

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$$Gini(D) = 1 - \left(\frac{6}{10}\right)^2 - \left(\frac{4}{10}\right)^2 = 0.480 \Rightarrow \text{ادامه می دهیم}$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$$Gini_{Job}(D) = \frac{7}{10} \times \left(1 - \left(\frac{4}{7}\right)^2 - \left(\frac{3}{7}\right)^2\right) + \frac{3}{10} \times \left(1 - \left(\frac{0}{3}\right)^2 - \left(\frac{3}{3}\right)^2\right) = 0.343$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$$GiniHouse(D) = \frac{5}{10} \times \left( 1 - \left( \frac{4}{5} \right)^2 - \left( \frac{1}{5} \right)^2 \right) + \frac{5}{10} \times \left( 1 - \left( \frac{0}{5} \right)^2 - \left( \frac{5}{5} \right)^2 \right) = 0.160$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

{Old}, {Middle, Young}

$$GiniAge(D) = \frac{3}{10} \times \left( 1 - \left( \frac{1}{3} \right)^2 - \left( \frac{2}{3} \right)^2 \right) + \frac{7}{10} \times \left( 1 - \left( \frac{3}{7} \right)^2 - \left( \frac{4}{7} \right)^2 \right) = 0.476$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$\{Middle\}, \{Old, Young\}$

$$GiniAge(D) = \frac{4}{10} \times \left( 1 - \left( \frac{2}{4} \right)^2 - \left( \frac{2}{4} \right)^2 \right) + \frac{6}{10} \times \left( 1 - \left( \frac{2}{6} \right)^2 - \left( \frac{4}{6} \right)^2 \right) = 0.467$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$\{Young\}, \{Middle, Old\}$

$$GiniAge(D) = \frac{3}{10} \times \left( 1 - \left( \frac{1}{3} \right)^2 - \left( \frac{2}{3} \right)^2 \right) + \frac{7}{10} \times \left( 1 - \left( \frac{3}{7} \right)^2 - \left( \frac{4}{7} \right)^2 \right) = 0.476$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$\{Excellent\}, \{Good, Fair\}$

$$GiniCredit(D) = \frac{2}{10} \times \left( 1 - \left( \frac{0}{2} \right)^2 - \left( \frac{2}{2} \right)^2 \right) + \frac{8}{10} \times \left( 1 - \left( \frac{4}{8} \right)^2 - \left( \frac{4}{8} \right)^2 \right) = 0.400$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$\{Good\}, \{Excellent, Fair\}$

$$GiniCredit(D) = \frac{4}{10} \times \left( 1 - \left( \frac{1}{4} \right)^2 - \left( \frac{3}{4} \right)^2 \right) + \frac{6}{10} \times \left( 1 - \left( \frac{3}{6} \right)^2 - \left( \frac{3}{6} \right)^2 \right) = 0.450$$

ID	Age	Job	House	Credit	Class
1	Old	False	True	Excellent	Yes
2	Old	False	True	Good	Yes
3	Middle	False	False	Fair	No
4	Middle	True	True	Good	Yes
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
7	Middle	False	True	Excellent	Yes
8	Young	True	False	Good	Yes
9	Young	True	True	Fair	Yes
10	Middle	False	False	Good	No

$\{Fair\}, \{Excellent, Good\}$

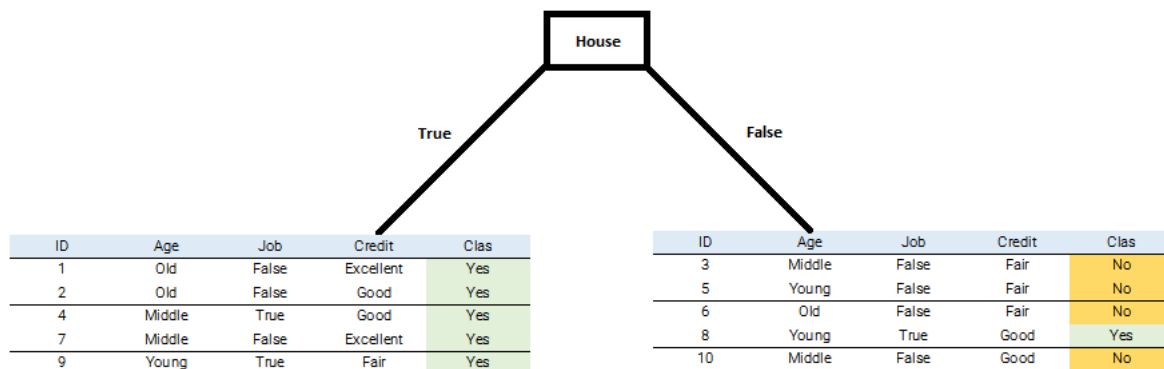
$$GiniCredit(D) = \frac{4}{10} \times \left( 1 - \left( \frac{3}{4} \right)^2 - \left( \frac{1}{4} \right)^2 \right) + \frac{6}{10} \times \left( 1 - \left( \frac{1}{6} \right)^2 - \left( \frac{5}{6} \right)^2 \right) = 0.317$$

از آنجایی که  $GiniHouse(D) = 0.160$  کوچکترین مقدار است بنابراین ابتدا بر اساس ویژگی House درخت ایجاد می‌گردد.

$$Gini(House) = Gini(D) - GiniHouse(D) = 0.480 - 0.160 = 0.320$$

ID	Age	Job	<u>House</u>	Credit	Class
1	Old	False	<u>True</u>	Excellent	Yes
2	Old	False	<u>True</u>	Good	Yes
4	Middle	True	<u>True</u>	Good	Yes
7	Middle	False	<u>True</u>	Excellent	Yes
9	Young	True	<u>True</u>	Fair	Yes

ID	Age	Job	House	Credit	Class
3	Middle	False	False	Fair	No
5	Young	False	False	Fair	No
6	Old	False	False	Fair	No
8	Young	True	False	Good	Yes
10	Middle	False	False	Good	No



شاخه سمت چپ:

ID	Age	Job	Credit	Class
1	Old	False	Excellent	Yes
2	Old	False	Good	Yes
4	Middle	True	Good	Yes
7	Middle	False	Excellent	Yes
9	Young	True	Fair	Yes

$$Gini(D) = 1 - \left(\frac{0}{5}\right)^2 - \left(\frac{5}{5}\right)^2 = 0 \Rightarrow \text{ادامه نمی‌دهیم}$$

با توجه به این که  $Gini(D) = 0$  است بنابراین شاخه سمت چپ ادامه پیدا نکرده و به برگ خواهیم رسید.

شاخه سمت راست:

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$$Gini(D) = 1 - \left(\frac{4}{5}\right)^2 - \left(\frac{1}{5}\right)^2 = 0.320 \Rightarrow \text{ادامه می‌دهیم}$$

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$\{Old\}, \{Middle, Young\}$

$$GiniAge(D) = \frac{1}{5} \times \left( 1 - \left( \frac{1}{1} \right)^2 - \left( \frac{0}{1} \right)^2 \right) + \frac{4}{5} \times \left( 1 - \left( \frac{3}{4} \right)^2 - \left( \frac{1}{4} \right)^2 \right) = 0.300$$

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$\{Middle\}, \{Old, Young\}$

$$GiniAge(D) = \frac{2}{5} \times \left( 1 - \left( \frac{2}{2} \right)^2 - \left( \frac{0}{2} \right)^2 \right) + \frac{3}{5} \times \left( 1 - \left( \frac{2}{3} \right)^2 - \left( \frac{1}{3} \right)^2 \right) = 0.267$$

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$\{Young\}, \{Middle, Old\}$

$$GiniAge(D) = \frac{2}{5} \times \left( 1 - \left( \frac{1}{2} \right)^2 - \left( \frac{1}{2} \right)^2 \right) + \frac{3}{5} \times \left( 1 - \left( \frac{3}{3} \right)^2 - \left( \frac{0}{3} \right)^2 \right) = 0.200$$

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$$GiniJob(D) = \frac{4}{5} \times \left( 1 - \left( \frac{4}{4} \right)^2 - \left( \frac{0}{4} \right)^2 \right) + \frac{1}{5} \times \left( 1 - \left( \frac{0}{1} \right)^2 - \left( \frac{1}{1} \right)^2 \right) = 0$$

ID	Age	Job	Credit	Class
3	Middle	False	Fair	No
5	Young	False	Fair	No
6	Old	False	Fair	No
8	Young	True	Good	Yes
10	Middle	False	Good	No

$$GiniCredit(D) = \frac{3}{5} \times \left( 1 - \left( \frac{3}{3} \right)^2 - \left( \frac{0}{3} \right)^2 \right) + \frac{2}{5} \times \left( 1 - \left( \frac{1}{2} \right)^2 - \left( \frac{1}{2} \right)^2 \right) = 0.200$$

از آنجایی که  $GiniJob(D) = 0$  کوچک‌ترین مقدار است بنابراین بر اساس ویژگی Job رشد درخت ادامه می‌یابد.

$$Gini(Job) = Gini(D) - GiniJob(D) = 0.320 - 0 = 0.320$$

ID	Age	Job	Credit	Class
3	Middle	<u>False</u>	Fair	No
5	Young	<u>False</u>	Fair	No
6	Old	<u>False</u>	Fair	No
10	Middle	<u>False</u>	Good	No

ID	Age	Job	Credit	Class
8	Young	<u>True</u>	Good	Yes

در اینجا با توجه به اینکه به‌واسطه تقسیم بر اساس ویژگی Job دو جدول ایجاد می‌گردد که یکی کاملاً متعلق به کلاس NO و دیگری کاملاً متعلق به کلاس Yes است، نیازی به ادامه محاسبات نیست؛ بنابراین ساختار نهایی درخت تصمیم به شکل زیر خواهد بود.



