

Finding a derivative

1. $g(x) = (2x^4 + 7)(x - 6)$

$$g'(x) = (2x^4 + 7)(1) + (8x^3)(x - 6)$$

Product Rule

$$uv' + u'v$$

$$\begin{aligned} &= 2x^4 + 7 + 8x^4 - 48x^3 \\ &= 10x^4 - 48x^3 + 7 \end{aligned}$$

2. $f(x) = \frac{3x-4}{x^3-2}$

Quotient Rule

$$= \frac{3(x^3-2) - (3x-4)(3x^2)}{(x^3-2)^2} \quad \frac{u'v - uv'}{v^2}$$

$$= \frac{3x^3 - 6 - 9x^3 + 12x^2}{x^6 - 4x^3 + 4}$$

$$= \frac{-6x^3 + 12x^2 - 6}{x^6 - 4x^3 + 4}$$

$$3. \ y = \frac{\cos x}{x^3}$$

Quotient Rule

$$\frac{u'v - uv'}{v^2}$$

$$y' = \frac{-\sin x (x^3) - \cos x (3x^2)}{(x^3)^2}$$

$$= \frac{-x^3 \sin x - 3x^2 \cos x}{x^6}$$

$$= \frac{x^2 (-x \sin x - 3 \cos x)}{x^6}$$

$$= \frac{-x \sin x - 3 \cos x}{x^4}$$

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