

1a)

$$P(\text{Smart, Study, Pass}) = P(\text{Pass}|\text{Smart, Study}) * P(\text{Study}) * P(\text{Smart})$$

1b)

Smart	Study	Pass	Probability
-smart	-study	pass	.0839
-smart	-study	-pass	.3359
-smart	study	pass	.1679
-smart	study	-pass	.1120
smart	-study	pass	.126
smart	-study	-pass	.054
smart	study	pass	.1139
smart	study	-pass	.006

1c)

$$P(\text{Smart}|\text{Pass AND -Study}) = (P(\text{Pass AND -Study AND Smart})) / (P(\text{Pass AND -Study}))$$
$$= 0.6$$

1d)

$$P(\text{-Study}|\text{Smart AND -Pass}) = (P(\text{-Pass AND -Study AND Smart})) / (P(\text{-Pass AND Smart}))$$
$$= 0.9$$

1e)

$$P(\text{Pass}|\text{Smart}) = \sum P(\text{Pass}|\text{Smart, Study}) * P(\text{Study})$$
$$= 0.8$$

1f)

$$P(\text{Pass}|\text{Study}) = \sum P(\text{Pass}|\text{Smart, Study}) * P(\text{Smart})$$
$$= 0.705$$

2a)

$$P(\text{Cold, Sneeze, Allergic, Scratches, Cat}) = P(\text{Sneeze}|\text{Cold, Allergic}) * P(\text{Cold}) * P(\text{Allergic}|\text{Cat}) * P(\text{Scratches}|\text{Cat}) * P(\text{Cat})$$

2b)

$$= P(\text{Sneeze}|\text{-Cold, Allergic}) * P(\text{-Cold}) * P(\text{Allergic}|\text{Cat}) * P(\text{Scratches}|\text{Cat}) * P(\text{Cat})$$
$$= 0.0049$$

2c)

$$= (P(\text{-Cold, Sneeze, Allergic, Scratches, Cat})) / (P(\text{-Cold, Sneeze, Allergic, Scratches})) \\ = 0.754$$

2d)

$$= (P(\text{Scratches}|\text{Cat}) * P(\text{Cat})) / (P(\text{Scratches}))$$

$$P(\text{Scratches}) = P(\text{Scratches}|\text{Cat}) * P(\text{Cat}) + P(\text{Scratches}|\text{-Cat}) * P(\text{-Cat}) \\ = 0.059$$

2e)

With 5 binary variables, we would need to compute $2^5=32$ joint probabilities.

3a)

```
(:action start-car
:parameters (?car)
:precondition (and (at ?car)
                   (have-key)
                   (charged-battery ?car)
                   (has-gas ?car))
:effect (and (running ?car)
             (at ?car)
             (have-key)))
```

3b)

$\text{Poss}(\text{Start}(\text{car}),s) \leftrightarrow \text{At}(\text{car},s) \text{ AND } \text{HaveKey}(s) \text{ AND } \text{ChargedBatter}(\text{car},s) \text{ AND } \text{HasGas}(\text{car},s)$

Effects:

$\text{Running}(\text{car}, \text{do}(\text{Start}(\text{car}),s))$

$\text{At}(\text{car}, \text{do}(\text{Start}(\text{car}),s)) \text{ AND } \text{HaveKey}(\text{do}(\text{Start}(\text{car}),s))$

3c)

$\forall c=\text{car}, \text{HasGas}(c, \text{do}(\text{Start}(\text{car}),s)) \leftrightarrow \text{HasGas}(c,s)$