

1x3 Matrix for MEET ME MONDAY

$$u \cdot u = 39$$

$$u \cdot v = -3$$

$$v \cdot v = 79$$

$(u + 2v) \cdot (3u + v)$ distributing

$$3u \cdot u + u \cdot v + 3u \cdot 2v + 2v \cdot v$$

$$39(3) + (-3) + 6(\cancel{u \cdot v}) + 2(79)$$

-3

$$117 - 3 - 18 + 158$$

$$295 - 21$$

$$= 254$$

$$\begin{array}{r} 158 \\ 117 \\ \hline 275 \end{array}$$

$$\begin{array}{r} 275 \\ 21 \\ \hline 254 \end{array}$$

If u and v in W , $u+v$ in W

If u in W , scalar $c \cdot u$ in W

Cryptography

0 = _	14 = N
1 = A	15 = O
2 = B	16 = P
3 = C	17 = Q
4 = D	18 = R
5 = E	19 = S
6 = F	20 = T
7 = G	21 = U
8 = H	22 = V
9 = I	23 = W
10 = J	24 = X
11 = K	25 = Y
12 = L	26 = Z
13 = M	

$$A = \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix}$$

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Encrypt ROSES ARE RED

$$\begin{matrix} R & O & S & E & S & - & A & R & E & - & R & E & D \\ [18 & 15 & 19] & [5 & 19 & 0] & [1 & 18 & 5] & [0 & 18 & 5] & [4 & 0 & 0] \end{matrix}$$

$$[18 \ 15 \ 19] \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = [22 \ -40 \ 5]$$

$$[5 \ 19 \ 0] \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = [-14 \ 9 \ 67]$$

$$[1 \ 18 \ 5] \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = [-12 \ 11 \ 36]$$

$$[0 \ 18 \ 5] \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = [-13 \ 13 \ 34]$$

$$[4 \ 0 \ 0] \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = [4 \ -8 \ 8]$$

REF
0]

$$\begin{bmatrix} 18 & 15 & 19 \end{bmatrix} \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = \begin{bmatrix} 22 & -40 & 5 \end{bmatrix}$$

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$$\begin{bmatrix} 4 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix} = \begin{bmatrix} 4 & -8 & 8 \end{bmatrix}$$

$$\begin{matrix} 22 & -40 & 5 & -14 & 9 & 67 & -12 & 11 & 36 \\ -13 & 13 & 34 & 4 & -8 & 8 \end{matrix}$$

Augmented matrix

$$A = \begin{bmatrix} 1 & -2 & 2 \\ -1 & 1 & 3 \\ 1 & -1 & -4 \end{bmatrix}$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 8 & 1 & 2 & 0 \\ -1 & 1 & 3 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right] \quad -R_1 + R_2 \rightarrow R_2$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 8 & 1 & 2 & 0 \\ 0 & 1 & -5 & -1 & -1 & 0 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right] \quad 5R_3 + R_2 \rightarrow R_2$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 8 & 1 & 2 & 0 \\ 0 & 1 & 0 & -1 & -6 & -5 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right] \quad -8R_3 + R_1 \rightarrow R_1$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 0 & 1 & 10 & 8 \\ 0 & 1 & 0 & -1 & -6 & -5 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right] \quad -R_1 \rightarrow R_1$$

$$\left[\begin{array}{ccc|ccc} 1 & 0 & 0 & -1 & -10 & -8 \\ 0 & 1 & 0 & -1 & -6 & -5 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right]$$

$$\left[\begin{array}{ccc|ccc} 1 & -2 & 2 & 1 & 0 & 0 \\ -1 & 1 & 3 & 0 & 1 & 0 \\ 1 & -1 & -4 & 0 & 0 & 1 \end{array} \right] \quad 2R_2 + R_1 \rightarrow R_1$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 8 & 1 & 2 & 0 \\ -1 & 1 & 3 & 0 & 1 & 0 \\ 1 & -1 & -4 & 0 & 0 & 1 \end{array} \right] \quad \begin{matrix} R_2 + R_3 \rightarrow R_3 \\ -R_3 \rightarrow R_3 \end{matrix}$$

$$\left[\begin{array}{ccc|ccc} -1 & 0 & 8 & 1 & 2 & 0 \\ -1 & 1 & 3 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & -1 & -1 \end{array} \right]$$

22 -40 5 -14 9 67 -12 11 36
-13 13 34 4 -8 8

$$A^{-1} = \begin{bmatrix} -1 & -10 & -8 \\ -1 & -6 & -5 \\ 0 & -1 & -1 \end{bmatrix}$$