

Exercises in Physics  
Assignment # 3

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P1.

$$v_x = \frac{dx}{dt} = 6t - 4$$

$$v_y = \frac{dy}{dt} = 8t - t^2$$

$$a_x = \frac{dv_x}{dt} = 6$$

$$a_y = \frac{dv_y}{dt} = 8 - 2t$$

$$\begin{aligned} a &= \sqrt{a_x^2 + a_y^2} \\ &= \sqrt{6^2 + (8 - 2 \times 2)^2} \\ &= 2\sqrt{13} \end{aligned}$$

$$\begin{aligned} v &= \sqrt{v_x^2 + v_y^2} \\ &= \sqrt{(6 \times 2)^2 + (8 \times 2 - 2^2)^2} \\ &= \sqrt{(6 \times 2)^2 + (8 \times 2 - 2^2)^2} \\ &= 12\sqrt{2} \end{aligned}$$

P3.

$$\theta = 50^\circ$$

$$t = \frac{x}{v_x^2} = \frac{4}{v_0 \cos 50} = \frac{4}{0.643v_0}$$

$$y = y_0 + y_{0yt} + \frac{1}{2}gt^2$$

$$3 = 2.1 + 0.643v_0 \cdot \frac{4}{0.643v_0} - \frac{1}{2} \times 9.8 \frac{4^2}{0.643v_0^2}$$

$$3 = 6.1 - 4.9 \times \frac{4}{0.643v_0}^2$$

$$\frac{4}{0.643v_0}^2 = \frac{3.1}{4.9}$$

$$\frac{4}{0.643v_0} = \sqrt{\frac{3.1}{4.9}}$$

$$0.643v_0 = 5.03m/s$$

$$v_0 = 7.821m/s$$

P4.

$$v_0 = 30m/s$$

$$2\alpha - \phi = \cos^{-1} \frac{\frac{gx^2}{v_0^2} - h}{\sqrt{h^2 + x^2}}$$

$$\phi = \tan^{-1} \frac{x}{h}$$

$$\phi = \tan^{-1} \frac{110}{24} = 77.69^\circ$$

$$2\alpha - \phi = \cos^{-1} \frac{\frac{9.8 \times 110^2}{30^2} - 110}{\sqrt{24^2 + 110^2}}$$

$$2\alpha - \phi = 78.85^\circ$$

$$2\alpha = 156.54$$

$$\alpha = 78.27^\circ$$