DSP Midterm Exam

Monday, May 24, 2021

Question 1: T or F, Multiple Choice, and Short Answer
(Estimated time: 5-10 minutes)

1. **T** or **F**: The time index n for DT signals usually has units of seconds.

2. **T** or **F**: DT signals are typically plotted as a series of lollipops.

3. **T** or **F**: A DT frequency of π is considered a high frequency.

4. **T** or **F**: A DT frequency of 2π is considered a low frequency.

5. **T** or **F**: The DTFT of a DT signal is periodic with a period of 2π.

6. The DTFT of a rectangle is a:
   (a) Sine wave
   (b) Periodic sinc
   (c) Rectangle
   (d) None of the above

7. The DTFT of a single impulse is:
   (a) A single impulse
   (b) A constant
   (c) Infinite
   (d) None of the above

8. A DT signal is given as follows:
$$x(n) = \big(3\delta(n) - 5\delta(n-1) + 3\delta(n-2)\big)u(n+1)$$
   The value of $x(n)$ at $n = 3$ is:
   (a) 0
   (b) 0.25
   (c) 0.5
   (d) 1
   (e) None of the above

9. A DT signal $x(n)$ is given as follows:

$$x(n) = 101$$

The length of $x(n)$ is:

(a) 0

(b) 1

(c) 101

(d) ∞

(e) None of the above

10. A DT signal $x(n)$ is given as follows:

$$x(n) = \text{rect}_5(n)$$

We want to create a new signal $y(n)$ that is identical to $x(n)$ but is centered about $n = 0$ (i.e., we want a rectangle that is symmetric about time zero). To create $y(n)$, we should use:

(a) $y(n) = x(2n)$

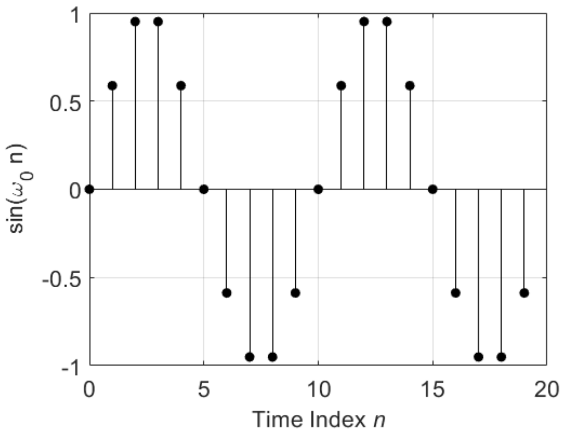
(b) $y(n) = x(n + 2)$

(c) $y(n) = x(n - 2)$

(d) $y(n) = x(n + 2) + x(n - 2)$

(e) None of the above

11. Two cycles of a DT sine wave $\sin(\omega_0 n)$ are shown in the following plot:



The value of ω_0 is:

(a) $1/5$

(b) $\pi/5$

(c) 5

(d) 5π

(e) None of the above

12. Two DT signals, $x_1(n)$ and $x_2(n)$, are given as follows:

$$x_1(n) = \delta(n+1) + \delta(n-1)$$

$$x_2(n) = \delta(n) - \delta(n-1)$$

In the space provided below, sketch the convolution of these two signals. You must show your work to receive credit.

13. A DT signal $x(n)$ is given as follows:

$$x(n) = \delta(n+2) + 2\delta(n) + \delta(n-2)$$

Which of the following is the DTFT $X\left(e^{j\omega}\right)$ of this signal?

(a) $e^{j2\omega} + 2 + e^{-j2\omega}$

(b) $2e^{j\omega} + 2 + 2e^{-j\omega}$

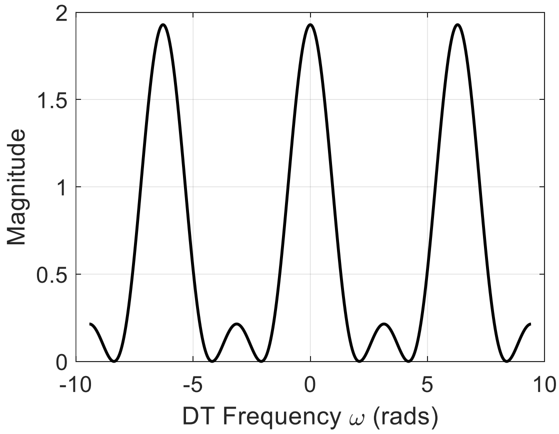
(c) $\delta(2\omega) + 2\delta(\omega) + \delta(-2\omega)$

(d) $2\delta(\omega) + \delta(2\omega) - 2\delta(\omega)$

(e) None of the above

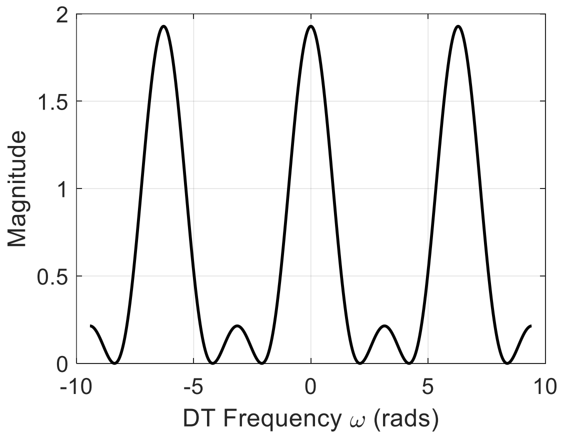
14. In simple terms, describe the key difference between the DTFT of $\mathrm{rect}_3(n)$ and the DTFT of $\mathrm{rect}_3(n+1)$:

15. A DT signal $x(n)$ has a magnitude spectrum as shown below (showing the range -3π to $+3\pi$):

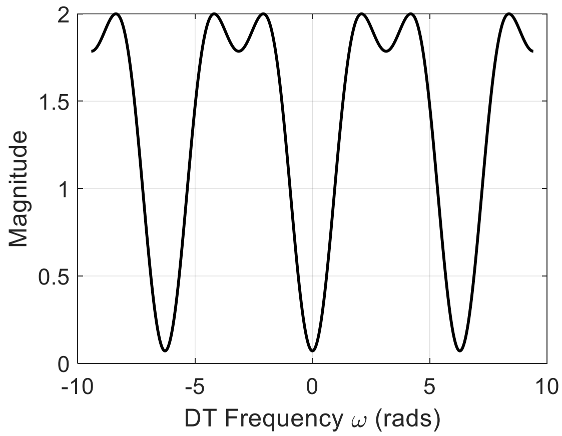


The magnitude spectrum of $x(n-2)$ would look like:

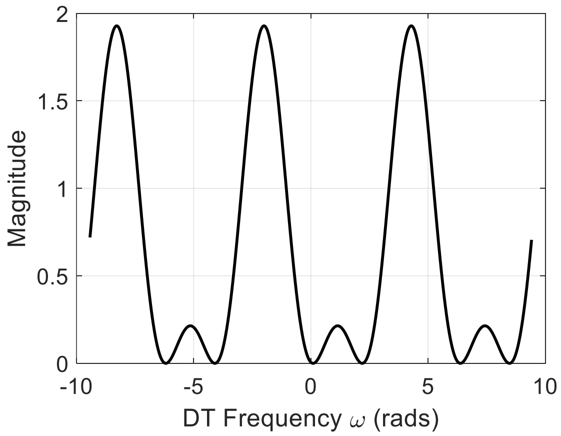
(a)



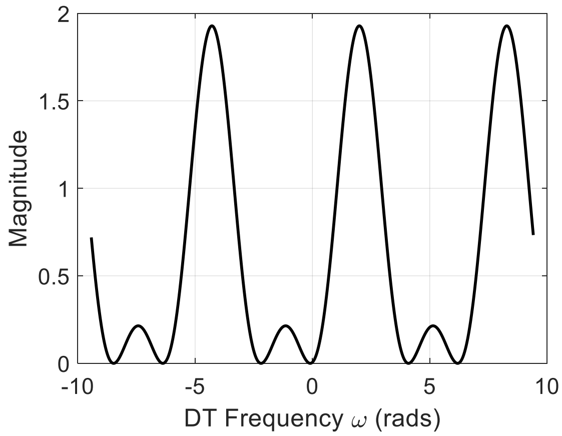
(b)



(c)

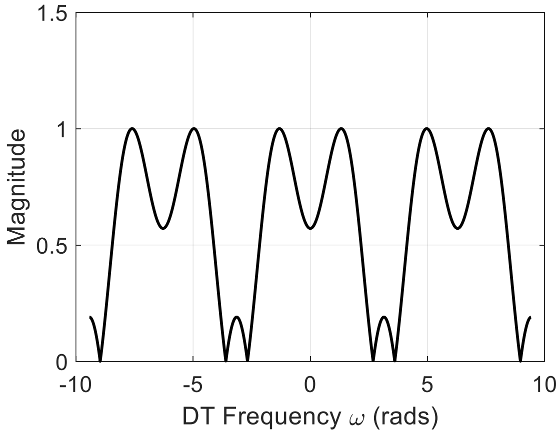


(d)



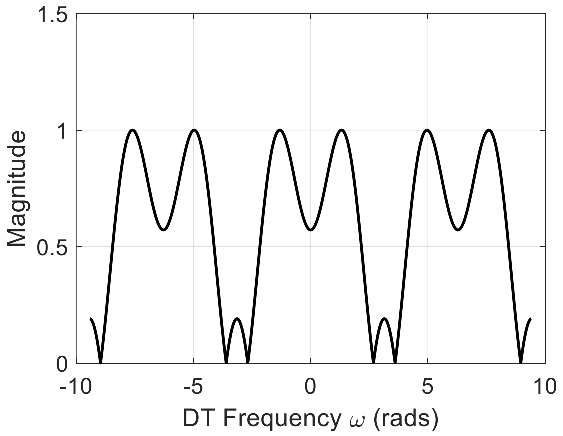
(e) None of the above

16. A DT signal $x(n)$ has a magnitude spectrum as shown below (showing the range -3π to $+3\pi$):

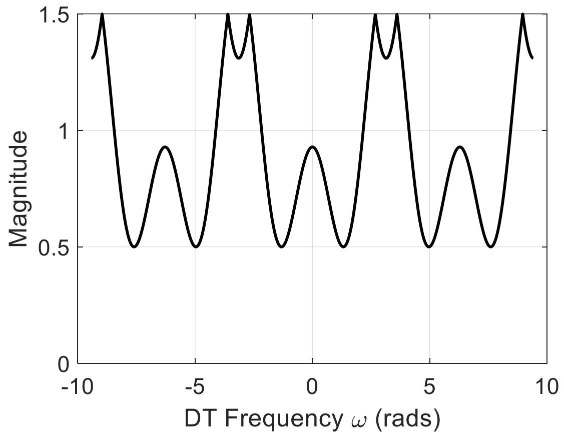


The magnitude spectrum of $-1.5x(n)$ would look like:

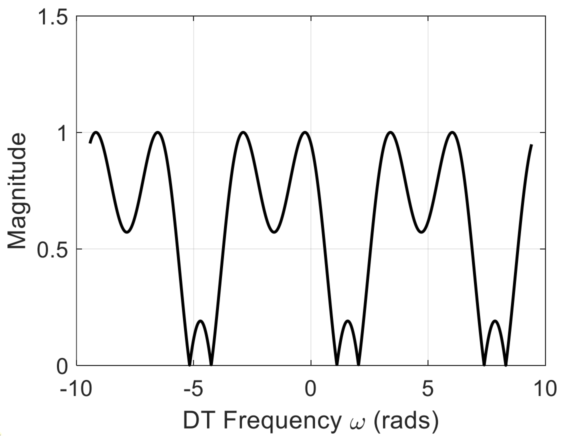
(a)



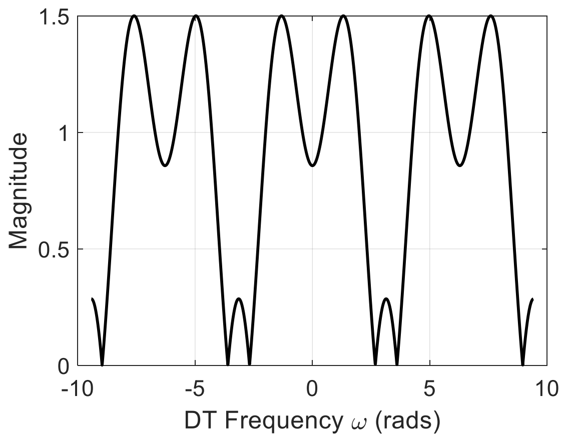
(b)



(c)

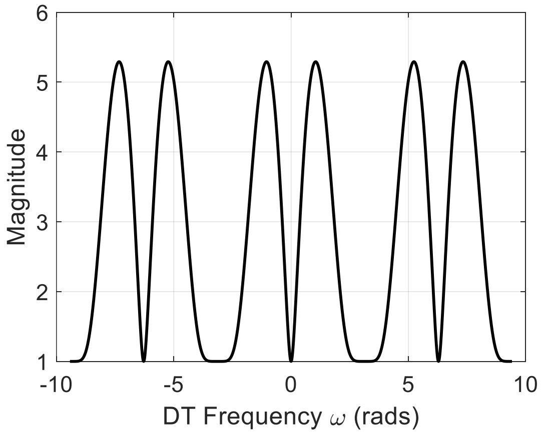


(d)



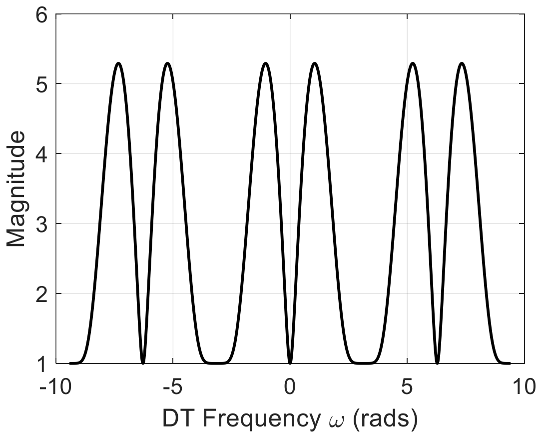
(e) None of the above

17. A DT signal $x(n)$ has a magnitude spectrum as shown below (showing the range -3π to $+3\pi$):

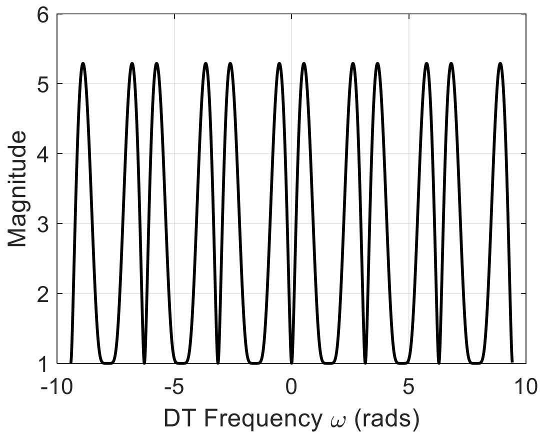


The magnitude spectrum of $\cos(\pi n)\, x(n)$ would look like:

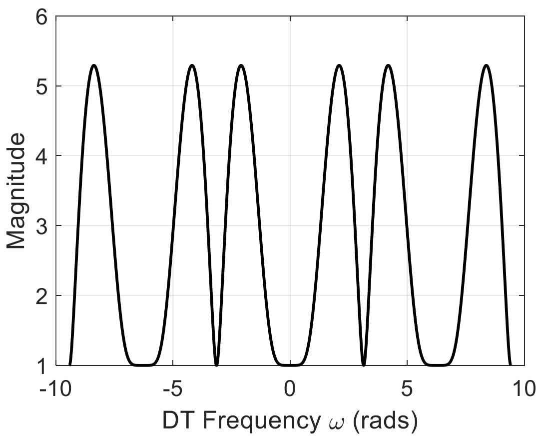
(a)



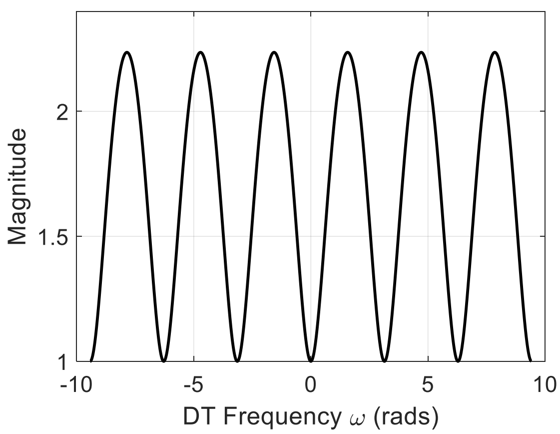
(b)



(c)



(d)



(e) None of the above