \land
      theDisjointClassExpressions \in \mathcal{F} (ClassExpression) \land
      (the Disjoint Class Expressions \times \{aDisjoint Union\}) \not\subseteq A\_disjoint Class Expressions\_disjoint Union
Λ
             \forall
                      added.(
                                      added
                                                   \in
                                                            the Disjoint Class Expressions
                                                                                                 \Rightarrow
```

```
A\_disjointClassExpressions\_disjointUnion[{added}] = \emptyset)
   THEN
       A\_disjointClassExpressions\_disjointUnion := (A\_disjointClassExpressions\_disjointUnion
\Rightarrow \{aDisjointUnion\}) \cup (theDisjointClassExpressions \times \{aDisjointUnion\})
   END;
   DisjointClasses\_SetClassExpressions(aDisjointClasses, theClassExpressions) =
             aDisjointClasses \in DisjointClasses \land
       theClassExpressions \in \mathcal{F} (ClassExpression) \land
       (theClassExpressions \times \{aDisjointClasses\}) \not\subseteq disjointClassExp \land
       \mathbf{card}(theClassExpressions) \geq 2 \land
       \forall \ added.(\ added \in theClassExpressions \Rightarrow disjointClassExp[\{added\}] = \emptyset)
       disjointClassExp := (disjointClassExp \Rightarrow \{aDisjointClasses\}) \cup (theClassExpressions \times \{aDisjointClassExp \})
\{aDisjointClasses\}
   END;
   SubClassOf\_SetSubClassExpression(aSubClassOf,aSubClassExpression) =
             aSubClassOf \in SubClassOf \land
       aSubClassExpression \in ClassExpression \land
       \{(aSubClassOf \mapsto aSubClassExpression)\} \not\subseteq subClassExp \land
       subClassExp^{-1} [\{aSubClassExpression\}] = \emptyset
   THEN
       subClassExp := (\{aSubClassOf\} \triangleleft subClassExp) \cup \{(aSubClassOf \mapsto aSubClassExpres-
sion)
   END;
   SubClassOf\_SetSuperClassExpression(aSubClassOf\_aSuperClassExpression) =
   PRE
             aSubClassOf \in SubClassOf \land
       aSuperClassExpression \in ClassExpression \land
       \{(aSubClassOf \mapsto aSuperClassExpression)\} \not\subseteq superClassExp \land
       superClassExp^{-1} [\{aSuperClassExpression\}] = \emptyset
   THEN
       superClassExp := (\{aSubClassOf\} \triangleleft superClassExp) \cup \{(aSubClassOf \mapsto aSuperClassEx-
pression)
   END;
   Declaration\_SetEntity(aDeclaration, aEntity) =
             aDeclaration \in Declaration \land
       aEntity \in Entity \land
       \{(aDeclaration \mapsto aEntity)\} \not\subseteq A\_entity\_declaration \land
       A\_entity\_declaration \ ^{-1} \ [\{aEntity\}] = \emptyset
   THEN
```

 ${\bf ObjectComplementOf\_SetClassExpression} (a ObjectComplementOf, a ClassExpression)$ 

 $A\_entity\_declaration := (\{aDeclaration\} \lessdot A\_entity\_declaration) \cup \{(aDeclaration \mapsto$ 

aEntity)} **END**;

=

```
aObjectComplementOf \in ObjectComplementOf \land
  PRE
      aClassExpression \in ClassExpression \land
      \{(aObjectComplementOf \mapsto aClassExpression)\} \not\subseteq A\_classExpression\_objectComplementOf
      A\_classExpression\_objectComplementOf^{-1} [\{aClassExpression\}] = \emptyset
   THEN
      A\_classExpression\_objectComplementOf
                                                              (\{aObjectComplementOf\}
                                                :=
                                                                                               ∢
A\_classExpression\_objectComplementOf) \cup \{(aObjectComplementOf \mapsto aClassExpression)\}
   END;
   \mathbf{ObjectOneOf\_SetIndividuals}(aObjectOneOf, theIndividuals) =
           aObjectOneOf \in ObjectOneOf \land
      theIndividuals \in \mathcal{F} (Individual) \land
      (\{aObjectOneOf\} \times theIndividuals) \not\subseteq A\_individuals\_objectOneOf
   THEN
      (\{aObjectOneOf\} \times theIndividuals)
   END;
   ObjectHasValue\_SetObjectPropertyExpression(aObjectHasValue,aObjectPropertyExpression)
   \mathbf{PRE}
            aObjectHasValue \in ObjectHasValue \land
      aObjectPropertyExpression \in ObjectPropertyExpression \land
      \{(aObjectHasValue \mapsto aObjectPropertyExpression)\} \not\subseteq A\_objectPropertyExpression\_objectHasValue
\wedge
      A\_objectPropertyExpression\_objectHasValue \ ^{-1} \ [\{aObjectPropertyExpression\}] = \emptyset
   THEN
      A\_objectPropertyExpression\_objectHasValue
                                                                   (\{aObjectHasValue\})
                                                        :=
A\_objectPropertyExpression\_objectHasValue \cup {(aObjectHasValue \mapsto aObjectPropertyEx-
pression)
  END;
   ObjectHasValue\_SetIndividual(aObjectHasValue,aIndividual) =
   \mathbf{PRE}
           aObjectHasValue \in ObjectHasValue \land
      aIndividual \in Individual \land
      \{(aObjectHasValue \mapsto aIndividual)\} \not\subseteq A\_individual\_objectHasValue
   THEN
      A\_individual\_objectHasValue := (\{aObjectHasValue\} \triangleleft A\_individual\_objectHasValue) \cup
\{(aObjectHasValue \mapsto aIndividual)\}
   END;
   ObjectPropertyExpression\_SetObjectProperty(aObjectPropertyExpression\_aObjectProperty)
   PRE
           aObjectPropertyExpression \in ObjectPropertyExpression \land
      aObjectProperty \in ObjectProperty \land
      \{(aObjectPropertyExpression \mapsto aObjectProperty)\} \not\subseteq A\_objectProperty\_objectPropertyExpression
   THEN
                                                            (\{aObjectPropertyExpression\}
      A\_objectProperty\_objectPropertyExpression
                                                    :=
                                                                                               \triangleleft
```

```
A\_objectProperty\_objectPropertyExpression \cup \{(aObjectPropertyExpression \mapsto aObjectPropertyExpression \mapsto aObjectPro
Property)
        END;
         {\bf ObjectSome Values From\_SetObjectProperty Expression} (a ObjectSome Values From\_a Object Property Expression) (a Object Some Values From\_a Object Property Expression) (a Object From\_a Object 
                                   aObjectSomeValuesFrom \, \in \, ObjectSomeValuesFrom \, \, \land \, \,
                  aObjectPropertyExpression \in ObjectPropertyExpression \land
                  \{(aObjectSomeValuesFrom\}\}
                                                                                                                                                                   aObjectPropertyExpression)}
                                                                                                                                                                                                                                                                                         \not\subseteq
A\_objectPropertyExpression\_objectSomeValuesFrom \land
                  A\_objectPropertyExpression\_objectSomeValuesFrom \ ^{-1} \ [\{aObjectPropertyExpression\}] =
Ø
        THEN
                  A\_objectPropertyExpression\_objectSomeValuesFrom := (\{aObjectSomeValuesFrom\} \  \  \, \  \  \, \  \  \, \  \  \, \}
A\_objectPropertyExpression\_objectSomeValuesFrom) \cup \{(aObjectSomeValuesFrom \mapsto aObject-
PropertyExpression)
        END;
         {\bf Object Some Values From\_Set Class Expression} (\textit{aObjectSome Values From}, \textit{aClass Expression})
        PRE
                                   aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
                  aClassExpression \in ClassExpression \land
                  \{(aObjectSomeValuesFrom \mapsto aClassExpression)\} \not\subseteq A\_classExpression\_objectSomeValuesFrom
\wedge
                  A\_classExpression\_objectSomeValuesFrom^{-1} [\{aClassExpression\}] = \emptyset
        THEN
                  A\_classExpression\_objectSomeValuesFrom :=
                                                                                                                                                                                      (\{aObjectSomeValuesFrom\})
A\_classExpression\_objectSomeValuesFrom) \cup \{(aObjectSomeValuesFrom \mapsto aClassExpression\_objectSomeValuesFrom) \}
        END;
        \textbf{ObjectAllValuesFrom\_SetObjectPropertyExpression} (a \textit{ObjectAllValuesFrom}, a \textit{ObjectPropertyExpression}) \\
        PRE
                                   aObjectAllValuesFrom \in ObjectAllValuesFrom \land
                  aObjectPropertyExpression \in ObjectPropertyExpression \land
                  \{(aObjectAllValuesFrom \}\}
                                                                                                                                                               aObjectPropertyExpression)}
                                                                                                                         \mapsto
                                                                                                                                                                                                                                                                                         \not\subseteq
A\_objectPropertyExpression\_objectAllValuesFrom \land
                  A\_objectPropertyExpression\_objectAllValuesFrom \ ^{-1} \ [\{aObjectPropertyExpression\}] = \emptyset
        THEN
                  A\_objectPropertyExpression\_objectAllValuesFrom := ({aObjectAllValuesFrom})
A\_objectPropertyExpression\_objectAllValuesFrom \cup {(aObjectAllValuesFrom \mapsto aObject-
PropertyExpression)
        END;
         {f ObjectAllValuesFrom\_SetClassExpression}(aObjectAllValuesFrom,aClassExpression) =
                                   aObjectAllValuesFrom \in ObjectAllValuesFrom \land
                  aClassExpression \in ClassExpression \land
                  \{(aObjectAllValuesFrom \mapsto aClassExpression)\} \not\subseteq A\_classExpression\_objectAllValuesFrom
\land
                  A\_classExpression\_objectAllValuesFrom ^{-1} [\{aClassExpression\}] = \emptyset
```

```
THEN
      A_classExpression_objectAllValuesFrom
                                              :=
                                                            (\{aObjectAllValuesFrom\})
                                                                                           \triangleleft
A\_classExpression\_objectAllValuesFrom) \cup \{(aObjectAllValuesFrom \mapsto aClassExpression)\}
  END;
  xOwl\_UnsetAxioms(aXOwl) =
           aXOwl \in XOwl
  \mathbf{PRE}
  THEN
      axioms := axioms \Rightarrow \{aXOwl\}
  END;
  {\bf ClassAssertion\_UnsetClassExpression}(aClassAssertion) =
  \mathbf{PRE}
           aClassAssertion \in ClassAssertion
  THEN
     A\_classExpression\_classAssertion
                                                              \{aClassAssertion\}
                                               :=
A\_classExpression\_classAssertion
  END;
  ClassAssertion\_UnsetIndividual(aClassAssertion) =
          aClassAssertion \in ClassAssertion
  THEN
      A\_individual\_classAssertion := \{aClassAssertion\} \prec A\_individual\_classAssertion\}
  END;
  ClassExpression\_UnsetClass(aClassExpression) =
  \mathbf{PRE}
           aClassExpression \in ClassExpression
  THEN
      classOfClassExp := \{aClassExpression\} \lhd classOfClassExp
  END;
  ClassAxiom\_UnsetAxiomAnnotations(aClassAxiom) =
  PRE
           aClassAxiom \in ClassAxiom
      axiomAnnotations := axiomAnnotations \Rightarrow \{aClassAxiom\}
  END;
  EquivalentClasses\_UnsetClassExpressions(aEquivalentClasses) =
  PRE
           aEquivalentClasses \in EquivalentClasses
  THEN
      A\_classExpressions\_equivalentClasses := A\_classExpressions\_equivalentClasses
\{aEquivalentClasses\}
  END;
  DisjointUnion\_UnsetClass(aDisjointUnion) =
  \mathbf{PRE}
           aDisjointUnion \in DisjointUnion
```

```
A\_class\_disjointUnion := \{aDisjointUnion\} \triangleleft A\_class\_disjointUnion\}
  END;
  DisjointUnion\_UnsetDisjointClassExpressions(aDisjointUnion) =
           aDisjointUnion \in DisjointUnion
  THEN
      A\_disjointClassExpressions\_disjointUnion := A\_disjointClassExpressions\_disjointUnion
\Rightarrow \{aDisjointUnion\}
   END;
  Declaration_UnsetEntity(aDeclaration) =
           aDeclaration \in Declaration
  \mathbf{PRE}
  THEN
      A\_entity\_declaration := \{aDeclaration\} \prec A\_entity\_declaration
  END;
  ObjectComplementOf\_UnsetClassExpression(aObjectComplementOf) =
           aObjectComplementOf \in ObjectComplementOf
  \mathbf{PRE}
  THEN
      A\_classExpression\_objectComplementOf
                                                             \{aObjectComplementOf\}
                                                   :=
                                                                                            \triangleleft
A\_classExpression\_objectComplementOf
  END;
  ObjectOneOf\_UnsetIndividuals(aObjectOneOf) =
           aObjectOneOf \in ObjectOneOf
  THEN
      A\_individuals\_objectOneOf := \{aObjectOneOf\} \prec A\_individuals\_objectOneOf\}
  END;
  ObjectHasValue\_UnsetObjectPropertyExpression(aObjectHasValue) =
  PRE
           aObjectHasValue \in ObjectHasValue
  THEN
      A\_objectPropertyExpression\_objectHasValue
                                                                 \{aObjectHasValue\}
                                                        :=
                                                                                            \triangleleft
A\_objectPropertyExpression\_objectHasValue
  END;
  ObjectHasValue\_UnsetIndividual(aObjectHasValue) =
           aObjectHasValue \in ObjectHasValue
  THEN
      A\_individual\_objectHasValue := \{aObjectHasValue\} \prec A\_individual\_objectHasValue\}
  END;
  \mathbf{ObjectPropertyExpression\_UnsetObjectProperty}(aObjectPropertyExpression) =
           aObjectPropertyExpression \in ObjectPropertyExpression
  PRE
  THEN
                                                           \{aObjectPropertyExpression\}
      A\_objectProperty\_objectPropertyExpression
                                                                                            \triangleleft
```

 $A\_objectProperty\_objectPropertyExpression$ 

```
END;
  ObjectSomeValuesFrom\_UnsetObjectPropertyExpression(aObjectSomeValuesFrom)
  \mathbf{PRE}
          aObjectSomeValuesFrom \in ObjectSomeValuesFrom
  THEN
     A\_objectPropertyExpression\_objectSomeValuesFrom
  END;
  {f ObjectSomeValuesFrom\_UnsetClassExpression}(aObjectSomeValuesFrom) =
          aObjectSomeValuesFrom \in ObjectSomeValuesFrom
  THEN
                                                       \{aObjectSomeValuesFrom\}
     A\_classExpression\_objectSomeValuesFrom
                                               :=
                                                                                    \triangleleft
A\_classExpression\_objectSomeValuesFrom
  END;
  ObjectAllValuesFrom\_UnsetObjectPropertyExpression(aObjectAllValuesFrom) =
          aObjectAllValuesFrom \in ObjectAllValuesFrom
  THEN
     A\_objectPropertyExpression\_objectAllValuesFrom
                                                           { aObjectAllValuesFrom}
                                                    :=
A\_objectPropertyExpression\_objectAllValuesFrom
  END;
  ObjectAllValuesFrom\_UnsetClassExpression(aObjectAllValuesFrom) =
          aObjectAllValuesFrom \in ObjectAllValuesFrom
  THEN
     A\_classExpression\_objectAllValuesFrom
                                               :=
                                                        { aObjectAllValuesFrom}
                                                                                    \triangleleft
A\_classExpression\_objectAllValuesFrom
  END;
  xOwl\_AddAxioms(aXOwl,aAxioms) =
          aXOwl \in XOwl \land
  PRE
     aAxioms \in Axiom \land
     (aAxioms \mapsto aXOwl) \not\in axioms \land
     axioms[\{aAxioms\}] = \emptyset
  THEN
     axioms := axioms \cup \{(aAxioms \mapsto aXOwl)\}
  END;
  ClassAxiom\_AddAxiomAnnotations(aClassAxiom,aAxiomAnnotations) =
  PRE
          aClassAxiom \in ClassAxiom \land
     aAxiomAnnotations \in Annotation \land
     (aAxiomAnnotations \mapsto aClassAxiom) \not\in axiomAnnotations \land
     axiomAnnotations[\{aAxiomAnnotations\}] = \emptyset
  THEN
```

 $axiomAnnotations := axiomAnnotations \cup \{(aAxiomAnnotations \mapsto aClassAxiom)\}$ 

```
Equivalent Classes_AddClassExpressions (aEquivalent Classes, aClassExpressions) =
                            aEquivalentClasses \in EquivalentClasses \land
               aClassExpressions \in ClassExpression \land
               (aClassExpressions \mapsto aEquivalentClasses) \not\in A\_classExpressions\_equivalentClasses \land
               A\_classExpressions\_equivalentClasses[\{aClassExpressions\}] = \emptyset
       THEN
               A\_classExpressions\_equivalentClasses
                                                                                                                                A\_classExpressions\_equivalentClasses
                                                                                                                  :=
                                                                                                                                                                                                                                    \bigcup
\{(aClassExpressions \mapsto aEquivalentClasses)\}
       END;
       {f Disjoint Union\_Add Disjoint Class Expressions}(aDisjoint Union,aDisjoint Class Expressions)
      PRE
                            aDisjointUnion \in DisjointUnion \land
               aDisjointClassExpressions \in ClassExpression \land
               (aDisjointClassExpressions \mapsto aDisjointUnion) \not\in A\_disjointClassExpressions\_disjointUnion
Λ
               A\_disjointClassExpressions\_disjointUnion[\{aDisjointClassExpressions\}] = \emptyset
       THEN
               A\_disjointClassExpressions\_disjointUnion := A\_disjointClassExpressions\_disjointUnion
\cup \{(aDisjointClassExpressions \mapsto aDisjointUnion)\}
       END;
      DisjointClasses\_AddClassExpressions(aDisjointClasses,aClassExpressions) =
                            aDisjointClasses \in DisjointClasses \land
               aClassExpressions \in ClassExpression \land
               (aClassExpressions \mapsto aDisjointClasses) \notin disjointClassExp \land
               disjointClassExp[\{aClassExpressions\}] = \emptyset
       THEN
               disjointClassExp := disjointClassExp \cup \{(aClassExpressions \mapsto aDisjointClasses)\}
      END;
       ObjectOneOf\_AddIndividuals(aObjectOneOf,aIndividuals) =
                            aObjectOneOf \in ObjectOneOf \land
               aIndividuals \in Individual \land
               (aObjectOneOf \mapsto aIndividuals) \notin A\_individuals\_objectOneOf
               A\_individuals\_objectOneOf := A\_individuals\_objectOneOf \cup \{(aObjectOneOf \mapsto aIndividuals\_objectOneOf \mapsto
uals)
       END;
      xOwl\_RemoveAxioms(aXOwl,aAxioms) =
                            aXOwl \in XOwl \land
               aAxioms \in Axiom \land
               (aAxioms \mapsto aXOwl) \in axioms
       THEN
               axioms := axioms - \{(aAxioms \mapsto aXOwl)\}
```

END;

```
END;
  ClassAssertion\_RemoveClassExpression(aClassAssertion, aClassExpression) =
           aClassAssertion \in ClassAssertion \land
      aClassExpression \in ClassExpression \land
      (aClassAssertion \mapsto aClassExpression) \in A\_classExpression\_classAssertion
  THEN
      A\_classExpression\_classAssertion
                                                        A\_classExpression\_classAssertion
                                               :=
\{(aClassAssertion \mapsto aClassExpression)\}
  END;
   ClassAssertion\_RemoveIndividual(aClassAssertion,aIndividual) =
  PRE
           aClassAssertion \in ClassAssertion \land
      aIndividual \in Individual \land
      (aClassAssertion \mapsto aIndividual) \in A\_individual\_classAssertion
  THEN
      A\_individual\_classAssertion := A\_individual\_classAssertion - \{(aClassAssertion \mapsto aIn-
dividual)
  END;
   ClassExpression\_RemoveClass(aClassExpression, aClass) =
           aClassExpression \in ClassExpression \land
      aClass \in Class \land
      (aClassExpression \mapsto aClass) \in classOfClassExp
  THEN
      classOfClassExp := classOfClassExp - \{(aClassExpression \mapsto aClass)\}
  END;
  ClassAxiom\_RemoveAxiomAnnotations(aClassAxiom,aAxiomAnnotations) =
           aClassAxiom \in ClassAxiom \land
      aAxiomAnnotations \in Annotation \land
      (aAxiomAnnotations \mapsto aClassAxiom) \in axiomAnnotations
      axiomAnnotations := axiomAnnotations - \{(aAxiomAnnotations \mapsto aClassAxiom)\}
  END;
  \textbf{EquivalentClasses\_RemoveClassExpressions} (\textit{aEquivalentClasses}, \textit{aClassExpressions}) = \\
           aEquivalentClasses \in EquivalentClasses \land
      aClassExpressions \in ClassExpression \land
      (aClassExpressions \mapsto aEquivalentClasses) \in A\_classExpressions\_equivalentClasses
  THEN
      A\_classExpressions\_equivalentClasses
                                                      A\_classExpressions\_equivalentClasses
                                                :=
\{(aClassExpressions \mapsto aEquivalentClasses)\}
  END;
  DisjointUnion\_RemoveClass(aDisjointUnion, aClass) =
  \mathbf{PRE}
           aDisjointUnion \in DisjointUnion \land
      aClass \in Class \land
      (aDisjointUnion \mapsto aClass) \in A\_class\_disjointUnion
```

```
THEN
      A\_class\_disjointUnion := A\_class\_disjointUnion - \{(aDisjointUnion \mapsto aClass)\}
   END;
  {f Disjoint Union\_Remove Disjoint Class Expressions}(aDisjoint Union, aDisjoint Class Expressions)
  PRE
            aDisjointUnion \in DisjointUnion \land
      aDisjointClassExpressions \in ClassExpression \land
      (aDisjointClassExpressions \mapsto aDisjointUnion) \in A\_disjointClassExpressions\_disjointUnion
   THEN
      A\_disjointClassExpressions\_disjointUnion := A\_disjointClassExpressions\_disjointUnion -
\{(aDisjointClassExpressions \mapsto aDisjointUnion)\}
   END;
  DisjointClasses\_RemoveClassExpressions(aDisjointClasses,aClassExpressions) =
            aDisjointClasses \in DisjointClasses \land
      aClassExpressions \in ClassExpression \land
      (aClassExpressions \mapsto aDisjointClasses) \in disjointClassExp \land
      \operatorname{card}(\operatorname{disjoint} \operatorname{Class} \operatorname{Exp}^{-1} [\{\operatorname{aDisjoint} \operatorname{Classes}\}]) \geq 3
   THEN
      disjointClassExp := disjointClassExp - \{(aClassExpressions \mapsto aDisjointClasses)\}
   END;
  \mathbf{Declaration\_RemoveEntity}(aDeclaration, aEntity) =
            aDeclaration \in Declaration \land
      aEntity \in Entity \land
      (aDeclaration \mapsto aEntity) \in A\_entity\_declaration
      A\_entity\_declaration := A\_entity\_declaration - \{(aDeclaration \mapsto aEntity)\}
  END;
   ObjectComplementOf\_RemoveClassExpression(aObjectComplementOf,aClassExpression)
  PRE
            aObjectComplementOf \in ObjectComplementOf \land
      aClassExpression \in ClassExpression \land
      (aObjectComplementOf \mapsto aClassExpression) \in A\_classExpression\_objectComplementOf
      A\_classExpression\_objectComplementOf := A\_classExpression\_objectComplementOf -
\{(aObjectComplementOf \mapsto aClassExpression)\}
   END;
   \mathbf{ObjectOneOf\_RemoveIndividuals}(aObjectOneOf,aIndividuals) =
            aObjectOneOf \in ObjectOneOf \land
      aIndividuals \in Individual \land
      (aObjectOneOf \mapsto aIndividuals) \in A\_individuals\_objectOneOf
   THEN
      A\_individuals\_objectOneOf := A\_individuals\_objectOneOf - \{(aObjectOneOf \mapsto aIndividuals\_objectOneOf \mapsto aIndividuals\_objectOneOf \}
```

uals)

```
END;
              {\bf Object Has Value\_Remove Object Property Expression} (a Object Has Value, a Object Property Expression) (a Object Has Value, a Object Has Value, a Object Property Expression) (a Object Has Value, a Object Has
                                                           aObjectHasValue \in ObjectHasValue \land
              PRE
                               aObjectPropertyExpression \in ObjectPropertyExpression \land
                               (aObjectHasValue \mapsto aObjectPropertyExpression) \in A\_objectPropertyExpression\_objectHasValue
              THEN
                              A\_objectPropertyExpression\_objectHasValue := A\_objectPropertyExpression\_objectHasValue
- \{(aObjectHasValue \mapsto aObjectPropertyExpression)\}
              END;
              \mathbf{ObjectHasValue\_RemoveIndividual}(\mathit{aObjectHasValue}, \mathit{aIndividual}) =
                                                           aObjectHasValue \in ObjectHasValue \land
                               aIndividual \in Individual \land
                               (aObjectHasValue \mapsto aIndividual) \in A\_individual\_objectHasValue
              THEN
                               A\_individual\_objectHasValue := A\_individual\_objectHasValue - \{(aObjectHasValue \mapsto
aIndividual)}
             END;
               {f Object Property Expression\_Remove Object Property} (a Object Property Expression\_a Object Propert
             \mathbf{PRE}
                                                           aObjectPropertyExpression \in ObjectPropertyExpression \land
                               aObjectProperty \in ObjectProperty \land
                               (aObjectPropertyExpression \mapsto aObjectProperty) \in A\_objectProperty\_objectPropertyExpression
                               A\_objectProperty\_objectPropertyExpression := A\_objectProperty\_objectPropertyExpression
- \{(aObjectPropertyExpression \mapsto aObjectProperty)\}
              END;
               {\bf ObjectSome Values From\_Remove Object Property Expression} (\textit{aObjectSome Values From}, \textit{aObject Property Expression}) (\textit{aObjectSome Values From}, \textit{aObject Property Expression}) (\textit{aObject Some Values From}, \textit{aObject Some}, \textit{aObject Some}, \textit{aObject Some}, \textit{aObject Some}, \textit{aObject So
                                                           aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
                               aObjectPropertyExpression \in ObjectPropertyExpression \land
                               (aObjectSome\ ValuesFrom
                                                                                                                                                                                                                                                                                          aObjectPropertyExpression)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 \in
A\_objectPropertyExpression\_objectSomeValuesFrom
                               A\_objectPropertyExpression\_objectSomeValuesFrom := A\_objectPropertyExpression\_objectFrom := A\_objectPropertyExpression\_objectFrom := A\_objectPropertyExpression\_objectFrom := A\_objectFrom :
- \{(aObjectSomeValuesFrom \mapsto aObjectPropertyExpression)\}
              END;
               {f ObjectSomeValuesFrom\_RemoveClassExpression} (aObjectSomeValuesFrom, aClassExpression)
                                                           aObjectSomeValuesFrom \in ObjectSomeValuesFrom \land
              PRE
                               aClassExpression \in ClassExpression \land
                               (aObjectSome\ ValuesFrom \mapsto aClassExpression) \in A\_classExpression\_objectSome\ ValuesFrom
              THEN
```

 $A\_classExpression\_objectSomeValuesFrom := A\_classExpression\_objectSomeValuesFrom$ 

```
- \{(aObjectSomeValuesFrom \mapsto aClassExpression)\}
           END;
          {\bf ObjectAll Values From\_Remove Object Property Expression} (a Object All Values From\_a Object Property Expression) (a Object
                                         aObjectAllValuesFrom \in ObjectAllValuesFrom \land
          PRE
                      aObjectPropertyExpression \in ObjectPropertyExpression \land
                      (aObjectAllValuesFrom
                                                                                                                                                \mapsto
                                                                                                                                                                                                 aObjectPropertyExpression)
                                                                                                                                                                                                                                                                                                                                                \in
A\_objectPropertyExpression\_objectAllValuesFrom
          THEN
                      A\_objectPropertyExpression\_objectAllValuesFrom := A\_objectAllValuesFrom := A\_objectAllValuesFr
- \{(aObjectAllValuesFrom \mapsto aObjectPropertyExpression)\}
          END;
          {\bf ObjectAllValuesFrom\_RemoveClassExpression} (a ObjectAllValuesFrom\_a ClassExpression)
                                         aObjectAllValuesFrom \in ObjectAllValuesFrom \land
          PRE
                      aClassExpression \in ClassExpression \land
                      (aObjectAllValuesFrom \mapsto aClassExpression) \in A\_classExpression\_objectAllValuesFrom
          THEN
                      A\_classExpression\_objectAllValuesFrom := A\_classExpression\_objectAllValuesFrom -
\{(aObjectAllValuesFrom \mapsto aClassExpression)\}
          END;
          result \leftarrow \mathbf{xOwl\_GetOntologyIRI}(aXOwl) =
                                         aXOwl \in XOwl \land
                      aXOwl \in \mathbf{dom}(xOwl\_ontologyIRI)
          THEN
                      result := xOwl\_ontologyIRI(aXOwl)
          END;
          result \leftarrow \mathbf{xOwl\_GetVersionIRI}(aXOwl) =
                                         aXOwl \in XOwl \land
                      aXOwl \in \mathbf{dom}(xOwl\_versionIRI)
          THEN
                      result := xOwl\_versionIRI(aXOwl)
          END;
          result \leftarrow \mathbf{Entity\_GetName}(aEntity) =
                                         aEntity \in Entity \land
                      aEntity \in \mathbf{dom}(Entity\_name)
          THEN
                      result := Entity\_name(aEntity)
          END;
          result \leftarrow \mathbf{Annotation\_GetAnnotationValue}(aAnnotation) =
                                         aAnnotation \in Annotation \land
                      aAnnotation \in \mathbf{dom}(Annotation\_annotationValue)
```

```
THEN
     result := Annotation\_annotationValue(aAnnotation)
  END;
  xOwl\_SetOntologyIRI(aXOwl,aOntologyIRI) =
  PRE aXOwl \in XOwl \land
      aOntologyIRI \in STRING
  THEN
     xOwl\_ontologyIRI := (\{aXOwl\} \lessdot xOwl\_ontologyIRI) \cup \{(aXOwl \mapsto aOntologyIRI)\}
  END;
  xOwl\_SetVersionIRI(aXOwl,aVersionIRI) =
  PRE aXOwl \in XOwl \land
     aVersionIRI \in STRING
     xOwl\_versionIRI := (\{aXOwl\} \triangleleft xOwl\_versionIRI) \cup \{(aXOwl \mapsto aVersionIRI)\}
  END;
  Entity\_SetName(aEntity,aName) =
           aEntity \in Entity \land
  \mathbf{PRE}
     aName \in STRING
  THEN
     Entity\_name := (\{aEntity\} \triangleleft Entity\_name) \cup \{(aEntity \mapsto aName)\}
  END;
  Annotation\_SetAnnotationValue(aAnnotation, aAnnotationValue) =
           aAnnotation \in Annotation \land
      aAnnotationValue \in STRING
  THEN
      Annotation\_annotationValue := (\{aAnnotation\} \triangleleft Annotation\_annotationValue) \cup
\{(aAnnotation \mapsto aAnnotation Value)\}
  END;
  xOwl\_UnsetOntologyIRI(aXOwl) =
  PRE aXOwl \in XOwl
  THEN
     xOwl\_ontologyIRI := \{aXOwl\} \lessdot xOwl\_ontologyIRI
  END;
  xOwl\_UnsetVersionIRI(aXOwl) =
  PRE aXOwl \in XOwl
  THEN
     xOwl\_versionIRI := \{aXOwl\} \lessdot xOwl\_versionIRI
  END;
  Entity\_UnsetName(aEntity) =
  \mathbf{PRE}
           aEntity \in Entity
```

```
THEN
      Entity\_name := \{aEntity\} \lessdot Entity\_name
  END;
   Annotation\_UnsetAnnotationValue(aAnnotation) =
           aAnnotation \in Annotation
   THEN
      Annotation\_annotationValue := \{aAnnotation\} \prec Annotation\_annotationValue\}
  END;
  xOwl\_RemoveOntologyIRI(aXOwl,aOntologyIRI) =
           aXOwl \in XOwl \land
      aOntologyIRI \in STRING \land
      \{(aXOwl \mapsto aOntologyIRI)\} \subseteq xOwl\_ontologyIRI
      xOwl\_ontologyIRI := xOwl\_ontologyIRI - \{(aXOwl \mapsto aOntologyIRI)\}
  END;
  xOwl\_RemoveVersionIRI(aXOwl, aVersionIRI) =
           aXOwl \in XOwl \land
  \mathbf{PRE}
      aVersionIRI \in STRING \land
      \{(aXOwl \mapsto aVersionIRI)\} \subseteq xOwl\_versionIRI
  THEN
      xOwl\_versionIRI := xOwl\_versionIRI - \{(aXOwl \mapsto aVersionIRI)\}
  END;
  Entity\_RemoveName(aEntity,aName) =
           aEntity \in Entity \land
      aName \in STRING \land
      \{(aEntity \mapsto aName)\} \subseteq Entity\_name
   THEN
      Entity\_name := Entity\_name - \{(aEntity \mapsto aName)\}
   END;
   Annotation\_RemoveAnnotationValue(aAnnotation, aAnnotationValue) =
           aAnnotation \in Annotation \land
      aAnnotationValue \in STRING \land
      \{(aAnnotation \mapsto aAnnotation Value)\} \subseteq Annotation\_annotation Value
      Annotation\_annotationValue := Annotation\_annotationValue - \{(aAnnotation \mapsto aAnno-annotationValue)\}
tation Value)}
   END
END
```