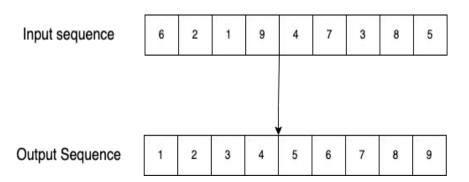
Histogram Sort with Sampling

Course: COMP 5704
Parallel Algorithms and Application in Data Science
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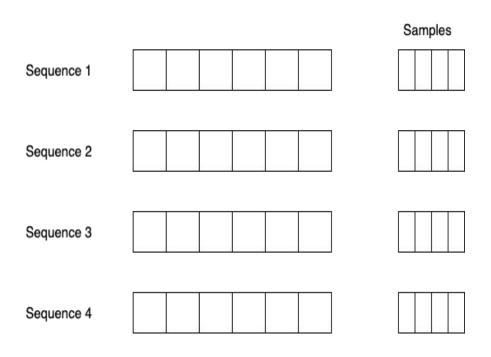
Introduction

- What is Sorting?
- Why do we need it?
- Types of Sorting:
 - Sequential
 - Parallel
- Chief goal of parallel sorting



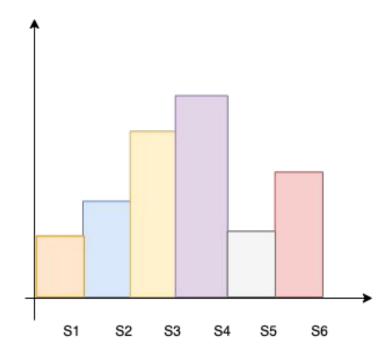
Sample Sort

- 1. Sample: ps keys
- 2. Split: p-1 keys are selected
- 3. Exchange data: pth bucket to pth processor



Histogram Sort

- 1. Broadcast a probe
- 2. Create local histogram
- 3. Sum to form global histogram
- 4. Finalize splitters

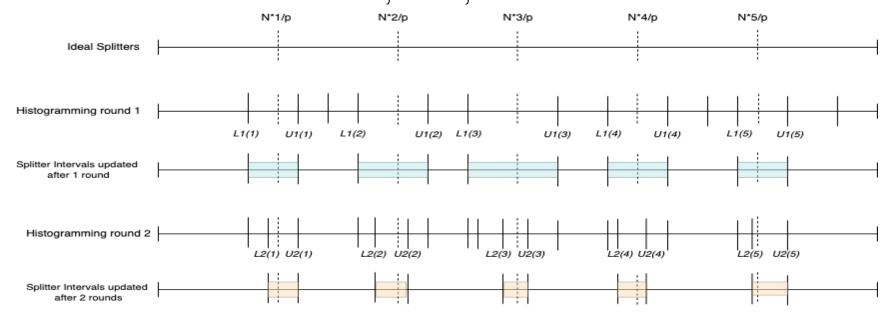


Histogram Sort with Sampling

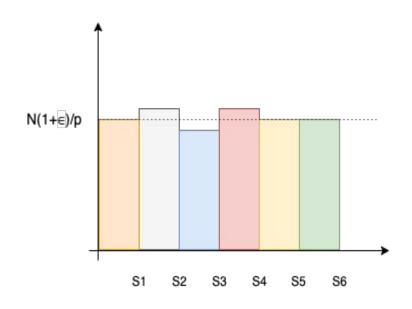
- Goal: Approximate Splitting => $N(1+\varepsilon)/p$
- Processor i owns all keys greater than equal to S(i) and less than S(i+1) := Global balancing
- Input keys: A(0),...,A(N-1)
- Redistributed to: I(0),...,I(N-1), where if A(j)=I(k), it has rank k.
- Satisfactory splitter: S(i) = I(χ (i)), where χ (i) $\in \tau_i = \left[\frac{Ni}{p} \frac{N\epsilon}{2p}, \frac{Ni}{p} + \frac{N\epsilon}{2p}\right]$
- Two Major steps:
 - Sampling
 - Histogramming

Histogram Sort with Sampling

- 1. Each processor picks samples with probability ps_1/N and broadcast.
- 2. Create a local histogram at each processor and sum them at central processor
- 3. Maintain a lower and upper bound $L_i(i)$ and $U_i(i)$ and update splitter intervals



- 4. Sample using new intervals for j+1th round.
- 5. If j=k,
 - a. Histogramming phase is complete and move to next step.
- b. Else, if *j*<*k*, samples are collected at central processor, and move towards next round of histogramming.
- 6. Finally, the key closest to *Ni/p* is chosen as the ith splitter.



Ideal Splitting

Experimental setup

Charm++

- C++ based
- Supports MPI communication protocol
- Divides into processor elements called *chares*.
- Steps:
 - Local Sorting
 - Splitter Determination
 - Data exchange

Expected results of HSS

- Sampling ratio $s = O(p \sqrt[k]{\log p})$ and $k = \log(\log p/\epsilon)$
- O(p) samples can achieve global sorting in $O(\log N/p + \log \log p)$ rounds
- Costs:
 - Computation in local Sorting: O((N/p) log N/p)
 - Sampling: O(S) at local processor and O(S log p) for sorting at central processor
 - Computing local histogram: O(S log N/p)
 - Computation of sampling and histogramming per stage: $O(r \log((\log r)/\epsilon)) \log N)$
- Communication overhead due to multiple stage sorting.
- Overall histogramming rounds: $\Theta(\log \log p)$
- Overall sample size: $\Theta(p \log \log p)$

HSS compared to other algorithms

AMS-sort

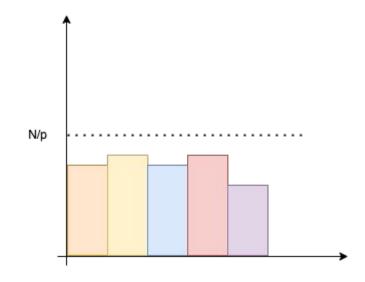
- Better for one round of histogramming by $\Theta(min(\log p, 1/\epsilon))$
- HSS achieves a globally-balanced splitting, making it easily generalizable
- Takes approximately 3x time for splitting phase than HSS

HykSort

- Requires at least $\Omega(\log(p)/\log^2\log(p))$ times more samples.
- Slower convergence of splitters

Questions

- 1. Do more processors mean better performance?
- 2. Is it possible to have the resulting histogram look like this?
- 3. What would the worst case be?



Thank you!