

Data set - 12 test scores (out of 100)

85, 92, 76, 88, 90, 95, 68, 82, 91, 87, 78, 94

1) Mean (Average)

$$\text{Mean} = \frac{\text{Sum of all scores}}{\text{number of scores.}}$$

$$= \frac{85 + 92 + 76 + 88 + 90 + 95 + 68 + 82 + 91 + 87 + 78 + 94}{12}$$

$$= \frac{1026}{12} = 85.5$$

$$\text{Mean} = 85.5$$

2) Median (middle value)

Step 1: Sort in ascending order

68, 76, 78, 82, 85, 87, 88, 90, 91, 92, 94, 95

Step 2: middle value.

Median = avg of 6th and 7th numbers

$$6^{\text{th}} = 87, 7^{\text{th}} = 88$$

$$\text{Median} = \frac{87 + 88}{2} = \frac{175}{2} = 87.5$$

$$\text{Median} = 87.5$$

3. Variance

$$s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1}$$

Step 1: Find deviations from mean (85.5)

Score x_i	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
68	$68 - 85.5 = -17.5$	306.25
76	-9.5	90.25
78	-7.5	56.25
82	-3.5	12.25
85	-0.5	0.25
87	1.5	2.25
88	2.5	6.25
90	4.5	20.25
91	5.5	30.25
92	6.5	42.25
94	8.5	72.25
95	9.5	90.25
Total		729

$$\text{Variance} = \frac{729}{12-1} = \frac{729}{11} \approx 66.27$$

$$\text{Variance} = 66.27$$

4. Standard Deviation

$$SD = \sqrt{\text{Variance}} = \sqrt{66.27} \simeq 8.14$$

$$SD = 8.14$$

5. probability of a score > 90

Step 1 : count scores $> 90 \Rightarrow 4$ scores

$$P(x > 90) = \frac{4}{12} = \frac{1}{3} \simeq 0.333$$

Probability $\simeq 0.33$ (33 %)