

## Session 16: Assignment 1

### Problem Statement 1:

A test is conducted which is consisting of 20 MCQs (multiple choices questions) with every MCQ having its four options out of which only one is correct. Determine the probability that a person undertaking that test has answered exactly 5 questions wrong.

### Solution:

Formula to calculate k successes in n trials =  $C(n, k) s^k (1-s)^{(n-k)}$

Here,  $n = 20$ ,  $n - k = 5$ ,  $k = 20 - 5 = 15$

Here the probability of success = probability of giving a right answer =  $s = 1/4$

Hence, the probability of failure =  $1 - 1/4 = 3/4$

So,  $P$  (exactly 5 out of 20 answers incorrect) =  $C(20, 5) (1/4)^5 (3/4)^{15}$

→→→  $P$  (5 out of 20) =

$(20 \times 19 \times 18 \times 17 \times 16) (5 \times 4 \times 3 \times 2 \times 1) (20 \times 19 \times 18 \times 17 \times 16) (5 \times 4 \times 3 \times 2 \times 1) (1/4)^5 (3/4)^{15}$

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**= 0.000034 (approximately)**

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### Problem Statement 2:

A die marked A to E is rolled 50 times. Find the probability of getting a "D" exactly 5 times.

### Solution:

Here,  $n = 50$ ,  $k = 5$ ,  $n - k = 45$ .

The probability of success = probability of getting a "D" =  $s = 1/5$

Hence, the probability of failure = probability of not getting a "D" =  $1 - s = 4/5$ .

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**Problem Statement 3:**

Two balls are drawn at random in succession without replacement from an urn containing 4 red balls and 6 black balls. Find the probabilities of all the possible outcomes.

**Solution:**

First determine the probabilities of the events.

| Table of Probability of events |                      |
|--------------------------------|----------------------|
| Events                         | Probability          |
| RR                             | $(4/10)(3/9) = 2/15$ |
| RB                             | $(4/10)(6/9) = 4/15$ |
| BR                             | $(6/10)(4/9) = 4/15$ |
| BB                             | $(6/10)(5/9) = 1/3$  |

The probability of 0 black balls (RR) is  $2/15$

The probability of 1 black ball is (RB or BR) is  $4/15 + 4/15 = 8/15$

The probability of 2 black balls (BB) is  $1/3$

**If Z is the random variable representing the number black balls. The probability distribution will be :**

| Z | p(Z)   |
|---|--------|
| 0 | $2/15$ |
| 1 | $8/15$ |
| 2 | $1/3$  |

**Notice that the sum of the probabilities =  $2/15 + 8/15 + 1/3 = 1$**

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