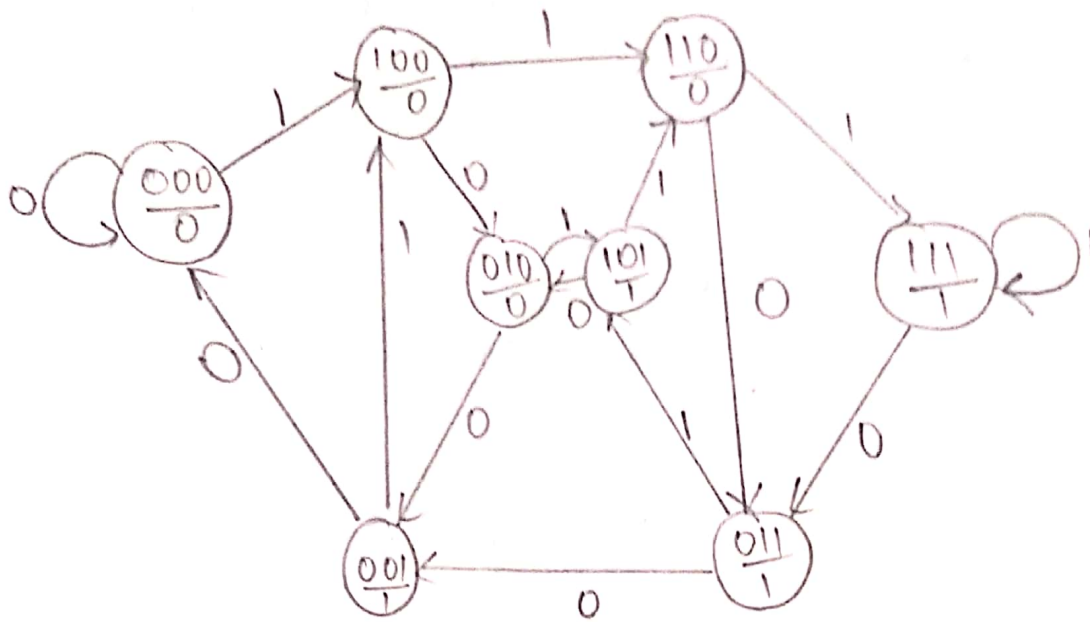


①



As the output depends only on the present state  
hence Moore state machine.

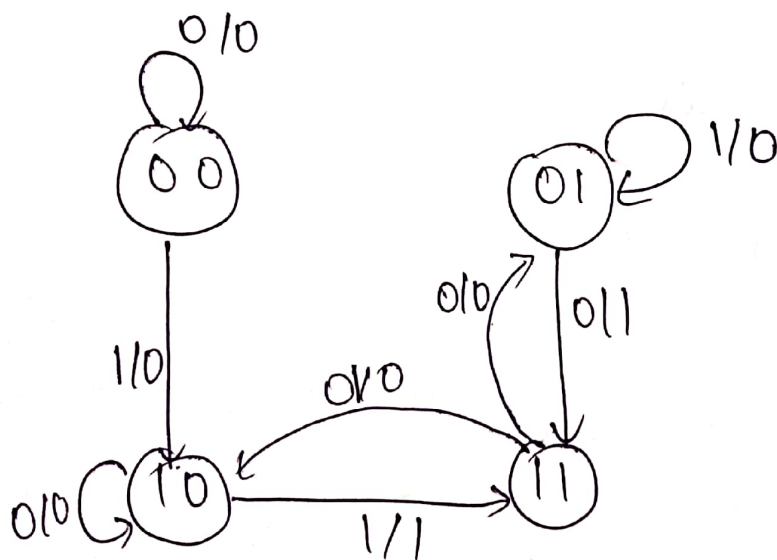
② For the given circuit

$J_A = X\bar{B} + \bar{X}B = X \oplus B$
$K_A = \bar{X}B$
$J_B = XA$
$K_B = XA$
$Out = AB$

$x = 0$   
 $A$

A	B	x	$x \oplus B$ $J_A$	$\bar{x} B$ $K_A$	$x A$ $J_B$	$\bar{x} A$ $K_B$	$A^+$	$B^+$	$A B$ Out
0	0	0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	1	0	0
0	1	0	1	1	0	0	1	1	1
0	1	1	0	0	0	0	0	1	0
1	0	0	0	0	0	0	1	0	0
1	0	1	1	0	1	1	1	1	1
1	1	0	1	1	0	0	0	1	0
1	1	1	0	0	1	1	1	0	0

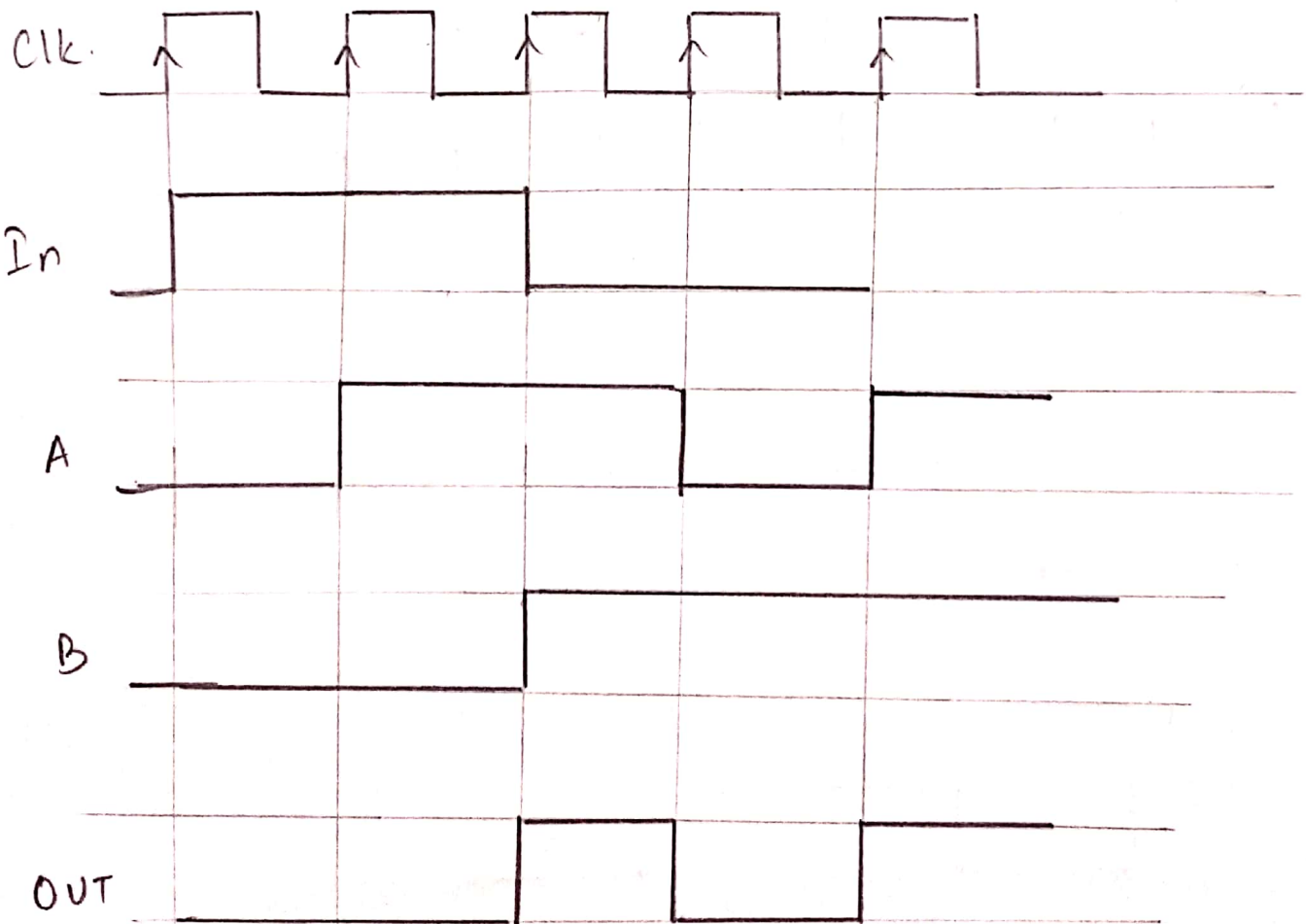
State representation



State graph

$$X = 01100$$

A	B	X	$X \oplus B$ $J_A$	$\bar{X} B$ $K_A$	$X A$ $J_B$	$\bar{X} A$ $K_B$	$A^+$	$B^+$	Out = (AA)
0	0	0	0	0	0	0	0	0	0
0	0	1	1	0	0	0	1	0	0
1	0	1	1	0	1	1	1	1	<del>0</del> 1
1	1	0	1	1	0	0	0	1	0
0	1	0	1	1	0	0	1	1	1



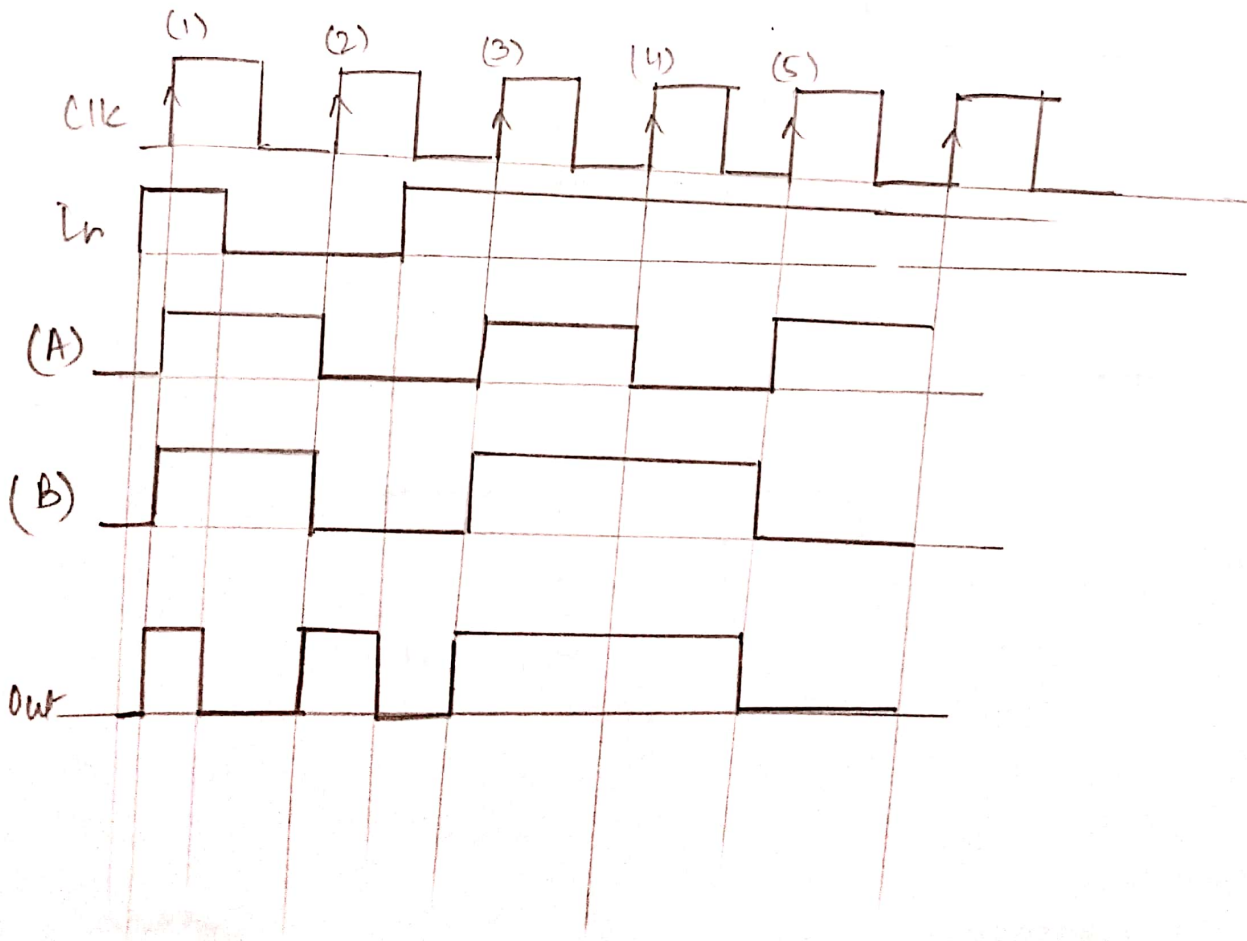
(3)  $J_1 = X$   $K_1 = \bar{X} + Q_2$

$J_2 = X$   $K_2 = \bar{Q}_1 + \bar{X}$

Out =  $X \oplus \bar{Q}_2$

$K_1 = 1$

A	B	In	$J_A$	$K_A$	$J_B$	$K_B$	$A^+$	$B^+$	Out
0	0	1	1	0	1	0	1	1	
1	1	0	0	1	0	1	0	0	
0	0	1	1	0	1	1	1	1	
1	1	1	1	1	1	0	0	1	
0	1	1	1	1	1	1	1	0	



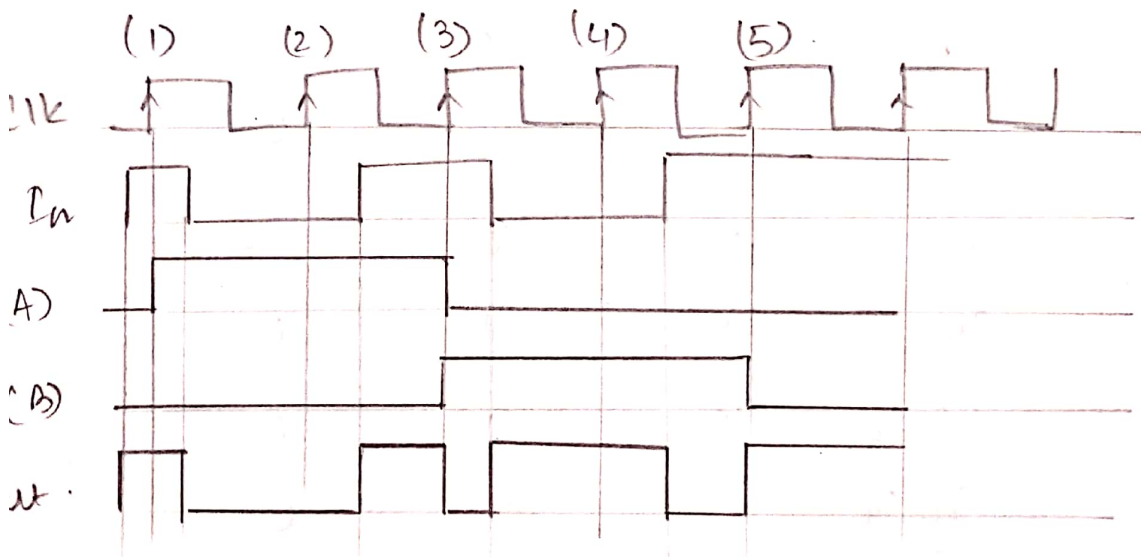
$$k_1 = k_2 = x.$$

$$J_1 = \bar{Q}_2 x$$

$$Q_{out} = x \oplus Q_2$$

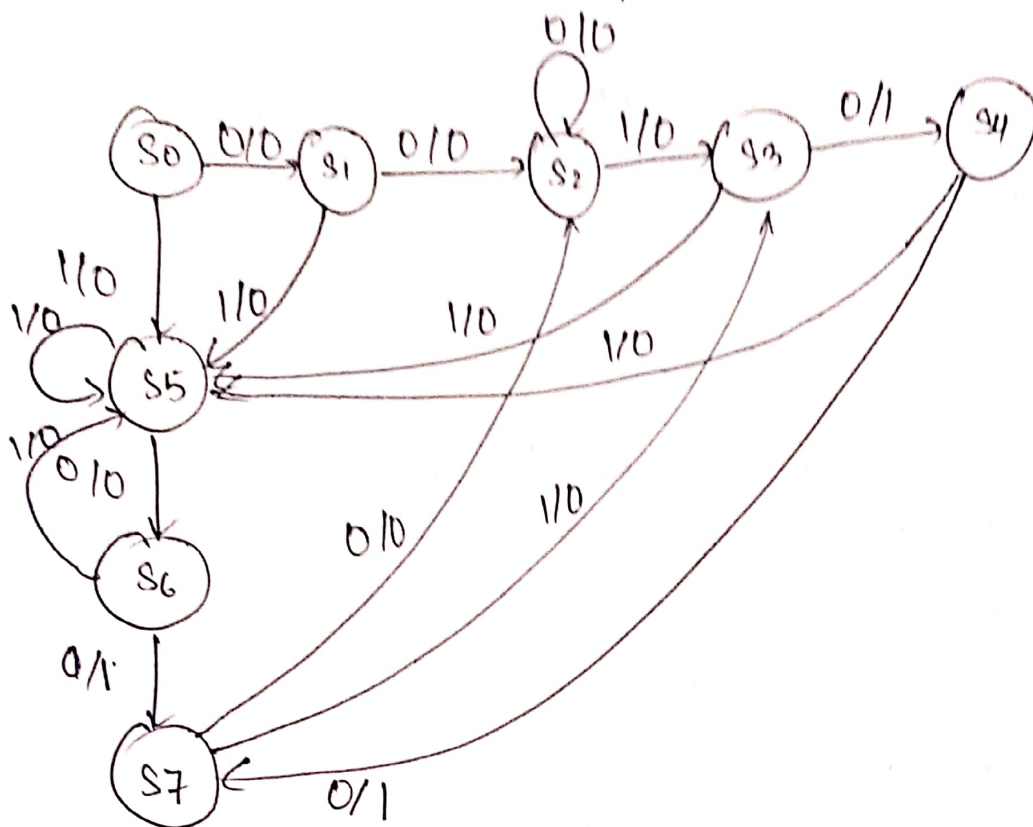
$$J_2 = x Q_1$$

A	B	$I_n$	$J_A$	$K_A$	$J_B$	$K_B$	$A^+$	$B^+$	Out
0	0	1	1	1	0	1	1	0	
1	0	0	0	0	0	0	1	0	
1	0	1	1	1	1	1	0	1	
0	1	0	0	0	0	0	0	1	
0	1	1	0	1	0	1	0	0	





⑤ to detect 0010 / 100



Present state	Next state		Output	
	X=0	X=1	X=0	X=1
S <sub>0</sub>	S <sub>1</sub>	S <sub>5</sub>	0	0
S <sub>1</sub>	S <sub>2</sub>	S <sub>5</sub>	0	0
S <sub>2</sub>	S <sub>2</sub>	S <sub>3</sub>	0	0
S <sub>3</sub>	S <sub>4</sub>	S <sub>5</sub>	1	0
S <sub>4</sub>	<del>S<sub>4</sub></del> S <sub>2</sub>	S <sub>5</sub>	1	0
S <sub>5</sub>	<del>S<sub>6</sub></del> S <sub>4</sub>	S <sub>5</sub>	0	0
S <sub>6</sub>	S <sub>7</sub>	S <sub>5</sub>	1	0
S <sub>7</sub>	S <sub>2</sub>	S <sub>3</sub>	0	0

From here  $S_2 = S_7$  and  $S_6 = S_4$

$\therefore S_6$  and  $S_7$  redundant states.

State table.

A	B	C	In	$A^+$	$B^+$	$C^+$	Out
0	0	0	0	0	0	0	0
0	0	0	1	1	0	1	0
0	0	1	0	0	1	0	0
0	0	1	1	1	0	1	0
0	1	0	0	0	1	0	0
0	1	0	1	0	1	1	0
0	1	1	0	1	0	0	1
0	1	1	1	1	0	1	0
1	0	0	0	0	1	0	1
1	0	0	1	1	0	1	0
1	0	1	0	1	0	0	0
1	0	1	1	1	0	1	0

$A^+$

	$\bar{C}\bar{X}$	$\bar{C}X$	$CX$	$C\bar{X}$
$\bar{A}\bar{B}$	0	1	1	0
$\bar{A}B$	0	0	1	1
$AB$	x	x	x	x
$A\bar{B}$	0	1	1	1

$$A^+ = \bar{B}X + BC + CX + AC$$

$B^+$

	$\bar{C}\bar{X}$	$\bar{C}X$	$CX$	$C\bar{X}$
$\bar{A}\bar{B}$	0	0	0	1
$\bar{A}B$	1	1	0	0
$AB$	x	x	x	x
$A\bar{B}$	1	0	0	0

$$B^+ = A\bar{C}\bar{X} + B\bar{C} + \bar{A}\bar{B}C\bar{X}$$

out

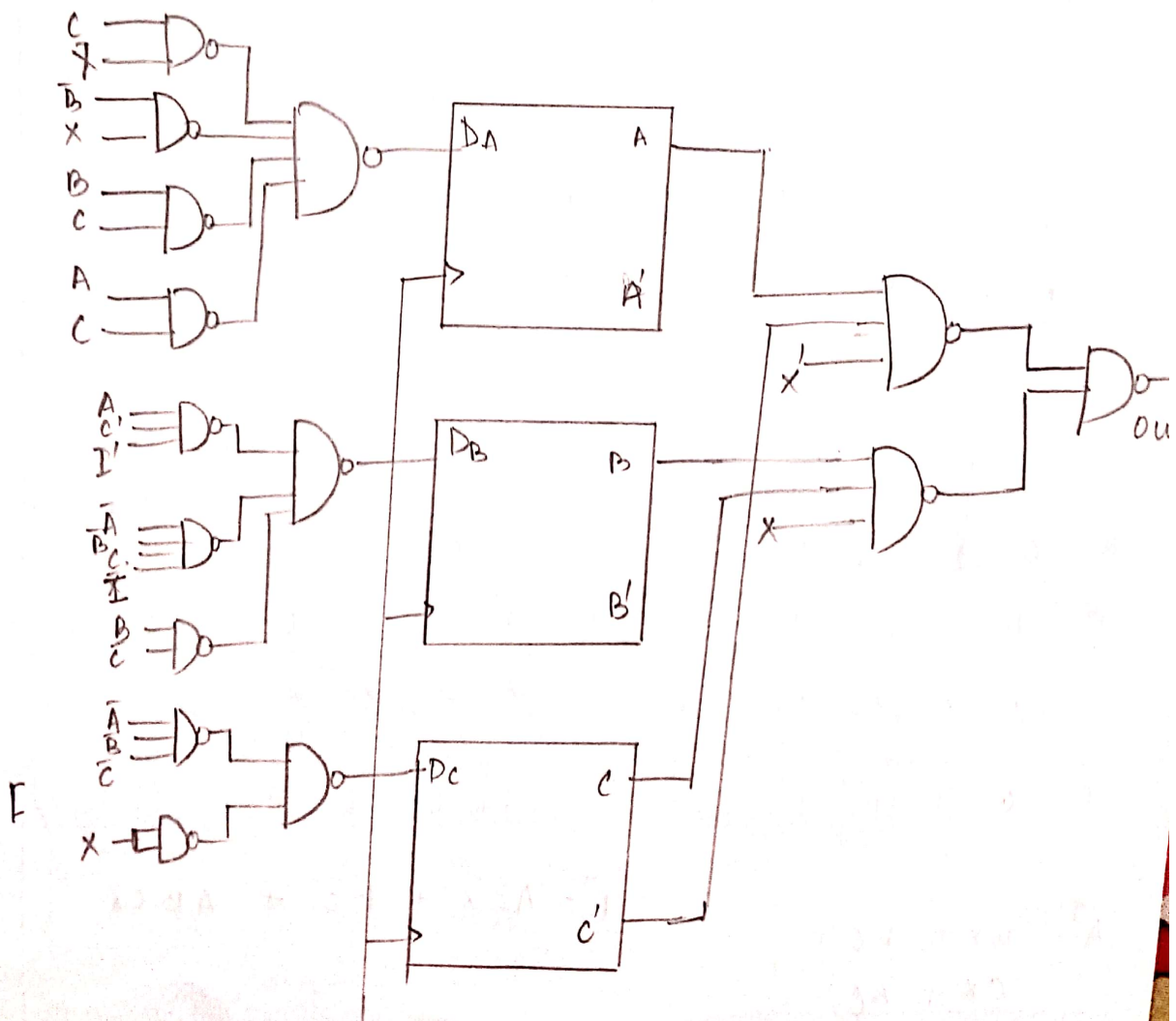
	$\bar{C}X$	$\bar{C}\bar{X}$	$CX$	$C\bar{X}$
$\bar{A}\bar{B}$	0	0	0	0
$\bar{A}B$	0	0	0	1
$AB$	x	x	x	x
$A\bar{B}$	1	0	0	0

$out = A\bar{C}\bar{X} + B C\bar{X}$

$C^+$

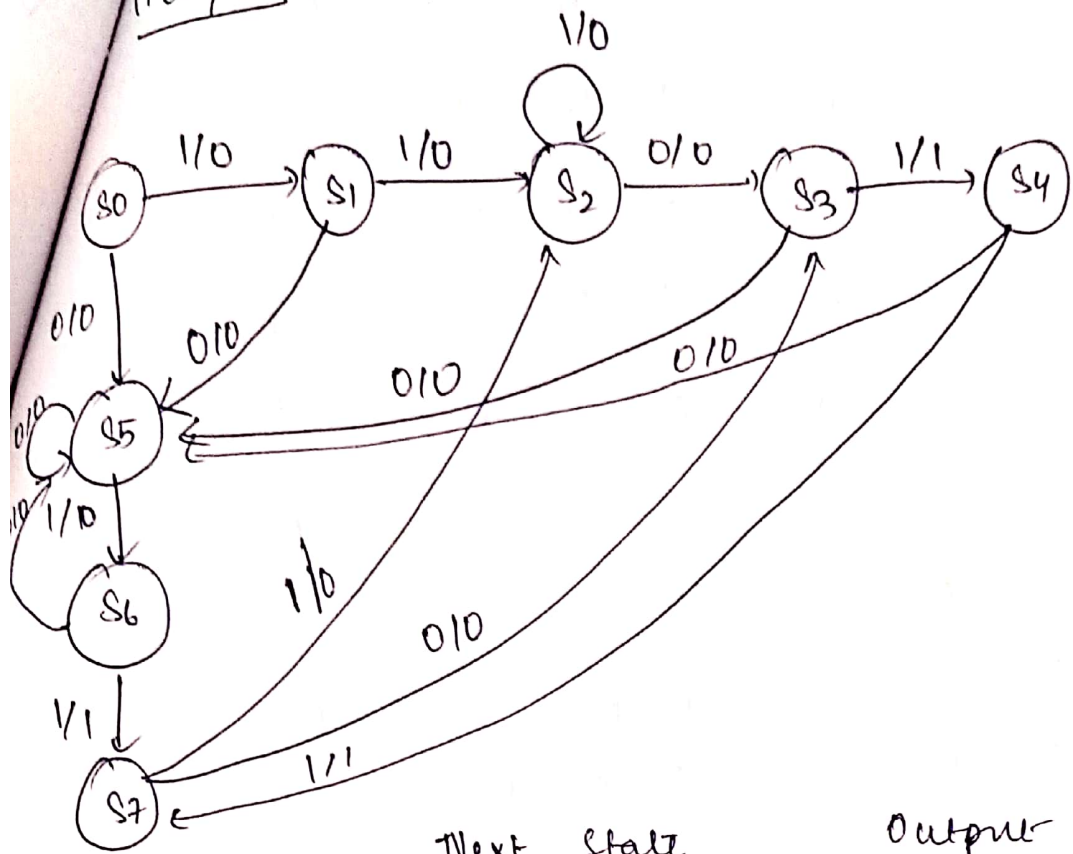
	$\bar{C}X$	$\bar{C}\bar{X}$	$CX$	$C\bar{X}$
$\bar{A}\bar{B}$	1	1	1	0
$\bar{A}B$	0	1	1	0
$AB$	x	x	x	x
$A\bar{B}$	0	1	1	0

$C^+ = \bar{A}\bar{B}\bar{C} + X$





1101/011



Present	Next State		Output	
	X=0	X=1	X=0	X=1
S <sub>0</sub>	S <sub>5</sub>	S <sub>1</sub>	0	0
S <sub>1</sub>	S <sub>5</sub>	S <sub>2</sub>	0	0
S <sub>2</sub>	S <sub>3</sub>	S <sub>2</sub>	0	0
S <sub>3</sub>	S <sub>5</sub>	S <sub>4</sub>	0	1
S <sub>4</sub>	S <sub>5</sub>	S <sub>2</sub>	0	1
S <sub>5</sub>	S <sub>5</sub>	S <sub>6</sub>	0	0
S <sub>6</sub>	S <sub>5</sub>	S <sub>7</sub>	0	0
S <sub>7</sub>	S <sub>3</sub>	S <sub>2</sub>	0	0

From here  $S_7 = S_2$   
and  $S_4 = S_6$

A	B	C	In	$A^+$	$B^+$	$C^+$	Output
0	0	0	0	1	0	1	0
0	0	0	1	0	0	1	0
0	0	1	0	1	0	1	0
0	0	1	1	0	1	0	0
0	1	0	0	0	1	1	0
0	1	0	1	0	1	0	0
0	1	1	0	1	0	1	0
0	1	1	1	1	0	0	1
1	0	0	0	1	0	1	0
1	0	0	1	0	1	0	1
1	0	1	0	1	0	1	0
1	0	1	1	1	0	0	0

$A^+$

	$\bar{C}\bar{X}$	$\bar{C}X$	$C\bar{X}$	$CX$
$\bar{A}\bar{B}$	1	0	0	1
$\bar{A}B$	0	0	1	1
$A\bar{B}$	$\times$	$\times$	$\times$	$\times$
$AB$	1	0	1	1

$$A^+ = C\bar{X} + \bar{B}\bar{X} + B\bar{C} + AC$$

$$= AC + BC + \bar{B}\bar{X} + C\bar{X}$$

$B^+$

	$\bar{C}\bar{X}$	$\bar{C}X$	$C\bar{X}$	$CX$
$\bar{A}\bar{B}$	0	0	1	0
$\bar{A}B$	1	1	0	0
$A\bar{B}$	$\times$	$\times$	$\times$	$\times$
$AB$	0	1	0	0

$$B^+ = B\bar{C} + A\bar{C}X + \bar{A}\bar{B}CX$$

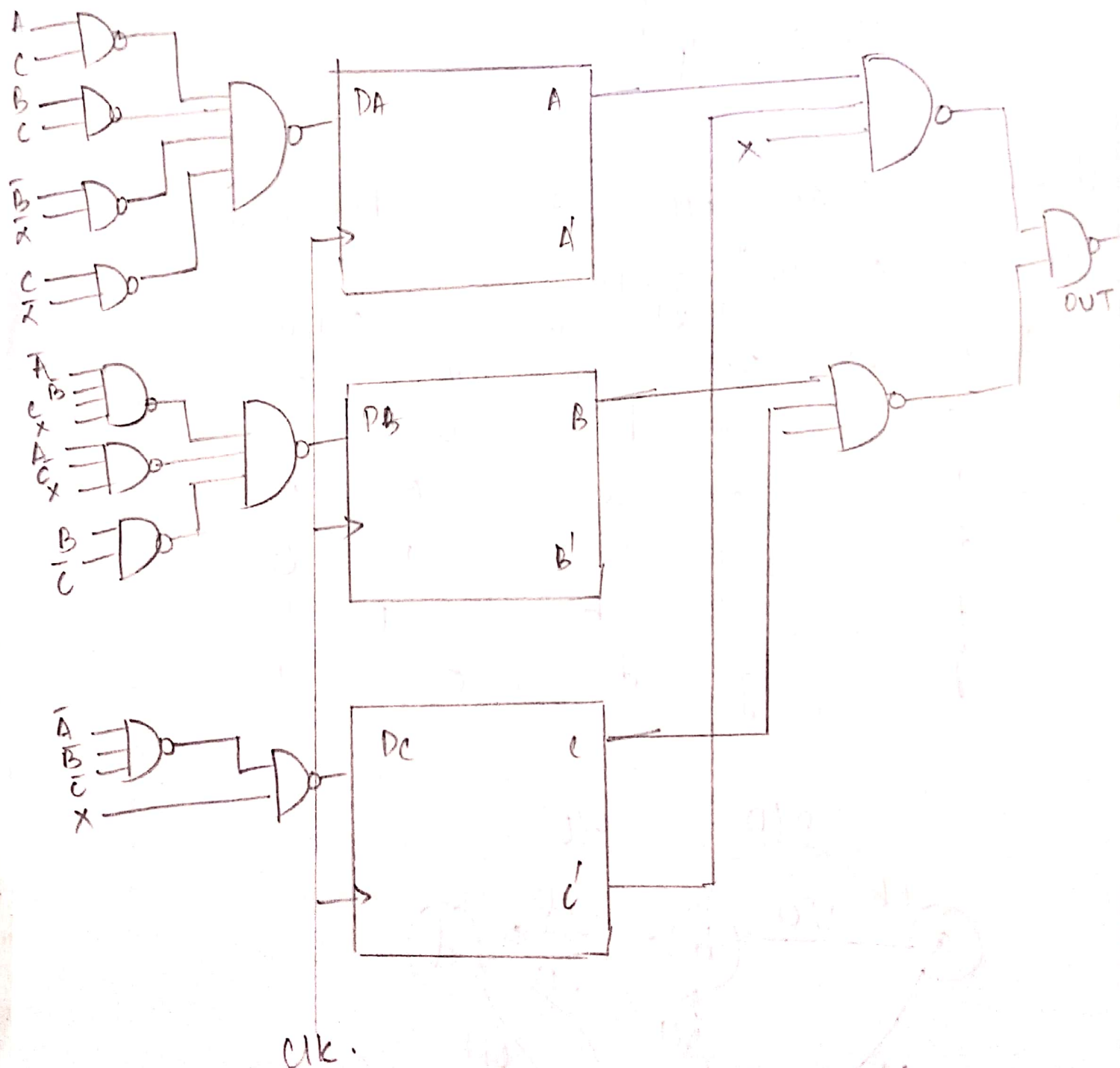
1	1	0	1
1	0	0	0
x	x	x	x
1	0	0	1

$$c^t = \bar{X} + \bar{A}\bar{B}\bar{C}$$

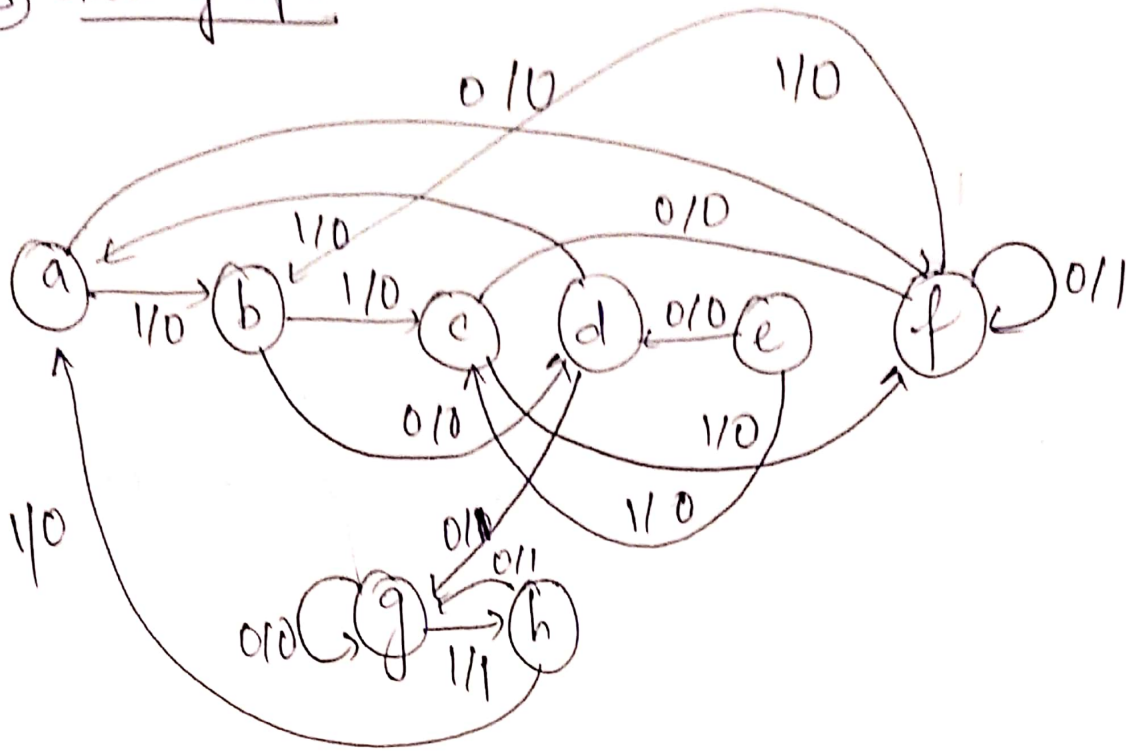
Out:

0	0	0	0
0	0	1	0
x	1	1	1
0	1	0	0

$$out = A\bar{C}X + BCX$$



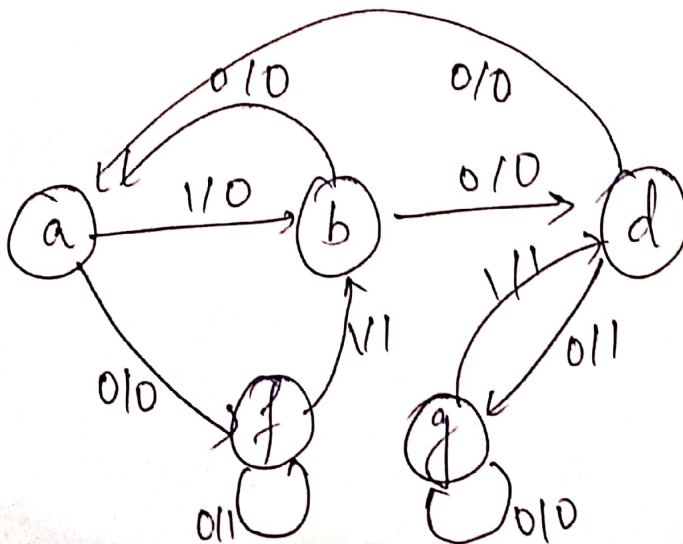
# ⑧ State graph



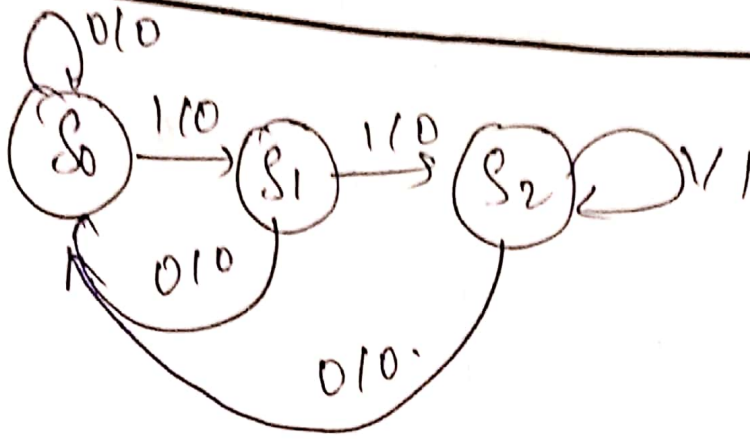
from the state graph,  $d=h$  ;  $b=e$  ;  $a=c$

So reduced state graph.

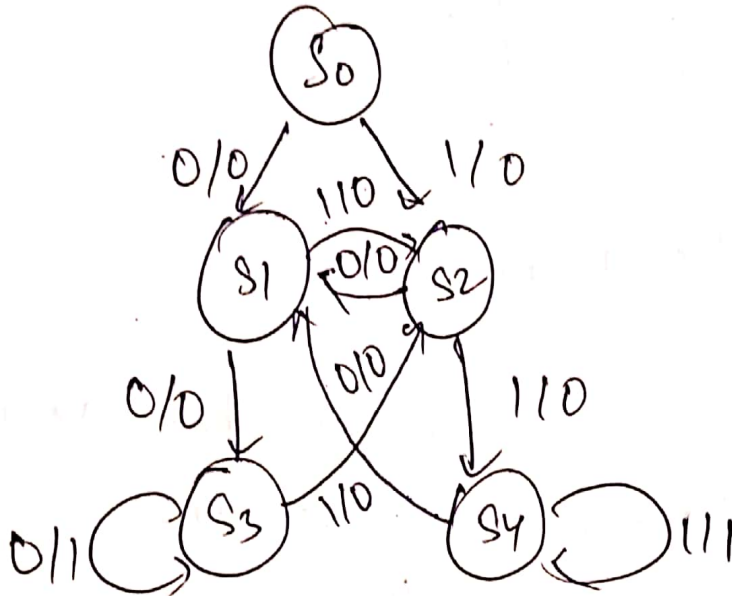
Present state	Next state		Output	
	$x=0$	$x=1$	$x=0$	$x=1$
a	f	b	0	0
b	d	a	0	0
d	g	a	1	0
f	f	b	1	1
g	g	d	0	1



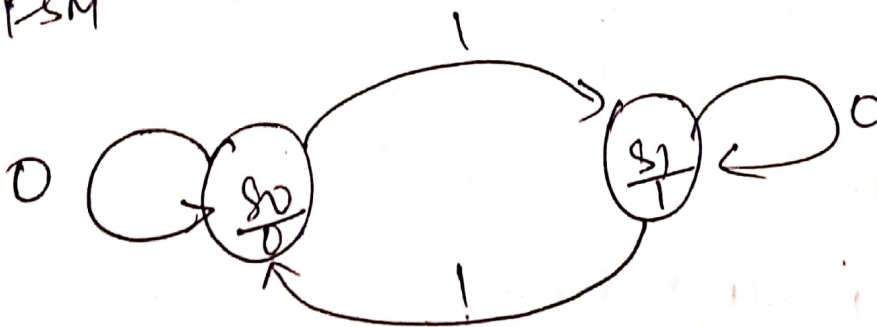
9



10



The output of this FSM to the following FSM





$$\textcircled{11} \quad T_{\min} = (T_{\text{clk-q}})_{\text{longest}} + T_{\text{setup}} + (T_{\text{or-gate}})_{\text{longest}}$$

$$= 12 \text{ ns} + 5 \text{ ns} + 4 \text{ ns}.$$

$$T_{\min} = 21 \text{ ns}.$$

$$\Rightarrow f_{\max} = \frac{10^9}{21} \text{ Hz}$$

$$\text{Minimum delay} = (6+1) \text{ ns}.$$

the minimum delay should have positive slack for  
hold time =  $7 \text{ ns} - 3 \text{ ns}$   
=  $4 \text{ ns}$ .

$\therefore$  Minimum time after rising edge at which the input can change

$$= 21 \text{ ns} - 4 \text{ ns}$$

$$= 17 \text{ ns} \rightarrow \text{latest time}.$$

$$\text{earliest time} = 21 \text{ ns} - 17 \text{ ns} + 3 \text{ ns}$$

$$= 7 \text{ ns}$$

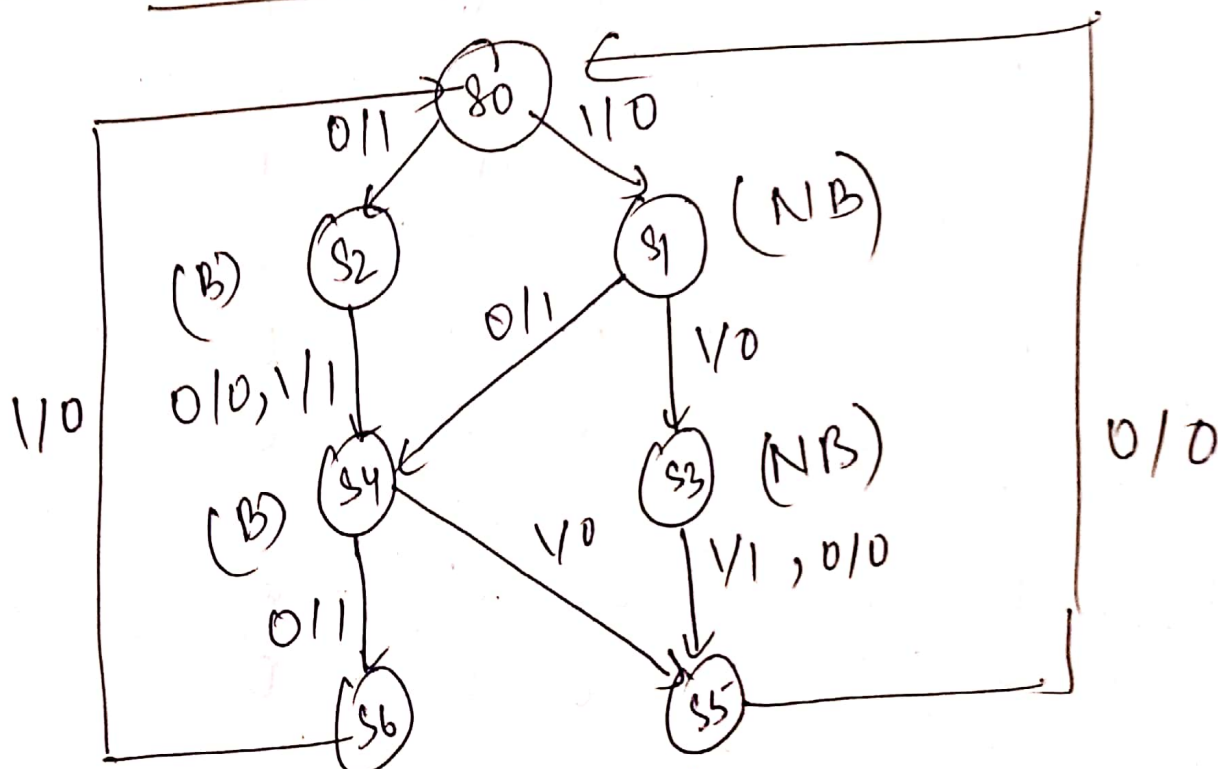
(12)  $T_{min} = (T_{clk-q})_{longest} + (T_{c.c})_{longest} + T_{setup}$   
 $= 24ns + 16ns + 8ns$   
 $= 48ns$

$$f_{max} = \frac{10^9}{48} \text{ Hz}$$

$T_{earliest}$  can be changed at 12ns.

$T_{latest}$  can be changed at 38ns.

(7) FSM for excess 3 to BCD



	0	1	0	1
$S_0$	$S_2$	$S_1$	1	0
$S_1$	$S_4$	$S_3$	1	0
$S_2$	$S_4$	$S_4$	0	1
$S_3$	$S_5$	$S_5$	0	1
$S_4$	$S_6$	$S_5$	1	0
$S_5$	$S_0$	-	0	x
$S_6$	-	$S_0$	x	0

A	B	C	$Z_n$	$A^+$	$B^+$	$C^+$	out
0	0	0	0	0	1	0	1
0	0	0	1	0	0	1	0
0	0	1	0	1	0	0	1
0	0	1	1	<u>0</u>	1	1	<u>0</u>
0	1	0	0	1	0	0	0
0	1	0	1	1	0	0	1
0	1	1	0	1	0	1	0
0	1	1	1	<u>1</u>	0	1	<u>1</u>
1	0	0	0	1	1	0	1
1	0	0	1	1	0	1	0
1	0	1	0	0	0	0	0
1	0	1	1	<u>x</u>	x	x	<u>x</u>
1	1	0	0	x	x	x	x
1	1	0	1	0	0	0	0

$\Rightarrow$  gives

$$A^+ = \bar{A}B + \bar{A}C\bar{I} + A\bar{B}\bar{C}$$

$$B^+ = \bar{B}\bar{C}\bar{I} + \bar{B}C\bar{I}$$

$$C^+ = C\bar{I} + B\bar{I} + BC$$

$$\text{out} = \bar{A}\bar{B}\bar{I} + A\bar{C}\bar{I} + B\bar{I}$$

