

# Fairness Constraints for Graph Embeddings\*

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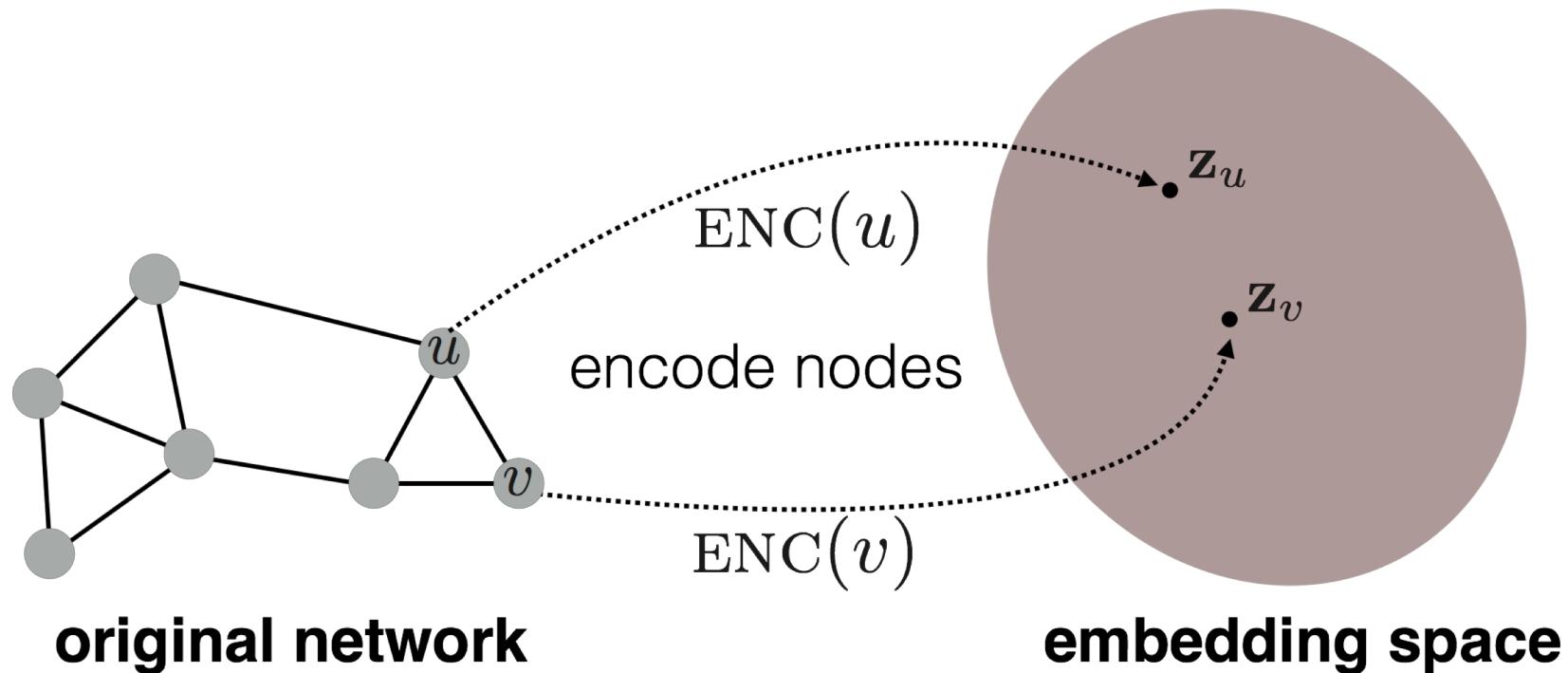
Visiting Researcher at Facebook AI Research



\*Joint work with my  
PhD student Joey Bose,  
to appear in ICML 2019 ([pdf](#))

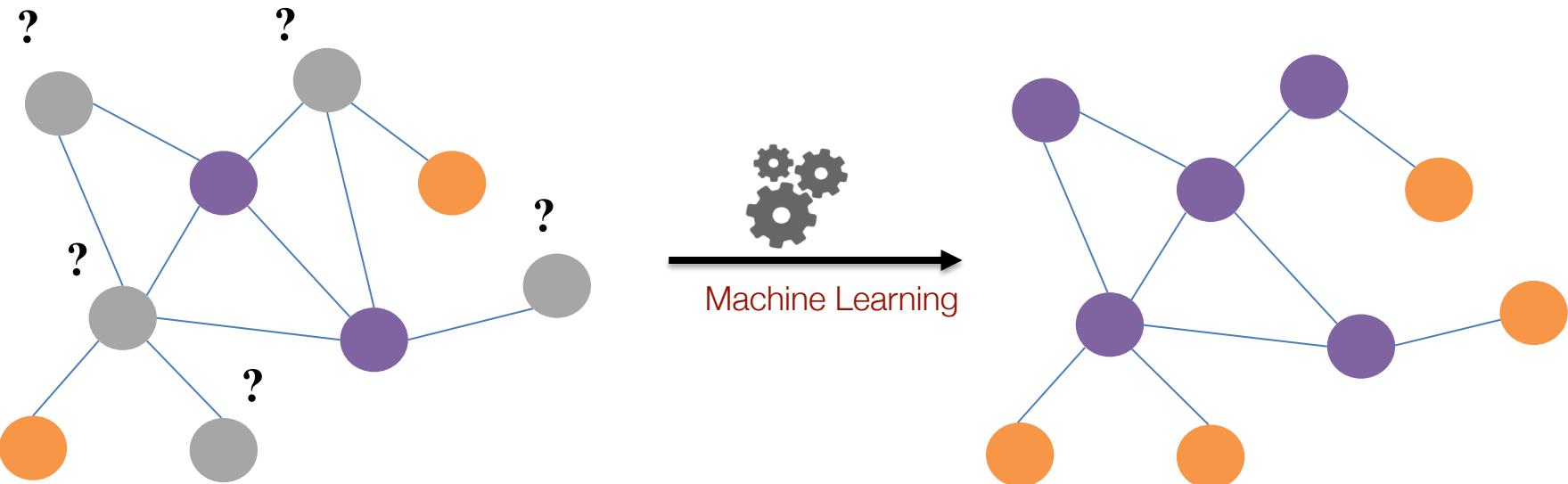
# Graph embeddings

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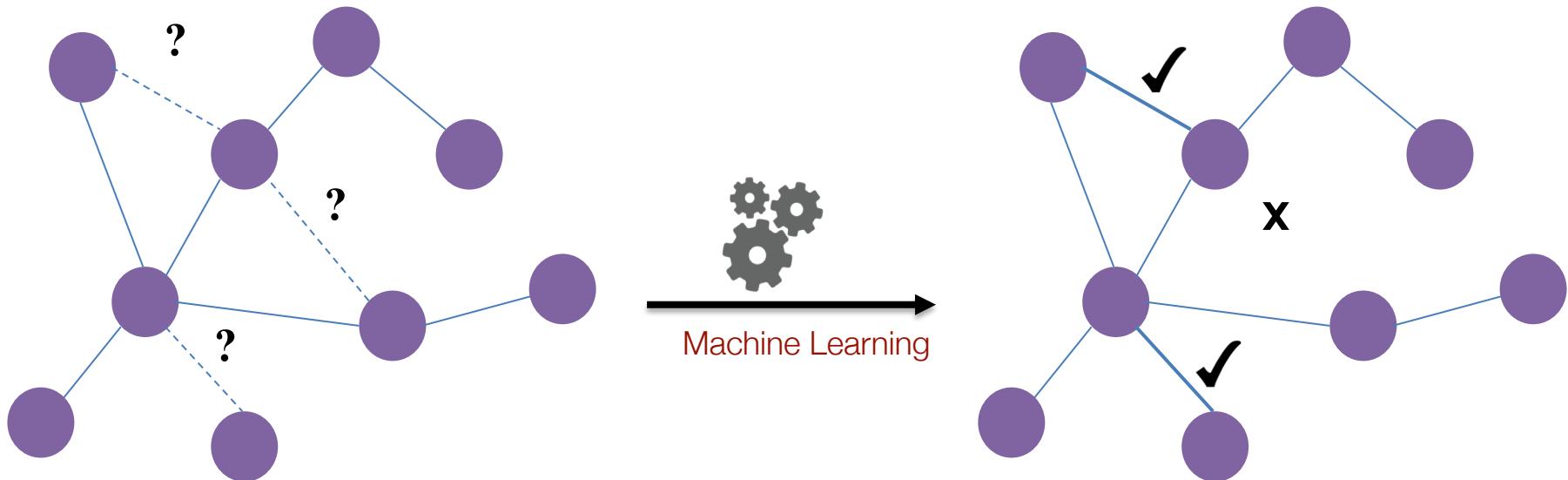
# Application: Node classification

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# Application: Link prediction

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# Becoming ubiquitous in social applications

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- Graph embedding techniques are a powerful approach for social recommendations, bot detection, content screening, behavior prediction, geo-localization,
  - E.g., Facebook, Huawei, Uber Eats, Pinterest, LinkedIn, WeChat
- Classic collaborative filtering approaches can be re-interpreted in a more general graph embedding framework.

# But what about fairness and privacy?

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- Graph embeddings designed to capture **everything** that might be useful for the objective.
- Even if we don't provide the model information about **sensitive attributes** (e.g., gender or age), the model **will use this information**.
- What if a user doesn't want this information used?

# Fairness from a pragmatic perspective

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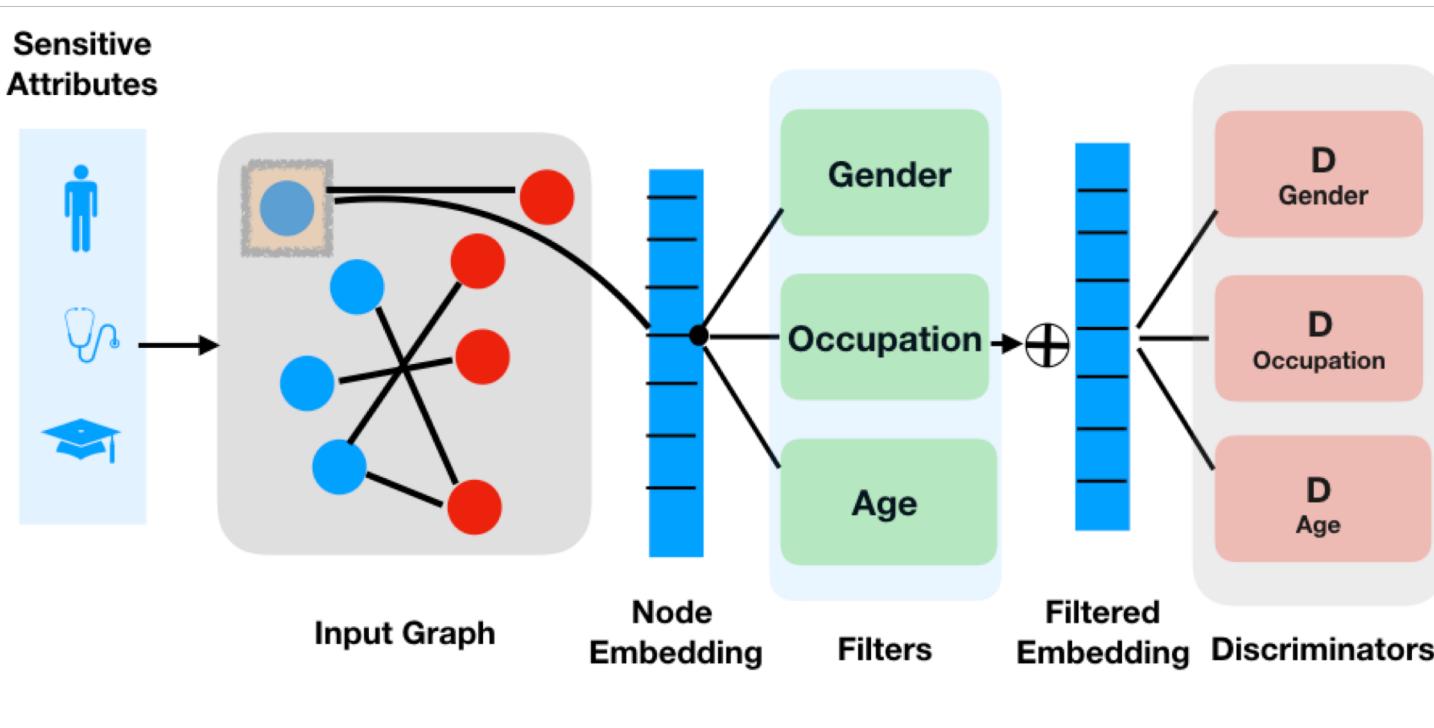
- Strict privacy and discrimination concerns are one motivation.
- But what if users just don't want their recommendations do depend on certain attributes?
- What if users want the system to “ignore” parts of their demographics or past behavior?

# Fairness in graph embeddings

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- **Basic idea:** How can we learn node embeddings that are invariant to particular sensitive attributes?
- **Challenges:**
  - Graph data is not i.i.d.
  - There is not just one classification task that we are trying to enforce fairness on.
  - There are often many *possible* sensitive attributes.

# Our work: Fairness in graph embeddings



# Preliminaries and set-up

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- Learning an encoder function to map nodes to embeddings:

$$\mathbf{z}_v = \text{ENC}(v)$$

- Using these embeddings to “score” the likelihood of a relationship between nodes:

$$s(e) = s(\langle \mathbf{z}_u, r, \mathbf{z}_v \rangle) \quad s(e) > s(e'), \forall e \in \mathcal{E}, e' \in \bar{\mathcal{E}}.$$

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Score of a (possible) edge is a function of the two node embeddings and the relation type.

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Goal: Train the embeddings (with a subset of the true edges) so that the score for all real edges is larger than all non-edges.

# Preliminaries and set-up

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- Generic loss function:

$$\sum_{e \in \mathcal{E}_{\text{train}}} L_{\text{edge}}(s(e), s(e_1^-), \dots, s(e_m^-))$$

Sum over (batch of) training edges.

Task-specific loss function

Score assigned to positive/real edge.

Scores assigned to random negative sample edges.

The diagram illustrates the components of a generic loss function. It features a mathematical expression with annotations pointing to specific parts. The expression is a summation over training edges, where each edge's score is compared against scores of multiple negative edges using a task-specific loss function. The annotations use colored arrows to map the mathematical symbols to their meanings: a red arrow for the summation index, an orange arrow for the loss function, a purple arrow for the positive edge score, and a blue arrow for the negative edge scores.

# Preliminaries and set-up: Concrete examples

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- Score functions:
- Loss-functions:

# Preliminaries and set-up: Concrete examples

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  - Dot-product:  $s(e) = s(\langle \mathbf{z}_u, r, \mathbf{z}_v \rangle) = \mathbf{z}_u^\top \mathbf{z}_v$
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  - TransE:  $s(e) = s(\langle \mathbf{z}_u, r, \mathbf{z}_v \rangle) = -\|\mathbf{z}_u + \mathbf{r} - \mathbf{z}_v\|_2^2$
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- Loss-functions:
  - Max-margin:  $L_{\text{edge}}(s(e), s(e_1^-), \dots, s(e_m^-)) = \sum_{i=1}^m \max(1 - s(e) + s(e_i^-), 0)$

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  - Cross-entropy:  $L_{\text{edge}}(s(e), s(e_1^-), \dots, s(e_m^-)) = -\log(\sigma(s(e))) - \sum_{i=1}^m \log(1 - \sigma(s(e_i^-)))$

# Formalizing fairness

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- How do we ensure fairness in this context?

# Formalizing fairness

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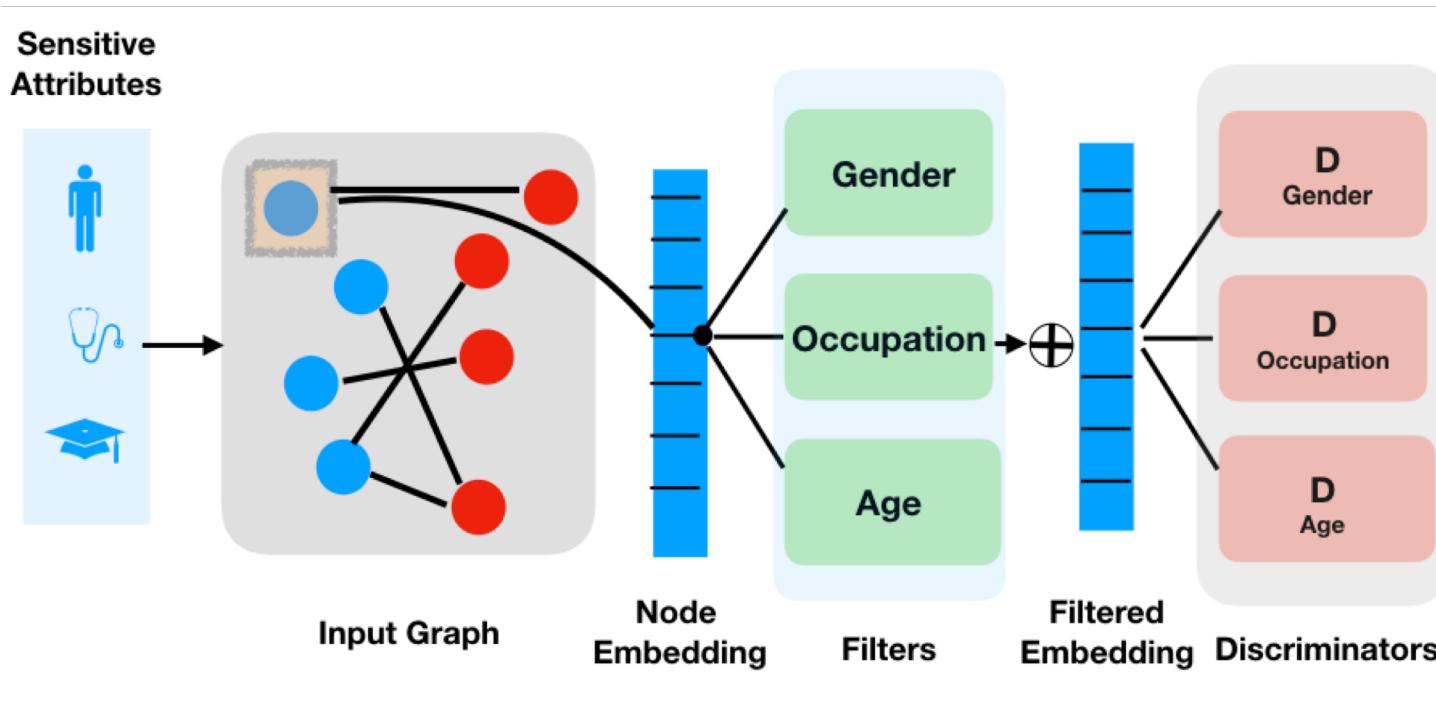
- How do we ensure fairness in this context?
- Solution: **representational invariance**
  - Want embeddings to be independent from the attributes:

$$\mathbf{z}_u \perp a_u, \quad \forall u \in \mathcal{V}$$

- Which is equivalent to minimizing the mutual information between the embeddings and the attributes:

$$I(\mathbf{z}_u, a_u^k) = 0, k \in S, \forall u \in \mathcal{V}$$

# Enforcing fairness through an adversary



# Enforcing fairness through an adversary

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- Key component 1: Compositional encoder.
- Given a set of attributes, it outputs “filtered” embeddings that should be invariant to those attributes.

$$\text{C-ENC}(u, S) = \frac{1}{|S|} \sum_{k \in S} f_k(\text{ENC}(u))$$

Input: node ID and set of sensitive attributes

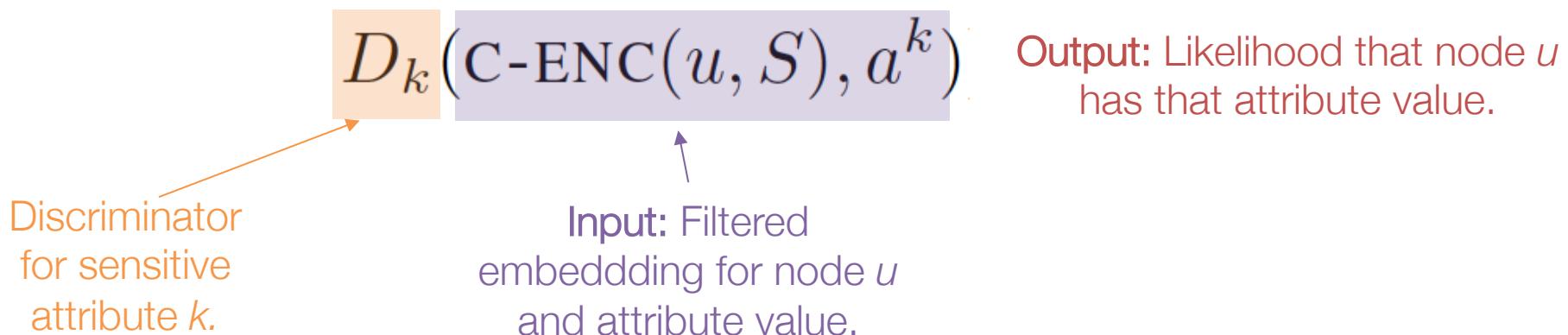
Sum over all sensitive attributes

Trainable filter function (neural network) outputs embedding that is invariant to attribute  $k$ .

# Enforcing fairness through an adversary

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- Key component 2: Adversarial discriminators
- For each sensitive attribute, train an adversarial discriminator that tries to predict that sensitive attribute from the filtered embeddings:



# Enforcing fairness through an adversary

- Putting it all together in an adversarial loss:

$$L(e) = L_{\text{edge}}(s(e), s(e_1^-), \dots, s(e_m^-)) + \lambda \sum_{k \in S} \sum_{a^k \in \mathcal{A}_k} \log(D_k(\text{c-ENC}(u, S), a^k))$$

Constant that determines the strength of the fairness constraints

Original loss function for the edge prediction task

Likelihood of discriminator predicting the sensitive attributes.

# Enforcing fairness through an adversary

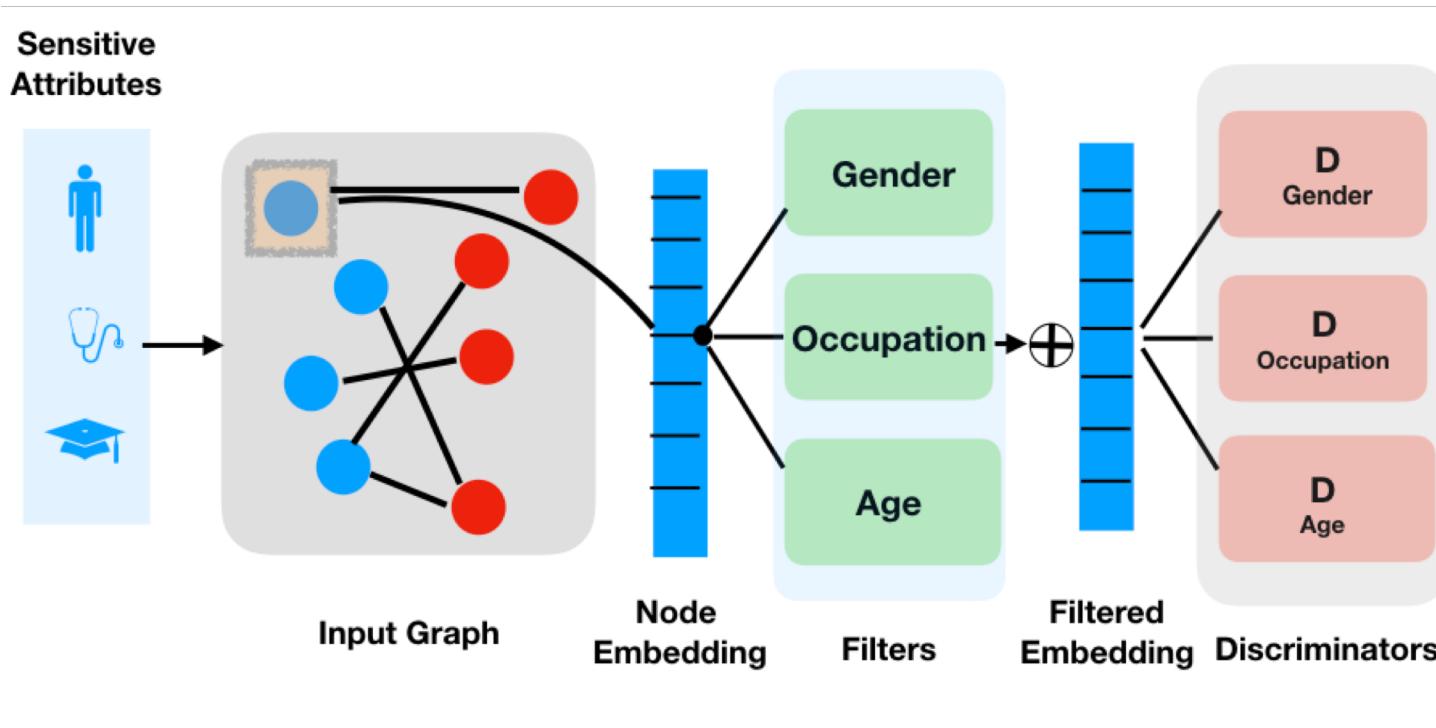
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- Putting it all together in an adversarial loss:

$$\begin{aligned} L(e) = & L_{\text{edge}}(s(e), s(e_1^-), \dots, s(e_m^-)) \\ & + \lambda \sum_{k \in S} \sum_{a^k \in \mathcal{A}_k} \log(D_k(\text{C-ENC}(u, S), a^k)) \end{aligned}$$

- During training the encoder tries to minimize this loss and the adversarial discriminators are trained to maximize it.

# Enforcing fairness through an adversary



# Dataset 1: MovieLens-1M

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- Classic recommender system benchmark.
  - Bipartite graph between users and movies.
- 
- **Nodes (~10,000):** Users and movies
  - **Edges (~1,000,000):** Rating a user gives a movie
  - **Sensitive attributes:**
    - Gender
    - Age (binned to become a categorical attribute)
    - Occupation

# Dataset 2: Reddit

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- Derived from public Reddit comments.
  - Bipartite graph between users and communities.
- 
- **Nodes (~300,000):** Users and communities
  - **Edges (~7,000,000):** Whether a user commented on that community
  - **Sensitive attributes:** Randomly select 50 communities to be “sensitive” communities

# Dataset 3: Freebase 15k-237

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- Derived from classic knowledge base completion benchmark.
- Knowledge graph between set of typed entities.
- **Nodes (~15,000):** Users and communities
- **Edges (~150,000):** 237 different relation types (e.g., married\_to, born\_in, capital\_of, director\_of)
- **Sensitive attributes:** Randomly selected 3 entity type annotations (e.g., is\_actor) to be “sensitive attributes”

# Experiments: Three questions

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1. What is the cost of invariance?
2. What is the impact of compositionality?
3. Can we generalize to unseen combinations of attributes?

# MovieLens: Fairness results

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- How strongly can we enforce fairness?
- Compare three approaches to enforcing fairness:
  - No adversary (i.e., just train on the recommendation task)
  - Independent adversarial model for each attribute
  - Full compositional model

MOVIELENS1M	BASELINE No Ad- VERSARY	GENDER ADVERSARY	AGE ADVERSARY	OCCUPATION ADVERSARY	COMP. ADVERSARY	MAJORITY CLASSIFIER	RANDOM CLASSIFIER
GENDER	0.712	0.532	0.541	0.551	0.511	0.5	0.5
AGE	0.412	0.341	0.333	0.321	0.313	0.367	0.141
OCCUPATION	0.146	0.141	0.108	0.131	0.121	0.126	0.05

# MovieLens: Fairness results

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- How strongly can we enforce fairness?
- Evaluate how well a two-layer MLP can classify the sensitive attributes from the learned node embeddings.
  - AUC for the binary gender attribute
  - Micro-averaged F1-score for the age and occupation attributes.

MOVIELENS1M	BASELINE No Ad- VERSARY	GENDER ADVERSARY	AGE ADVERSARY	OCCUPATION ADVERSARY	COMP. ADVERSARY	MAJORITY CLASSIFIER	RANDOM CLASSIFIER
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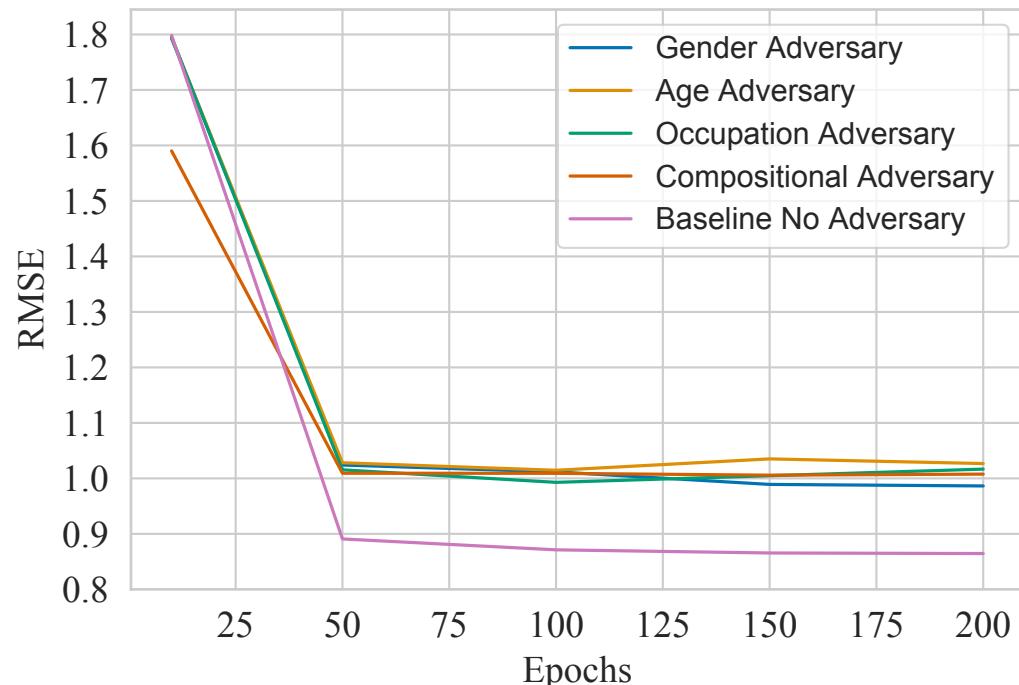
- Key takeaways:
  - After applying the compositional adversary, accuracy is no better than majority classifier!
  - Performance of compositional adversary on par with independent adversaries!

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# MovieLens: Impact on recommendations

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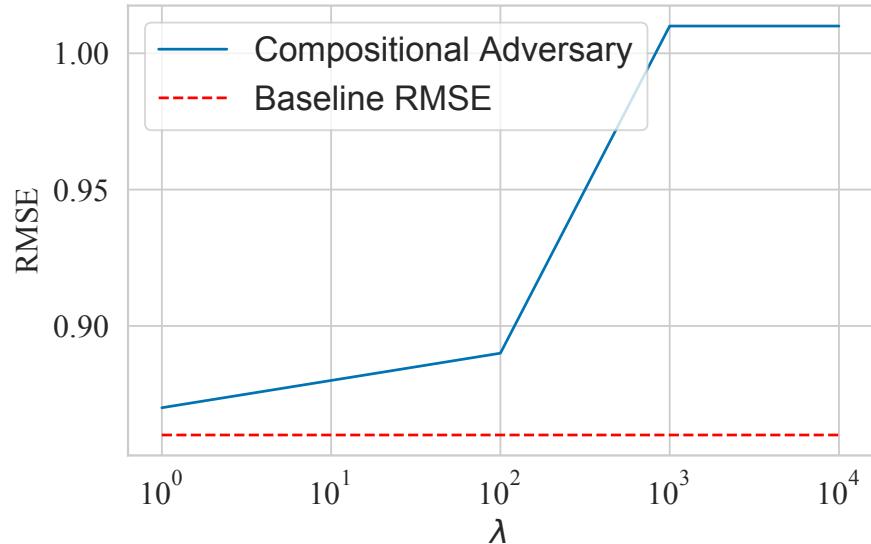
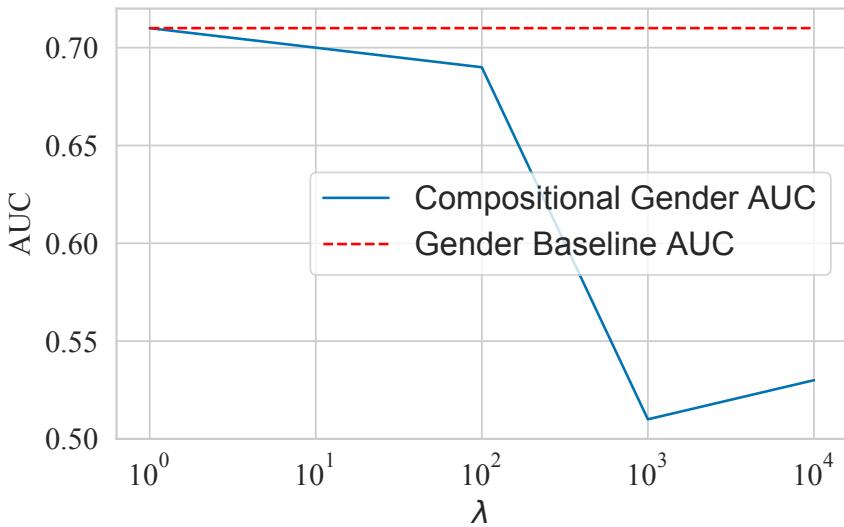
- Evaluate recommendation performance (RMSE) with and without enforcing fairness.
- There is a drop in accuracy, but not catastrophic.



# MovieLens: Trade-off

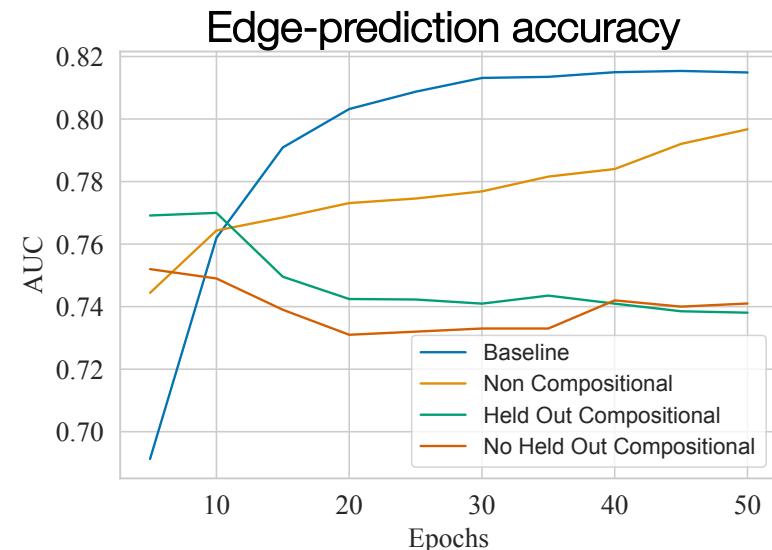
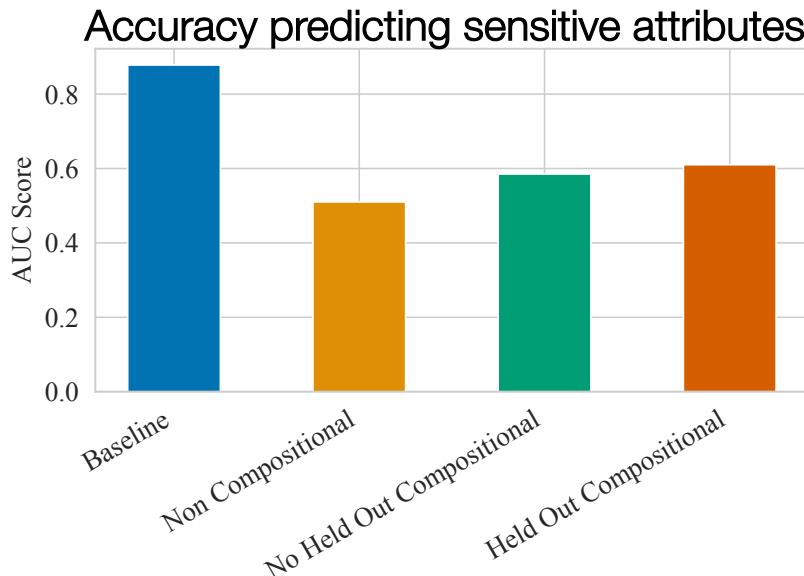
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- $\lambda$  allows trade-off between fairness and recommendation performance.



# Reddit results: Fairness

- Same set-up as MovieLens, but here we have 10 sensitive attributes.
- Again, able to strongly enforce fairness, but at a non-trivial cost.



# Freebase results

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- On the synthetic Freebase data we see that enforcing fairness leads to a significant drop in task performance.

Ability to predict sensitive attributes (measured in AUC)  
and the impact on task-performance (mean rank)

FB 15k-237	BASELINE	NON	COMP.
	NO AD-	COMP. AD-	COMP. ADVERSARY
	VERSARY	VERSARY	
ATTRIBUTE 0	0.97	0.82	0.77
ATTRIBUTE 1	0.99	0.81	0.79
ATTRIBUTE 2	0.98	0.81	0.81
MEAN RANK	285	320	542

# Conclusions and outlook

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- Fairness in network representation learning is an understudied issue.
- We can enforce fairness in a flexible way, but at a cost.
- There is no perfect notion of fairness.