

MAP4C Mid-Term Exam Review

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1 Algebra

1. Expand and simplify.

$$\begin{aligned} \text{a) } (p-4)(p+5) \\ &= p^2 + 5p - 4p - 20 \\ &= p^2 + p - 20 \end{aligned}$$

$$\begin{aligned} \text{b) } (n+8)(n+2) \\ &= n^2 + 2n + 8n + 16 \\ &= n^2 + 10n + 16 \end{aligned}$$

$$\begin{aligned} \text{c) } (m+3)(m-7) \\ &= m^2 - 7m + 3m - 21 \\ &= m^2 - 4m - 21 \end{aligned}$$

$$\begin{aligned} \text{d) } (w-4)(w-6) \\ &= w^2 - 6w - 4w + 24 \\ &= w^2 - 10w + 24 \end{aligned}$$

$$\begin{aligned} \text{e) } (2x-3)(5x-4) \\ &= 10x^2 - 8x - 15x + 12 \\ &= 10x^2 - 23x + 12 \end{aligned}$$

$$\begin{aligned} \text{f) } (y-5)(2y+9) \\ &= 2y^2 + 9y - 10y - 45 \\ &= 2y^2 - y - 45 \end{aligned}$$

$$\begin{aligned} \text{g) } (3a+1)(4a+1) \\ &= 12a^2 + 3a + 4a + 1 \\ &= 12a^2 + 7a + 1 \end{aligned}$$

$$\begin{aligned} \text{h) } (7-x)(4+x) \\ &= 28 + 7x - 4x - x^2 \\ &= 28 + 3x - x^2 \end{aligned}$$

$$\begin{aligned}
 i) & (x-6)(x+6) \\
 &= x^2 + 6x - 6x - 36 \\
 &= x^2 - 36
 \end{aligned}$$

$$\begin{aligned}
 j) & (x+2)^2 \\
 &= (x+2)(x+2) \\
 &= x^2 + 2x + 2x + 4 \\
 &= x^2 + 4x + 4
 \end{aligned}$$

$$\begin{aligned}
 k) & (y+11)(y-11) \\
 &= y^2 - 11y + 11y - 121 \\
 &= y^2 - 121
 \end{aligned}$$

$$\begin{aligned}
 l) & (z-5)^2 \\
 &= (z-5)(z-5) \\
 &= z^2 - 5z - 5z + 25 \\
 &= z^2 - 10z + 25
 \end{aligned}$$

2. *Expand and simplify.*

$$\begin{aligned}
 a) & 4(x-2)(3x-5) \\
 &= (4x-8)(3x-5) \\
 &= 12x^2 - 20x - 24x + 40 \\
 &= 12x^2 - 44x + 40
 \end{aligned}$$

$$\begin{aligned}
 b) & (4x-3)^2 - 5(3x^2-5x+7) \\
 &= (4x-3)(4x-3) - (15x^2-25x+35) \\
 &= (16x^2-12x-12x+9) - (15x^2-25x+35) \\
 &= 16x^2-24x+9 - 15x^2-25x+35 \\
 &= x^2+x-26
 \end{aligned}$$

3. *Find an expression for the area of each shape.*

$$\begin{aligned}
 a) & (2x-5)(x+1) \\
 &= 2x^2 + 2x - 5x - 5 \\
 &= 2x^2 - 3x - 5
 \end{aligned}$$

$$\begin{aligned}
 b) & (5x)(8x+3) - (3x+1)(4x+4) \\
 &= 40x^2 + 3x - 12x^2 + 12x + 4x + 4 \\
 &= 28x^2 + 16x + 4
 \end{aligned}$$

4. *Factor each of the following completely.*

$$\begin{aligned}
 a) & 18 - 12x \\
 &= 6(3 - 2x)
 \end{aligned}$$

$$b) 21w^2 - 28x + 35$$

$$= 7(3w^2 - 4w + 5)$$

$$\begin{aligned} c) \quad & 24x^2 + 16x \\ &= 8(3x^2 + 2x) \end{aligned}$$

$$\begin{aligned} d) \quad & 15x^3 - 20a^2 + 24a \\ &= 5a(3a^2 - 4a + 5) \end{aligned}$$

$$\begin{aligned} e) \quad & 20m^2 - 30m \\ &= 10m(2m - 3) \end{aligned}$$

$$\begin{aligned} f) \quad & 27k^3 - 36k^5 \\ &= 9k^3(3 - 4k^2) \end{aligned}$$

$$\begin{aligned} g) \quad & n^2 - 144 \\ &= (n - 12)(n + 12) \end{aligned}$$

$$\begin{aligned} h) \quad & (81 - x^2) \\ &= (9 + x)(9 - x) \end{aligned}$$

$$\begin{aligned} i) \quad & 5m^2 - 80 \\ &= 5(m^2 - 16) \end{aligned}$$

$$\begin{aligned} j) \quad & 10x^2 - 90 \\ &= 10(x^2 - 9) \end{aligned}$$

$$\begin{aligned} k) \quad & x^2 + 5x + 6 \\ &= (x + 2)(x + 3) \end{aligned}$$

$$\begin{aligned} l) \quad & a^2 - a - 30 \\ &= (a - 6)(a + 5) \end{aligned}$$

$$\begin{aligned} m) \quad & x^2 + 3x - 10 \\ &= (x + 5)(x - 2) \end{aligned}$$

$$\begin{aligned} n) \quad & m^2 - 9m + 20 \\ &= (m - 5)(m - 4) \end{aligned}$$

$$\begin{aligned} o) \quad & x^2 + 6x - 27 \\ &= (x - 3)(x + 9) \end{aligned}$$

$$\begin{aligned} p) \quad & 3x^2 - 6x - 105 \\ &= 3(x^2 - 2x - 35) \\ &= 3(x - 7)(x + 5) \end{aligned}$$

$$q) \quad 5x^2 + 17x + 6$$

$$= (5x + 2)(x + 3)$$

$$\begin{aligned} r) \quad & 5x^2 - 7x - 6 \\ &= (x - 2)(5x + 3) \end{aligned}$$

$$\begin{aligned} s) \quad & 3n^2 + 10n + 3 \\ &= (3n + 1)(n + 3) \end{aligned}$$

$$t) \quad 2x^2 + 9x + 4$$

5. *Solve each quadratic equation.*

$$\begin{aligned} a) \quad & x^2 - 7x + 10 = 0 \\ &= (x - 5)(x - 2) \end{aligned}$$

$$\begin{aligned} b) \quad & x^2 - x - 12 = 0 \\ &= (x - 4)(x + 3) \end{aligned}$$

$$\begin{aligned} c) \quad & x^2 - 25 = 0 \\ &= (x + 5)(x - 5) \end{aligned}$$

$$\begin{aligned} d) \quad & x^2 - 3x = 10 \\ & x^2 - 3x - 10 = 0 \\ &= (x - 5)(x + 2) \end{aligned}$$

$$\begin{aligned} e) \quad & x^2 + 10x + 25 = 0 \\ &= (x + 5)(x + 5) \end{aligned}$$

$$\begin{aligned} f) \quad & x^2 + 81 = 81x \\ & x^2 + 81 - 81x = 0 \\ &= (x - 9)(x - 9) \end{aligned}$$

2 Budgets

1. The Marcella family spends 250 dollars per week on groceries. How much should they budget monthly for their grocery costs?

- A. 1000 dollars
- B. 1083.33 dollars
- C. 541.67 dollars
- D. 500 dollars

Answer: 250 dollars per week x 52 weeks per year \div 12 *months in a year*
 $= 1083.33$ *dollars (D.)*

2. *Which is not a tenant's responsibility?*

- A. *Pay rent on time.*

B. Give 60 written notice before moving out

C. Pay property tax

D. Repair any damage he or she causes

Answer : D. Repair any damage he/she causes. Tenants are not liable for damage costs, unless it w

3. Explain the difference between fixed and variable costs in relation to renting or owning your own

Fixes expenses :

–Mortgage

–Rent (if applicable)

–Property taxes (if paying monthly)

–House/tenant insurance

–Utility bills

–Lease/car loan payment

–Life/health insurance

Vehicle insurance

Charity monthly donations

Variable costs :

–Groceries

–Personal items

–Fuel public transportation

–Parking

Clothing

Eating out

Entertainment

Alcohol/ tobacco/ gambling

–Miscellaneous

4. Raj is moving to London to attend college. He finds two housing options near campus.

Option 1 : Room in a home shared with three other students. Rent is 350 dollars plus one quarter of

Option 2 : One bedroom basement apartment in a house. Rent is 470 dollars including all utilities. M

a) What would be the annual rent for each option?

Option 1 : 350 dollars a month, plus one quarter of all utilities (undetermined)

Option 2 : 470 dollars a month, including utilities

c) I would recommend option 1. One quarter of the cost of utilities can't be more than 120 dollars, m