

# Benchmarking Evaluation Metrics for Tubular Structure Segmentation in Biomedical Images

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JSPS



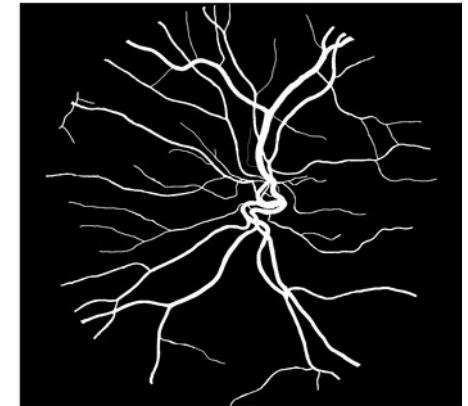
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ShapeMI MICCAI Workshop, 27<sup>th</sup> Sept. 2025

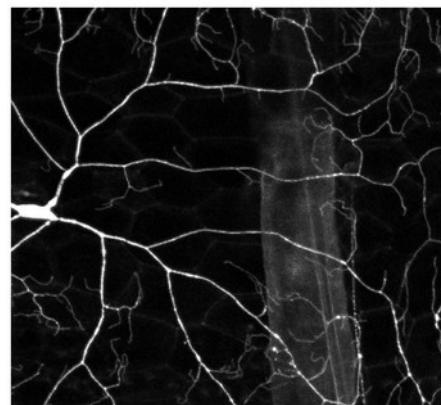
# Introduction

- **Tubular tree-like structures** are common in biology and medicine : vascular networks airways, neuronal trees
- The **segmentation** of these structures is crucial for many downstream applications : tracing, numerical simulation

retinal images



neuron microscopy image



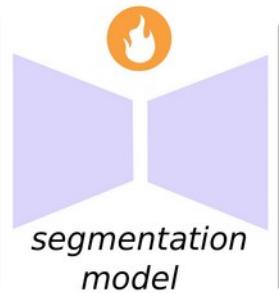
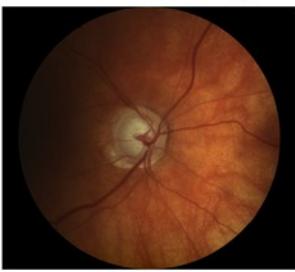
*Figure 1. Example of biomedical images showing tubular, tree-like structures and the target segmentation.*

# Introduction

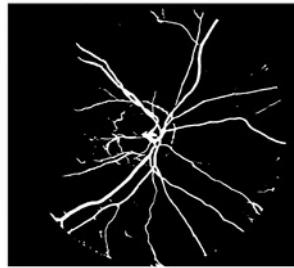
- Deep learning has led to tremendous progress in biomedical image segmentation.

## 1) model training

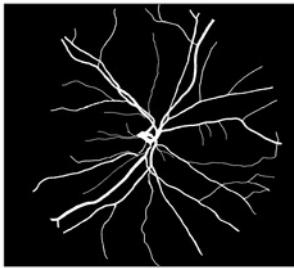
*train set image*



*prediction  $P$*

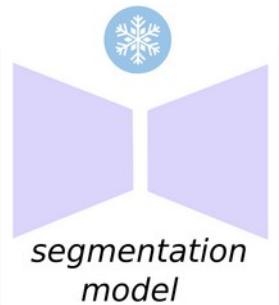


*label  $L$*

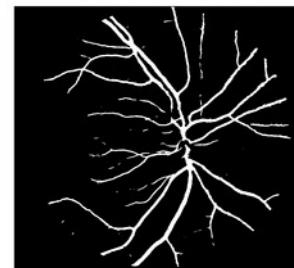


## 2) model evaluation

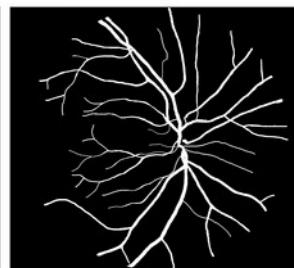
*test set image*



*prediction  $P$*



*label  $L$*



*Figure 2. Importance of quality metrics.*

# Introduction

- To **train and evaluate** segmentation models, we need to design **metrics** measuring the **quality** of a predicted segmentation compared to the ground-truth labels.

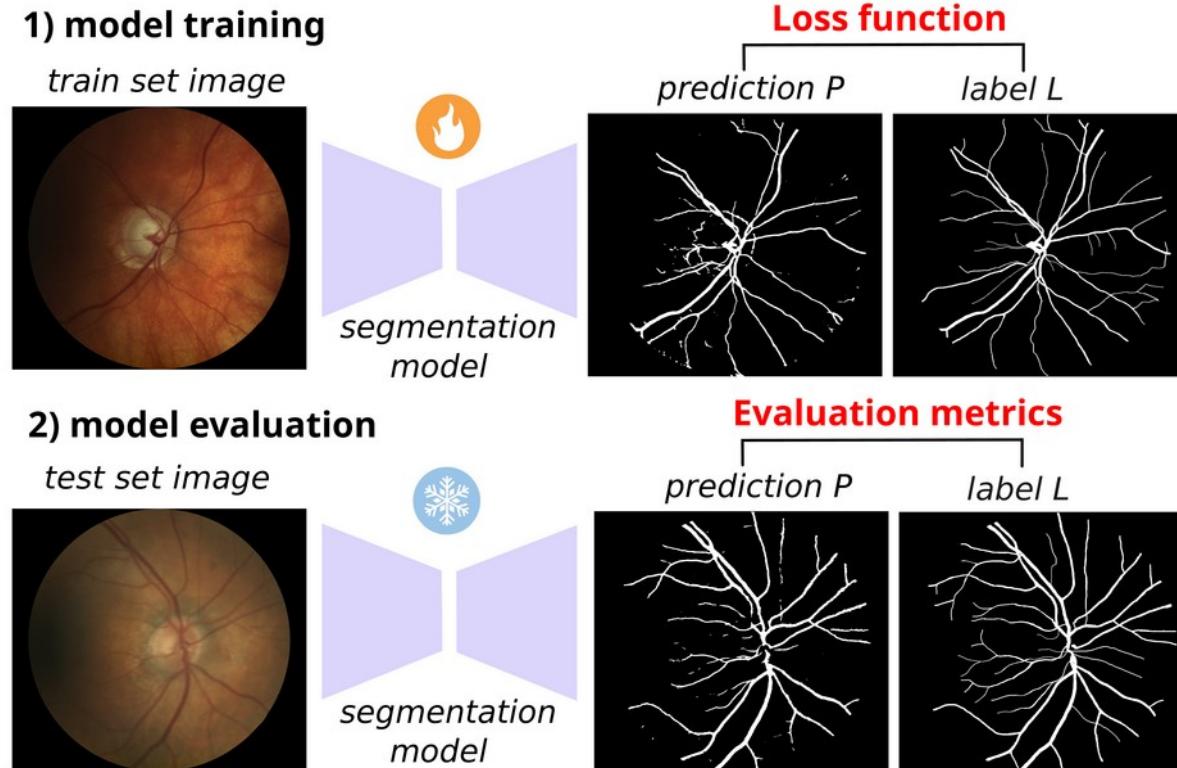
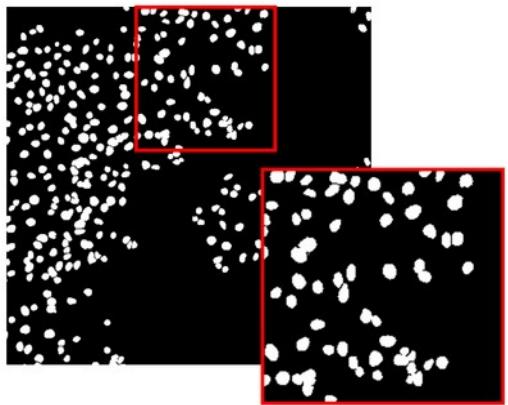


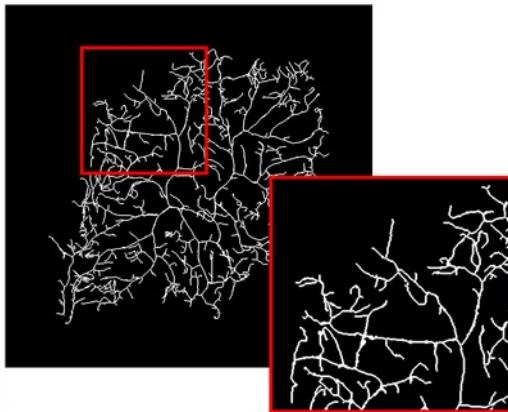
Figure 2. Importance of quality metrics.

# Introduction

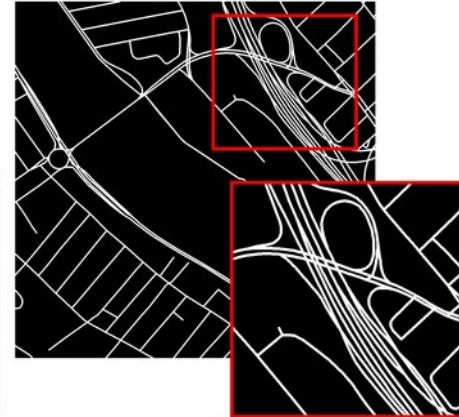
- Tubular structure segmentation offers unique **challenges**, leading to the design of **various metrics and loss functions** in recent years.



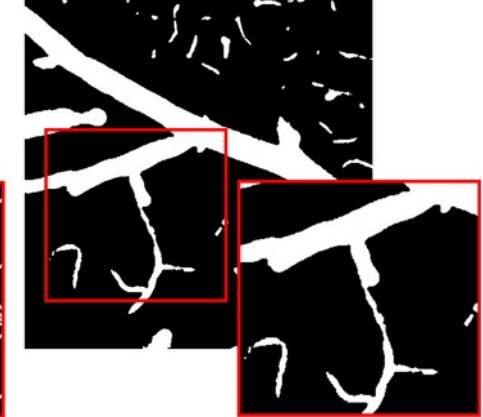
multiple objects



thin branches



close branches

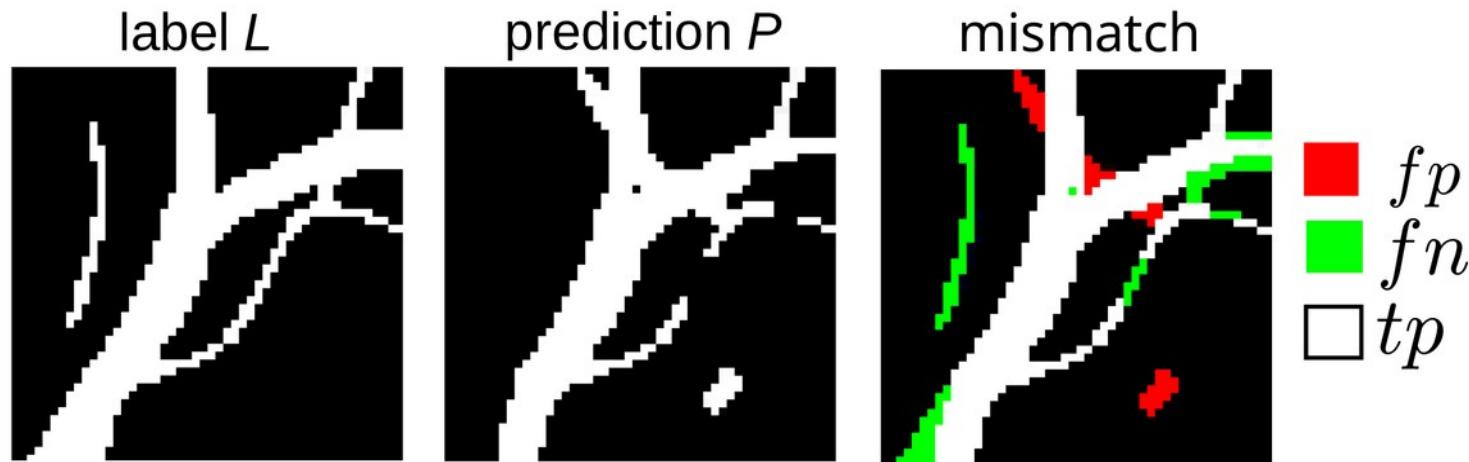


branch size imbalance

*Figure 3. Challenges of tubular structure segmentation.*

## Introduction – Overlap-based quality metrics

- The **Dice** score is based on the pixel-wise mismatch between label and prediction.



*Figure 4. Illustration of the Dice calculation.  
( $tp$  = true positives,  $fn$  = false,  $fp$  = false postives)*

# Introduction – Skeleton-based quality metrics

- The **cIDice**<sup>1</sup> relies on the **skeleton** mismatch.
- The **cbDice**<sup>2</sup> includes the **distance to boundaries**.

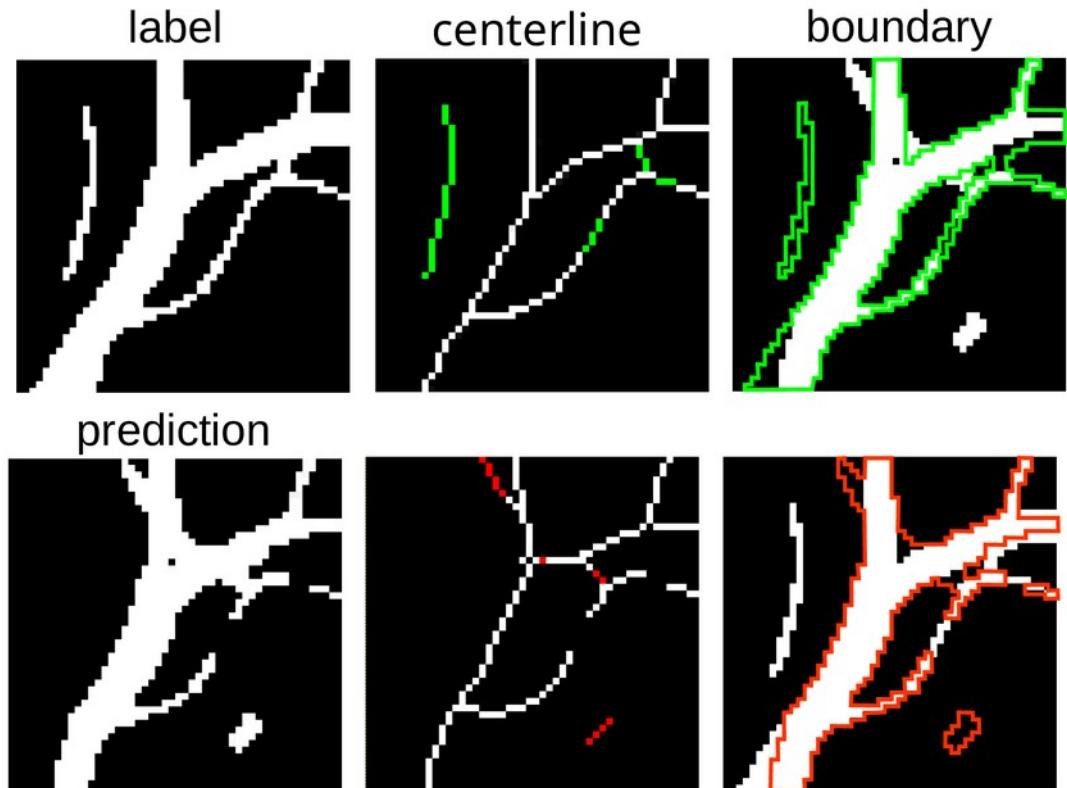


Figure 5. Illustration of the cIDice and cbDice.

## Introduction – Algebraic topology quality metrics

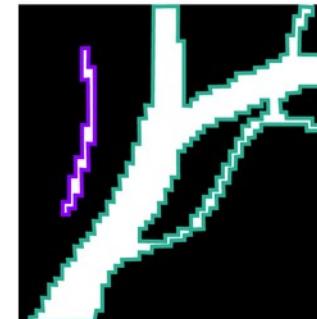
$\beta_0$  = number of **connected components CC**

$\beta_1$  = number of **holes** in the image

- The **Betti error**  $\beta^{err}$  is the difference between the Betti numbers of the label and prediction.

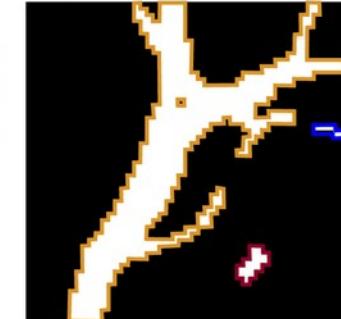
### a) connected components

$$\beta_0(L) = 2$$



label  $L$

$$\beta_0(P) = 3$$



prediction  $P$

$$\beta_0^{err} = 1$$

### b) holes

$$\beta_1(L) = 1$$



label  $L$

$$\beta_1(P) = 1$$



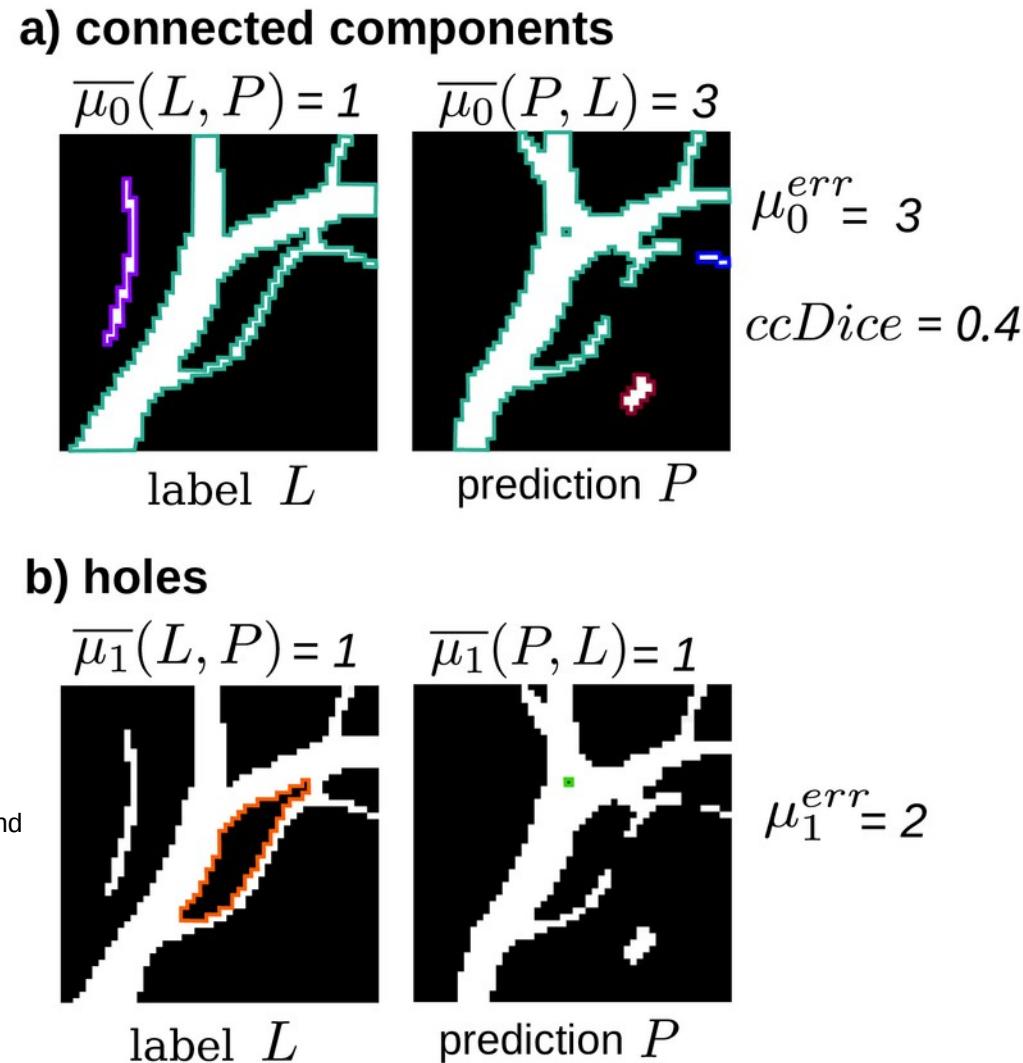
prediction  $P$

$$\beta_1^{err} = 0$$

Figure 6. Illustration of the Betti error calculation.

## Introduction – Algebraic topology quality metrics

- The **Betti matching error**<sup>3</sup>  $\mu^{err}$  and the **ccDice**<sup>4</sup> are matching CC and holes.



<sup>3</sup>Stucki, Nico, et al. "Topologically faithful image segmentation via induced matching of persistence barcodes." International Conference on Machine Learning, 2023.

<sup>4</sup>Rougé, Pierre, Odyssée Merveille, and Nicolas Passat. "ccDice: A topology-aware Dice score based on connected components." International Workshop on Topology-and Graph-Informed Imaging Informatics, MICCAI 2024.

*Figure 7. Illustration of the Betti matching and ccDice calculation.*

## Challenge

- Which metric / loss shall I use? How to be sure than the metric reflects my expectations?  
→ Quality is **subjective**, making it difficult to assess the **strengths and weaknesses** of each metric.

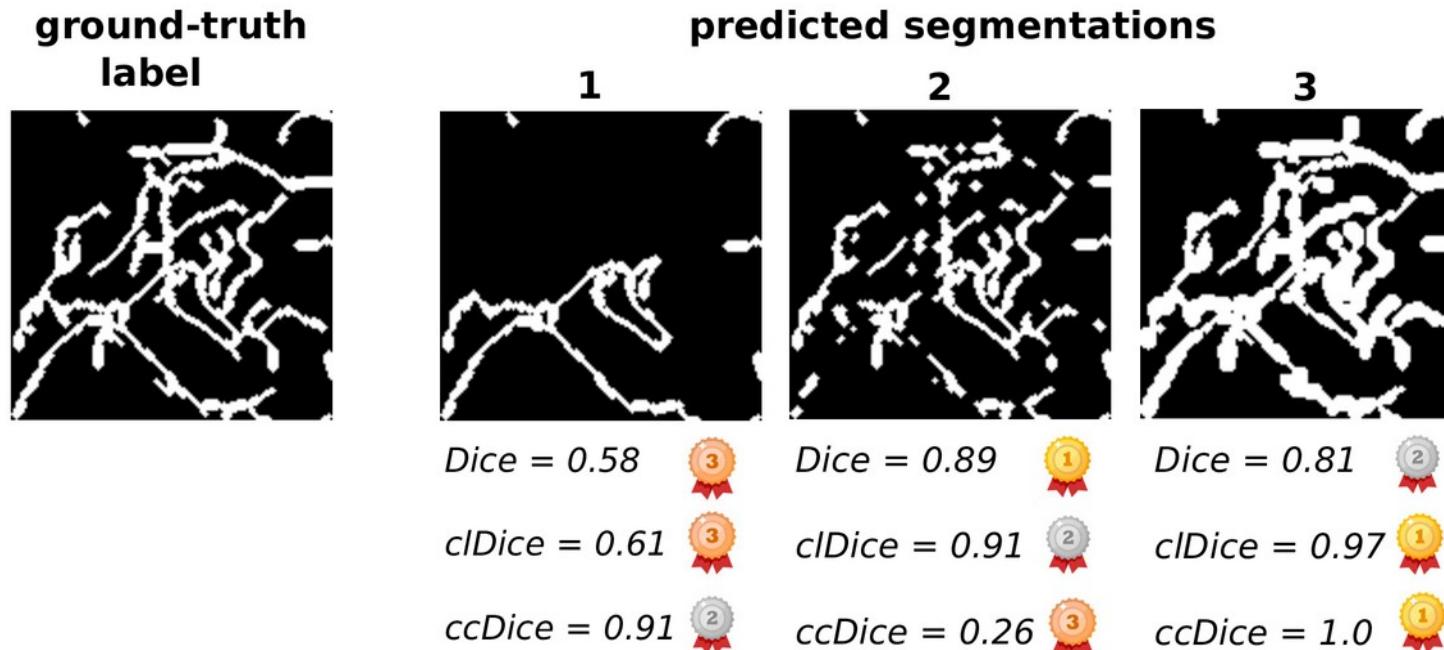


Figure 8. Which is the best segmentation?

# State-of-the-art

## How to evaluate quality metrics?

- 1) Use handcrafted examples to show the metric behavior in specific cases<sup>2,4</sup>
- 2) Ask experts to identify pitfalls and make recommendations (*Metrics Reloaded project*)<sup>5,6</sup>
- 3) Evaluate metrics based on their correlation to subjective visual scores attributed by experts<sup>7</sup>

<sup>5</sup>Maier-Hein, Lena, et al. "Metrics reloaded: recommendations for image analysis validation." *Nature methods*, 2024

<sup>6</sup>Reinke, Annika, et al. "Understanding metric-related pitfalls in image analysis validation." *Nature methods*, 2024

<sup>7</sup>Aydin, Orhun Utku, et al. "An evaluation of performance measures for arterial brain vessel segmentation." *BMC medical imaging*, 2021

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### Limitations

- No study focusing on **topology-preserving metrics** so far
- Relying on **experts** to grade images or identify pitfalls : **time-consuming**, hard to apply to new metrics
- Limited to the **specific contexts**, such as particular application or dataset.

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- ~~Relying on experts to grade images or identify pitfalls : time consuming, hard to apply to new metrics~~
- ~~Limited to the specific contexts, such as particular application or dataset.~~

→ We propose a new approach to benchmark metrics without the need for expert knowledge!

## Proposed approach

- Depending on the application, different segmentation errors have different importance or “**weight**”.

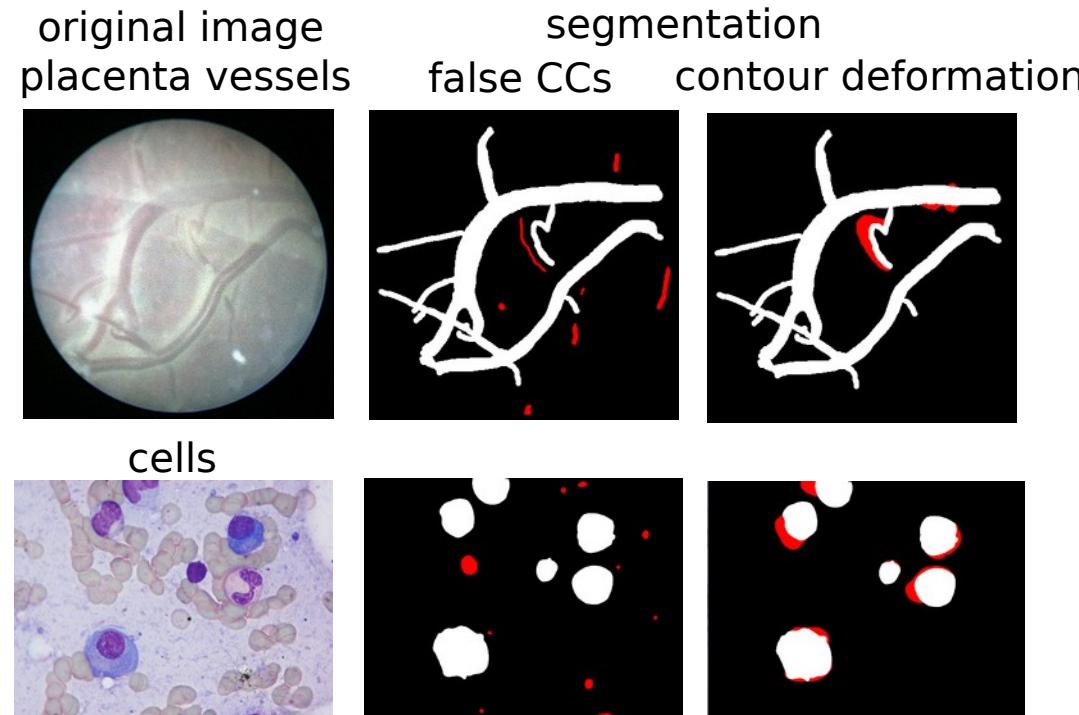


Figure 9. Illustration of different types of segmentation errors. Images from the PSVFM<sup>8</sup> and Neurips 2022 dataset<sup>9</sup>.

<sup>8</sup>Bano, Sophia, et al. "Deep placental vessel segmentation for fetoscopic mosaicking." MICCAI, 2020.

<sup>9</sup>Ma, Jun, et al. "The multimodality cell segmentation challenge: toward universal solutions." Nature methods, 2024

## Proposed approach

- Break down error types into **easily interpretable categories** (e.g. false component, deformation...)
- Estimate the “**weight**” that a given metric attributes to each type of errors.

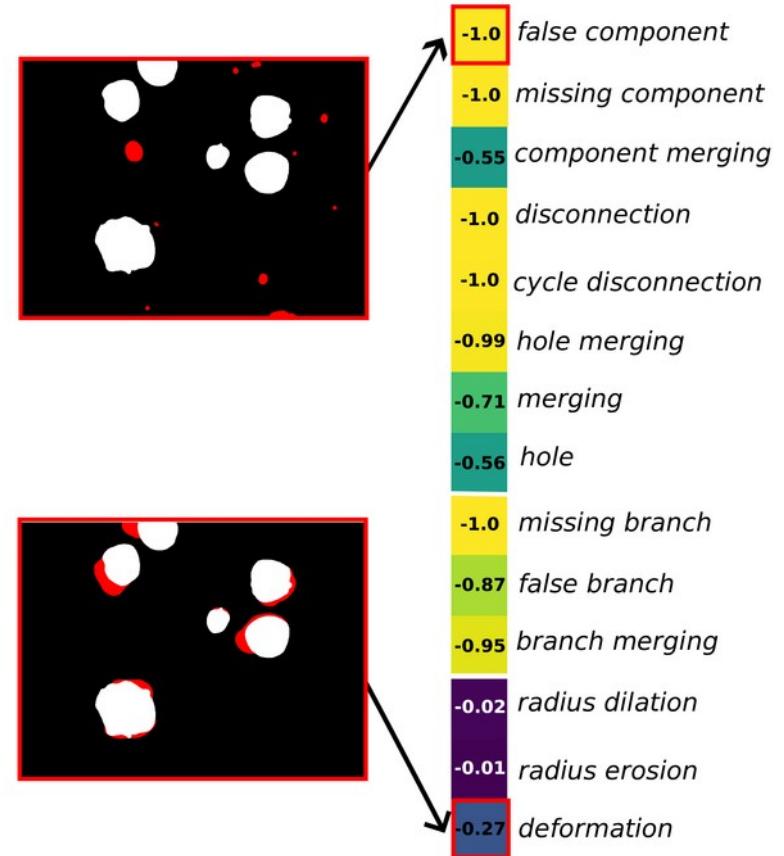


Figure 10. Estimated weights for each type of segmentation errors.

# Proposed approach

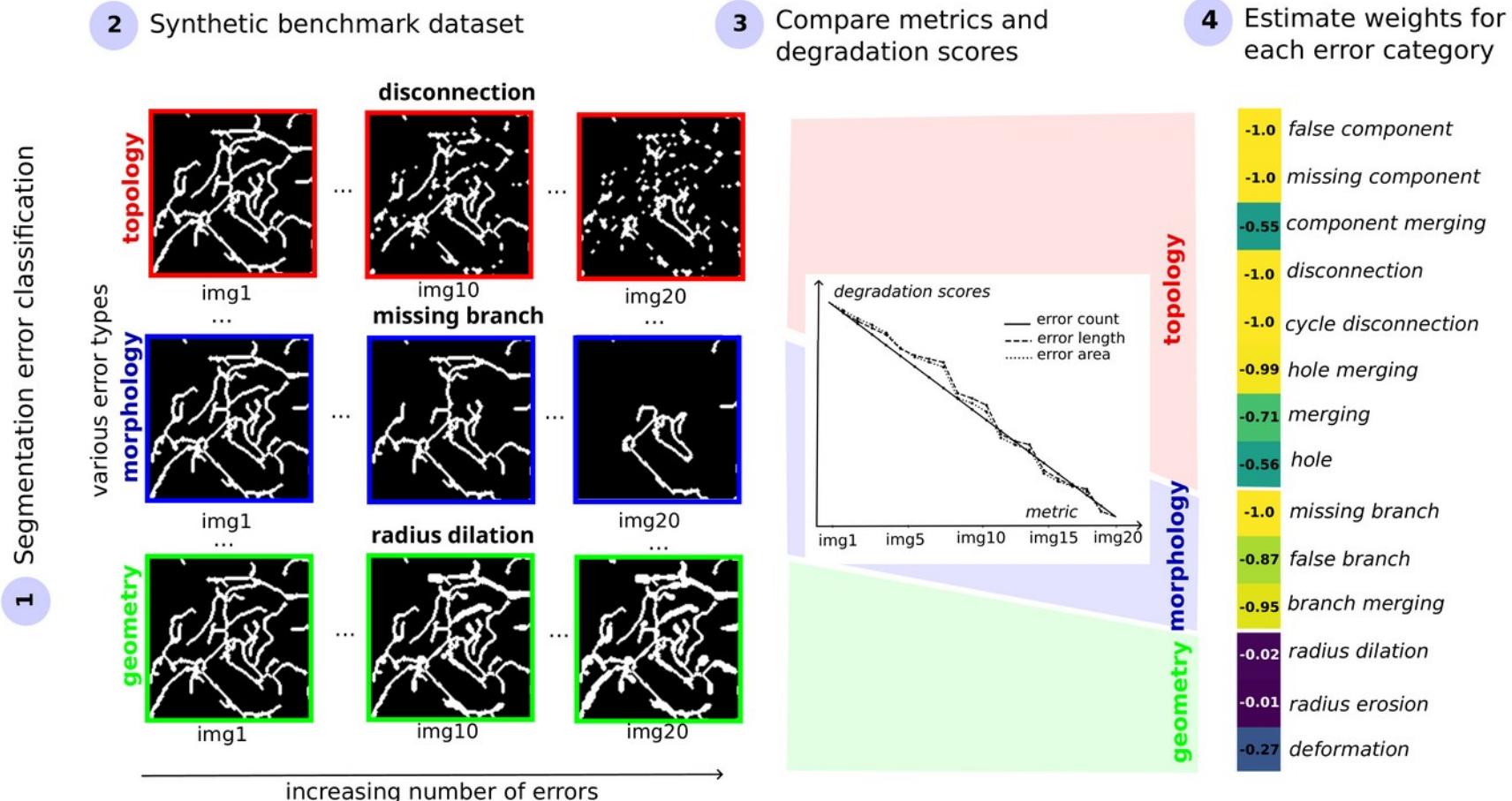


Figure 11. Overview of the proposed method.

# Method – Error classification

- We introduce a new distinction between “**topology**”, “**morphology**” and “**geometry**”.

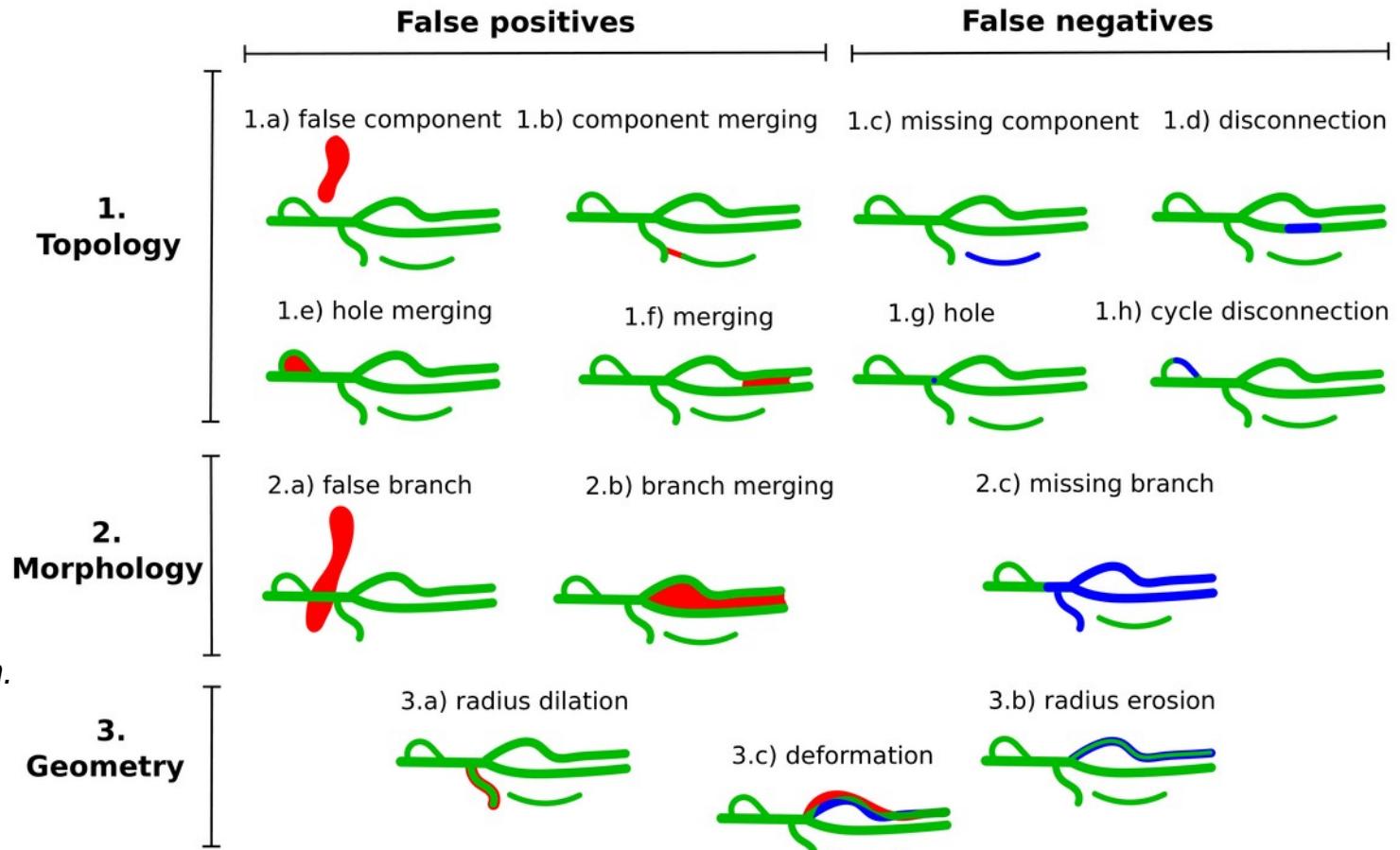
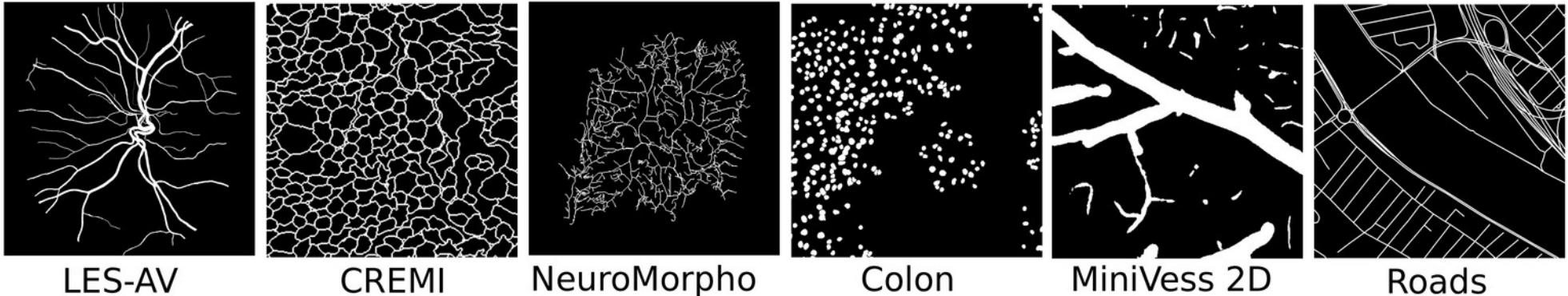


Figure 12. The proposed Segmentation error classification.

## Method – Synthetic benchmark dataset

- We selected 3 labels from 6 public datasets.



<sup>10</sup>Cremi. miccai challenge on circuit reconstruction from electron microscopy images <https://cremi.org/> (2016), accessed: 2024-02-12

<sup>11</sup>Ljosa, V., Sokolnicki, K.L., Carpenter, A.E.: Annotated high-throughput microscopy image sets for validation. *Nature methods*, 2012

<sup>12</sup>Tecuanl, C., Ljungquist, B., Ascoli, G.A.: Accelerating the continuous community sharing of digital neuromorphology data. *FASEB BioAdvances*, 2024

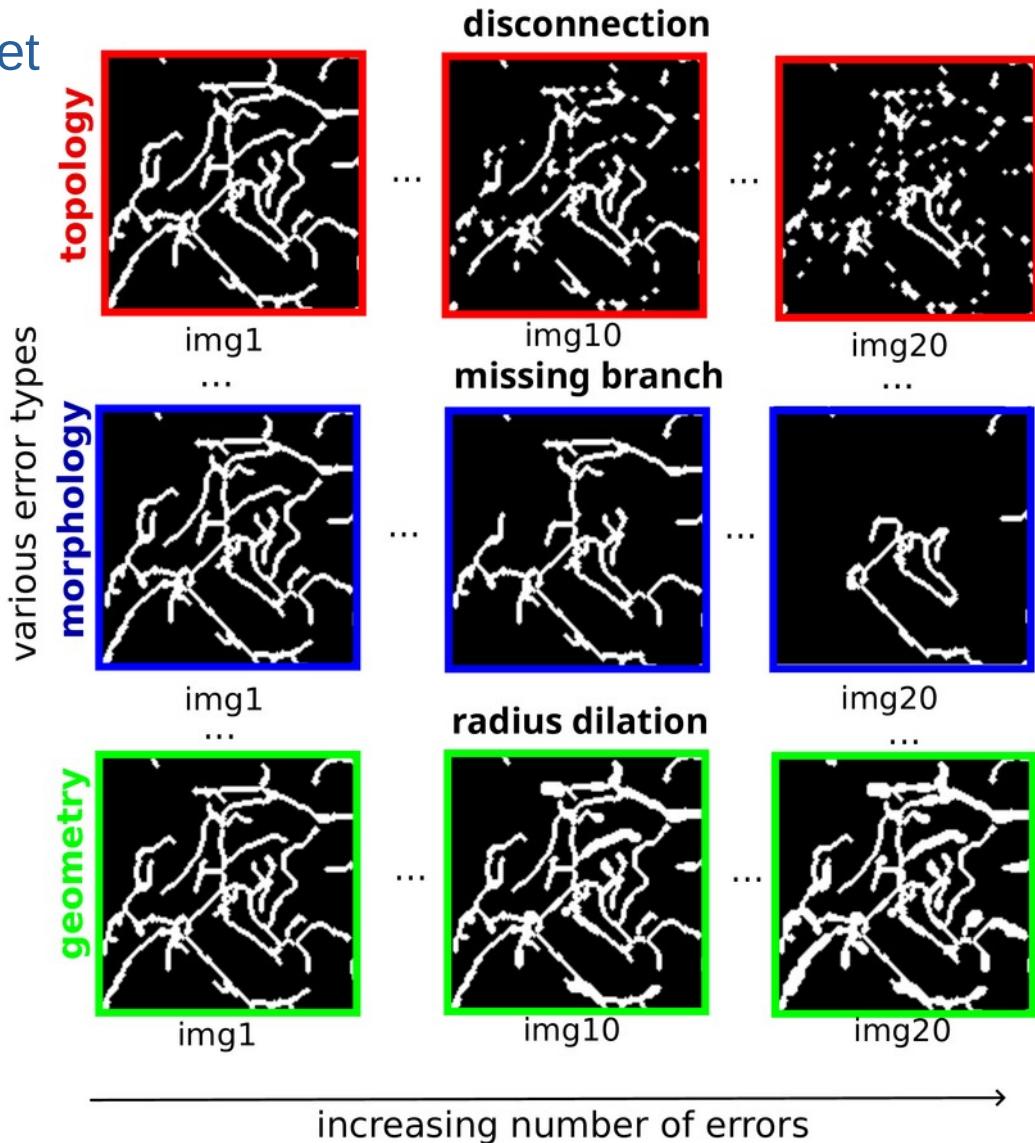
<sup>13</sup>Mnih, V.: Machine Learning for Aerial Image Labeling. Ph.D. thesis, University of Toronto, 2013

<sup>14</sup>Odstrcilik, J., Kolar, R., Budai, A., Hornegger, J., Jan, J., Gazarek, J., Kubena, T., Cernosek, P., Svoboda, O., Angelopoulou, E.: Retinal vessel segmentation by improved matched filtering: evaluation on a new high-resolution fundus image database. *IET Image Processing*, 2013

<sup>15</sup>Poon, C., Teikari, P., Rachmadi, M.F., Skibbe, H., Hyynnen, K.: A dataset of rodent cerebrovasculature from in vivo multiphoton fluorescence microscopy imaging. *Scientific Data*, 2023

## Method – Synthetic benchmark dataset

- We **cumulatively add errors** from each category to mimic predicted segmentations.



## Method – Degradation scores

- We design **degradation scores** to quantify the degradation of synthetic images. We consider three **error properties** : the error “area”, the error “length” and the error “count”.

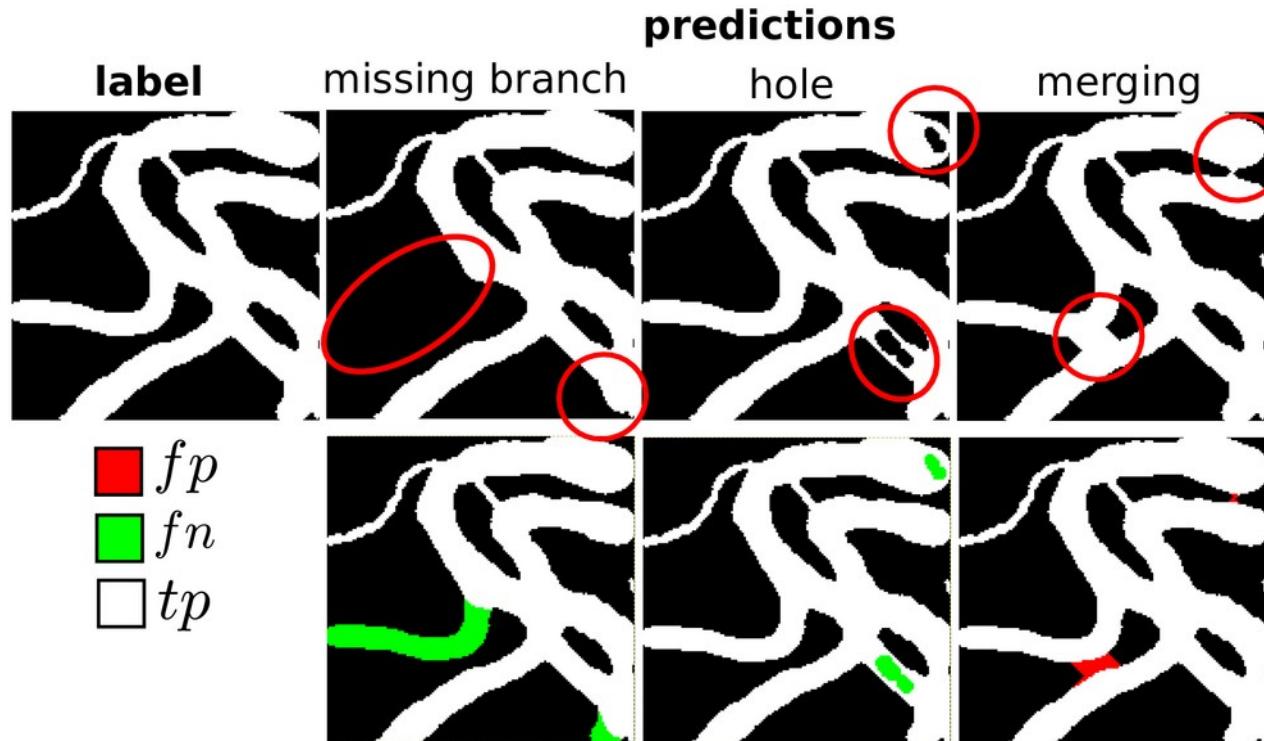


Figure 13. Calculation of the degradation scores for the property “area”.

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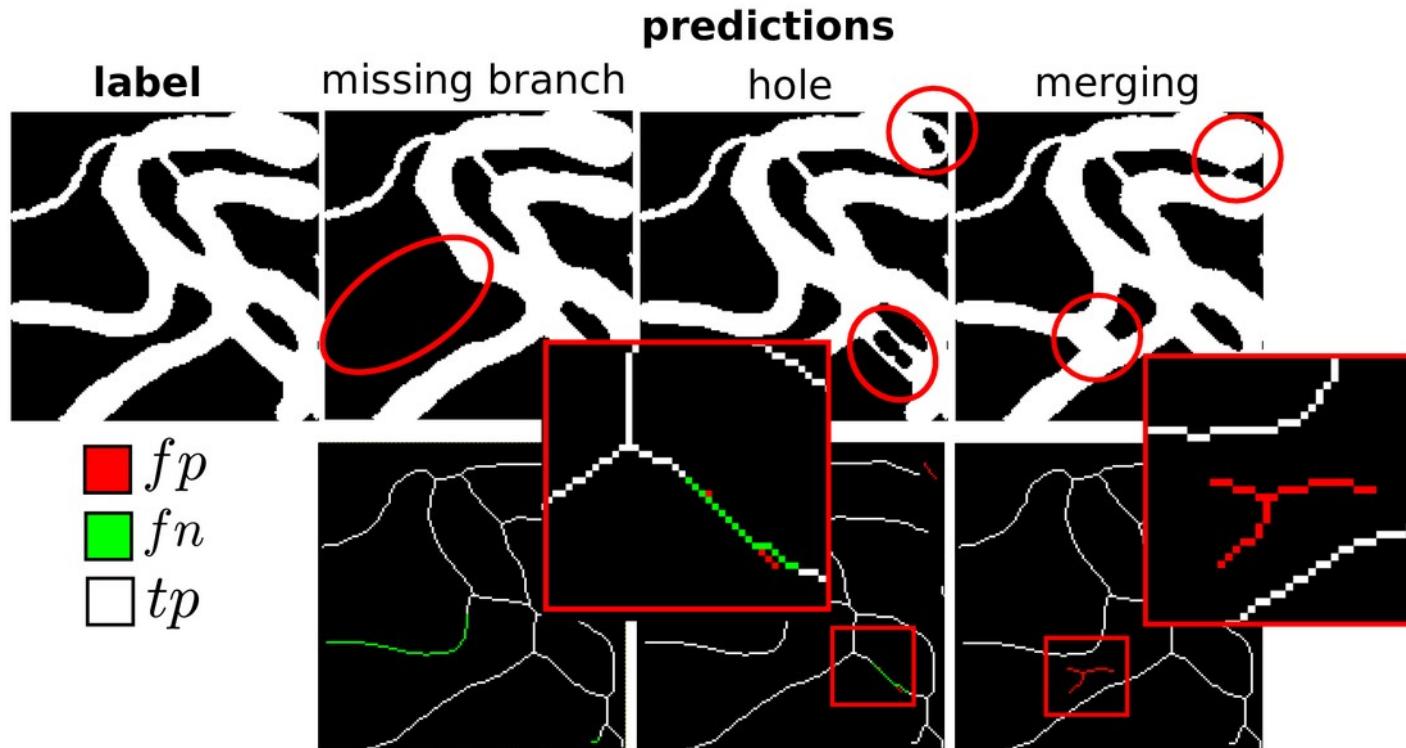
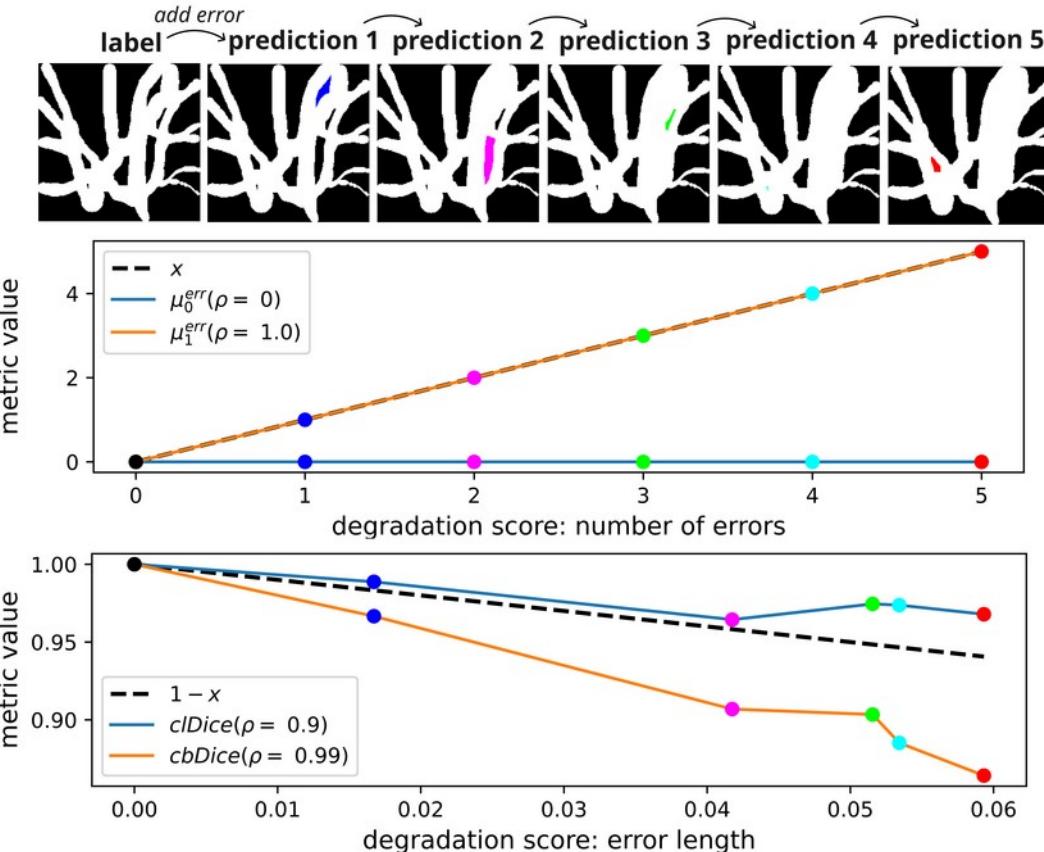


Figure 14. Calculation of the degradation scores for the property “length”.

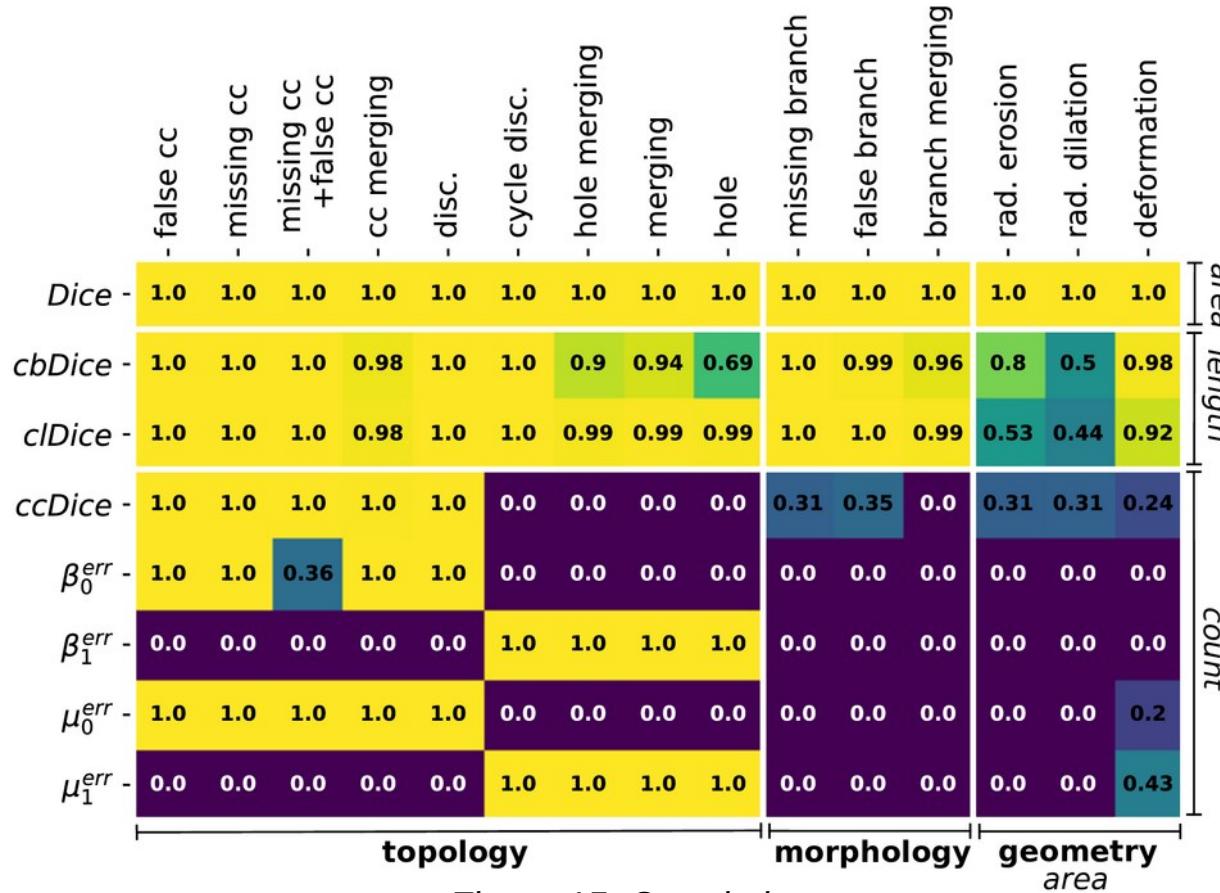
## Method – Correlation and weights estimation



- **Correlation** (absolute Pearson coefficient)
  - = Is the metric sensitive to one type of error ( $\rho = 1$ ) or not ( $\rho = 0$ )?
- **Weight** (slope of fitted linear function)
  - = How strongly does the metric penalize a given type of error?

## Results – Correlation analysis

- ( $\rho = 0$ ) : Does not account for this type of error  
 ( $\rho > 0.9$ ) : Good estimator of the type of error  
 ( $\rho < 0.9$ ) : Influenced by the error (limitation?)



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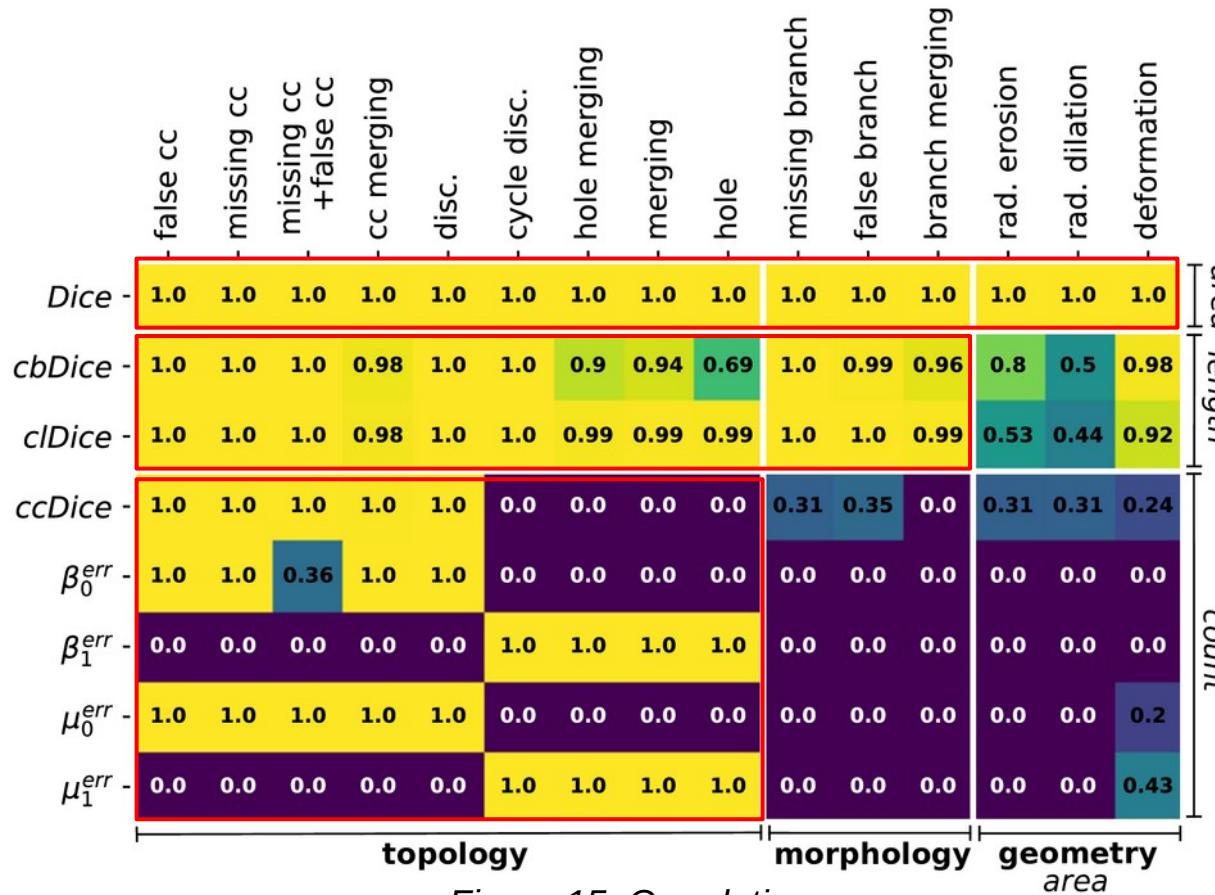


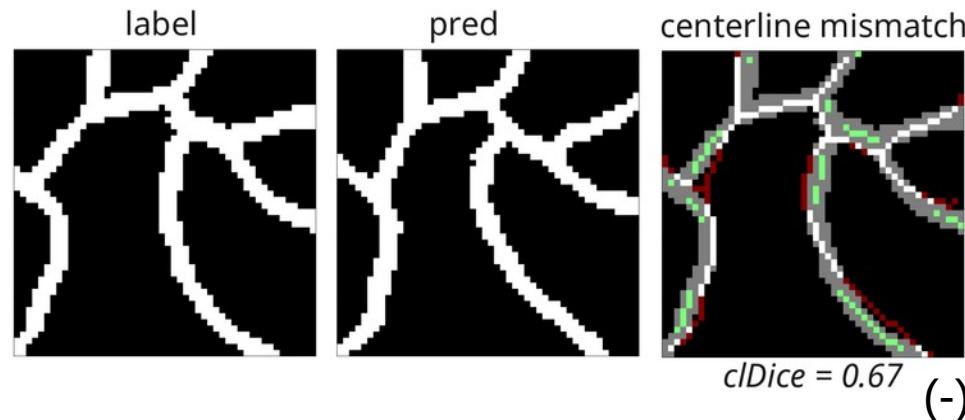
Figure 15. Correlation array.

## Results – Correlation analysis

- The cIDice is affected by **radius change and deformations**.

	corr															
	- false cc	- missing cc	- missing cc	- +false cc	- cc merging	- disc.	- cycle disc.	- hole merging	- merging	- hole	- missing branch	- false branch	- branch merging	- rad. erosion	- rad. dilation	- deformation
<i>cbDice</i>	1.0	1.0	1.0	0.98	1.0	1.0	1.0	0.9	0.94	0.69	1.0	0.99	0.96	0.8	0.5	0.98
<i>cIDice</i>	1.0	1.0	1.0	0.98	1.0	1.0	1.0	0.99	0.99	0.99	1.0	1.0	0.99	0.53	0.44	0.92
weights																
<i>cbDice</i>	-0.98	-0.95	-1.0	-0.51	-1.2	-1.07	-2.59	-1.52	-0.66	-0.98	-0.77	-2.49	0.07	-0.03	-1.35	
<i>cIDice</i>	-1.0	-1.0	-1.0	-0.55	-1.0	-1.0	-0.99	-0.71	-0.56	-1.0	-0.87	-0.95	-0.02	-0.01	-0.27	
	topology						morphology						geometry area			

Figure 16. Correlations and weights for the *cIDice* and *cbDice*.



*Figure 17. Illustration of the clDice behavior.*

## Results – Correlation analysis

- The cIDice may overlook **holes** and **merging**.

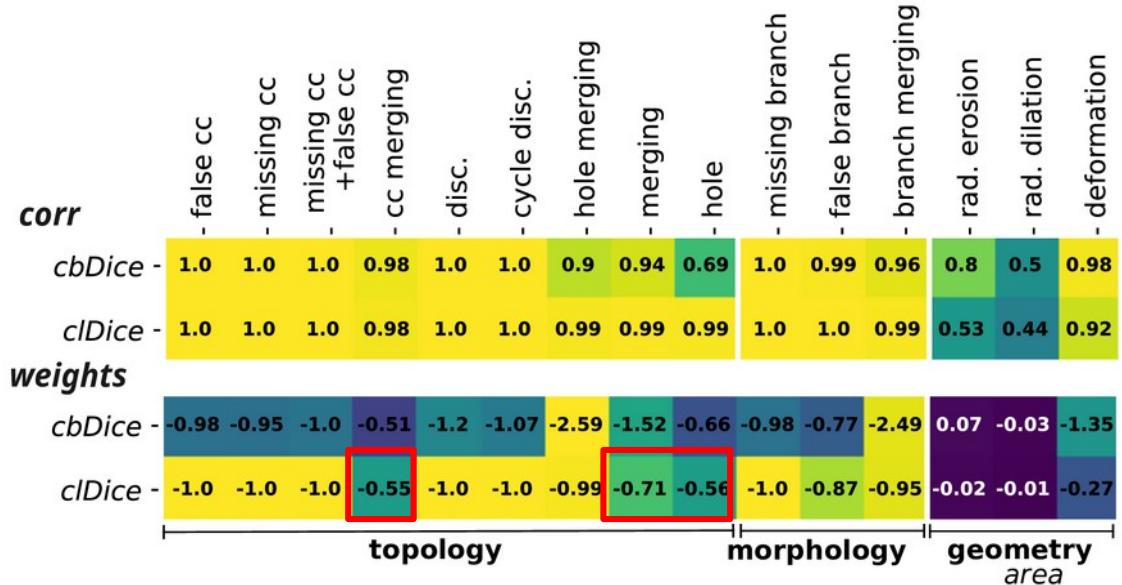


Figure 18. Correlations and weights for the *cIDice* and *cbDice*.

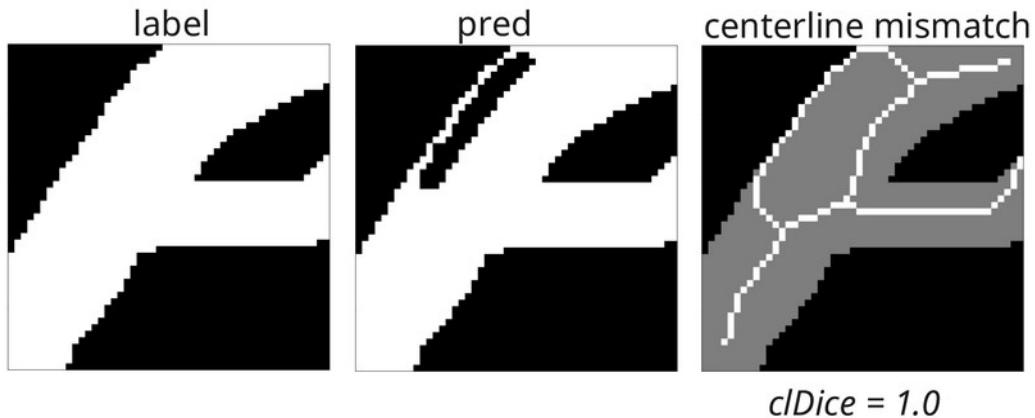


Figure 19. Illustration of the *cIDice* behavior.

## Results – Correlation analysis

- The ccDice and Betti metrics **ignores morphological errors** (e.g. missing branches)

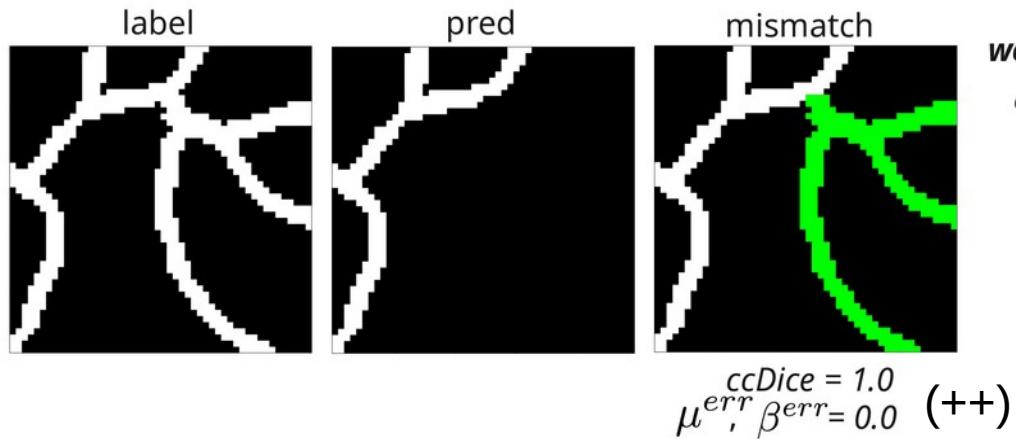


Figure 20. Illustration of the metric's behavior.

<i>corr</i>	- false cc	- missing cc	- missing cc +false cc	- cc merging	- disc.	- cycle disc.	- hole merging	- merging	- hole	- missing branch	- false branch	- branch merging	- rad. erosion	- rad. dilation	- deformation
ccDice	1.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.31	0.35	0.0	0.31	0.31	0.24
$\beta_0^{err}$	1.0	1.0	0.36	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
$\beta_1^{err}$	0.0	0.0	0.0	0.0	0.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0
$\mu_0^{err}$	1.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.2
$\mu_1^{err}$	0.0	0.0	0.0	0.0	0.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.43

<i>weights</i>	topology					morphology				geometry					
	ccDice	$\beta_0^{err}$	$\beta_1^{err}$	$\mu_0^{err}$	$\mu_1^{err}$	ccDice	$\beta_0^{err}$	$\beta_1^{err}$	$\mu_0^{err}$	$\mu_1^{err}$	ccDice	$\beta_0^{err}$	$\beta_1^{err}$	$\mu_0^{err}$	$\mu_1^{err}$
ccDice	-1.0	-1.0	-1.0	-1.19	-1.15	0.0	-0.0	0.0	0.0	-0.05	0.04	-0.0	-0.11	-0.21	-0.45
$\beta_0^{err}$	1.0	1.0	0.14	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
$\beta_1^{err}$	0.0	0.0	0.0	0.0	0.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0
$\mu_0^{err}$	1.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0	0.0
$\mu_1^{err}$	0.0	0.0	0.0	0.0	0.0	1.0	1.0	1.0	1.0	0.0	0.0	0.0	0.0	0.0	0.0

Figure 21. Correlations and weights for the ccDice and Betti metrics.

# Conclusion

## Contributions

- First classification of segmentation errors for tubular structures
- Method to generate synthetic segmentation with a given type of error
- New approach to visualize and interpret the metrics behavior

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## Advantages +

- No need for expert knowledge on the metrics
- Automated (easy to apply to new metrics)
- Covers a large range of applications and contexts (can find unexpected pitfalls!)

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- Method to generate synthetic segmentation with a given type of error
- New approach to visualize and interpret the metrics behavior

## Advantages +

- No need for expert knowledge on the metrics
- Automated (easy to apply to new metrics)
- Covers a large range of applications and contexts (can find unexpected pitfalls!)

## Limitations -

- Degradation scores may not reflect the desired metric behavior.
- Necessary to consider more error properties (boundary, center-of-mass)