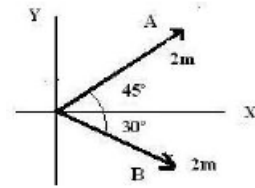


## VECTOR CALCULUS

1. Given the vectors  $\vec{A}$  and  $\vec{B}$ , determine:

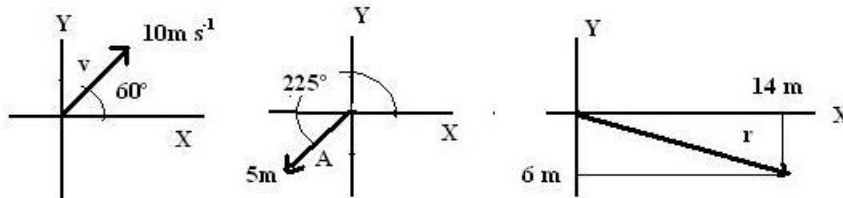
- Their cartesian coordinates
- The vectors:  $\vec{A} + \vec{B}$ ;  $\vec{A} - \vec{B}$ ;  $\vec{B} - \vec{A}$ ;  $2\vec{A} - \vec{B}$
- Graphically, the vectors of part b.



2. A vector  $\vec{A}$  has a magnitude of 8 m and makes an angle of  $37^\circ$  with the OX axis. Also consider the vectors  $\vec{B} = 3\vec{i} - 5\vec{j}$  and  $\vec{C} = -6\vec{i} + 3\vec{j}$ . Determine the vectors:  $\vec{A} + \vec{C}$ ;  $\vec{A} - 2\vec{B}$ ;  $\vec{A} - 2\vec{B} + 3\vec{C}$ ;  $\vec{A} \cdot \vec{B}$ ;  $\vec{A} \times \vec{B}$ ;  $\vec{B} \cdot \vec{C}$ ;  $2\vec{A} \times \vec{C}$ .

3. Calculate the magnitude and direction of the following vectors:  $\vec{A} = 4\vec{i} + 3\vec{j}$ ;  $\vec{B} = 10\vec{i} - 7\vec{j}$ ;  $\vec{A} + \vec{B}$ ;  $\vec{A} \times \vec{B}$ .

4. Determine the following vectors, in terms of  $\vec{i}$  and  $\vec{j}$ :



5. The cartesian components of a vector are:  $A_x = -10$  and  $A_y = 6$ ,  $\vec{B} = 3\vec{i} + 5\vec{j}$  and  $\vec{C} = 3\vec{i} + 4\vec{j}$ . Calculate:
- The angle that the vector  $\vec{A}$  makes with the positive OX axis.
  - The angle between the vectors  $\vec{A}$  and  $\vec{B}$ .
  - The unitary vector of  $\vec{C}$ .
  - The projection of  $\vec{A}$  in the direction of  $\vec{C}$ .