

HW 3

① $91_{10} + (6)_{16}$

$$\begin{array}{r} \frac{0}{128} \frac{1}{64} \frac{0}{32} \frac{1}{16} \frac{1}{8} \frac{0}{4} \frac{1}{2} \frac{1}{1} + \frac{1}{1} \frac{1}{1} \frac{0}{1} \frac{0}{1} \frac{0}{1} \frac{1}{1} \frac{1}{1} \frac{0}{1} \\ \begin{array}{r} 01011011 \\ + 11000110 \\ \hline 100100001 \end{array} \\ \begin{array}{r} 256 \\ 32 \\ 1 \end{array} \end{array} = \boxed{33_{10}} = \boxed{289_{10}} \text{ unsigned floating point}$$

② $118 - 11_{10}$

$$\begin{array}{r} \frac{0}{64} \frac{1}{32} \frac{0}{16} \frac{1}{8} \frac{0}{4} \frac{0}{2} \frac{0}{1} \frac{1}{1} + \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{0}{1} \frac{1}{1} \frac{0}{1} \frac{1}{1} \\ \hline 1000000110_2 \\ \begin{array}{r} 1 \\ \uparrow \end{array} \end{array} \begin{array}{r} 4 \\ 2 \end{array} \text{ Signed (+) floating point} = \boxed{6_{10}}$$

$$\begin{array}{r} \frac{0}{64} \frac{0}{32} \frac{0}{16} \frac{0}{8} \frac{1}{4} \frac{0}{2} \frac{1}{1} \frac{1}{1} = 11_{10} \\ \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{0}{1} \frac{1}{1} \frac{0}{1} \frac{0}{1} \\ + \frac{1}{1} \\ \hline 11110101_2 = -11_{10} \end{array}$$

③ $12.3125_{10} + 011012_{Q2}$

$$\begin{array}{r} \frac{1}{8} \frac{1}{4} \frac{0}{2} \frac{0}{1} \frac{0}{.5} \frac{1}{.25} \frac{0}{.125} \frac{1}{.0625} \\ + 0001.1000_2 \\ \hline 1101.1101_2 = \boxed{13.8125_{10}} \text{ unsigned fixed point} \end{array}$$

④ $5.75_{10} - 7.125_{10}$

$$\begin{array}{r} \frac{0}{8} \frac{1}{4} \frac{0}{2} \frac{1}{1} \frac{1}{.5} \frac{1}{.25} \frac{0}{.125} \frac{0}{.0625} \\ + 0101.1100 \\ + 1000.1110 \\ \hline 1110.1010_2 = -2_{10} + .625_{10} = \boxed{-1.375_{10}} \text{ signed fixed point} \end{array}$$

$$\begin{array}{r} \frac{0}{8} \frac{1}{4} \frac{1}{2} \frac{1}{1} \frac{0}{.5} \frac{0}{.25} \frac{1}{.125} \frac{0}{.0625} = 7.125_{10} \\ \frac{1}{1} \frac{0}{1} \frac{0}{1} \frac{0}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1} \frac{1}{1} \\ + \frac{4}{1} \frac{1}{1} \\ \hline 1000.1110 = -7.125_{10} \end{array}$$

⑤ $9_{10} \cdot 3_{10}$

~~0000 1001~~
~~+ 0001 1~~
~~0001 001~~
~~0000 010~~
~~0000 000~~
~~0000 000~~
~~0000 101~~

1001
 0011
 1001
 10010
 000000
 0000000
 0000000
 0011011₂ = 27₁₀

unsigned floating point

⑥ $(-5)_{10} \cdot (-6)_{10}$

0101 = 5₂
 1010
 + 1
 1011 = -5₂

0110 = 6₂
 1001
 + 1
 1010 = -6₂

1011
 1010
 0000
 1110110
 000000
 1011000
~~1000110~~
 100110000
 0000011110₂ = 30₁₀

Signed(+) floating point

⑦ $9.5_{10} \cdot 2.625_{10}$

1001.1
 0010.1010

1001.1
 x 10.101
 10011
 00000
 10011
 00000

10011
 00000
 10011
 11000.11111₂ = 24.9375₁₀

unsigned fixed point

⑧ $(-1.25)_{10} \cdot 3.5_{10}$

~~1.01~~
~~0.10~~
~~0.1~~

1110.11 I₄Q₂
 0011.1 I₄Q₁
 111011
 1110110
 + 11101100

negative 011.101₂ I₄Q₃
 -5₁₀ - .625₁₀
 = -4.375₁₀

signed fixed point