

Simple Linear Regression

```
In [166]: import numpy as np

import seaborn as sns
import matplotlib.pyplot as plt

% matplotlib inline
```

```
In [167]: iris = sns.load_dataset('iris')
nsamples = 5
iris.sample(nsamples)
```

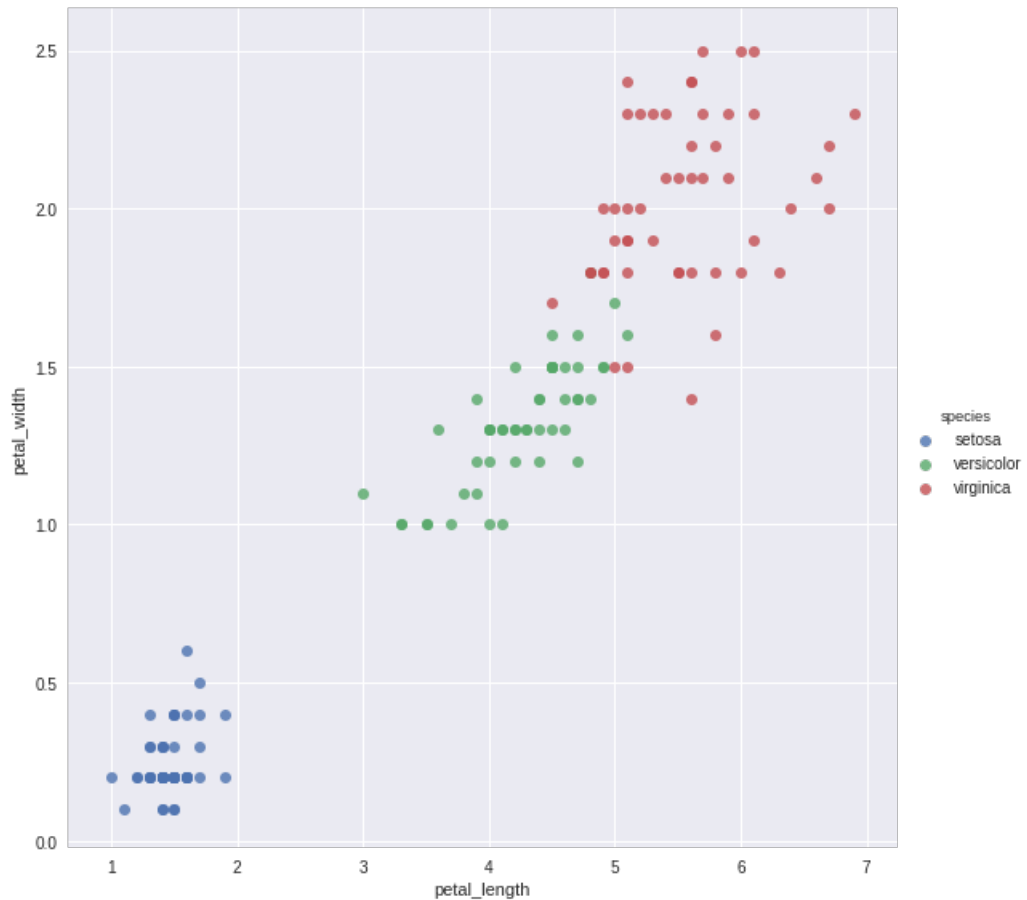
Out[167]:

| | sepal_length | sepal_width | petal_length | petal_width | species |
|-----|--------------|-------------|--------------|-------------|------------|
| 49 | 5.0 | 3.3 | 1.4 | 0.2 | setosa |
| 141 | 6.9 | 3.1 | 5.1 | 2.3 | virginica |
| 63 | 6.1 | 2.9 | 4.7 | 1.4 | versicolor |
| 94 | 5.6 | 2.7 | 4.2 | 1.3 | versicolor |
| 143 | 6.8 | 3.2 | 5.9 | 2.3 | virginica |

```
In [168]: column = { 'feature': 'petal_length', 'target': 'petal_width' }
```

```
In [169]: sns.lmplot(x = column['feature'], y = column['target'], data = iris, fit_reg = False, hue = 'species', size = 8)
```

```
Out[169]: <seaborn.axisgrid.FacetGrid at 0x7f9e9f795b38>
```



```
In [170]: x, y = iris[column['feature']], iris[column['target']]
```

```
In [171]: from scipy.stats import pearsonr
```

```
In [172]: r, p = pearsonr(x, y)
r
```

```
Out[172]: 0.96286543140279612
```

```
In [173]: def predict(x, beta0, beta1):
          return beta0 + beta1 * x
```

```
In [200]: def plot(beta0, beta1):
          sns.lmplot(x = column['feature'], y = column['target'], data = iris, fit_reg = False, hue = 'species', size = 8)
          plt.plot(x, predict(x, beta0, beta1))
```

```
In [201]: beta0, beta1 = np.random.rand(2)
          beta0, beta1
```

```
Out[201]: (0.94634819241045165, 0.23293986319851268)
```

```
In [202]: from prettytable import PrettyTable
          from IPython.core.display import display, HTML
```

```
In [203]: def display_table(beta0, beta1):
            table = PrettyTable(['$i$',
                                '$x_{i}$',
                                '$y_{i}$',
                                '$\hat{y}_{i}$',
                                '$(y_{i}-\hat{y}_{i})$',
                                '$(y_{i}-\hat{y}_{i})^2$'])

            size = len(x)
            m = 0
            rows = [ ]

            for i in range(size):
                p = predict(x[i], beta0, beta1)
                e = y[i] - p
                s = np.power(e, 2)
                m = m + s

                rows.append([i + 1, x[i], y[i], p, e, s])

            for i in range(10):
                table.add_row(rows[i])

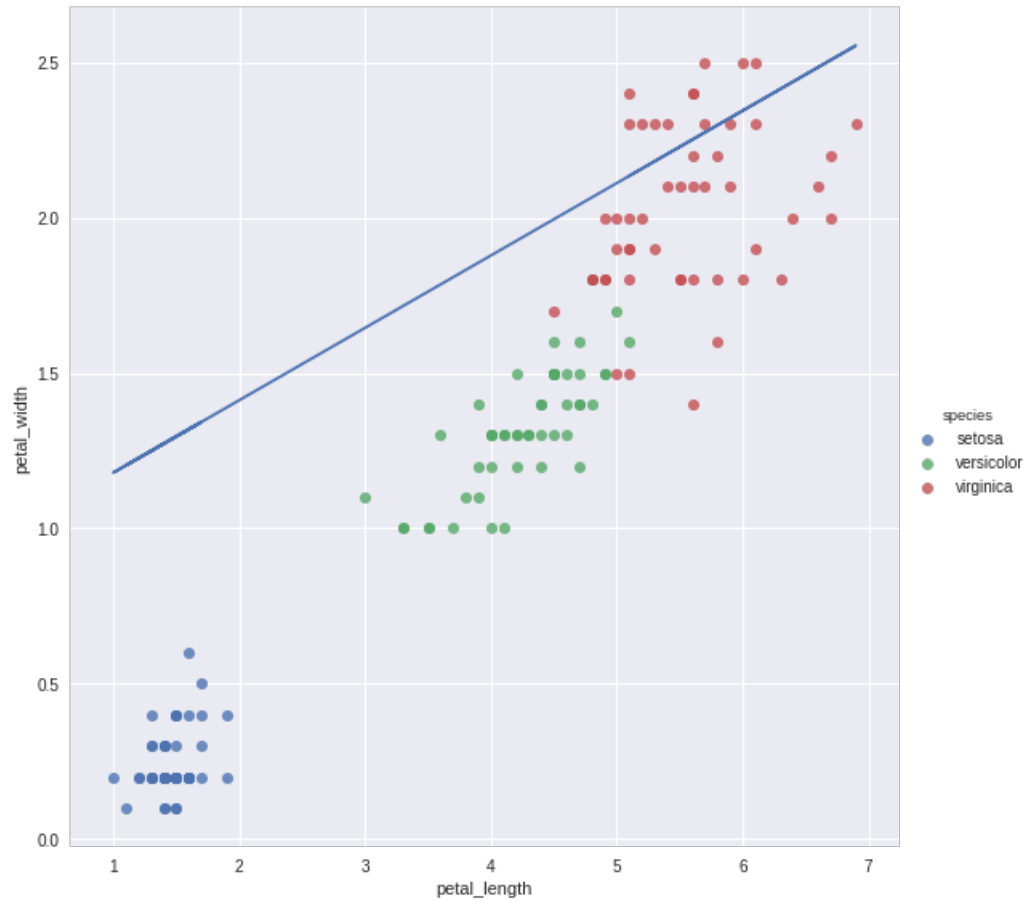
            table.add_row(['', '', '', '', '', m])

            display(HTML(table.get_html_string()))
```

```
In [204]: display_table(beta0, beta1)
```

| i | x_i | y_i | \hat{y}_i | $(y_i - \hat{y}_i)$ | $(y_i - \hat{y}_i)^2$ |
|-----|-------|-------|---------------|---------------------|-----------------------|
| 1 | 1.4 | 0.2 | 1.27246400089 | -1.07246400089 | 1.1501790332 |
| 2 | 1.4 | 0.2 | 1.27246400089 | -1.07246400089 | 1.1501790332 |
| 3 | 1.3 | 0.2 | 1.24917001457 | -1.04917001457 | 1.10075771947 |
| 4 | 1.5 | 0.2 | 1.29575798721 | -1.09575798721 | 1.20068556653 |
| 5 | 1.4 | 0.2 | 1.27246400089 | -1.07246400089 | 1.1501790332 |
| 6 | 1.7 | 0.4 | 1.34234595985 | -0.942345959848 | 0.888015908042 |
| 7 | 1.4 | 0.3 | 1.27246400089 | -0.972464000888 | 0.945686233024 |
| 8 | 1.5 | 0.2 | 1.29575798721 | -1.09575798721 | 1.20068556653 |
| 9 | 1.4 | 0.2 | 1.27246400089 | -1.07246400089 | 1.1501790332 |
| 10 | 1.5 | 0.1 | 1.29575798721 | -1.19575798721 | 1.42983716397 |
| | | | | | 79.9363589781 |

```
In [205]: plot(beta0, beta1)
```



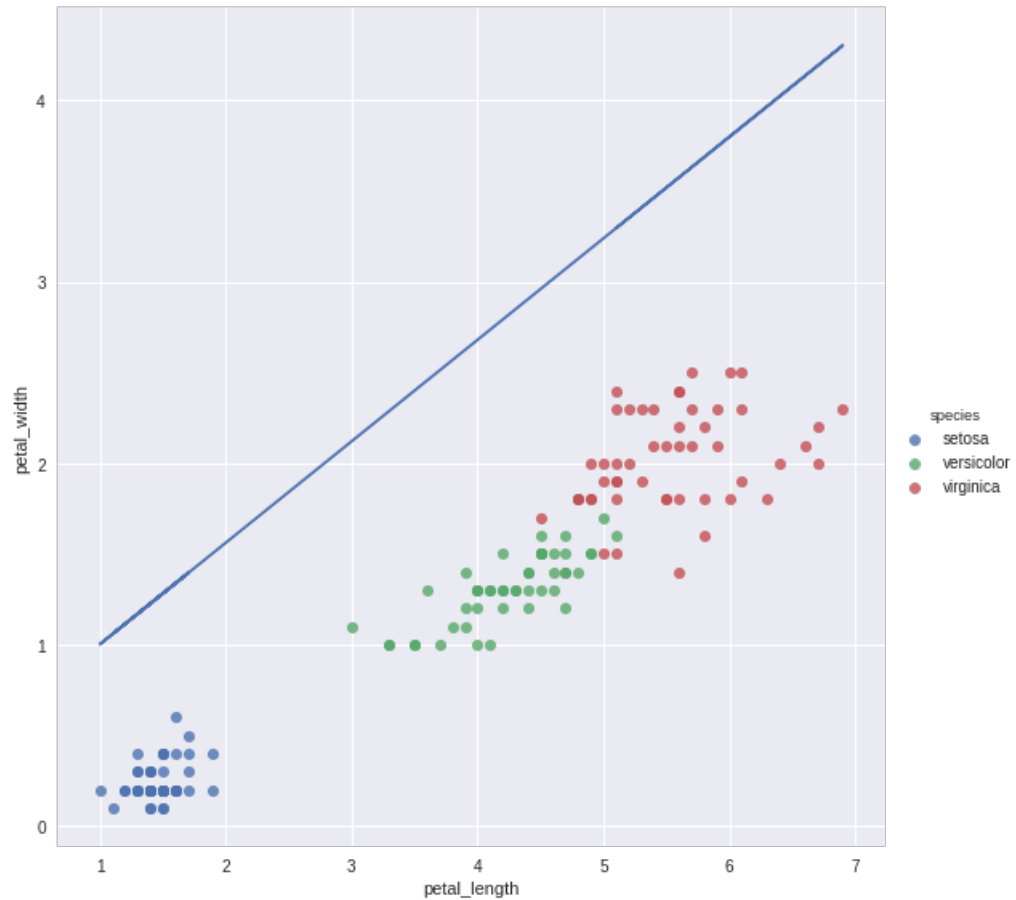
```
In [206]: beta0, beta1 = np.random.rand(2)
          beta0, beta1
```

```
Out[206]: (0.44395852212752296, 0.55909523711243136)
```

```
In [207]: display_table(beta0, beta1)
```

| i | x_i | y_i | \hat{y}_i | $(y_i - \hat{y}_i)$ | $(y_i - \hat{y}_i)^2$ |
|-----|-------|-------|---------------|---------------------|-----------------------|
| 1 | 1.4 | 0.2 | 1.22669185408 | -1.02669185408 | 1.05409616324 |
| 2 | 1.4 | 0.2 | 1.22669185408 | -1.02669185408 | 1.05409616324 |
| 3 | 1.3 | 0.2 | 1.17078233037 | -0.970782330374 | 0.942418332966 |
| 4 | 1.5 | 0.2 | 1.2826013778 | -1.0826013778 | 1.17202574321 |
| 5 | 1.4 | 0.2 | 1.22669185408 | -1.02669185408 | 1.05409616324 |
| 6 | 1.7 | 0.4 | 1.39442042522 | -0.994420425219 | 0.988871982092 |
| 7 | 1.4 | 0.3 | 1.22669185408 | -0.926691854085 | 0.858757792427 |
| 8 | 1.5 | 0.2 | 1.2826013778 | -1.0826013778 | 1.17202574321 |
| 9 | 1.4 | 0.2 | 1.22669185408 | -1.02669185408 | 1.05409616324 |
| 10 | 1.5 | 0.1 | 1.2826013778 | -1.1826013778 | 1.39854601877 |
| | | | | | 287.488595635 |

```
In [208]: plot(beta0, beta1)
```



```
In [209]: from sklearn.linear_model import LinearRegression
lr = LinearRegression()
lr.fit(x.values.reshape((len(x), 1)), y.values.reshape((len(y), 1)))
```

```
Out[209]: LinearRegression(copy_X=True, fit_intercept=True, n_jobs=1, normalize=False)
```

```
In [210]: beta0 = lr.intercept_[0]
beta1 = lr.coef_[0,0]
beta0, beta1
```

```
Out[210]: (-0.36307552131902909, 0.41575541635241153)
```

```
In [211]: display_table(beta0, beta1)
```

| i | x_i | y_i | \hat{y}_i | $(y_i - \hat{y}_i)$ | $(y_i - \hat{y}_i)^2$ |
|-----|-------|-------|----------------|---------------------|-----------------------|
| 1 | 1.4 | 0.2 | 0.218982061574 | -0.0189820615743 | 0.000360318661612 |
| 2 | 1.4 | 0.2 | 0.218982061574 | -0.0189820615743 | 0.000360318661612 |
| 3 | 1.3 | 0.2 | 0.177406519939 | 0.0225934800609 | 0.000510465341262 |
| 4 | 1.5 | 0.2 | 0.26055760321 | -0.0605576032096 | 0.00366722330649 |
| 5 | 1.4 | 0.2 | 0.218982061574 | -0.0189820615743 | 0.000360318661612 |
| 6 | 1.7 | 0.4 | 0.34370868648 | 0.0562913135199 | 0.0031687119778 |
| 7 | 1.4 | 0.3 | 0.218982061574 | 0.0810179384257 | 0.00656390634674 |
| 8 | 1.5 | 0.2 | 0.26055760321 | -0.0605576032096 | 0.00366722330649 |
| 9 | 1.4 | 0.2 | 0.218982061574 | -0.0189820615743 | 0.000360318661612 |
| 10 | 1.5 | 0.1 | 0.26055760321 | -0.16055760321 | 0.0257787439484 |
| | | | | | 6.31009637925 |

```
In [247]: sns.lmplot(x = column['feature'], y = column['target'], data = iris, fit_
eg = False, hue = 'species', size = 8)
plt.plot(x, predict(x, beta0, beta1))
```

```
Out[247]: [<matplotlib.lines.Line2D at 0x7f9e9f331710>]
```

