REVISING THE KEPLER-11 SYSTEM: A TESTAMENT TO THE IMPORTANCE OF PRECISE STELLAR CHARACTERIZATION

MEGAN BEDELL 1 , JACOB L. BEAN 1 , JORGE MELÉNDEZ 2 , SEAN MILLS 1 , DAN FABRYCKY 1 , MARTIN ASPLUND 3 , IVAN RAMÍREZ 4 , FAN LIU 3 , DAVID YONG 3

Draft version July 25, 2016

ABSTRACT

The six planets of the Kepler-11 system are the archetypal example of a population of surprisingly low-density transiting planets revealed by the Kepler mission. We have determined the stellar chemical composition of Kepler-11 to unprecedented precision using an extremely high quality spectrum from Keck-HIRES (R \simeq 67000, SNR \simeq 280). Contrary to previously published results, our spectroscopic constraints indicate that Kepler-11 is a young main-sequence solar twin. The revised stellar parameters raise the densities of the Kepler-11 planets by about 30%, making them more typical of the emerging class of "puffy" close-in exoplanets. We obtain photospheric abundances of 22 elements and find that Kepler-11 is enhanced in refractory materials relative to the solar abundance pattern. We additionally analyze the Kepler transits and transit timing variations (TTVs) using a photodynamical model and discuss the tension between spectroscopic and TTV-based stellar density estimates.

Subject headings: stars: abundances, stars: fundamental parameters, techniques: spectroscopic

1. INTRODUCTION

Five years after their initial discovery, the six planets of the Kepler-11 system remain a crown jewel of *Kepler* science results (?). All six planets orbit a Sun-like host star at low eccentricies in a largely co-planar, tightly packed configuration. The formation and long-term stability of the system remains an open question (see e.g. ???). (say more about resonance, STIPs)

In addition to their unusually tight system architecture, the Kepler-11 planets are noteworthy in another sense: their measured masses and radii place them among the lowest-density super-Earths known to date. Transit timing variations (TTVs) have been measured for all six planets. In the discovery paper,? derived mass constraints for the five inner planets based on TTVs from six quarters of Kepler data. ? reanalyzed the same data using a photodynamical model and found similar results, with an additional constraint on the outermost planet mass. The system was later revisited by? using fourteen quarters of Kepler data. All three analyses estimate mean densities of $\leq 0.5 \ \rho_{\oplus}$ for all planets in the system, implying a considerable gas envelope on even the smaller super-Earths. This result has considerable repercussions for potential formation system scenarios (cite).

Mean planet densities derived from transits and TTVs (or from transits and radial velocities) have a strong dependence on the properties of the host star. Since the transit depth observationally constrains the ratio of planetary radius to stellar radius, the planet volume depends

on the assumed stellar radius to the third power. The planet mass found from TTV inversion is correlated with the stellar mass. Host star characterization is therefore a critical part of measuring planet densities.

In past works, Kepler-11 has been characterized only through spectroscopic analysis of low to modest signalto-noise data. ??? all use spectra taken by Keck with $SNR \leq 40$ and apply the Spectroscopy Made Easy package (SME, ?) to perform matching to a library of synthetic spectra. The resulting stellar atmospheric parameters, when compared with stellar evolution models, indicate that Kepler-11 is a slightly evolved solar analog with (mass, radius). No independent measurements of the stellar density (e.g. from asteroseismology or parallax) are available. Analysis of the stellar composition is also minimal. ? perform an equivalent width (EW) analysis on one of these Keck spectra to derive abundances of three α -elements and find that Kepler-11 has moderately low abundances of Ca, Cr, and Ti; however, the line list employed is quite limited with ≤ 5 lines per element.

Kepler-11's well-characterized planetary system makes it a prime target for more detailed spectroscopic study. In this work, we present an analysis of a new, very high SNR spectrum. We use equivalent widths to measure the stellar properties and abundances of 22 elements at high precision.

2. Data

Owing to its relative faintness (V = 14.2, ?), Kepler-11 was previously observed only at a signal-to-noise ratio insufficient for high-precision spectroscopic characterization. We dedicated nearly 8 hours of Keck I time to obtaining a higher quality spectrum. Over the course of two consecutive nights (July 26-27 2015), we made 22 1200-s exposures of Kepler-11 for a co-added result of SNR \simeq 280. For these observations, HIRES was used with the B2 slit and kv387 filter, yielding a resolution R \simeq 67000 and wavelength coverage between 390 and 830 nm.

We also observed the Sun (using Ceres) and nine bright

E-mail: mbedell@oddjob.uchicago.edu

 Department of Astronomy and Astrophysics, University of Chicago, 5640 S. Ellis Ave, Chicago, IL 60637, USA
 Departmento de Astronomia do IAG/USP, Universidade de

² Departamento de Astronomia do IAG/USP, Universidade de São Paulo, Rua do Matão 1226, Cidade Universitária, 05508-900 São Paulo, SP, Brazil

³ Research School of Astronomy and Astrophysics, The Australian National University, Cotter Road, Weston, ACT 2611, Australia

 4 McDonald Observatory and Department of Astronomy, University of Texas at Austin, USA

2 Bedell et al.

potential Kepler-11 twins with the same instrumental setup and similar SNR. The Kepler-11 twins were selected by imposing criteria of $5600 \le T_{\rm eff} \ge 5750$ K and $4.2 \le \log g \ge 4.4$ dex on databases of previously published stellar parameters (??). Preference was given to stars likely to be thick-disk members with approximately solar metallicity. These criteria were set based on the original spectroscopic analysis of Kepler-11 by ?, who found $T_{\rm eff} = 5680 \pm 100$ K, $\log g = 4.3 \pm 0.2$ dex, [Fe/H] = 0.0 ± 0.1 dex, and a significant chance of Kepler-11's being a thick disk member based on its kinematics.

The spectral extraction was performed by the Mauna Kea Echelle Extraction (MAKEE) pipeline. All Kepler-11 spectra were then co-added using IRAF's scombine. Continuum normalization was done by fitting low-order polynomial functions to each order, with care to use the same functional order for a given spectral order on every stellar spectrum to avoid bias in the subsequent differential analysis. Doppler corrections were applied using IRAF's dopcor task.

(details about Kepler lightcurve?)

3. STELLAR PROPERTIES FROM SPECTROSCOPIC ANALYSIS

The fundamental properties of Kepler-11 and its potential twins were derived from an equivalent width analysis. We hand-measured 94 Fe I and 17 Fe II spectral lines using IRAF's *splot*. The line list was chosen (criteria, cite). Equivalent widths were measured by carefully choosing local continua as described in ? to maximize differential precision between the spectra. The full line list and measured equivalent widths are available in Table 2.

The stellar effective temperature, $\log g$, metallicity [Fe/H], and microturbulence v_t were determined by imposing requirements of excitation and ionization balance on the iron abundances derived by MOOG (?). It is important to note that we exclusively used the differential abundance measurements relative to the solar spectrum. By directly comparing line-by-line differential abundances of spectrally similar stars, we minimize the influence of stellar model systematics on the final parameters and abundances (see e.g. ?). Parameter solutions were found iteratively using the q^2 python package. Uncertainties were determined by propagating scatter among the measured line abundances as described in ??.

The resulting stellar parameters for all observed stars are given in Table 1. The $T_{\rm eff}$ and $\log g$ for Kepler-11 are significantly higher than previously determined values. For example, ? find $T_{\rm eff}=5666\pm60$ K, $\log g=4.28\pm0.07$ dex, and $[{\rm Fe/H}]=0.00\pm0.04$ dex, while we find $T_{\rm eff}=5839\pm7$ K, $\log g=4.45\pm0.02$ dex, and $[{\rm Fe/H}]=0.06\pm0.01$ dex. Potential sources of this tension include the substantially different SNR of spectra used and the difference in analysis technique. ? and other previous analyses use SME, which employs a library of synthetic spectra to do spectral matching.

Our revised stellar parameters securely place Kepler-11 in the solar twin category. This can be seen even by eye: as depicted in Figure 1, at high SNR Kepler-11's

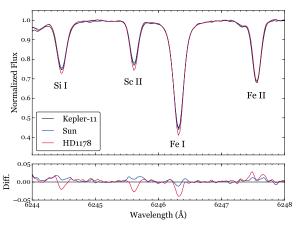


FIG. 1.— A small section of the Keck-HIRES spectra of the Sun (blue), Kepler-11 (black), and HD1178 (red), which has fundamental parameters similar to those given by ? for Kepler-11. Residuals for flux relative to the Kepler-11 spectrum are plotted in the lower panel.

spectrum is nearly identical to the solar spectrum and distinctly different from that of HD1178, the star from our sample whose fundamental parameters most closely match those found by $\ref{eq:holdsym}$. In particular, the solar-like log g for Kepler-11 implies that it is denser and less evolved than previously thought.

We used stellar evolutionary models to estimate the mass, radius, and age of Kepler-11. Yonsei-Yale isochrones were fit using q^2 . We also applied Dartmouth and Basti isochrones using the *isochrones* python package for fitting. All three models gave results consistent within well below 1σ . From these fits, we estimate a stellar mass $M_{\star} = 1.04 \pm 0.01 \ M_{\odot}$, radius $R_{\star} = 1.00 \pm 0.02 \ R_{\odot}$, and age 2.8 ± 0.8 Gyr. This gives a stellar density $\rho_{\star} = 1.47 \pm 0.09$ g cm⁻³.

4. ALTERNATIVE STELLAR AGE INDICATORS

While mass, radius, and density cannot be measured through other methods from the stellar spectrum, stellar age has multiple known proxies. We used several alternate methods to measure the age of Kepler-11 as an independent test of its evolutionary state. The results unanimously agree upon a sub-solar age for Kepler-11. Details of the methods used follow.

4.1. Stellar Rotation

The apparent rotation rate $v\sin i$ was measured using five saturated lines (Fe I 6027.050 Å, 6151.618 Å, 6165.360 Å, 6705.102 Å, and Ni I 6767.772 Å) from the Keck spectrum. The procedure used is described in depth in ?, and will be summarized here. We first measured the macroturbulence value v_{macro} for each line in the solar reference spectrum with MOOG synth. We then calculated v_{macro} for Kepler-11 using the measured solar values and the empirical relation given in Equation 1 of ?. Finally, MOOG synth was used to find $v\sin i$ for each line in Kepler-11's spectrum with v_{macro} fixed to the calculated value.

The five lines give a consistent result of $v\sin i = 2.2 \pm 0.2$ km s⁻¹. Assuming alignment of the stellar spin axis with the orbital axis of its transiting planets, we can take

⁵IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy (AURA) under cooperative agreement with the National Science Foundation.

 $^{^6 {\}it https://github.com/astroChasqui/q2}$

Kepler-11 3

Spectrum	$T_{ m eff}$	σ_T	$\log g$	σ_{logg}	v_t	σ_{v_t}	[M/H]	$\sigma_{[M/H]}$
	(K)	(K)	(dex)	(dex)	$({\rm km}\ {\rm s}^{-1})$	$({\rm km} \; {\rm s}^{-1})$	(dex)	(dex)
Sun (Ceres) a	5777	_	4.44	-	0.97	_	0.0	-
K11	5840	7	4.46	0.02	1.00	0.02	0.063	0.007
HD1178	5644	10	4.34	0.03	0.89	0.03	0.013	0.010
HD10145	5627	20	4.33	0.05	0.81	0.06	-0.017	0.021
HD16623	5833	47	4.51	0.09	1.07	0.10	-0.434	0.034
HD20329	5592	16	4.32	0.04	0.80	0.05	-0.094	0.015
HD21727	5608	21	4.32	0.06	0.82	0.07	0.010	0.020
HD21774	5757	27	4.33	0.06	0.99	0.06	0.251	0.024
HD28474	5808	43	4.60	0.08	1.06	0.10	-0.578	0.030
HD176733	5597	15	4.33	0.04	0.77	0.05	-0.012	0.014
HD191069	5739	29	4.33	0.09	1.03	0.08	-0.029	0.025

TABLE 1
SUMMARY OF DERIVED FUNDAMENTAL STELLAR PROPERTIES.

^aUsed as reference star.

Fig. 2.— Spectra and synthetic fit for Kepler-11 (red) and the Sun (blue) around the Li I 6707.8~Å line.

 $v\sin i$ as the true rotational velocity. This translates to an age of **x** using **x**, or **x** from ?'s updated relation.

4.2. Lithium Abundance

The lithium abundance of Kepler-11 was measured by synthesizing the Li I 6707.8 Å line with MOOG synth. The line list was adopted from ? and includes blends of atomic and molecular lines. We find a lithium abundance of $A(\text{Li}) = 1.26 \pm 0.05$, higher than the solar value of 1.11 at the level of 3σ (Figure 2). This implies a sub-solar age.

4.3. [Y/Mg] Abundance Ratio

Recent works by ? and ? have identified the ratio of yttrium to magnesium abundances as an excellent proxy for age in main-sequence Sun-like stars. We measured these abundances as described in Section 5 and found a [Y/Mg] ratio of \mathbf{x} . Using the age relation from ?, this suggests an age of 4.0 ± 0.7 Gyr.

4.4. Chromospheric Emission

We measured the chromospheric emission level of Kepler-11 using the Ca II H&K lines in the spectrum.

5. STELLAR ABUNDANCES

We measured photospheric abundances using the curve-of-growth technique for 20 other elements (excluding lithium, whose synthesis-based abundance determination is discussed in Section 4.2). As with the iron lines, all equivalent widths were measured by hand and lineby-line differential abundances determined with MOOG using q^2 . The line list was adapted from (details). Hyperfine structure corrections were applied for Co I, Cu I, Mn I, V I, and Y II following (cite). Carbon abundances were measured by a combination of C I and CH lines. Errors on the final abundances were found by adding in quadrature the intrinsic scatter of the lines and the uncertainty propagated from errors on the stellar parameters, as described in (). The measured equivalent widths are given in Table 2, and resulting abundances for all stars are in Table 3.

Kepler-11's status as a solar twin enables direct comparison of its abundance pattern to that of the Sun and other known solar twins. Of particular interest is the

question of trends in elemental abundances with condensation temperature (T_c) . As shown by ?, the solar abundance pattern is unusual in its depletion of refractory elements relative to volatiles. This depletion has been interpreted as "missing" rocky material that is locked up in the Solar System planets (?). Building up the number of stars with precisely characterized abundance patterns and planetary systems can help to test this possibility.

We apply corrections for the effects of galactic chemical evolution (GCE), which can change the abundance patterns and T_c trends of stars at varying ages (??). We correct each abundance [X/H] using the prescription of ?, who fit hyperbolic relations to [X/H] as a function of stellar age for a sample of solar twins. We then use the corrected abundances and T_c values from Table 8 of ? to search for a trend. For this part of the analysis, all measured states of a given element (e.g. CI and CH, TiI and TiII, etc.) were combined with a weighted average for the overall elemental abundance.

Based on our analysis, Kepler-11 appears to be a "typical" solar twin: that is, its abundance pattern is enhanced in refractories relative to the solar pattern (Figure 3). The significance of this enhancement depends on the stellar age adopted for the GCE correction. Without GCE correction applied, the T_c slope is significant only at the 2σ level, whereas adopting an age of 2.8 Gyr enhances the slope to nearly 5σ . (compare to Melendez2009)

6. STELLAR PROPERTIES FROM TRANSIT & TTV ANALYSIS

7. DISCUSSION

7.1. Discrepancies in Stellar Densities

The stellar densities found through spectroscopic characterization (1.47 \pm 0.09 g cm⁻³) and photodynamical modeling (1.13 \pm 0.07 g cm⁻³) are inconsistent at the level of $\sim 3\sigma$. While spectroscopically-derived densities can be strongly dependent on imperfect stellar isochrone models, we note that in this case Kepler-11's extreme similarity to the Sun places it near the anchor point of most models, increasing the accuracy of isochronal analysis. Moreover, multiple independent methods support the result of a young, non-evolved age and therefore a solar-like density for Kepler-11.

An alternative hypothesis is that some bias in the transit analysis has resulted in an erroneously low inferred stellar density. As described by ?, multiple effects can bias the density measured by transits, including stel-

4 Bedell et al.

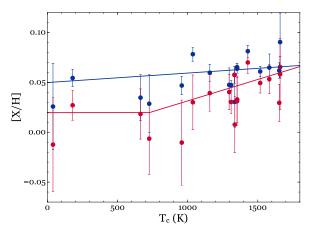


Fig. 3.— Differential element abundances of Kepler-11 as a function of the condensation temperature of the element within the protoplanetary disk. The spectral abundances are plotted in blue, and abundances after a GCE correction is applied are in red. Best-fit models were derived using a

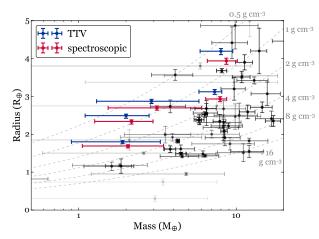


FIG. 4.— Exoplanets with measured masses and radii. Transparencies of the black points scale with the relative error on planet parameters. Kepler-11 a-e are plotted in red (using the transit and TTV-derived parameters) and blue (adjusted by the spectroscopic stellar parameters). Dashed lines show fixed mean densities.

lar activity, blended background sources, and non-zero planet eccentricities. (discuss in detail)

7.2. Implications for Planets

The mass and radius of Kepler-11 has considerable repercussions for its planetary system. We approximate the planet mass derived from TTVs as a linear function of the assumed stellar mass. The planet radius also has a linear dependence on stellar radius, since only the relative surface areas of planet and star can be measured by the transit depth. The stellar properties obtained through spectroscopic analysis therefore raise the planet masses by a factor of 8% and lower the planet radii by a factor of 6% relative to the transit and TTV-derived values. The results are shown in Figure 4.

Adopting the stellar properties from spectroscopic analysis raises the mean densities of the Kepler-11 planets by $\sim 30\%$. This change may go a long way in resolving...

8. CONCLUSION

Using an extremely high-quality spectrum of the multiplanet host star Kepler-11, we have...

M.B. is supported by a National Science Foundation Graduate Research Fellowship under Grant No. DGE-1144082. J.L.B. acknowledges support for this work from the NSF (grant number AST-1313119) and the Alfred P. Sloan Foundation. J.M. thanks FAPESP (2012/24392-2).

Facilities: Keck:I (HIRES), Kepler

REFERENCES

Adibekyan, V. Z., Delgado Mena, E., Sousa, S. G., et al. 2012a, A&A, 547, A36

Adibekyan, V. Z., Sousa, S. G., Santos, N. C., et al. 2012b, A&A, 545, A32

Bedell, M., Meléndez, J., Bean, J. L., et al. 2014, ApJ, 795, 23
Bensby, T., Feltzing, S., & Oey, M. S. 2014, A&A, 562, A71
Chambers, J. E. 2010, ApJ, 724, 92

dos Santos, L. A., Meléndez, J., do Nascimento, Jr., J.-D., et al. 2016, A&A, arXiv:1606.06214

Epstein, C. R., Johnson, J. a., Dong, S., et al. 2010, The Astrophysical Journal, 709, 447

Hands, T. O., Alexander, R. D., & Dehnen, W. 2014, MNRAS, 445, 749

Ikoma, M., & Hori, Y. 2012, ApJ, 753, 66 Kipping, D. M. 2014, MNRAS, 440, 2164

Lissauer, J. J., Fabrycky, D. C., Ford, E. B., et al. 2011, Nature, 470, 53

Kepler-115

- Lissauer, J. J., Jontof-Hutter, D., Rowe, J. F., et al. 2013, ApJ,
- Lodders, K. 2003, ApJ, 591, 1220 Mahajan, N., & Wu, Y. 2014, ApJ, 795, 32
- Meléndez, J., Asplund, M., Gustafsson, B., & Yong, D. 2009, ApJ, 704, L66
- Meléndez, J., Bergemann, M., Cohen, J. G., et al. 2012, A&A, 543, A29
- Migaszewski, C., Słonina, M., & Goździewski, K. 2012, MNRAS, 427, 770
- Nissen, P. E. 2015, A&A, 579, A52
- Ramírez, I., Meléndez, J., Bean, J., et al. 2014, A&A, 572, A48

- Rowe, J. F., Bryson, S. T., Marcy, G. W., et al. 2014, ApJ, 784,
- Sneden, C. A. 1973, PhD thesis, THE UNIVERSITY OF TEXAS AT AUSTIN.
- Spina, L., Meléndez, J., Karakas, A. I., et al. 2016a, A&A
- Spina, L., Meléndez, J., & Ramírez, I. 2016b, A&A, 585, A152
- Tucci Maia, M., Ramírez, I., Meléndez, J., et al. 2016, A&A, 590, A32
- Valenti, J. A., & Piskunov, N. 1996, A&AS, 118, 595

6 Bedell et al.

TABLE 2 LINE LIST AND MEASURED EQUIVALENT WIDTHS.

,	Wavelength	Species	EP	$\log(gf)$	Kepler-11	HD1178	HD10145	HD16623	HD20329	HD21727	HD21774	HD28474	HD176733	HD191069
:)TE	VOTE. — Table 2 is published in its	ublished	in its en	(ev) n its entirety in t	he	electronic edition of ApJ	(IIIA) (III f ApJ. A portion	rtion is show	is shown here for guidance r	ll se	arding its	form and cont	tent.	(MIIIA)

TABLE 3 DIFFERENTIAL ABUNDANCES [X/H].

							FeI																		Element N
ယ	υī	ဃ	4	20	6	17	92	∞	ĊΠ	10	9	11	18	ĊΠ	4	11	Ľ	4	14	2	ĊΠ	4	ဃ	4	N_{lines}
+	+	\mathbb{H}	\mathbb{H}	+	+	+	0.06 ± 0.03	+	+	+	+	\mathbb{H}	+	+	\mathbb{H}	+	+	+	+	+	+	+	\mathbb{H}	+	$_{ m Kepler-11}$
0.03 ± 0.12	-0.01 ± 0.01	0.05 ± 0.02	0.08 ± 0.03	0.00 ± 0.07	0.05 ± 0.04	0.02 ± 0.05	0.02 ± 0.04	-0.04 ± 0.03	0.01 ± 0.02	0.02 ± 0.03	0.07 ± 0.02	0.11 ± 0.05	0.12 ± 0.03	0.14 ± 0.06	0.09 ± 0.03	0.02 ± 0.14	0.07 ± 0.00	0.10 ± 0.04	0.04 ± 0.03	0.18 ± 0.02	0.39 ± 0.48	-0.03 ± 0.02	0.18 ± 0.08	0.12 ± 0.04	HD1178
-0.04 ± 0.13	-0.05 ± 0.03	0.01 ± 0.04	-0.02 ± 0.02	-0.03 ± 0.03	-0.04 ± 0.03	-0.02 ± 0.11	-0.02 ± 0.06	-0.07 ± 0.04	-0.02 ± 0.05	0.01 ± 0.07	-0.02 ± 0.03	0.01 ± 0.09	0.05 ± 0.05	0.03 ± 0.02	0.02 ± 0.03	-0.05 ± 0.17	0.02 ± 0.00	0.05 ± 0.03	-0.00 ± 0.01	0.03 ± 0.00	0.34 ± 0.48	-0.12 ± 0.05	0.08 ± 0.02	0.06 ± 0.12	HD10145
+	+	+	+	+	+	\vdash	-0.43 ± 0.09	\mathbb{H}	+	\vdash	+	+	+	+	+	\mathbb{H}	+	+	\vdash	+	+	+	+	\vdash	HD16623
-0.17 ± 0.09	-0.12 ± 0.03	0.07 ± 0.02	0.00 ± 0.01	-0.05 ± 0.04	0.01 ± 0.03	-0.10 ± 0.05	-0.09 ± 0.05	-0.18 ± 0.02	-0.08 ± 0.02	-0.06 ± 0.03	0.08 ± 0.09	0.11 ± 0.03	0.15 ± 0.03	0.14 ± 0.06	0.06 ± 0.06	0.18 ± 0.24	0.03 ± 0.00	0.03 ± 0.09	0.04 ± 0.05	0.18 ± 0.02	0.12 ± 0.20	-0.04 ± 0.04	0.18 ± 0.03	0.05 ± 0.08	HD20329
-0.05 ± 0.09	-0.04 ± 0.02	-0.00 ± 0.03	-0.00 ± 0.02	0.01 ± 0.05	-0.01 ± 0.03	0.00 ± 0.04	0.01 ± 0.08	-0.04 ± 0.03	0.01 ± 0.03	0.02 ± 0.03	0.04 ± 0.03	0.01 ± 0.10	0.07 ± 0.04	0.10 ± 0.05	0.03 ± 0.03	0.04 ± 0.15	0.01 ± 0.00	0.01 ± 0.03	0.02 ± 0.03	0.08 ± 0.00	0.35 ± 0.47	-0.08 ± 0.03	0.07 ± 0.03		HD21727
0.24 ± 0.05	0.23 ± 0.01	0.28 ± 0.05	0.32 ± 0.03	0.31 ± 0.16	0.26 ± 0.01	0.25 ± 0.03	0.25 ± 0.08	0.30 ± 0.03	0.24 ± 0.03	0.27 ± 0.03	0.28 ± 0.02	0.26 ± 0.04	0.24 ± 0.04	0.32 ± 0.02	0.27 ± 0.03	0.19 ± 0.08	0.15 ± 0.00	0.24 ± 0.03	0.25 ± 0.02	0.28 ± 0.01	0.36 ± 0.16	0.27 ± 0.03	0.20 ± 0.02	0.18 ± 0.04	HD21774
-0.65 ± 0.14	-0.61 ± 0.04	-0.52 ± 0.09	-0.59 ± 0.09	-0.60 ± 0.03	-0.45 ± 0.03	-0.58 ± 0.07	-0.58 ± 0.08	-0.75 ± 0.06	-0.55 ± 0.05	-0.60 ± 0.06	-0.48 ± 0.04	-0.37 ± 0.04	-0.41 ± 0.03	-0.41 ± 0.05	-0.33 ± 0.08	-0.47 ± 0.06	-0.42 ± 0.00	-0.36 ± 0.09	-0.44 ± 0.04	-0.45 ± 0.01	-0.27 ± 0.54	-0.54 ± 0.05	-0.25 ± 0.02	-0.07 ± 0.45	HD28474
-0.08 ± 0.29	-0.04 ± 0.03	0.00 ± 0.02	0.06 ± 0.03	0.00 ± 0.05	-0.02 ± 0.01	-0.02 ± 0.03	-0.01 ± 0.05	-0.02 ± 0.03	-0.03 ± 0.04	0.01 ± 0.03	-0.00 ± 0.02	-0.02 ± 0.03	0.02 ± 0.03	-0.00 ± 0.02	-0.01 ± 0.04	-0.07 ± 0.20	-0.00 ± 0.00	0.02 ± 0.05	-0.01 ± 0.02	0.04 ± 0.00	0.32 ± 0.48	-0.03 ± 0.03	0.05 ± 0.03	-0.00 ± 0.05	HD176733
0.04 ± 0.08	-0.08 ± 0.01	0.08 ± 0.02	0.06 ± 0.02	-0.01 ± 0.02	0.06 ± 0.02	-0.03 ± 0.04	-0.03 ± 0.09	-0.08 ± 0.02	-0.02 ± 0.02	-0.02 ± 0.02	0.04 ± 0.02	0.11 ± 0.04	0.08 ± 0.02	0.12 ± 0.04	0.08 ± 0.01	0.04 ± 0.03	0.08 ± 0.00	0.09 ± 0.05	0.04 ± 0.01	0.11 ± 0.01	0.35 ± 0.49	-0.01 ± 0.02	0.14 ± 0.02	0.07 ± 0.03	HD191069