1. Evolution of the biodiversity effects over time

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```
package loading
library(here)
## here() starts at /Users/meganedeziel/Documents/GitHub/Lemna_BEF
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
              1.1.2
                        v readr
                                    2.1.4
## v dplyr
## v forcats 1.0.0
                                    1.5.0
                        v stringr
## v ggplot2 3.4.2
                        v tibble
                                    3.2.1
## v lubridate 1.9.2
                                    1.3.0
                        v tidyr
## v purrr
              1.0.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(nlme)
##
## Attaching package: 'nlme'
## The following object is masked from 'package:dplyr':
##
##
       collapse
library(emmeans)
library(ggpubr)
library(grid)
library(car)
## Loading required package: carData
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
      recode
##
## The following object is masked from 'package:purrr':
##
##
       some
```

data importation

128

##

```
#Data on Net effect, CE, SE
NE_data<-read.csv(here("data", "NE_data.csv"), sep=";")</pre>
str(NE_data)
## 'data.frame':
                   132 obs. of 8 variables:
## $ Polyculture: chr "JOB1LmSp" "JOB1LmWc" "JOB1LmLt" "JOB1SpWc" ...
## $ Block
              : int 1 1 1 1 1 1 1 1 1 1 ...
## $ Composition: chr "LmSp" "LmWc" "LmLt" "SpWc" ...
## $ Days
                : int 0000000000...
## $ RYT
                : num 1 1 1 1 1 ...
## $ NE
                : num -1.093 -0.226 -2.291 -0.327 -0.186 ...
## $ CE
                : num 00000...
## $ SE
                : num -1.093 -0.226 -2.291 -0.327 -0.186 ...
#transform Composition, Block, Days as factor for further analyses
NE_data<-NE_data[, -1]</pre>
NE_data<-NE_data %>%
 mutate(across(c("Composition", "Block", "Days"),
               as.factor))
test homoscedasticity of variance
# Plot Raw data - NE against Days
PlotNE <- ggplot(NE_data, aes(x = Days, y = NE)) +
 geom_jitter(position=position_jitter(0.2)) +
 stat_summary(fun.data="mean_sdl", fun.args = list(mult=1),
              geom="pointrange", color = "red")+
 theme_classic() +
 labs(x="Days", y="NE (mg)") +
 scale_y_continuous(limits=c(-2000, 2000), breaks=seq(-2000, 2000, by=500))
leveneTest(NE ~ Days, data=NE_data) #the variance among the factor Days is NOT equal
## Levene's Test for Homogeneity of Variance (center = median)
         Df F value
                       Pr(>F)
## group 3 40.109 < 2.2e-16 ***
##
        128
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
PlotCE <- ggplot(NE data, aes(x = Days, y = CE)) +
 geom_jitter(position=position_jitter(0.2)) +
 stat_summary(fun.data="mean_sdl", fun.args = list(mult=1),
              geom="pointrange", color = "red")+
 theme_classic() +
 labs(x="Days", y="CE (mg)") +
 scale_y_continuous(limits=c(-2000, 2000), breaks=seq(-2000, 2000, by=500))
leveneTest(CE ~ Days, data=NE_data) #variance among the factor Days is NOT equal
## Levene's Test for Homogeneity of Variance (center = median)
         Df F value
                       Pr(>F)
## group 3 43.943 < 2.2e-16 ***
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
PlotSE <- ggplot(NE_data, aes(x = Days, y = SE)) +
  geom_jitter(position=position_jitter(0.2)) +
  stat_summary(fun.data="mean_sdl", fun.args = list(mult=1),
               geom="pointrange", color = "red")+
  theme_classic() +
  labs(x="Days", y="SE (mg)") +
  scale_y_continuous(limits=c(-2000, 2000), breaks=seq(-2000, 2000, by=500))
leveneTest(SE ~ Days, data=NE_data) #variance among the factor Days is NOT equal
## Levene's Test for Homogeneity of Variance (center = median)
          Df F value
                        Pr(>F)
           3 21.849 1.724e-11 ***
## group
##
         128
## -
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
#mean_sdl computes the mean plus or minus a constant times the standard deviation
#(here the constant (mult) =1), so we see mean + standard deviation in Red
#We can clearly see that the variance of NE, CE and SE increases over time
ggarrange(PlotNE, PlotCE, PlotSE, nrow=1, ncol=3)
## Warning: Removed 1 rows containing non-finite values (`stat_summary()`).
## Warning: Removed 1 rows containing missing values (`geom_point()`).
    2000
                                   2000
                                                                  2000
    1500
                                                                  1500
                                   1500
    1000
                                   1000
                                                                  1000
     500
                                    500
                                                                   500
NE (mg)
                                                              SE (mg)
                               CE (mg)
       0
                                      0
                                                                     0
    -500
                                   -500
                                                                  -500
   -1000
                                  -1000
                                                                 -1000
   -1500
                                  -1500
                                                                 -1500
   -2000
                                  -2000
                                                                 -2000
                                                                             20
                                               20
                                                   40
                20
                    40
                         60
                                                        60
                                                                                  40
                                                                                       60
                 Days
                                                Days
                                                                               Days
```

why we use the nlme::lme function to compute the ANOVAs

Since the variance of NE, CE, SE increases over time (heteroscedasticity in the residuals), we decided to use the function nlme::lme to make our ANOVAs, because the function allows to weight the variance by the factor Days. Observations with higher variability will have lower weights, allowing the model to give them less influence. This method is particularly relevant with repeated measures data as we have here.

The class pdMat, which represent positive-definite matrices, is used to represent variance-covariance matrices of random effects. We have have two blocks in the random effects variance-covariance matrix: one for Composition, and one for Block.

 $Sources: \ https://stackoverflow.com/questions/36643713/how-to-specify-different-random-effects-in-nlme-vs-lme4\ https://biostatmatt.com/archives/2718$

The varIdent function allows different variances according to the levels of a classification factor.

ANOVA 1: net effect through time

```
# Model testing the effect of Days on NE with Composition and Block as random factors and weighted by D
# Here we add a dummy factor just to include the whole dataset in a single block, to act as a grouping
NE_data$dummy<-factor(1)</pre>
#1.1-ASSESSING WHETHER THERE IS ANY STATISTICALLY SIGNIFICANT DIFFERENCE AMONG DAYS
#this first p-value aims to understand whether there is any statistically significant difference among
#in the model, pdBlocked combines the covariance structures of pdIdent Composition and pdIdent Block (i
# -1 means that there is no default overall intercept being estimated for the factors Composition and B
#pdIdent indicates that the random effects are assumed to have equal variances and no covariances.
#this whole syntax is actually a "trick" to specify non-nested crossed random effects in the nlme synta
#an equivalent way to specify the random effects could be : random=list(dummy=pdBlocked(list(pdIdent(~
modNE <- lme(NE ~ Days,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                                pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days), #residuals are allowed to have different variances for
              method="REML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
anova(modNE) #there is at least one statistically significant difference among certain levels of factor
##
               numDF denDF F-value p-value
                       128 0.00909 0.9242
## (Intercept)
                   1
## Days
                       128 32.54603 <.0001
print(getVarCov(modNE))
## Random effects variance covariance matrix
##
                       {\tt CompositionLmLt\ CompositionLmSp\ CompositionLmSpLt}
                                                                   0.0000
## CompositionLmLt
                                1.3912
                                                 0.0000
                                0.0000
                                                 1.3912
                                                                   0.0000
## CompositionLmSp
## CompositionLmSpLt
                                0.0000
                                                 0.0000
                                                                   1.3912
## CompositionLmSpWc
                                0.0000
                                                 0.0000
                                                                   0.0000
## CompositionLmSpWcLt
                                0.0000
                                                 0.0000
                                                                   0.0000
## CompositionLmWc
                                0.0000
                                                 0.0000
                                                                   0.0000
## CompositionLmWcLt
                                0.0000
                                                 0.0000
                                                                   0.0000
```

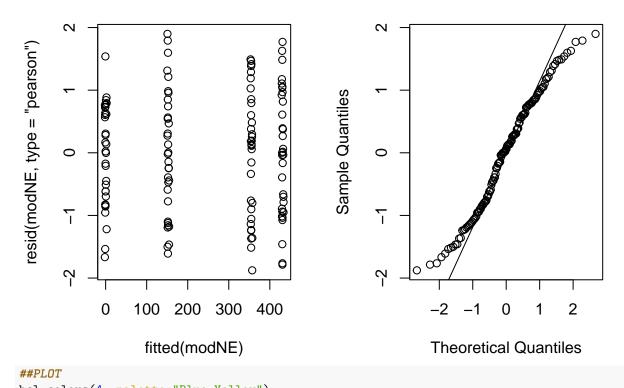
```
## CompositionSpLt
                                  0.0000
                                                   0.0000
                                                                       0.0000
                                                   0.0000
  CompositionSpWc
                                  0.0000
                                                                       0.0000
   CompositionSpWcLt
                                  0.0000
                                                   0.0000
                                                                       0.0000
   CompositionWcLt
                                  0.0000
                                                   0.0000
                                                                       0.0000
##
  Block1
                                  0.0000
                                                   0.0000
                                                                       0.0000
## Block2
                                  0.0000
                                                   0.0000
                                                                       0.0000
## Block3
                                  0.0000
                                                   0.0000
                                                                       0.0000
##
                        CompositionLmSpWc CompositionLmSpWcLt CompositionLmWc
   {\tt CompositionLmLt}
                                    0.0000
                                                          0.0000
                                                                           0.0000
##
   CompositionLmSp
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionLmSpLt
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionLmSpWc
                                    1.3912
                                                          0.0000
                                                                           0.0000
   CompositionLmSpWcLt
                                    0.0000
                                                                           0.0000
                                                          1.3912
   CompositionLmWc
                                    0.0000
                                                          0.0000
                                                                           1.3912
   CompositionLmWcLt
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionSpLt
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionSpWc
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionSpWcLt
                                    0.0000
                                                          0.0000
                                                                           0.0000
   CompositionWcLt
                                    0.0000
                                                          0.0000
                                                                           0.0000
## Block1
                                    0.0000
                                                          0.0000
                                                                           0.0000
## Block2
                                    0.0000
                                                          0.0000
                                                                           0.0000
## Block3
                                                          0.0000
                                    0.0000
                                                                           0.0000
##
                        {\tt CompositionLmWcLt\ CompositionSpLt\ CompositionSpWc}
                                                      0.0000
##
  CompositionLmLt
                                    0.0000
                                                                       0.0000
   CompositionLmSp
                                    0.0000
                                                      0.0000
                                                                       0.0000
   {\tt CompositionLmSpLt}
                                    0.0000
                                                      0.0000
                                                                       0.0000
   CompositionLmSpWc
                                                      0.0000
                                    0.0000
                                                                       0.0000
   {\tt CompositionLmSpWcLt}
                                    0.0000
                                                      0.0000
                                                                       0.0000
   CompositionLmWc
                                    0.0000
                                                      0.0000
                                                                       0.0000
   CompositionLmWcLt
                                    1.3912
                                                      0.0000
                                                                       0.0000
   CompositionSpLt
                                    0.0000
                                                      1.3912
                                                                       0.0000
   CompositionSpWc
                                    0.0000
                                                      0.0000
                                                                       1.3912
   CompositionSpWcLt
                                    0.0000
                                                      0.0000
                                                                       0.0000
   CompositionWcLt
                                    0.0000
                                                      0.0000
                                                                       0.0000
## Block1
                                    0.0000
                                                      0.0000
                                                                       0.0000
## Block2
                                    0.0000
                                                      0.0000
                                                                       0.0000
## Block3
                                    0.0000
                                                      0.0000
                                                                       0.0000
##
                        CompositionSpWcLt CompositionWcLt
                                                                         Block2
                                                               Block1
                                    0.0000
                                                      0.0000 0.000000 0.000000
##
   CompositionLmLt
##
   CompositionLmSp
                                    0.0000
                                                      0.0000 0.000000 0.000000
                                                      0.0000 0.000000 0.000000
   CompositionLmSpLt
                                    0.0000
   CompositionLmSpWc
                                    0.0000
                                                      0.0000 0.000000 0.000000
   CompositionLmSpWcLt
                                    0.0000
                                                      0.0000 0.000000 0.000000
   {\tt CompositionLmWc}
                                                      0.0000 0.000000 0.000000
                                    0.0000
   CompositionLmWcLt
                                    0.0000
                                                      0.0000 0.000000 0.000000
                                                      0.0000 0.000000 0.000000
   CompositionSpLt
                                    0.0000
   CompositionSpWc
                                    0.0000
                                                      0.0000 0.000000 0.000000
   CompositionSpWcLt
                                    1.3912
                                                      0.0000 0.000000 0.000000
   CompositionWcLt
                                    0.0000
                                                      1.3912 0.000000 0.000000
##
   Block1
                                    0.0000
                                                      0.0000 0.039774 0.000000
## Block2
                                                      0.0000 0.000000 0.039774
                                    0.0000
## Block3
                                    0.0000
                                                      0.0000 0.000000 0.000000
##
                          Block3
## CompositionLmLt
                        0.00000
```

```
## CompositionLmSp
                       0.000000
## CompositionLmSpLt
                       0.000000
## CompositionLmSpWc
                       0.000000
## CompositionLmSpWcLt 0.000000
## CompositionLmWc
                       0.000000
## CompositionLmWcLt
                       0.000000
## CompositionSpLt
                       0.000000
## CompositionSpWc
                       0.000000
## CompositionSpWcLt
                       0.000000
## CompositionWcLt
                       0.000000
## Block1
                       0.00000
## Block2
                       0.000000
## Block3
                       0.039774
     Standard Deviations: 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795 1.1795
#1.2-ASSESSING OVERALL EFFECT OF DAYS : likelihood ratio test
#"when assessing the overall treatment effects using a likelihood ratio test, one should use maximum li
modNE.ml <- lme(NE ~ Days,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                               pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
#null model
modNEO.ml <- lme(NE ~ 1,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                               pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
#overall p-value modNE
anova(modNEO.ml, modNE.ml) #overall, the factor days has a statistically significant effect on net effe
             Model df
                           AIC
                                    BIC
                                                     Test L.Ratio p-value
                                           logLik
## modNEO.ml
                 1 7 1542.353 1562.532 -764.1764
                 2 10 1480.475 1509.303 -730.2372 1 vs 2 67.87832 <.0001
#1.3-COMPARISON BETWEEN EACH DAY AND DAY O (CONTROL LEVEL)
summary(modNE)
## Linear mixed-effects model fit by REML
##
     Data: NE data
##
          AIC
                   BIC
                          logLik
     1451.485 1480.005 -715.7423
##
##
## Random effects:
## Composite Structure: Blocked
##
## Block 1: CompositionLmLt, CompositionLmSp, CompositionLmSpLt, CompositionLmSpWc, CompositionLmSpWcL
## Formula: ~Composition - 1 | dummy
```

```
## Structure: Multiple of an Identity
##
          CompositionLmLt CompositionLmSp CompositionLmSpLt CompositionLmSpWc
                 1.179503
                                 1.179503
                                                   1.179503
          CompositionLmSpWcLt CompositionLmWc CompositionLmWcLt CompositionSpLt
##
## StdDev:
                     1.179503
                                     1.179503
                                                       1.179503
##
          CompositionSpWc CompositionSpWcLt CompositionWcLt
                 1.179503
                                   1.179503
## StdDev:
##
## Block 2: Block1, Block2, Block3
## Formula: ~Block - 1 | dummy
## Structure: Multiple of an Identity
            Block1 Block2 Block3 Residual
## StdDev: 0.199435 0.199435 0.199435 0.2705557
##
## Variance function:
## Structure: Different standard deviations per stratum
## Formula: ~1 | Days
## Parameter estimates:
##
                   20
                             40
##
      1.0000 471.8876 1334.1800 2108.5545
## Fixed effects: NE ~ Days
                 Value Std.Error DF t-value p-value
## (Intercept) 0.0349 0.37676 128 0.092725 0.9263
              152.2021 22.22487 128 6.848277 0.0000
## Davs20
              354.9528 62.83682 128 5.648802 0.0000
## Days40
## Days60
              430.9378 99.30807 128 4.339404 0.0000
## Correlation:
          (Intr) Days20 Days40
## Days20 0
## Days40 0
                0
## Days60 0
                0
                       0
##
## Standardized Within-Group Residuals:
          Min
                       Q1
                                  Med
                                               QЗ
## -1.87672122 -0.80706311 0.06059949 0.76522023 1.89863861
## Number of Observations: 132
## Number of Groups: 1
#here we can see that NE is significantly greater at day 20, at day 40 and at day 60 than at day 0
#WHICH TREATMENTS ARE DIFFERENT FROM EACH OTHER?
contrast(emmeans(modNE, specs="Days"), "pairwise") #the effect of days on NE isn't statistically differ
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
## contrast
                   estimate
                               SE df t.ratio p.value
```

```
##
   Days0 - Days20
                        -152
                              22.2 128
                                        -6.848 <.0001
   Days0 - Days40
                        -355
                              62.8 128
                                        -5.649
                                               <.0001
##
                              99.3 128
                                               0.0002
   Days0 - Days60
                        -431
                                        -4.339
   Days20 - Days40
                        -203
                              66.7 128
                                        -3.042
                                               0.0149
##
##
   Days20 - Days60
                        -279 101.8 128
                                        -2.739
                                                0.0351
   Days40 - Days60
                         -76 117.5 128
                                        -0.647
                                               0.9166
##
## Degrees-of-freedom method: containment
## P value adjustment: tukey method for comparing a family of 4 estimates
#MODEL VALIDATION
par(mfrow=c(1,2))
plot(fitted(modNE), resid(modNE,type="pearson"))
qqnorm(resid(modNE,type="pearson"))
qqline(resid(modNE,type="pearson"))
```

Normal Q-Q Plot



```
hcl.colors(4, palette="Blue-Yellow")

## [1] "#2D3184" "#32AAB5" "#B3E7C5" "#F3F1E4"

#computing mean and standard deviation per day from raw data

mean<-as.vector(c(mean(NE_data[NE_data$Days==0, ]$NE), mean(NE_data[NE_data$Days==20, ]$NE), mean(NE_data$Days==20, ]$NE), mean(NE_data$Days=20, ]$NE), mean(NE_datayabayabay
```

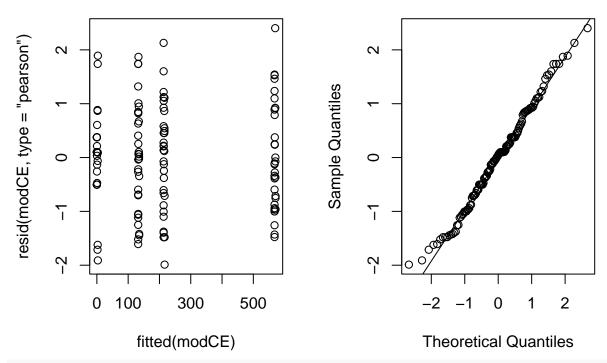
```
se<-as.vector(c(sd(NE_data[NE_data$Days==0, ]$NE)/sqrt(length(NE_data[NE_data$Days==0, ]$NE)), sd(NE_data
NE_meanse<-data.frame(
    days=c("0", "20", "40", "60"),
    mean=mean,
    se=se,
    label=c("a", "b", "c", "c"))</pre>
```

```
NE_meanse$ci<-NE_meanse$se*1.96</pre>
NEp<-ggplot(NE_meanse) +</pre>
  geom_bar(aes(x=days, y=mean), colour="black", fill="#2D3184", stat="identity", alpha=0.7) +
  \#geom\_errorbar(aes(x=days, ymin=mean-se, ymax=mean+se), width=0.4, colour="red", alpha=0.9, size=1.3)
  geom_errorbar(aes(x=days, ymin=mean-ci, ymax=mean+ci), width=0.4, colour="black", alpha=0.9, size=1.3
  geom_text(aes(x=days, y=mean+ci+100, label=label,), position=position_dodge(0.9), vjust=1, size=7) +
  theme classic() +
  theme(text=element_text(size=15), plot.title=element_text(vjust=2), panel.grid.major.y = element_line
  labs(x="Days of growth", y="NE", title="Net biodiversity effect", pch=8) +
  scale_y_continuous(limits=c(0, 1000), breaks=seq(0, 1000, by=200))
## Warning: Using `size` aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use `linewidth` instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
## Warning: The `size` argument of `element_line()` is deprecated as of ggplot2 3.4.0.
## i Please use the `linewidth` argument instead.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.
ANOVA 2: complementarity effect through time
modCE <- lme(CE ~ Days,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                               pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="REML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
anova(modCE) #there is at least one statistically significant difference among certain levels of factor
               numDF denDF F-value p-value
                       128 5.127877 0.0252
## (Intercept)
                   1
                       128 27.354690 <.0001
## Days
                   3
modCE.ml <- lme(CE ~ Days,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                               pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
#null model
modCEO.ml <- lme(CE ~ 1,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                               pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
```

```
control=list(msMaxIter=1000,
                                                              msMaxEval=1000))
anova(modCE0.ml, modCE.ml) #overall, the factor days has a statistically significant effect on compleme
                            Model df
                                                          AIC
                                                                              BIC
                                                                                             logLik
                                                                                                                Test L.Ratio p-value
## modCEO.ml
                                    1 7 1447.319 1467.499 -716.6597
## modCE.ml
                                     2 10 1394.119 1422.947 -687.0593 1 vs 2 59.20085 <.0001
summary(modCE)
## Linear mixed-effects model fit by REML
##
          Data: NE data
##
                     AIC
                                        BIC
                                                        logLik
          1365.367 1393.888 -672.6836
##
##
## Random effects:
##
      Composite Structure: Blocked
##
## Block 1: CompositionLmLt, CompositionLmSp, CompositionLmSpLt, CompositionLmSpWc, CompositionLmSpWcL
## Formula: ~Composition - 1 | dummy
## Structure: Multiple of an Identity
                       CompositionLmLt CompositionLmSp CompositionLmSpLt CompositionLmSpWc
##
## StdDev:
                                       1.203187
                                                                         1.203187
                                                                                                                1.203187
                       {\tt CompositionLmSpWcLt\ CompositionLmWc\ CompositionLmWcLt\ CompositionSpLt\ CompositionSpLt\ CompositionLmWcLt\ CompositionSpLt\ CompositionLmWcLt\ CompositionLmW
##
                                                1.203187
                                                                                  1.203187
                                                                                                                          1.203187
                       CompositionSpWc CompositionSpWcLt CompositionWcLt
##
## StdDev:
                                       1.203187
                                                                              1.203187
                                                                                                                1.203187
##
## Block 2: Block1, Block2, Block3
## Formula: ~Block - 1 | dummy
## Structure: Multiple of an Identity
                                Block1
                                                        Block2
##
                                                                                Block3
                                                                                                   Residual
## StdDev: 0.02276269 0.02276269 0.02276269 0.04379333
##
## Variance function:
## Structure: Different standard deviations per stratum
## Formula: ~1 | Days
##
        Parameter estimates:
##
                                           20
                                                                 40
                                                                                       60
##
               1.000 2592.952 6290.353 17723.190
## Fixed effects: CE ~ Days
##
                                       Value Std.Error DF t-value p-value
## (Intercept)
                                    0.8222
                                                       0.36309 128 2.264408 0.0252
## Days20
                               132.0337 19.76722 128 6.679426 0.0000
## Days40
                                213.3245 47.95413 128 4.448511 0.0000
## Days60
                                567.7921 135.11167 128 4.202391 0.0000
## Correlation:
                      (Intr) Days20 Days40
## Days20 0
## Days40 0
                                     0
## Days60 0
                                                    0
                                     0
## Standardized Within-Group Residuals:
```

```
Med
                       Q1
## -1.98913850 -0.66697556 0.04653119 0.61160543 2.40300123
## Number of Observations: 132
## Number of Groups: 1
#here we can see that CE is significantly greater at day 20, at day 40 and at day 60 than at day 0
contrast(emmeans(modCE, specs="Days"), "pairwise") #the effect of days on CE isn't statistically differ
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
                   estimate
## contrast
                               SE df t.ratio p.value
## Days0 - Days20
                     -132.0 19.8 128 -6.679 <.0001
## Days0 - Days40
                     -213.3 48.0 128 -4.449 0.0001
## Days0 - Days60
                     -567.8 135.1 128 -4.202 0.0003
## Days20 - Days40
                      -81.3 51.9 128 -1.567 0.4010
## Days20 - Days60
                    -435.8 136.6 128 -3.191 0.0095
## Days40 - Days60
                     -354.5 143.4 128 -2.472 0.0692
##
## Degrees-of-freedom method: containment
## P value adjustment: tukey method for comparing a family of 4 estimates
par(mfrow=c(1,2))
plot(fitted(modCE), resid(modCE, type="pearson"))
qqnorm(resid(modCE,type="pearson"))
qqline(resid(modCE,type="pearson"))
```

Normal Q-Q Plot



```
meanCE<-as.vector(c(mean(NE_data[NE_data$Days==0, ]$CE), mean(NE_data[NE_data$Days==20, ]$CE), mean(NE_
seCE<-as.vector(c(sd(NE_data[NE_data$Days==0, ]$CE)/sqrt(length(NE_data[NE_data$Days==0, ]$CE)), sd(NE_
CE_meanse<-data.frame(</pre>
  days=c("0", "20", "40", "60"),
 mean=meanCE,
  se=seCE,
  label=c("a", "b", "bc", "c"))
CE_meanse$ci<-CE_meanse$se*1.96
CEp<-ggplot(CE_meanse) +</pre>
  geom_bar(aes(x=days, y=mean), colour="black", fill="#2D3184", stat="identity", alpha=0.7) +
  \#geom\_errorbar(aes(x=days, ymin=mean-se, ymax=mean+se), width=0.4, colour="red", alpha=0.9, size=1.3)
  geom_errorbar(aes(x=days, ymin=mean-ci, ymax=mean+ci), width=0.4, colour="black", alpha=0.9, size=1.3
  geom_text(aes(x=days, y=mean+ci+100, label=label,), position=position_dodge(0.9), vjust=1, size=7) +
  theme_classic() +
  theme(text=element_text(size=15), plot.title=element_text(vjust=2), panel.grid.major.y = element_line
  labs(x="Days of growth", y="CE", title="Complementarity effect", pch=8) +
  scale_y_continuous(limits=c(0, 1000), breaks=seq(0, 1000, by=200))
```

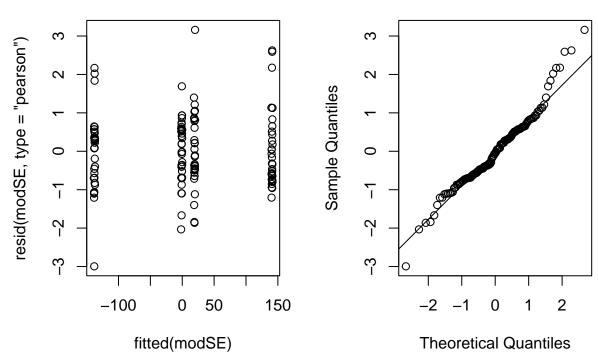
ANOVA 3: Selection effect through time

```
control=list(msMaxIter=1000,
                             msMaxEval=1000))
anova(modSE) #there is at least one statistically significant difference among certain levels of factor
               numDF denDF
                             F-value p-value
## (Intercept)
                   1
                       128 18.915587 <.0001
## Days
                   3
                       128 9.535597 <.0001
modSE.ml <- lme(SE ~ Days,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                                pdIdent(~Block-1)))),
              data=NE data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
#null model
modSE0.ml <- lme(SE ~ 1,</pre>
              random=list(dummy=pdBlocked(list(pdIdent(~Composition-1),
                                                pdIdent(~Block-1)))),
              data=NE_data,
              weights=varIdent(form=~ 1 | Days),
              method="ML",
              control=list(msMaxIter=1000,
                             msMaxEval=1000))
anova(modSE0.ml, modSE.ml) #overall, the factor days has a statistically significant effect on compleme
##
             Model df
                           AIC
                                    BIC
                                            logLik
                                                     Test L.Ratio p-value
## modSEO.ml
                 1 7 1357.574 1377.754 -671.7871
                 2 10 1339.454 1368.282 -659.7269 1 vs 2 24.12035 <.0001
## modSE.ml
summary(modSE)
## Linear mixed-effects model fit by REML
     Data: NE data
##
          AIC
                   BIC
                          logLik
     1315.568 1344.089 -647.7842
##
##
## Random effects:
## Composite Structure: Blocked
##
## Block 1: CompositionLmLt, CompositionLmSp, CompositionLmSpLt, CompositionLmSpWc, CompositionLmSpWcL
## Formula: ~Composition - 1 | dummy
## Structure: Multiple of an Identity
##
           CompositionLmLt CompositionLmSp CompositionLmSpLt CompositionLmSpWc
## StdDev:
                 0.4732538
                                 0.4732538
                                                    0.4732538
                                                                      0.4732538
##
           {\tt CompositionLmSpWcLt\ CompositionLmWc\ CompositionLmWcLt\ CompositionSpLt\ }
                     0.4732538
                                      0.4732538
                                                        0.4732538
                                                                        0.4732538
##
           CompositionSpWc CompositionSpWcLt CompositionWcLt
                 0.4732538
                                   0.4732538
## StdDev:
                                                    0.4732538
##
## Block 2: Block1, Block2, Block3
## Formula: ~Block - 1 | dummy
## Structure: Multiple of an Identity
```

```
Block2
                                 Block3 Residual
             Block1
## StdDev: 0.1760824 0.1760824 0.1760824 0.2573057
##
## Variance function:
## Structure: Different standard deviations per stratum
## Formula: ~1 | Days
## Parameter estimates:
##
                             40
                                       60
##
      1.0000 199.7767 695.0623 1815.6250
## Fixed effects: SE ~ Days
                   Value Std.Error DF
                                         t-value p-value
                           0.18084 128 -4.353388 0.0000
## (Intercept)
                -0.78725
## Days20
                20.16838
                           8.94835 128 2.253867 0.0259
## Days40
               141.62831 31.13268 128 4.549184 0.0000
## Days60
              -136.85423 81.32397 128 -1.682828 0.0948
   Correlation:
##
          (Intr) Days20 Days40
## Days20 -0.001
## Days40 0.000 0.000
## Days60 0.000 0.000 0.000
##
## Standardized Within-Group Residuals:
##
                       Q1
          Min
                                  Med
                                               QЗ
                                                          Max
## -2.99493534 -0.61529622 -0.04568812 0.56281949 3.16007848
##
## Number of Observations: 132
## Number of Groups: 1
#here we can see that CE is significantly greater at day 20, at day 40 than at day 0, but CE isn't sign
contrast(emmeans(modSE, specs="Days"), "pairwise") #the effect of days on SE is only different at Day 4
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Composition' is absent, its contrast will be ignored
## Warning in model.matrix.default(trms, m, contrasts.arg = contrasts): variable
## 'Block' is absent, its contrast will be ignored
## contrast
                   estimate
                               SE df t.ratio p.value
## Days0 - Days20
                      -20.2 8.95 128 -2.254 0.1146
## Days0 - Days40
                     -141.6 31.13 128 -4.549 0.0001
## Days0 - Days60
                      136.9 81.32 128
                                        1.683 0.3370
## Days20 - Days40
                     -121.5 32.39 128 -3.750 0.0015
## Days20 - Days60
                      157.0 81.81 128
                                       1.919 0.2251
## Days40 - Days60
                      278.5 87.08 128
                                       3.198 0.0093
## Degrees-of-freedom method: containment
## P value adjustment: tukey method for comparing a family of 4 estimates
par(mfrow=c(1,2))
plot(fitted(modSE), resid(modSE, type="pearson"))
```

```
qqnorm(resid(modSE,type="pearson"))
qqline(resid(modSE,type="pearson"))
```

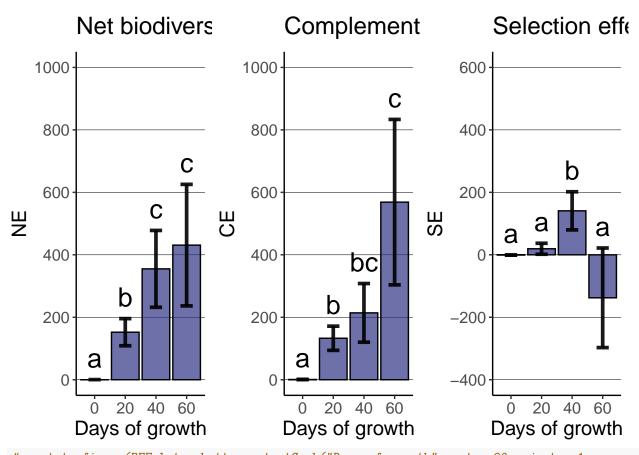
Normal Q-Q Plot



```
meanSE<-as.vector(c(mean(NE_data[NE_data$Days==0, ]$SE), mean(NE_data[NE_data$Days==20, ]$SE), mean(NE_
seSE<-as.vector(c(sd(NE_data[NE_data$Days==0, ]$SE)/sqrt(length(NE_data[NE_data$Days==0, ]$SE)), sd(NE_
SE_meanse<-data.frame(</pre>
  days=c("0", "20", "40", "60"),
  mean=meanSE,
  se=seSE,
  label=c("a", "a", "b", "a"))
SE_meanse$ci<-SE_meanse$se*1.96
SEp<-ggplot(SE_meanse) +</pre>
  geom bar(aes(x=days, y=mean), colour="black", fill="#2D3184", stat="identity", alpha=0.7) +
  #geom_errorbar(aes(x=days, ymin=mean-se, ymax=mean+se), width=0.4, colour="red", alpha=0.9, size=1.3)
  geom_errorbar(aes(x=days, ymin=mean-ci, ymax=mean+ci), width=0.4, colour="black", alpha=0.9, size=1.3
  geom_text(aes(x=days, y=mean+ci+100, label=label,), position=position_dodge(0.9), vjust=1, size=7) +
  theme_classic() +
  theme(text=element_text(size=15), plot.title=element_text(vjust=2), panel.grid.major.y = element_line
  labs(x="Days of growth", y="SE", title="Selection effect", pch=8) +
  scale_y_continuous(limits=c(-400, 600), breaks=seq(-400, 600, by=200))
###Final plots BEF through time
```

BEFplots<-ggarrange(NEp, CEp, SEp, nrow=1, ncol=3, common.legend = TRUE)

BEFplots



 $\#annotate_figure(BEFplots, bottom = textGrob("Days of growth", rot = 90, vjust = 1, gp = gpar(cex = 1.3))$