

Haskell Study Notes

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1 Types

1.1 Basic types

Haskell has many primitive types such as strings, characters, integers and floating point numbers.

```
1 "hello world" -- string
2 1234          -- integer
3 3.14         -- float
```

1.2 Typeclasses

Typeclasses are a way of sharing specific functionality between types. We can either implement our own instances of typeclasses, or let haskell *derive* them automatically.

They are kind of like Java interfaces.

Num is the generic base typeclass that all numbers derive from.

1. Integral numbers (*Integral* typeclass)

- *Int*: fixed precision integer with a min and maximum size
- *Integer*: supports **very** large integers

2. Floating point numbers (*Fractional* typeclass)

- *Float*: single precision floating point number
- *Double*: double precision floating point number

1.3 More on typeclasses

Anything that derives from

- *Show* can be printed
- *Read* can be read as a value
- *Eq* can be compared for equality with `==` and `/=`
- *Ord* can be compared and ordered with `j` and `j`

```

1 {-# LANGUAGE DuplicateRecordFields #-}
2
3 data Worker = Worker { name :: String, job :: String }
4   deriving (Show)
5
6 data Student = Student { name :: String, school :: String }
7   deriving (Show)
8
9
10 class Person a where
11   getName :: a -> String
12   getOccupation :: a -> String
13
14 instance Person Worker where
15   getName x = name (x :: Worker)
16   getOccupation x = "Working on " ++ job x
17
18 instance Person Student where
19   getName x = name (x :: Student)
20   getOccupation x = "Studying at " ++ school x

```

Figure 1: Demonstration of a custom typeclass for Person

2 Lists and Tuples

2.1 Lists

Haskell lists are represented as linked lists. A node in a linked list can either be *Nil* or a pointer to the *next node*. Lists have a *head* and a *tail*. Because of Haskell being lazily evaluated, lists can be infinite. *take* takes *n* items from a list, and *drop* drops *n* items from a list.

```
list = [1, 2, 3, 4, 5]
```

In the above list, the *head* is 1, and the *tail* is [2, 3, 4, 5]

The *splitAt* function splits a list into two parts at the element specified. Lists can be indexed using the *!!* operator.

2.1.1 List Comprehensions

List comprehensions are similar to how they work in Python. They must have at least one list that is the generator, which provides the input.

```
[ operation | x <- list ]
```

An example of a list comprehension:

```
[ x ^ 2 | x <- [1..10]]
```

2.2 Tuples

Haskell has tuples, triples, and *n-tuples*. Tuples have a *fst* and *snd* function which respectively gets either the first or second item.

swap (defined in **Data.Tuple**) swaps the items in a *tuple*

```
1 ("char", 20)
2
3 -- a triple
4 ("char", 20, "turtles")
```

3 Conditionals

3.1 If expressions

Haskell doesn't have if statements, however it has if expressions instead.

```
1 -- stolen from the haskell book
2 let x = 0
3 if (x + 1 == 1) then "AWESOME" else "wut"
```

3.2 Case expressions

Case expressions are similar to switch-case from languages like Java, and C++. Case expressions begin with `case x of` and their body contains all the different cases in the format *value* \rightarrow *return-value*.

```
1 pal xs =
2   case y of
3     True  -> "yes"
4     False -> "no"
5   where y = xs == reverse xs
```

It can also be used to *pattern match* against data types

```
1 data Animal = Cat | Dog
2 speak a =
3   case a of
4     Cat -> "meow"
5     Dog -> "bork"
```

3.3 Guards

There are also guards which can provide a nicer way of pattern matching instead of writing if-else expressions or case blocks. Guard blocks are written as a series of cases, along with a fallback case called **otherwise**

Cases are written in the format: “| *condition* = *value*.”

```
1 abs n
2   | n < 0      = -n
3   | otherwise = n
```

3.4 Pattern matching

Pattern matching is very common in Haskell. It allows great flexibility since you can pattern match against anything to extract values etc.

_ or *x* means a catch-all/fallback pattern to match on if all else fails

```
1 isItOne :: Int -> Bool
2 isItOne 1 = True
3 isItOne _ = False
```

3.4.1 Matching against data constructors

Pattern matching against data constructors is possible. The example defines two functions called **getName** and **getAccNumber** that pattern match on the *User* data constructor to extract either the name or account number.

```
1 data User = User String Int
2
3 getName :: User -> String
4 getName (User name _) = name
5
6 getAccNumber :: User -> Int
7 getAccNumber (User _ acc) = acc
```

1 2

¹If we don't use a field, we can use an _ just like pattern matching with functions to signify the field is ignored

²Pattern matching against data constructors can get real old if you have a lot of parameters. So an alternative to this that will be covered later is record types.

4 Functions

Functions are defined like `add x y = x + y`. All functions are pure, unless stated otherwise which means they cannot modify state, or perform side effects like input output, writing to a database, etc

4.1 Currying

By default, all functions are curried in Haskell. Given the following type signature

```
1 -- add takes two ints and returns an int
2 add :: Int -> Int -> Int
```

we would say that the function `add` takes two integers, and returns an integer. However, because of how currying works it actually means.

- `add` takes a *single* integer parameter
- and returns a function that takes another integer parameter, and eventually will return an integer itself.

Currying is useful because it means we can create new functions by *partially applying* functions to parameters.

`addOne 5` evaluates to `((add 1) 5)` which is then further reduced to the normal form .

```
1 add :: Int -> (Int -> Int)
2
3 addOne :: Int -> Int
4 addOne x = add 1
5
6 addOne 5
7 ((add 1) 5)
8 6
```

4.2 Higher-order functions

Higher order functions are functions that can accept functions as parameters `flip` is an example of a higher-order function.

Its type signature is `flip :: (a -> b -> c) -> b -> a -> c` and it can be partially applied like so

```
1 flipOne = flip 1
2 partialApply = flipOne 2 -- ((flip 1) 2)
```

4.3 Function composition

Composing functions is like a *right to left* pipeline. **f . g** can be read as **f** after **g**. In Haskell **.** is used since **o** is not a valid ASCII character.

So $(f \circ g) x = f (g x)$

1. first applies g
2. then applies f to the result of applying g
3. and makes a new function which takes a parameter x

Example of function composition in action

```
1 negate . sum $ [1,2,3,4,5]
2
3 -- which is equivalent to
4 negate (sum [1,2,3,4,5])
5 negate (15)
```

3

³ $\$$ is used since function application has the highest precedence, so Haskell will think we mean `negate . 15`. Alternatively, you can wrap it in brackets like `negate . (sum [1,2,3,4,5])`

5 Recursion

5.1 Factorial

A classic way of demonstrating recursion is factorial. $4!$ means $4 * 3 * 2 * 1$. The broken down steps can be seen below.

```
4! = 4 * 3 * 2 * 1
      12 * 2 * 1
          24 * 1
              24
4! = 24
```

The *factorial* function can be defined in Haskell. If there is no base case defined, the recursion will go on forever and will never stop.

```
1 fac :: Integer -> Integer
2 fac 0 = 1 -- base case
3 fac n = n * fac (n - 1)
4
```

5.2 More examples of recursion

Some more examples of recursion from *work/recursion.hs*.

```
1 -- Sums up the elements of a list using recursion
2 sum' [] = 0 -- base case
3 sum' (x:xs) = x + sum' xs
4
5 head' [] = error "empty list"
6 head' (x:xs) = x
7
8 -- Takes n elements from a list
9 take' n _
10 | n <= 0 = [] -- if n is 0, give back an empty list
11 take' n [] = [] -- base case 2
12 take' n (x:xs) = x:take' (n-1) xs -- prepend x to the list
13
14 -- Maps a function over a list
15 map' f [] = [] -- base case, empty list
16 map' f (x:xs) = f x:map' f xs
```

⁴*fac 0 = 1* is the base case since it will return 1, and stop the recursion.

5.3 Fold Styles

foldr folds a list from right to left, whereas *foldl* folds a list from left to right.

foldl stacks parentheses on the left where as *foldr* stacks them on the right
 $((0+1)+2)+3$ vs $(1+(2+(3+0)))$

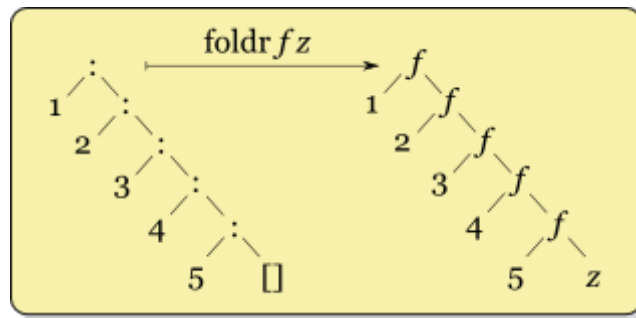


Figure 1: foldr recursion

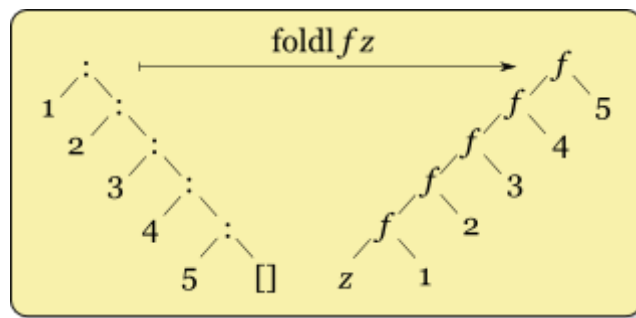


Figure 2: foldl recursion