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## 1 Problem: 1

LeNet-5, introduced by Yann LeCun et al. in the 1998 paper Gradient-Based Learning Applied to Document Recognition, is a pioneering convolutional neural network (CNN) architecture designed for handwritten digit recognition. It consists of seven layers (excluding input) that include convolutional layers, subsampling (pooling) layers, and fully connected layers. The architecture follows a hierarchical pattern: the input  $(28\times28$  grayscale images) is processed through two convolutional layers with  $5\times5$  filters, each followed by average pooling layers, reducing spatial dimensions while maintaining essential features.

## 1.1 Part a

- **Problem :** Implement LeNet-5 using PyTorch library in Python. Train the network using MNSIT dataset. Plot accuracy vs epochs and loss vs epochs. Consider a number of epochs till the training procedure converges.
- The code for implementing LeNet-5 was in file name "LeNet\_5.py" which is attached in zip file. Below is the values and graphs which is showing accuracy vs epochs and loss vs epoch.

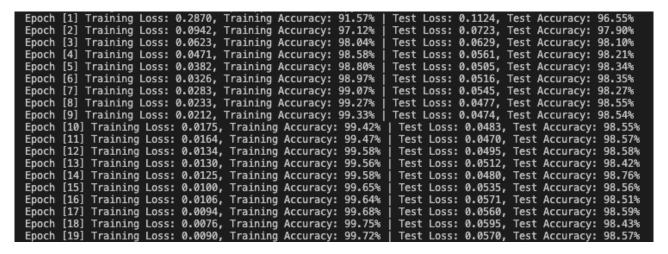


Figure 1: Values of training and testing

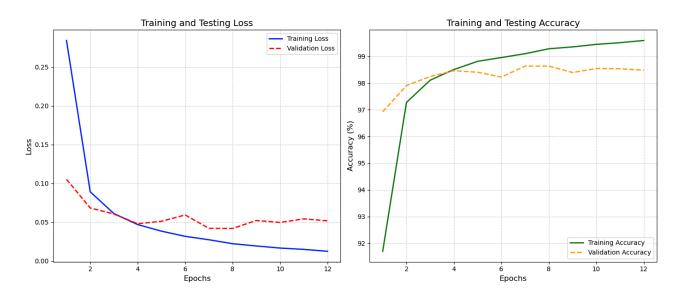


Figure 2: Accuracy vs Epochs and Loss vs Epochs

The graph consists of two subplots:

- Left Plot: Training and Testing Loss
  - \* Blue Solid Line: Training Loss
  - \* Red Dashed Line: Tetsing Loss
- Right Plot: Training and Testing Accuracy
  - \* Green Solid Line: Training Accuracy
  - \* Orange Dashed Line: Testing Accuracy

Each plot shows the performance of the model over multiple epochs, helping to analyze the training progress and detect overfitting or underfitting.

#### 1.2 Part b

- **Problem**: Replace all convolution layers with depth-wise separable convolution. Plot accuracy vs epochs and loss vs epochs. Consider a number of epochs till the training procedure converges.
- In the adapted LeNet-5 architecture, which replace all convolution layers with depth-wise separable convolutions, are used to enhance efficiency by decomposing standard convolution into two steps:
  - Depth-wise convolution
  - Point-wise convolution

This approach significantly reduces computational complexity and the number of parameters while preserving essential feature extraction capabilities.

The implementation of this modified architecture is implemented in Depth\_Wise\_Separable\_Convolution.py file within the provided zip file.

Below are the graphs illustrating accuracy and loss trends over multiple training epochs.

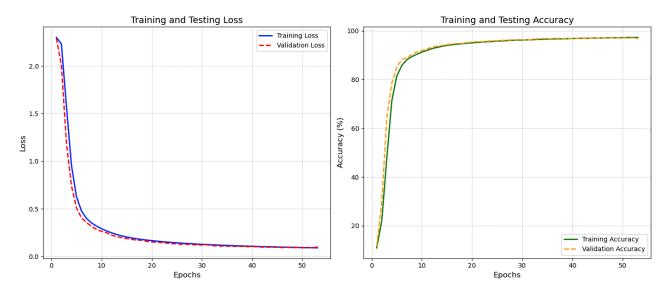


Figure 3: Accuracy vs Epochs and Loss vs Epochs

The graphs visualize the model's performance over multiple epochs.

- Left Plot: Loss vs. Epochs
  - \* Blue Solid Line: Training Loss
  - \* Red Dashed Line: Testing Loss
- Right Plot: Accuracy vs. Epochs

Epoch [1] Training Loss: 2.2996, Training Accuracy: 10.93%	Test Loss: 2.2916, Test Accuracy: 11.58%
Epoch [2] Training Loss: 2.2291, Training Accuracy: 21.79%	Test Loss: 2.0053, Test Accuracy: 29.80%
Epoch [3] Training Loss: 1.5757, Training Accuracy: 47.52%	Test Loss: 1.1886, Test Accuracy: 64.11%
Epoch [4] Training Loss: 0.9556, Training Accuracy: 71.12%	Test Loss: 0.7408, Test Accuracy: 78.43%
Epoch [5] Training Loss: 0.6261, Training Accuracy: 81.42%	Test Loss: 0.5087, Test Accuracy: 85.17%
Epoch [6] Training Loss: 0.4760, Training Accuracy: 85.76%	Test Loss: 0.4033, Test Accuracy: 88.18%
Epoch [7] Training Loss: 0.3977, Training Accuracy: 88.11%	Test Loss: 0.3559, Test Accuracy: 88.88%
Epoch [8] Training Loss: 0.3506, Training Accuracy: 89.39%	Test Loss: 0.3139, Test Accuracy: 90.31%
Epoch [9] Training Loss: 0.3170, Training Accuracy: 90.36%	Test Loss: 0.2824, Test Accuracy: 91.36%
Epoch [10] Training Loss: 0.2897, Training Accuracy: 91.25%	Test Loss: 0.2619, Test Accuracy: 91.87%
Epoch [11] Training Loss: 0.2666, Training Accuracy: 91.92%	Test Loss: 0.2474, Test Accuracy: 92.51%
Epoch [12] Training Loss: 0.2469, Training Accuracy: 92.64%	Test Loss: 0.2227, Test Accuracy: 93.26%
Epoch [13] Training Loss: 0.2297, Training Accuracy: 93.16%	Test Loss: 0.2069, Test Accuracy: 93.69%
Epoch [14] Training Loss: 0.2152, Training Accuracy: 93.58%	Test Loss: 0.1963, Test Accuracy: 93.93%
Epoch [15] Training Loss: 0.2031, Training Accuracy: 93.99%	Test Loss: 0.1868, Test Accuracy: 94.28%
Epoch [16] Training Loss: 0.1934, Training Accuracy: 94.25%	Test Loss: 0.1781, Test Accuracy: 94.56%
Epoch [17] Training Loss: 0.1849, Training Accuracy: 94.47%	Test Loss: 0.1698, Test Accuracy: 94.76%
Epoch [18] Training Loss: 0.1774, Training Accuracy: 94.66%	Test Loss: 0.1689, Test Accuracy: 94.77%
Epoch [19] Training Loss: 0.1707, Training Accuracy: 94.90%	Test Loss: 0.1577, Test Accuracy: 95.14%
Epoch [20] Training Loss: 0.1652, Training Accuracy: 95.02%	Test Loss: 0.1509, Test Accuracy: 95.36%
Epoch [21] Training Loss: 0.1596, Training Accuracy: 95.20%	Test Loss: 0.1489, Test Accuracy: 95.52%
Epoch [22] Training Loss: 0.1544, Training Accuracy: 95.37%	Test Loss: 0.1438, Test Accuracy: 95.55%
Epoch [23] Training Loss: 0.1503, Training Accuracy: 95.50%	Test Loss: 0.1384, Test Accuracy: 95.67%
Epoch [24] Training Loss: 0.1462, Training Accuracy: 95.58%	Test Loss: 0.1329, Test Accuracy: 95.90%
Epoch [25] Training Loss: 0.1421, Training Accuracy: 95.75%	Test Loss: 0.1324, Test Accuracy: 95.89%
Epoch [26] Training Loss: 0.1380, Training Accuracy: 95.83%	Test Loss: 0.1267, Test Accuracy: 96.05%
Epoch [27] Training Loss: 0.1348, Training Accuracy: 95.96%	Test Loss: 0.1269, Test Accuracy: 96.15%
Epoch [28] Training Loss: 0.1320, Training Accuracy: 96.08%	Test Loss: 0.1232, Test Accuracy: 96.25%
Epoch [29] Training Loss: 0.1288, Training Accuracy: 96.14%	Test Loss: 0.1195, Test Accuracy: 96.28%
Epoch [30] Training Loss: 0.1260, Training Accuracy: 96.18%	Test Loss: 0.1198, Test Accuracy: 96.36%
Epoch [31] Training Loss: 0.1237, Training Accuracy: 96.24%	Test Loss: 0.1215, Test Accuracy: 96.21%
Epoch [32] Training Loss: 0.1215, Training Accuracy: 96.31%	Test Loss: 0.1127, Test Accuracy: 96.46%
Epoch [33] Training Loss: 0.1189, Training Accuracy: 96.42%	Test Loss: 0.1097, Test Accuracy: 96.65%
Epoch [34] Training Loss: 0.1166, Training Accuracy: 96.49%	Test Loss: 0.1076, Test Accuracy: 96.82%
Epoch [35] Training Loss: 0.1145, Training Accuracy: 96.56%	Test Loss: 0.1071, Test Accuracy: 96.74%
Epoch [36] Training Loss: 0.1126, Training Accuracy: 96.62%	Test Loss: 0.1061, Test Accuracy: 96.77%
Epoch [37] Training Loss: 0.1106, Training Accuracy: 96.69%	Test Loss: 0.1038, Test Accuracy: 96.88%
Epoch [38] Training Loss: 0.1089, Training Accuracy: 96.66%	Test Loss: 0.1049, Test Accuracy: 96.70%
Epoch [39] Training Loss: 0.1072, Training Accuracy: 96.72%	Test Loss: 0.1012, Test Accuracy: 96.86%
Epoch [40] Training Loss: 0.1055, Training Accuracy: 96.80%	Test Loss: 0.1039, Test Accuracy: 96.81%
Epoch [41] Training Loss: 0.1034, Training Accuracy: 96.86%	Test Loss: 0.0996, Test Accuracy: 96.79%
Epoch [42] Training Loss: 0.1020, Training Accuracy: 96.92%	Test Loss: 0.0969, Test Accuracy: 96.92%
Epoch [43] Training Loss: 0.1012, Training Accuracy: 96.92%	Test Loss: 0.0966, Test Accuracy: 97.05%
Epoch [44] Training Loss: 0.0995, Training Accuracy: 96.98%	Test Loss: 0.0957, Test Accuracy: 96.94%
Epoch [45] Training Loss: 0.0984, Training Accuracy: 97.00%	Test Loss: 0.0951, Test Accuracy: 96.92%
Epoch [46] Training Loss: 0.0969, Training Accuracy: 97.05%	Test Loss: 0.0922, Test Accuracy: 97.02%
Epoch [47] Training Loss: 0.0954, Training Accuracy: 97.10%	Test Loss: 0.0964, Test Accuracy: 96.97%
Epoch [48] Training Loss: 0.0946, Training Accuracy: 97.12%	Test Loss: 0.0901, Test Accuracy: 97.13%
Epoch [49] Training Loss: 0.0934, Training Accuracy: 97.11%	Test Loss: 0.0945, Test Accuracy: 97.00%
Epoch [50] Training Loss: 0.0926, Training Accuracy: 97.16%	Test Loss: 0.0894, Test Accuracy: 97.09%
Epoch [51] Training Loss: 0.0910, Training Accuracy: 97.25%	Test Loss: 0.0931, Test Accuracy: 96.99%
Epoch [52] Training Loss: 0.0902, Training Accuracy: 97.25%	Test Loss: 0.0896, Test Accuracy: 97.12%
Epoch [53] Training Loss: 0.0892, Training Accuracy: 97.25%	Test Loss: 0.0988, Test Accuracy: 96.72%
	,

Figure 4: Values of training and testing

- \* Green Solid Line: Training Accuracy
- \* Orange Dashed Line: Testing Accuracy

These graphs help in analyzing the training progress and identifying potential overfitting or underfitting.

## 1.3 Part c

• **Problem :** What is the total number of multiply operations and addition operation with regular convolution (network obtain in a) and depth wise separable convolution (network obtain in b)?

We focus solely on the significant multiply/add operations in the three convolutional layers 1, 2, 3 and the two fully connected layers at the end (FC and Output), while generally disregarding the computational costs of the average pooling due to their minimal impact compared to the convolutions.

• Regular Convolution :

- Layer 1: 
$$32 \times 32 \times 1(Input) \rightarrow 28 \times 28 \times 6$$
 (Output), Kernel =  $5 \times 5$   
Number of Output elements =  $6 \times 28 \times 28 = 4704$ ,  
Multiplication of each output =  $1 \times (5 \times 5) = 25$ ,  
Multiplications =  $4704 \times 25 = 117,600$ ,  
Additions =  $117,600 - 4704 = 112,896$ .

- Layer 2:  $14 \times 14 \times 6(Input) \rightarrow 10 \times 10 \times 16$  (Output), Kernel =  $5 \times 5$ 

Number of Output elements = 
$$16 \times 10 \times 10 = 1600$$
,  
Multiplication of each output =  $(6 \times 5 \times 5) = 150$ ,  
Multiplications =  $1600 \times 150 = 240,000$ ,  
Additions =  $240,000 - 1600 = 238,400$ .

- Layer 3:  $5 \times 5 \times 16(Input) \rightarrow 1 \times 1 \times 120$  (Output), Kernel =  $5 \times 5$ 

Number of Output elements = 120,  
Multiplication of each output = 
$$(16 \times 5 \times 5) = 400$$
,  
Multiplications =  $120 \times 400 = 48,000$ ,  
Additions =  $48,000 - 120 = 47,880$ .

- **FC:**  $120 \rightarrow 84$ 

Multiplications = 
$$120 \times 84 = 10,080$$
,  
Additions =  $84 \times (120 - 1) = 9996$ .

- **Output:**  $84 \to 10$ 

Multiplications = 
$$84 \times 10 = 840$$
,  
Additions =  $10 \times (84 - 1) = 830$ .

- Total Regular Convolution:

Total Multiplications = 
$$416,520$$
,  
Total Additions =  $410,002$ .

- Depthwise-Separable Convolution Version
  - Layer 1:  $32 \times 32 \times 1(Input) \rightarrow 28 \times 28 \times 6$  (Output)

Depthwise Multiplications = 19,600,

Additions = 18,816,

Pointwise Multiplications = 4704,

Additions = 0,

Total (Layer\_1, DSC) = 24,304 and 18,816.

- Layer 2:  $14 \times 14 \times 6(Input) \rightarrow 10 \times 10 \times 16$  (Output)

Depthwise Multiplications = 
$$15,000$$
,  
Additions =  $14,400$ ,  
Pointwise Multiplications =  $9600$ ,  
Additions =  $8000$ ,  
Total (Layer\_2, DSC) =  $24,600$  and  $22,400$ .

- Layer 3:  $5 \times 5 \times 16(Input) \rightarrow 1 \times 1 \times 120$  (Output)

Depthwise Multiplications = 400,

Additions = 384,

Pointwise Multiplications = 1920,

Additions = 1800,

Total (Layer\_3, DSC) = 2320 and 2184.

- **FC:**  $120 \rightarrow 84$ 

Multiplications = 10,080, Additions = 9996.

- **Output:**  $84 \rightarrow 10$ 

Multiplications = 840, Additions = 830.

- Total Depthwise-Separable Convolution:

Total Multiplications = 62,144, Total Additions = 54,226.

#### 1.4 Part d

- **Problem :** Prepare a mathematical function (f) which maps number of operations in a regular convolutional layer to depth-wise separable convolutional layer. Specifically, derive f(x, other parameters) = y, where x is the number of operations in a regular convolution and y is the number operation in depth-wise operation resulting in same output size.
- Standard Convolution: Computational Complexity

Consider a convolutional layer with the following parameters:

- $-C_{in}$ : Number of input channels
- $-C_{out}$ : Number of output channels
- $-K_h \times K_w$ : Kernel size
- $-I_h \times I_w$ : Spatial dimensions of the output feature map

The total number of multiplication operations required for a conventional 2D convolution is computed as:

$$O_m = C_{in} \cdot C_{out} \cdot K_h \cdot K_w \cdot I_h \cdot I_w. \tag{1}$$

• Depth-wise Separable Convolution: Computational Complexity

It is composed of two sequential operations:

- 1. **Depth-wise Convolution**: Each input channel undergoes convolution independently using a  $K_h \times K_w$  filter.
- 2. **Point-wise Convolution**: A  $1 \times 1$  convolution integrates information across channels, generating  $C_{out}$  output channels.

## 1.5 Depth-wise Convolution

The total multiplication operations for depth-wise convolution are given by:

$$O_{dc} = C_{in} \cdot K_h \cdot K_w \cdot I_h \cdot I_w. \tag{2}$$

## • Point-wise Convolution

Since each output channel is formed by applying a  $1 \times 1$  convolution across all input channels, the total number of multiply operations is:

$$O_{pc} = C_{in} \cdot C_{out} \cdot I_h \cdot I_w. \tag{3}$$

## • Total Operations for Depth-wise Separable Convolution

Thus, the overall computational cost of depth wise separable convolution is:

$$O_{dsc} = C_{in} \cdot K_h \cdot K_w \cdot I_h \cdot I_w + C_{in} \cdot C_{out} \cdot I_h \cdot I_w. \tag{4}$$

• We derive value that transforms the computational cost of standard convolution  $(O_m)$  into that of depth-wise separable convolution  $(O_{dsc})$  as follows.

From the formula for standard convolution:

$$O_m = C_{in} \cdot C_{out} \cdot K_h \cdot K_w \cdot I_h \cdot I_w. \tag{5}$$

Rearranging for  $C_{in} \cdot I_h \cdot I_w$ :

$$C_{in} \cdot I_h \cdot I_w = \frac{O_m}{C_{out} \cdot K_h \cdot K_w}.$$
 (6)

Substituting into the depthwise-separable convolution equation:

$$O_{dsc} = \left(\frac{O_m}{C_{out} \cdot K_h \cdot K_w}\right) K_h \cdot K_w + \left(\frac{O_s}{C_{out} \cdot K_h \cdot K_w}\right) C_{out}. \tag{7}$$

Simplifying:

$$O_{dsc} = O_s \cdot \frac{K_h \cdot K_w + C_{out}}{K_h \cdot K_w \cdot C_{out}}.$$
 (8)

Thus, the transformation will be as follows:

$$=>O_s \cdot \frac{K_h \cdot K_w + C_{out}}{K_h \cdot K_w \cdot C_{out}}.$$
 (9)