Madine Learning Assignment 1 - EE 871 16EE 234 166100

1 Reddy - Mikks Problem:

(CE, CI = 3,2) - Taken from max = CEXE + CIXI = 3XE + 2XI Subjected to the constrains: class example

a) By using graphical method and libreoffice solver, the optimal point obtained is:

$$x_{\rm E} = \frac{10}{3} \qquad \tilde{z} =$$

b) 7 = 38 (optimal value) - Using graphical method and

e) Lagrange multiplieu for each of the constrains Lagrangian:

$$L(\underline{x},\underline{M}) = f(\underline{x}) + \sum_{j=1}^{6} M_{j}g_{j} \qquad M_{j} \leq 6$$

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$$L(\underline{x},\underline{M}) = f(\underline{x}) + \nabla_{x} (M_{1}g_{1}) + \nabla_{x} (M_{2}g_{2}) = 0$$

$$\begin{bmatrix} \frac{\partial z}{\partial x_{1}} \\ \frac{\partial z}{\partial x_{2}} \end{bmatrix} + \mu_{1} \begin{bmatrix} \frac{\partial g_{1}}{\partial x_{1}} \\ \frac{\partial g_{1}}{\partial x_{2}} \end{bmatrix} + \mu_{2} \begin{bmatrix} \frac{\partial g_{2}}{\partial x_{1}} \\ \frac{\partial g_{2}}{\partial x_{2}} \end{bmatrix} = 0$$

$$\begin{bmatrix} \frac{\partial}{\partial x_{1}} \\ \frac{\partial}{\partial x_{2}} \end{bmatrix} + \mu_{1} \begin{bmatrix} \frac{\partial}{\partial x_{1}} \\ \frac{\partial}{\partial x_{2}} \end{bmatrix} + \mu_{2} \begin{bmatrix} \frac{\partial}{\partial x_{2}} \\ \frac{\partial}{\partial x_{2}} \end{bmatrix} = 0$$

$$\begin{bmatrix} \frac{\partial}{\partial x_{1}} \\ \frac{\partial}{\partial x_{2}} \end{bmatrix} + \mu_{1} \begin{bmatrix} \frac{\partial}{\partial x_{2}} \\ \frac{\partial}{\partial x_{2}} \end{bmatrix} = 0$$

$$2\mu_{1} + \mu_{2} = -2$$

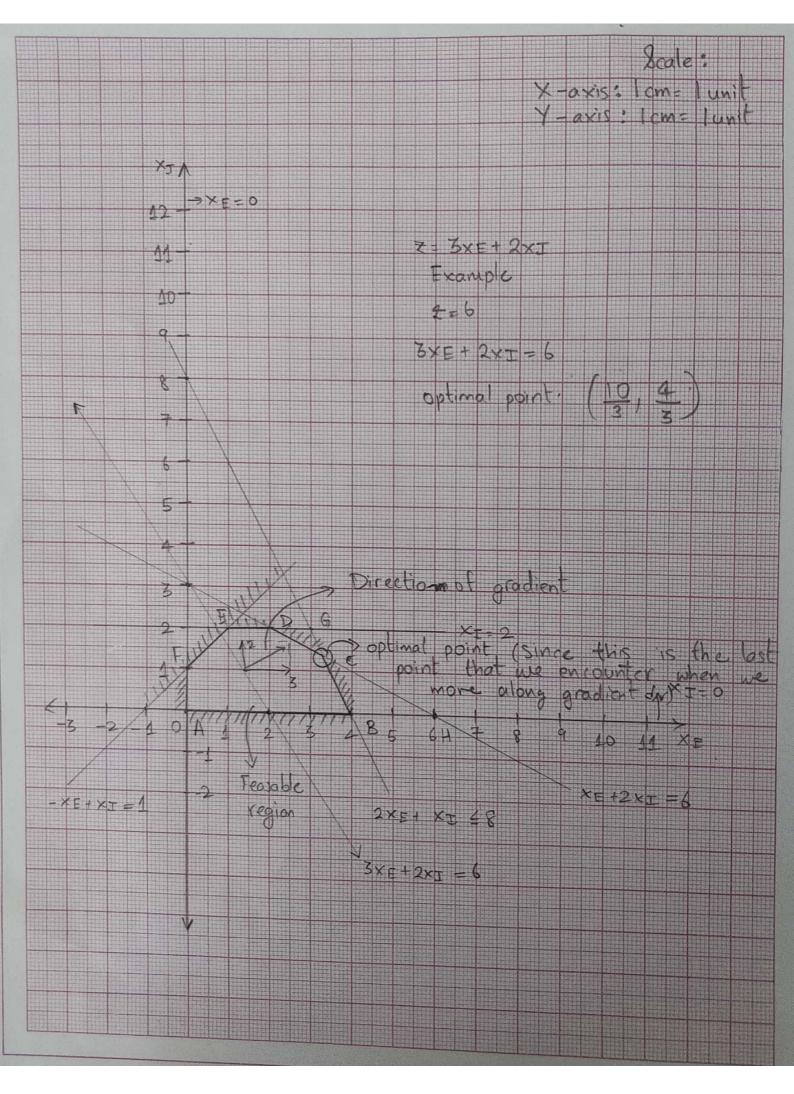
$$\mu_{1} + 2\mu_{2} = -3$$

$$-3\mu_{2} = 4 \implies$$

$$M_1 + 2M_2 = -3$$

$$-3M_2 = 4 \Rightarrow M_1 = -\frac{4}{3}, M_1 = -\frac{1}{3}$$

- d) ① and ② -> These constrains' intersection solution is obtained. These are binding lactive constrains
- 3,4,50 The solution is not obtained by the intersection of any of these points. Hence, then are alled non-binding, constrains.
 - e) For constains () and @ surplus value = 0, Rince the solution lies on these lines: -Optimal point (XE, XI) = (10, 4)



For the other constains

$$8_{3}^{2} = 1 + 10/3 - 4/3$$

$$8_{3}^{2} = 3$$

$$1/2 \times 1 - 2 + 8_4^2 = 0$$

$$8_4^2 = 2 - \frac{4}{3}$$
 $8_4^2 = \frac{2}{3}$

$$\frac{1}{6} - \times_{\text{I}} + \lambda_{\text{i}}^{2} = 0$$

$$\lambda_{\text{i}}^{2} = \times_{\text{I}}$$

$$-X_{E} + 3_{5}^{2} = 0$$

$$8_5^2 = x_E = \frac{10}{3}$$

f) > (osts of A and B are same)

Invest more money in resource B - since lagrange mulltiplier corresponding to resource B has a higher magnitude compared to that of resource A.

|M2| = 4/5 and |M1| = /3

|M3| > |M1|

For same change in the quantity of resources,

increase in income will be higher for resource D

Binding constrains are:

$$\frac{1}{2} \leq \frac{CE}{CI} \leq 2$$

$$\frac{1}{2} \leq \frac{3}{C_{I}} \leq 2$$

$$\frac{1}{2} \stackrel{C}{=} \stackrel{C}{=} \stackrel{E}{=} \stackrel{E}$$

The optimal value = 6 (value of inequire).

The range can be described as
$$\rightarrow$$
 $\left(\frac{10}{3}, \frac{4}{3}\right)$ to $\left(\frac{2}{2}\right)^2$

line segment

① Objective function of slope = slope of constrain@ objective function of the form:

The optimal solution is along the line segment BC

The optimal value = 8 (value of ineq constrain)

The range can be described as ->

$$(40)$$
 to $(\frac{10}{3}, \frac{4}{3}) \rightarrow line segment$

b) (1) For constrain 1 to be redundant; it must pass through point (7(3,2) and beyond that it will be redundant.

$$X_{E} + 2x_{I} \Rightarrow 3 + 2x_{2} = 7$$

For conshain (2) to be redundant; must pass through point H(6,0) and beyond that it will be redundant

2xE+XI => 2x6+0= 12 12×E+×I ≤ 12 | → constrain redundant constain 3 to be redundant pars through (6,3) and beyond that will be redundant $-\times_{I} + \times_{I} \Rightarrow -0+3$ -XE +XI < 3 For constrain 1 to be redundant, must pass through > $- \times E + \times I = 1$ XE + 2xT = 6 3x1 = 7

$$X_{I} \leq 2$$

$$X_{I} \leq \frac{7}{3} \Rightarrow \text{above this redundant}$$

For constrain (5) to be redundant, must poss through (-1,0) → [XE 7,-1] and left → redundant constrain (6) -> can never be redundant -> No point of intersection below that

(ii) Resource B was chosen in problem. If, for maximum reform, limit on resource B should be increased to 12 From 8. At these times , the gross income ".e \$18k#

(iii) The new x obtained from graph and libre office

$$x^{*} = \begin{bmatrix} x_{E} \\ x_{I} \end{bmatrix} = \begin{bmatrix} 6 \\ 0 \end{bmatrix}$$

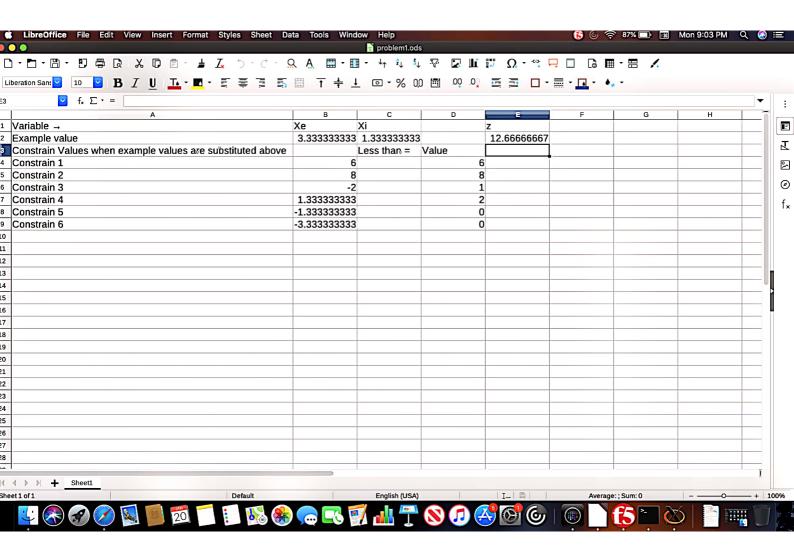
$$x^{*} = 3x_{E}^{*} + 2x_{I}^{*} = 3 \times 6 + 2 \times 0 = 18 \text{ k}$$

- 3) 2) a) (i) If the slope of the contour of the objective function is less than the slope of constrain (2) or is greater than the slope of constrain (2), then point (will remain the opinal solution. This is because when the value slope is between these 2 values (soid range), the point c is the farthest point in the feosoble region when mored along the gradient direction of the objective function. If the slope of direction of the objective function is first than the contours of the objective function is first than constrain 1, then point D will be the optimal solution. If more than that of constrain 2, point B becomes optimal solution.
 - 2) a) (ii) When objective function aligns with the constrain(1) his the line segment CD is the optimal solution. The objective function value remains same along that line segment. And the similar case happens for constrain (2) along line segment BC.
 - 2) b)(i) Resource, can be rendered redundant only if the intersection of attent 2 other constrains lie in the intersoble region of the space made by the constrains. The max constrain limit tells us the max amount of a particular resource that heeds to be stocked.

- 2) b) (ii) As calculated in 2b) if the resource limit of Resource B, ran be changed up to the value 12.

 If You do not need to shock more than 12 tons
 if resource B ito maximize income.
 - 26)(iii) Once resource limit is increosed to 12 tons, the new solutions are x = (6,0).

 At this value the gross income is $18 \times $$
- change the coefficients of the constrains will change the shape and area of the feasable region, as a result, the optimal solution will also change. It may so happen that the feasable region might become unbounded which might will might at push optimate 0, +00



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- 4.2 Surplus
- 5.1 Return rate
- 8.1 After (0,2)