

Pooling vs Voting:

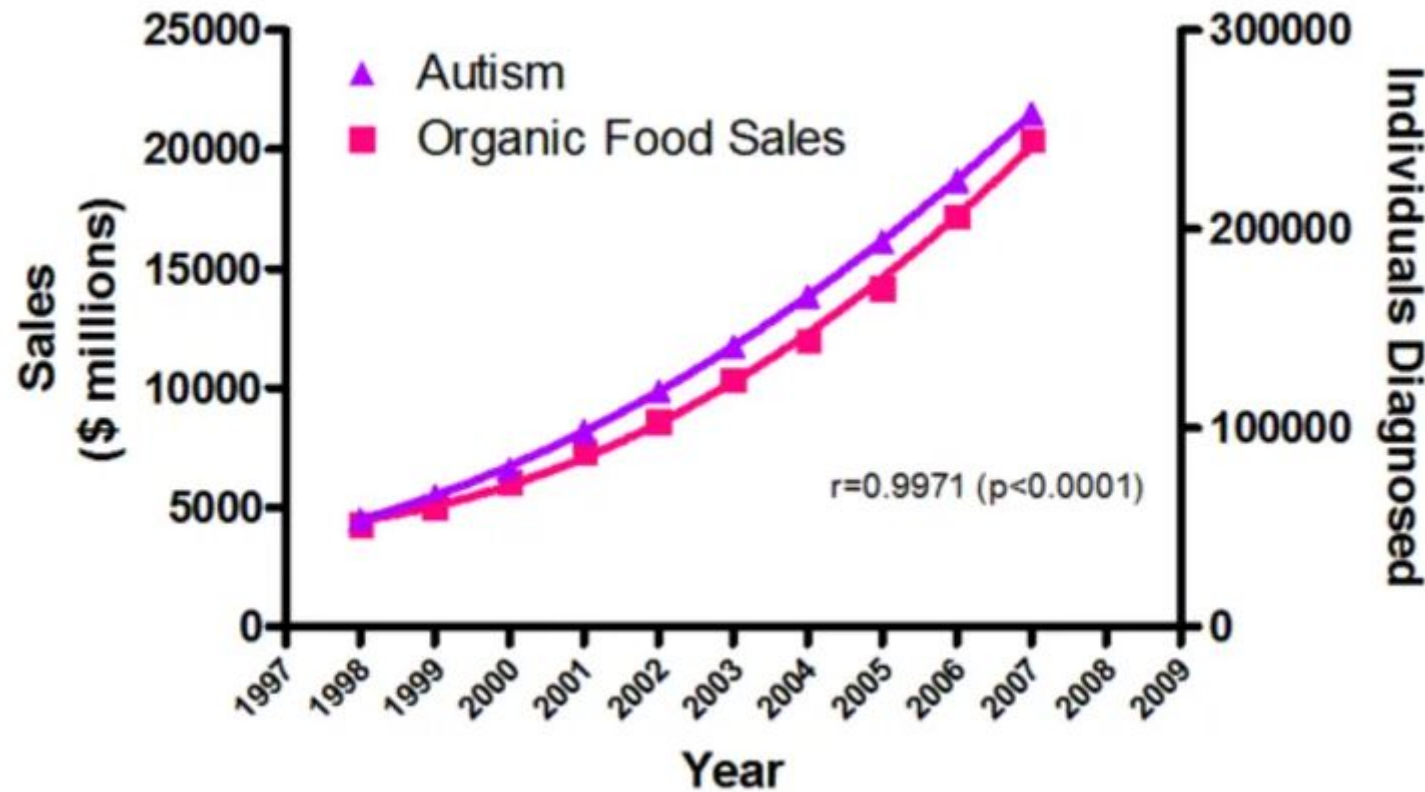
An Empirical Study of Learning Causal Structures

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Confusion over Causality and Correlation

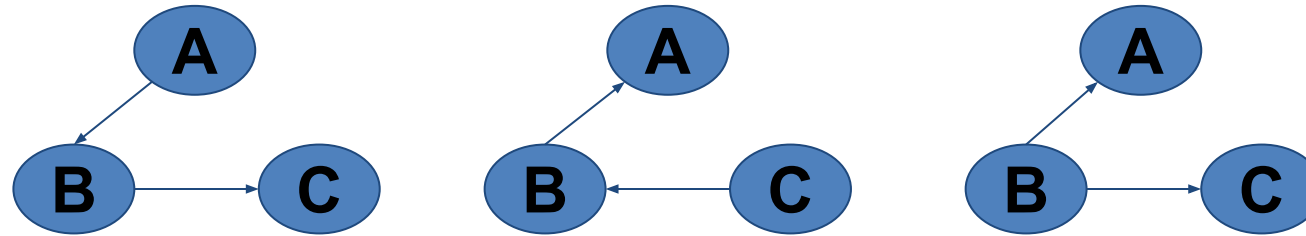
- Causally *unrelated* variables appear to be highly correlated
- *Spurious Correlation*, *Personal Anecdotes* & *Scientific Reporting* are unclear to determine *Causality*



Sources: Organic Trade Association, 2011 Organic Industry Survey; U.S. Department of Education, office of Special Education Programs, Data Analysis System (DANS), OMB# 1820-0043: "Children with Disabilities Receiving Special Education Under Part B of the Individuals with Disabilities Act

Effects of mixing Observational and Interventional data

- Observational data is cheap, accessible and identifies among Markov Equivalent structures
- Interventions are external manipulating of one or more variables in our system
- Enable us to differentiate among different causal structures compatible with an observation



Intervening at **B**



Switches on one of the 3 networks !!!

- A dependence on both observational and interventional experiments is important
- A common approach is to pool all the data and learn a single causal model for **Statistical Efficiency**.

Types of Intervention:

Perfect

Known, fixed target



Not applicable in Real World settings !!

Imperfect

Unreliable, Soft targets



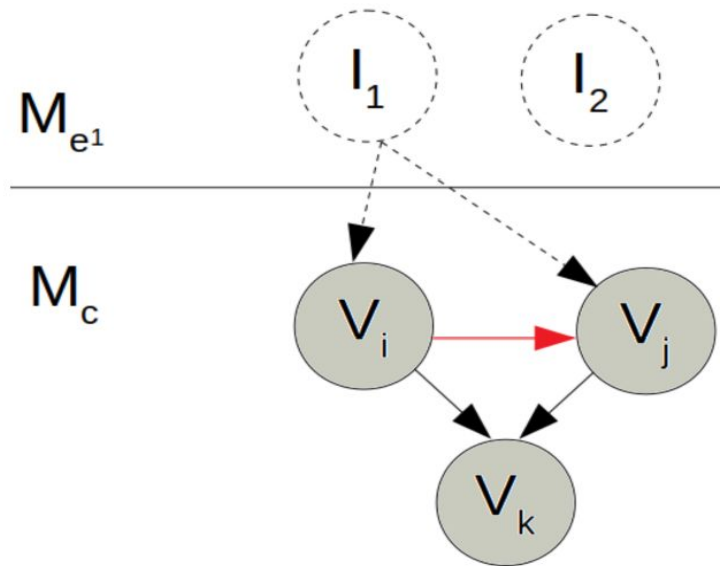
Uncertain

Unknown targets, Fat hands

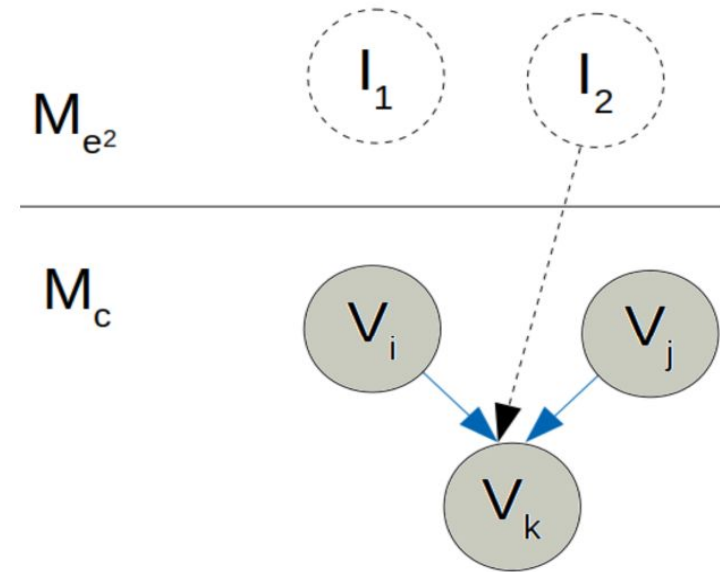


“off-target” effects of drugs, gene knockouts etc

Spurious Causal links



False Causal Dependence

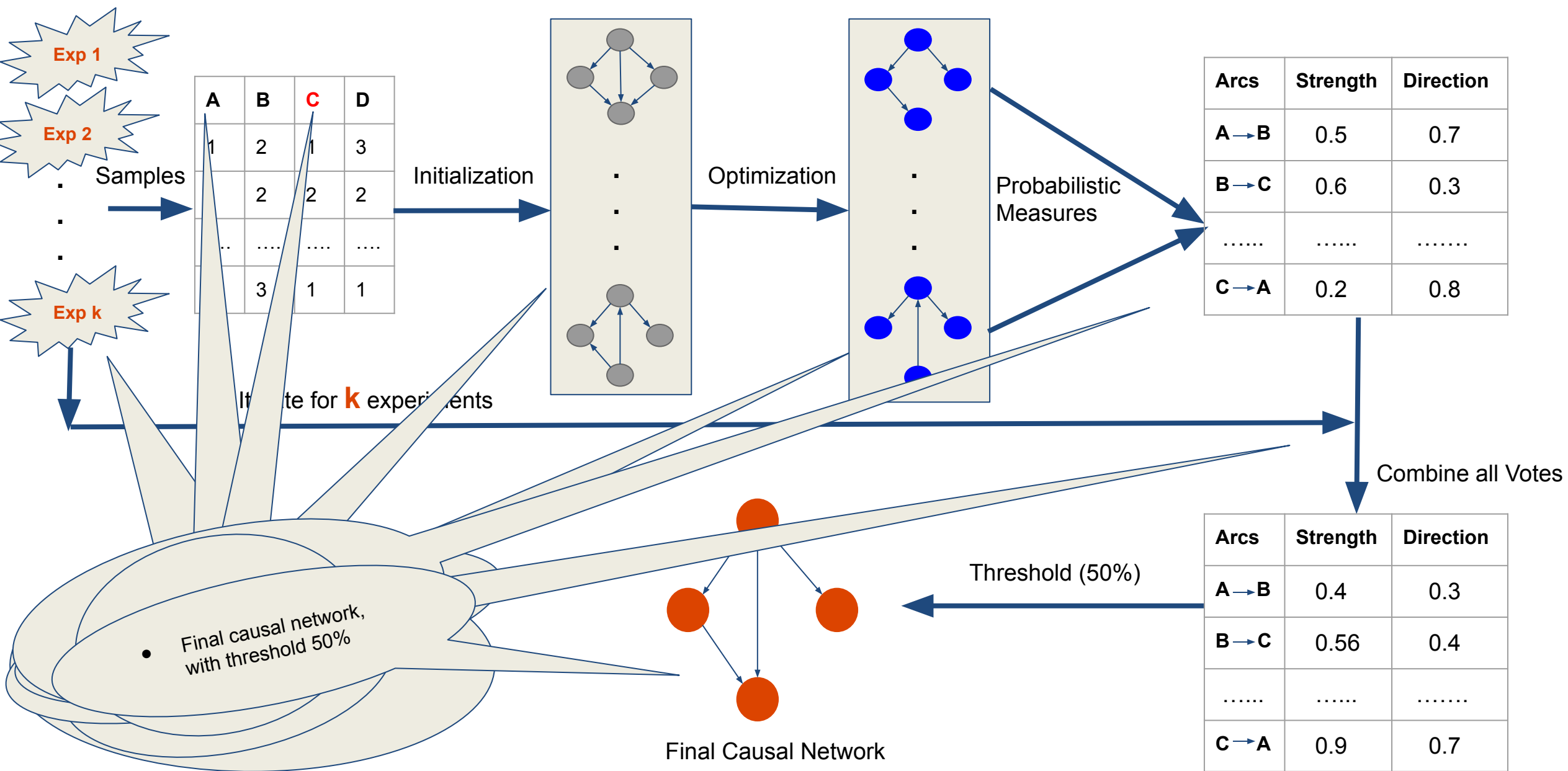


False Causal Independence

Contribution

- Detecting such spurious causal links might lose the very purpose of learning these networks
- We propose a way of handling uncertain interventions by learning causal information from different experiments separately and combining the results using a simple approach called “***Learn and Vote***”.
- We found that our approach achieves a significant reduction of false causal discovery.

Our Approach: *Learn and Vote*



Our Approach: Learn and Vote

ALGORITHM 1 Learn and Vote

Input: set of k experiments with dataset $D_1, D_2 \dots D_k$

Output: DAG $G^f = (E, V)$, final causal network

1: **procedure** OUR APPROACH

2: **for** $j=1$ to k **do**

3: N =nodes In D_j

4: intv =Intervened nodes in D_j

5: randomNet =createRandNet(N , 100)

6: **for** $l=1$ to 100 **do**

7: $\text{Net}[l]$ =Tabu($\text{randomNet}[l]$, intv)

8: $\text{arcProb}[j]$ =arcStrength(Net)

9: avgArcs = avgNetwork(arcProb)

10: G^f = learnDAG(avgArcs , Threshold)

- Total number of “ k ” experiments
- Can be observational or interventional

- Observed variables in our system

- Known Targets of intervention

- Score based searching

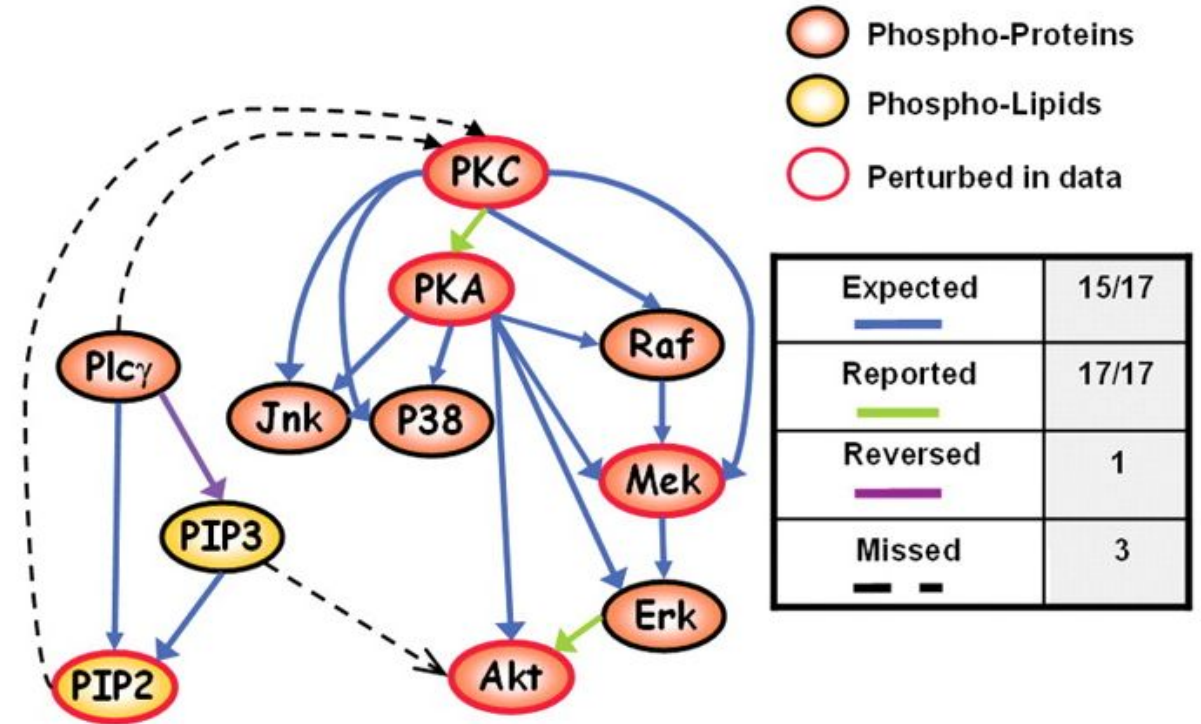
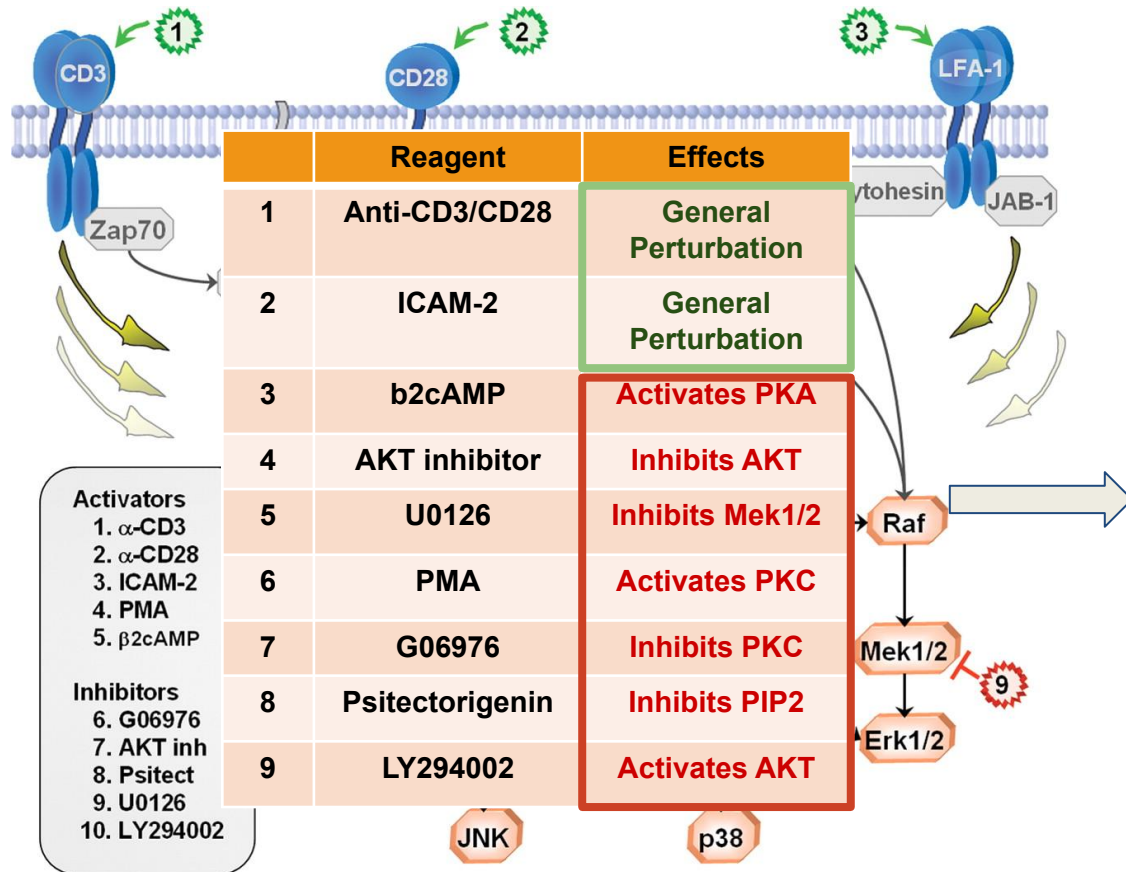
- Averaging over all experiments

- Initialization 100 DAGs

- List containing arc strength and direction in probability

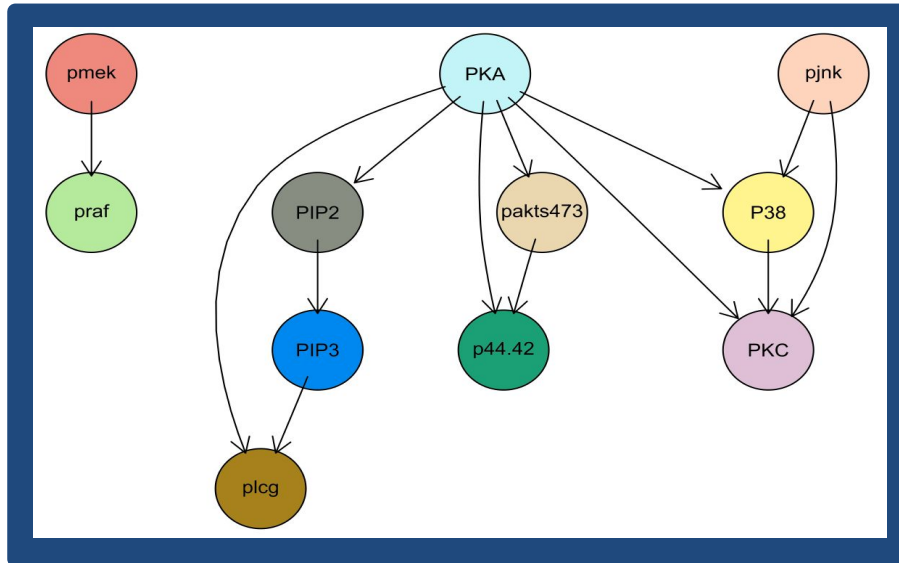
- Final causal network, with threshold 50%

An Application: Cell Signalling Networks



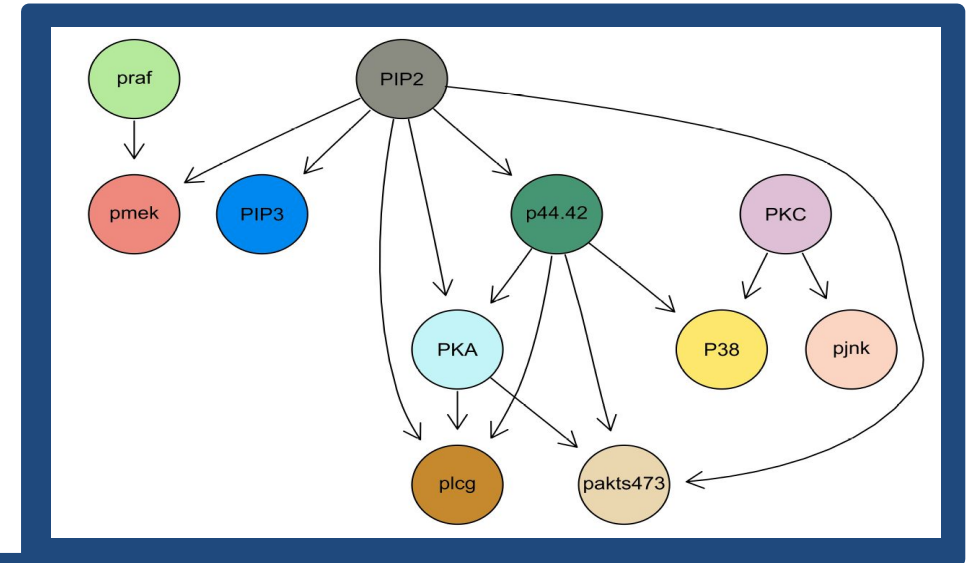
An Application: Biological Signalling Networks

Observational Study



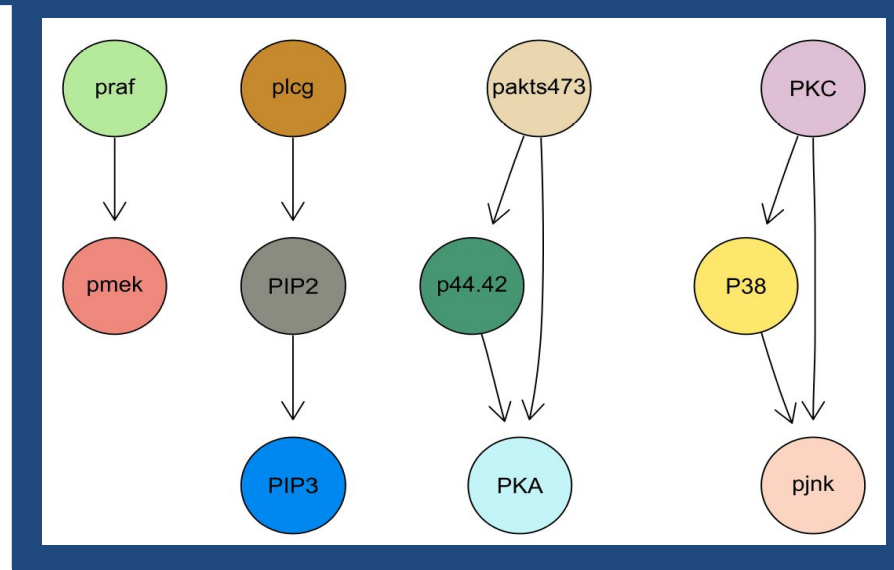
TP: 3, FP: 10, FN: 17

Observational + Interventional Study



TP: 5, FP: 10, FN: 15

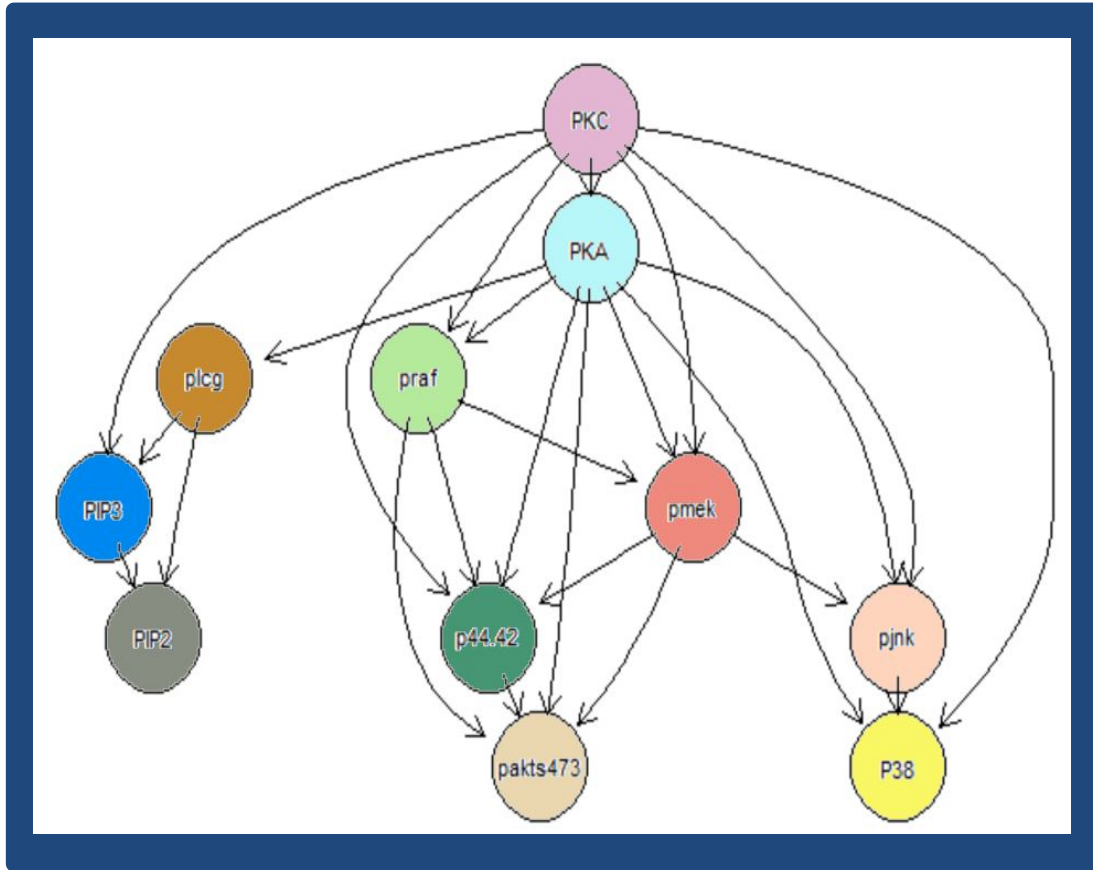
Learn and Vote



TP: 4, FP: 5, FN: 16

Networks Inferred

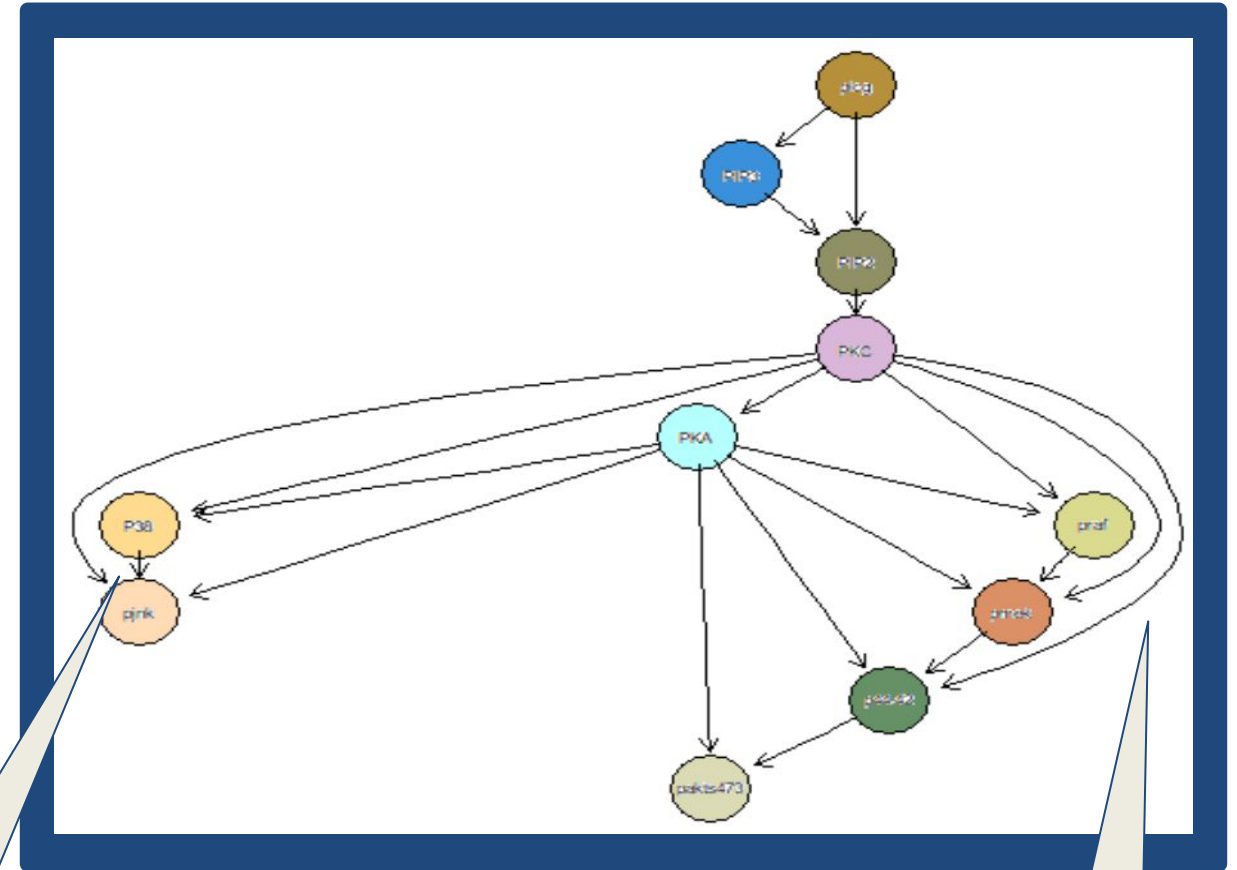
Sachs method reimplemented



TP: 17, FP: 8, FN: 3

P38 -> pjnk

Learn and Vote



TP: 18, FP: 2, FN: 2

PKC -> P44.42

Empirical Study

Datasets

- ❑ **Lizards** ..
Real world dataset of 3 nodes
Mutated Network: Intervened at 2 points
- ❑ **Asia** ..
Synthetic dataset of 8 nodes
Mutilated 1: 1 observation and 1 interventional study
Mutilated 2: 1 observation and 2 interventional study
- ❑ **Alarm** ..
Synthetic dataset of 37 nodes
Mutilated 1: 3 observation and 6 interventional study
Mutilated 2: 5 observation and 10 interventional study
- ❑ **Insurance** ..
Synthetic dataset of 27 nodes
Mutilated 1: 1 observation and 5 interventional study
Mutilated 2: 3 observation and 8 interventional study
- ❑ **GmInt** ..
Synthetic dataset of 8 nodes provided in the pcalg-R package

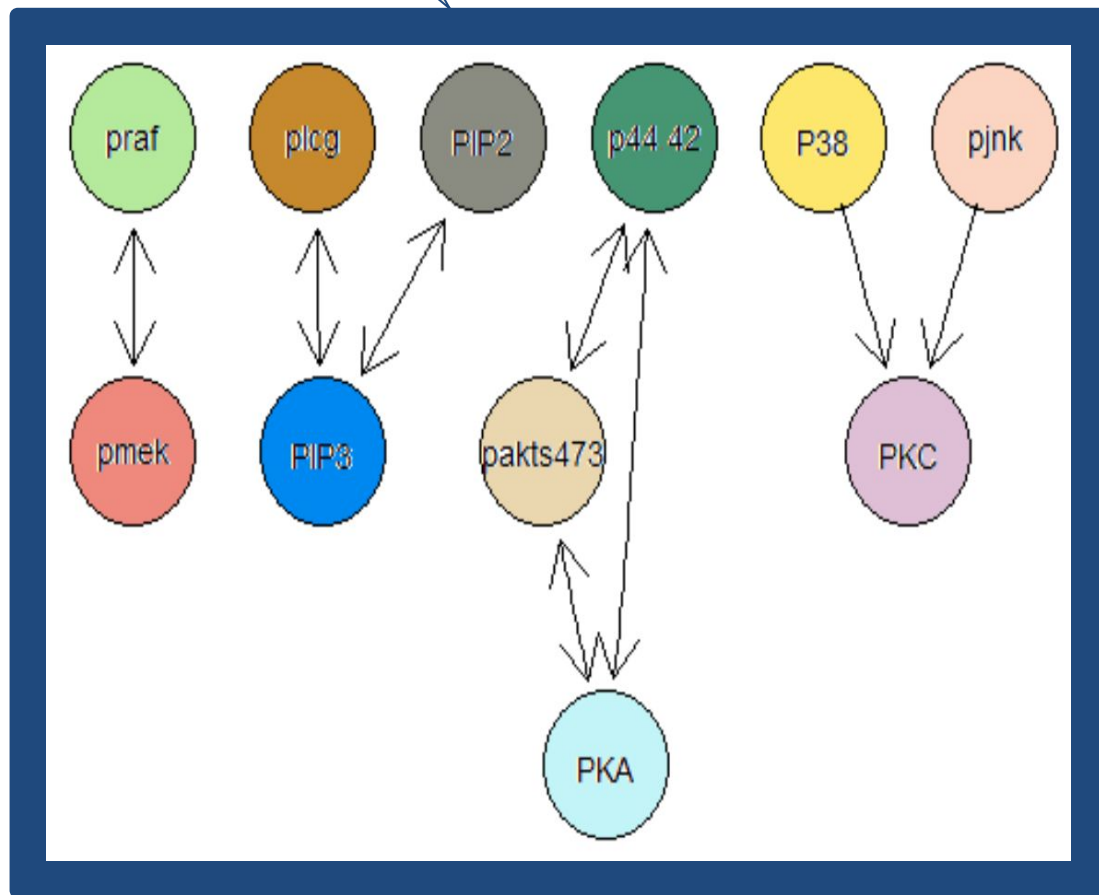
Popular Algorithms

- ❑ **PC** ..
An algorithm for fast recovery of sparse causal graphs (P Spirtes, C Glymour, 1991)
- ❑ **GDS** ..
Greedy DAG Search proposed by (A. Hauser and P. Bühlmann, 2012)
- ❑ **GIES** ..
(Hauser and Bühlmann, 2012) extended the greedy equivalence search to include interventions.
- ❑ **ICP** ..
“Causal inference using invariant prediction: identification and confidence intervals” Peters, Bühlmann and Meinshausen, 2015
- ❑ **simy** ..
Dynamic programming approach of Silander and Myllymäki (2006)

Networks Inferred

Good with
Observational data

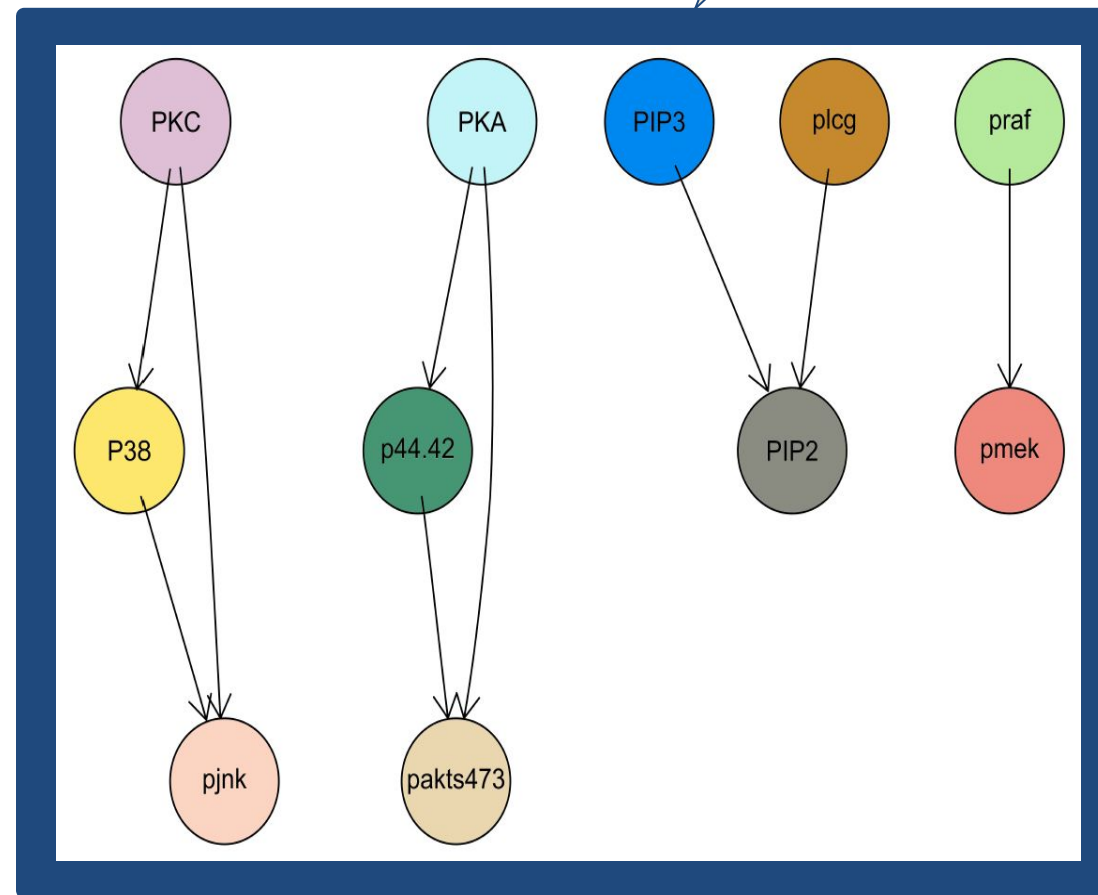
PC



TP: 8, FP: 6, FN: 12

Too Strict, but Reliable !!!

ICP



TP: 9, FP: 0, FN: 11
12

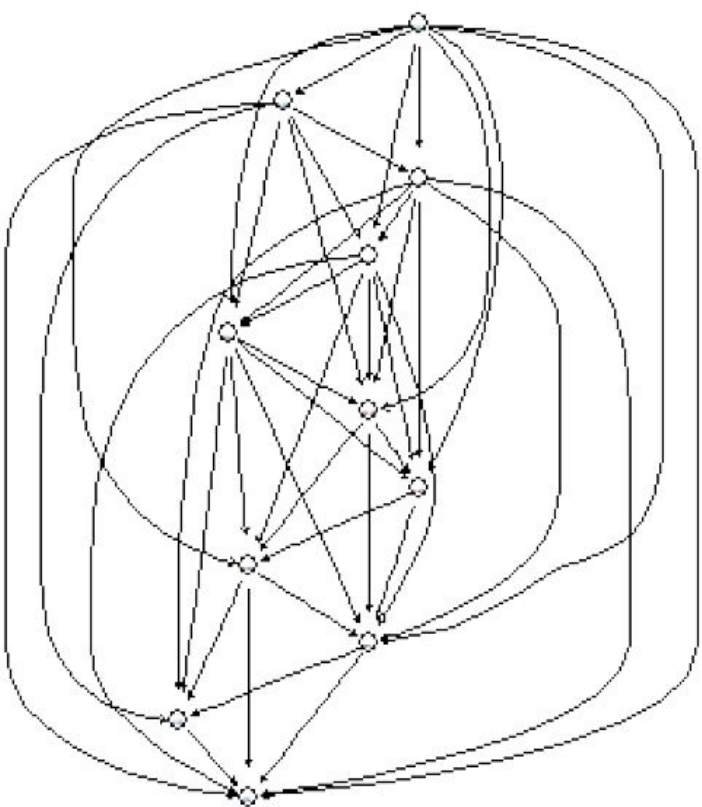
Greedy methods not
good with uncertain
interventions :-)

Networks Inferred

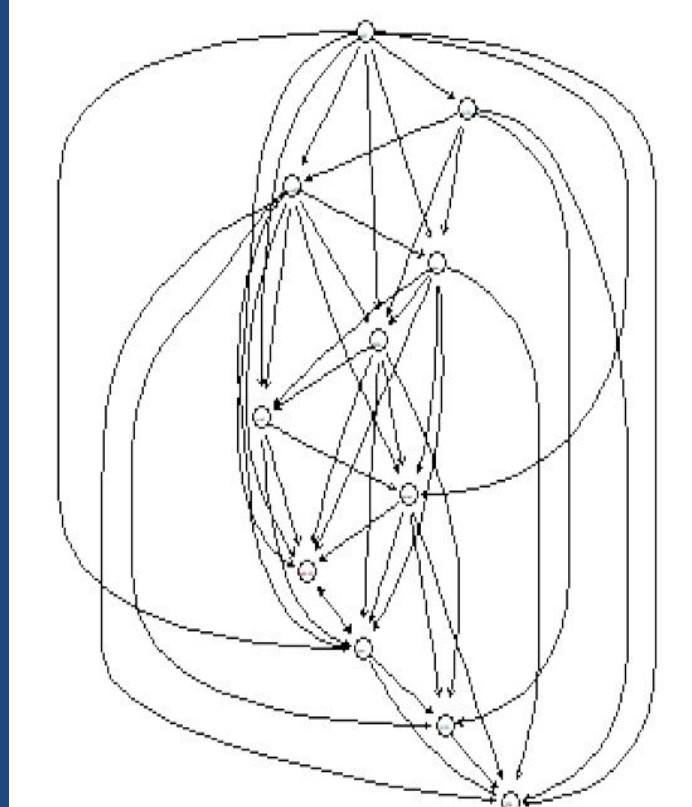
GDS

GIES

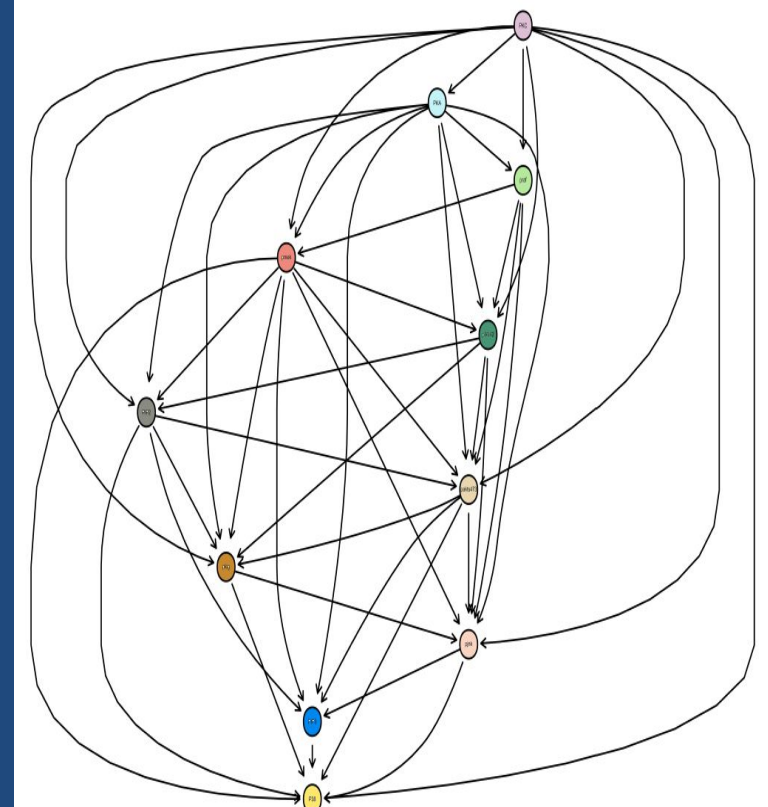
simy



TP: 18, FP: 25, FN: 2



TP: 17, FP: 28, FN: 3

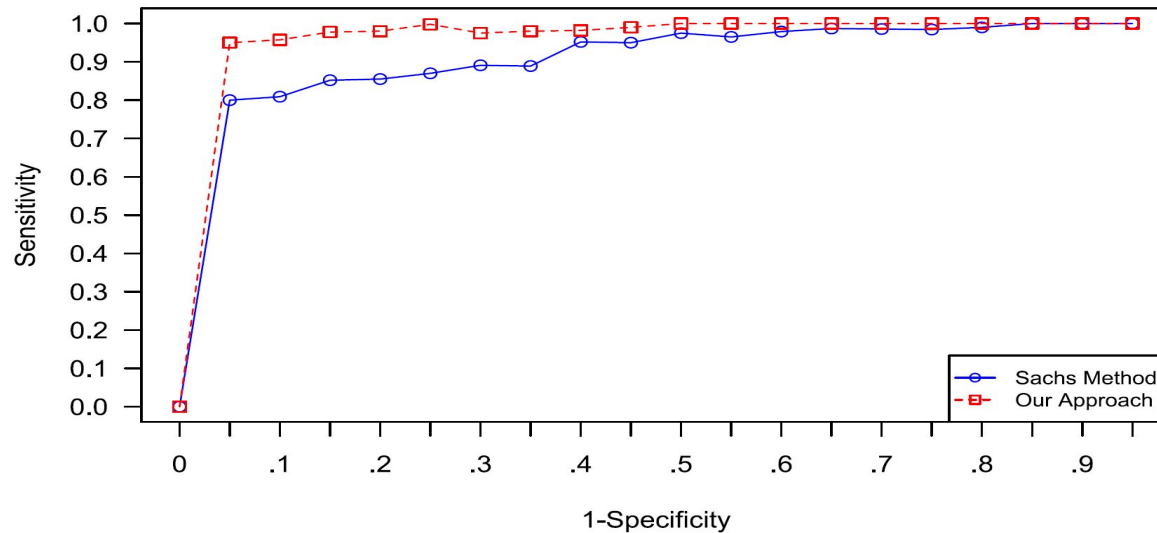


TP: 19, FP: 26, FN: 1

Comparative Benchmark

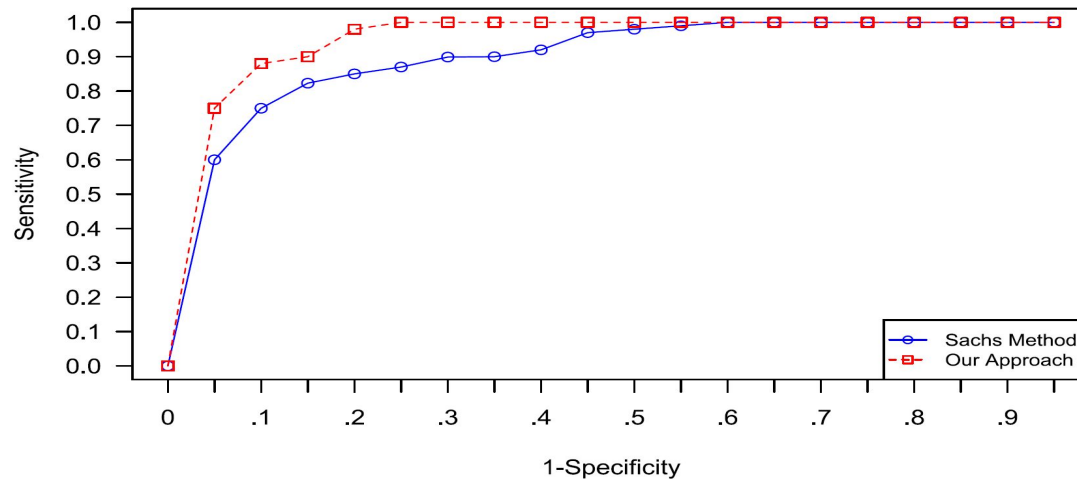
Dataset	Metric	Causal Discovery Algorithms						
		PC	GDS	GIES	ICP	simy	Sachs et al	Learn and Vote
Flow Cytometry	Precision	0.5714	0.4186	0.377	1	0.4222	0.68	0.89
	Recall	0.4	0.9	0.85	0.45	0.95	0.85	0.89
	F1 score	0.47	0.572	0.522	0.62	0.584	0.7558	0.89
Lizards	Precision	1	1	1	0	1	1	1
	Recall	1	1	1	0	1	0.5	0.5
	F1 score	1	1	1	0	1	0.667	0.667
Asia_mut1	Precision	1	0.625	0.625	1	0.31578	0.77	1
	Recall	0.75	0.625	0.625	0.5	0.75	0.875	0.75
	F1 score	0.857	0.625	0.625	0.666	0.4444	0.8237	0.857
Asia_mut2	Precision	1	0.85714	0.85714	1	0.3043	0.666	1
	Recall	0.75	0.75	0.75	0.5	0.875	0.75	0.75
	F1 score	0.857	0.8	0.8	0.666	0.4928	0.7058	0.857
gmInt	Precision	0.75	0.889	0.889	1	0.889	0.8571	1
	Recall	0.75	1	1	0.375	1	0.75	0.75
	F1 score	0.75	0.94	0.94	0.5454	0.94	0.8	0.857
Alarm_mut1	Precision	0.666	0.25	0.26	0.7	n/a	0.625	0.564
	Recall	0.434	0.217	0.26	0.26	n/a	0.4464	0.4
	F1 score	0.526	0.2325	0.26	0.38	n/a	0.52	0.468
Alarm_mut2	Precision	0.666	0.411	0.5128	0.6	n/a	0.725	0.769
	Recall	0.434	0.456	0.434	0.21	n/a	0.63	0.642
	F1 score	0.526	0.432	0.47	0.3115	n/a	0.675	0.7
Insurance_mut1	Precision	0.7143	0.36	0.3617	0.7	n/a	0.857	0.8
	Recall	0.288	0.3461	0.327	0.25	n/a	0.577	0.538
	F1 score	0.4107	0.352	0.3435	0.368	n/a	0.689	0.643
Insurance_mut2	Precision	0.7143	0.355	0.366	0.64	n/a	0.676	0.6857
	Recall	0.288	0.423	0.423	0.21	n/a	0.4423	0.4615
	F1 score	0.4107	0.386	0.392	0.316	n/a	0.535	0.5517

Performance Analysis with respect to ROC curve

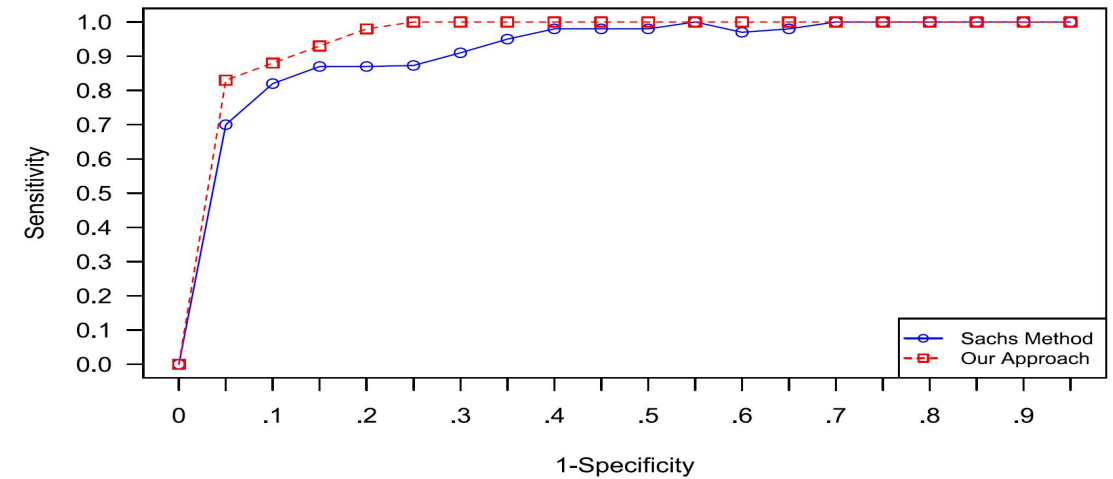


Flow Cytometry data

- We plot the ROC curve for the Flow cytometry data
- Compared the baseline method to Learn and vote
- Area under curve is greater across all thresholds
- Performance improves for “Learn and Vote”
- Intervening at informative targets improves performance

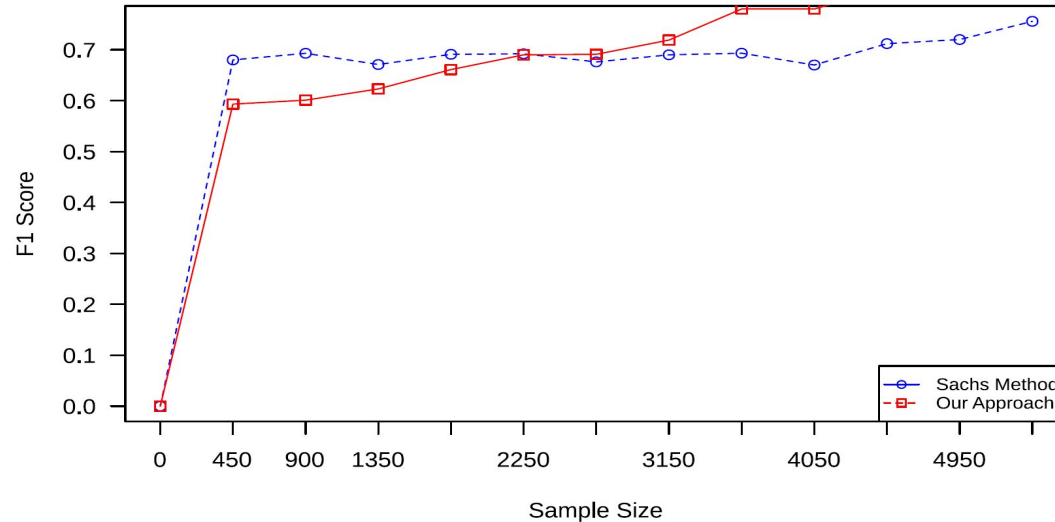


Asia_mut 1

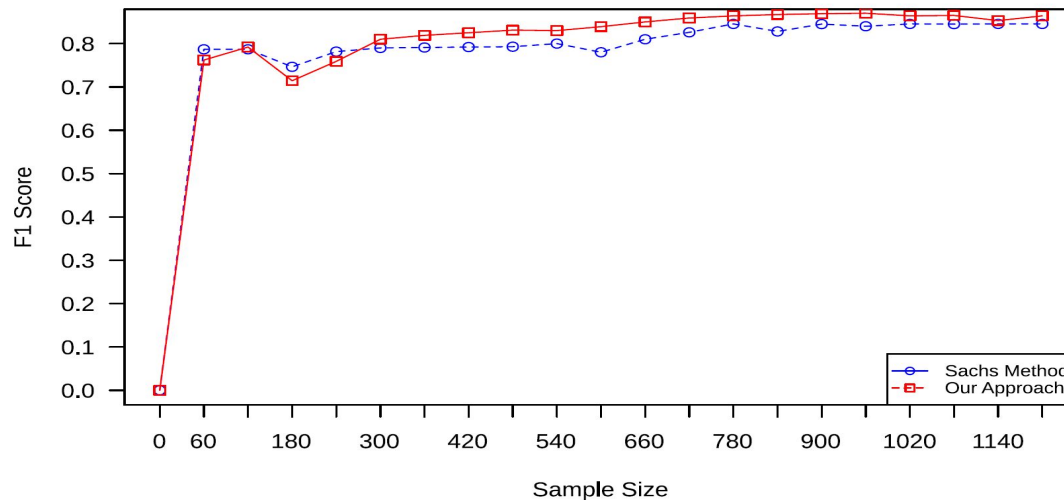


15 Asia_mut 2

Performance Analysis with respect to Sample size

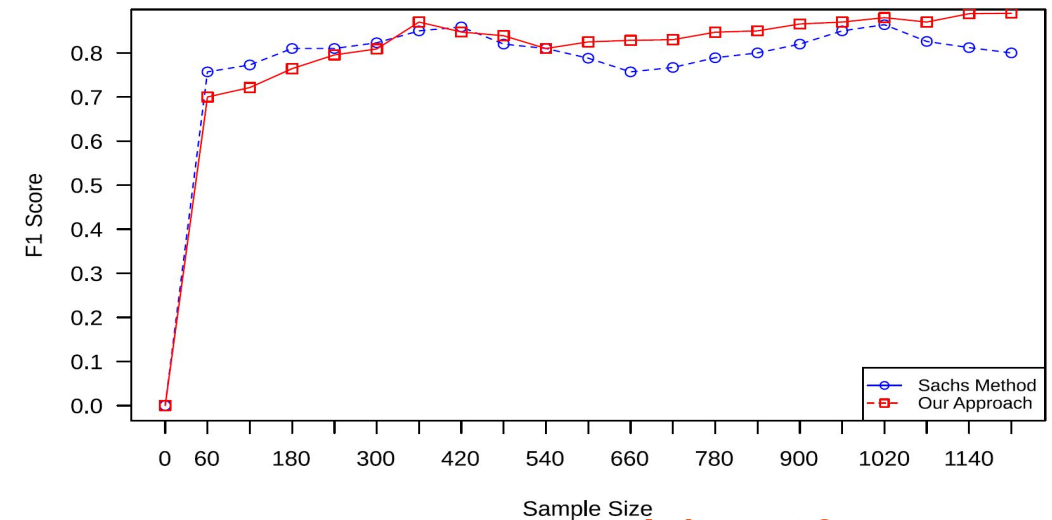


Flow Cytometry data



Asia_mut 1

- We plot the F1 score against various sample sizes
- Equal number of sample per experiment
- Compared the baseline method to Learn and vote
- Performance improves for “Learn and Vote” with larger sample size
- Pooling is a better than “Learn and Vote” with small sample size per experiments



Asia_mut 2

Limitations

- Approach is preliminary, needs more theoretical backing
- Does not work if dataset is too small
- We need equal samples of data per experiments

Future Directions

- Learning better given only Observations
- Categorizing which interventions are more informative
- Detecting presence of Latent variables

Thank You!

Any Questions?