

## مرحلة اول

$$\text{Entropy}(D1) = -4/10 * \log_2(4/10) - 6/10 * \log_2(6/10) = 0.9710$$

$\text{Domain}(\text{Age}) = \{\text{Old}, \text{Middle}, \text{Young}\};$

$$\begin{aligned} \text{Entropy}_{\text{Age}}(D1) &= 4/10 * (-3/4 * \log_2(3/4) - 1/3 * \log_2(1/3)) \\ &\quad + 3/10 * (-2/3 * \log_2(2/3) - 1/3 * \log_2(1/3)) \\ &\quad + 3/10 * (-1/3 * \log_2(1/3) - 2/3 * \log_2(2/3)) = 0.8868; \end{aligned}$$

$\text{Domain}(\text{Income}) = \{\text{High}, \text{Medium}, \text{Low}\};$

$$\begin{aligned} \text{Entropy}_{\text{Income}}(D1) &= 4/10 * (-4/4 * \log_2(4/4) - 0/4 * \log_2(0/4)) \\ &\quad + 4/10 * (-1/4 * \log_2(1/4) - 3/4 * \log_2(3/4)) \\ &\quad + 2/10 * (-1/2 * \log_2(1/2) - 1/2 * \log_2(1/2)) = 0.5245; \end{aligned}$$

$\text{Domain}(\text{Job}) = \{\text{Teacher}, \text{Student}\};$

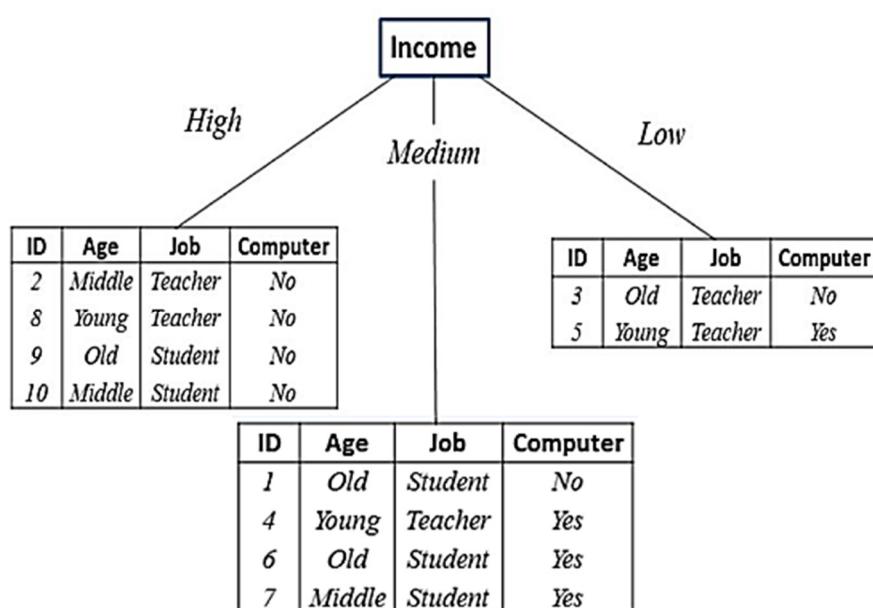
$$\begin{aligned} \text{Entropy}_{\text{Job}}(D1) &= 5/10 * (-3/5 * \log_2(3/5) - 2/5 * \log_2(2/5)) \\ &\quad + 5/10 * (-3/5 * \log_2(3/5) - 2/5 * \log_2(2/5)) = 0.9710; \end{aligned}$$

$$\text{Entropy}(D1) - \text{Entropy}_{\text{Age}}(D1) = 0.9710 - 0.8868;$$

$$\text{Entropy}(D1) - \text{Entropy}_{\text{Income}}(D1) = 0.9710 - 0.5245;$$

$$\text{Entropy}(D1) - \text{Entropy}_{\text{Job}}(D1) = 0.9710 - 0.9710;$$

تقسيم بر اساس دریافتی.



## مرحلة دوم

$$\text{Entropy}(D2\_1) = -\frac{1}{4} * \log_2(\frac{1}{4}) = 0$$

$$\text{Entropy}(D2\_2) = -\frac{1}{4} * \log_2(\frac{1}{4}) - \frac{3}{4} * \log_2(\frac{3}{4}) = 0.8113$$

Domain(Age) = {Old, Middle, Young};

$$\begin{aligned}\text{Entropy}_\text{Age}(D2\_2) &= \frac{1}{4} * (-\frac{1}{2} * \log_2(\frac{1}{2}) - \frac{1}{2} * \log_2(\frac{1}{2})) \\ &\quad + \frac{1}{4} * (-\frac{1}{3} * \log_2(\frac{1}{3}) - \frac{2}{3} * \log_2(\frac{2}{3})) \\ &\quad + \frac{1}{4} * (-\frac{1}{3} * \log_2(\frac{1}{3}) - \frac{2}{3} * \log_2(\frac{2}{3})) = 0.5000;\end{aligned}$$

Domain(Job) = {Teacher, Student};

$$\begin{aligned}\text{Entropy}_\text{Job}(D2\_2) &= \frac{1}{4} * (-\frac{1}{2} * \log_2(\frac{1}{2}) - \frac{1}{2} * \log_2(\frac{1}{2})) \\ &\quad + \frac{3}{4} * (-\frac{1}{3} * \log_2(\frac{1}{3}) - \frac{2}{3} * \log_2(\frac{2}{3})) = 0.6887;\end{aligned}$$

$$\text{Entropy}(D2\_2) - \text{Entropy}_\text{Age}(D2\_2) = 0.8113 - 0.5000;$$

$$\text{Entropy}(D2\_2) - \text{Entropy}_\text{Job}(D2\_2) = 0.8113 - 0.6887;$$

تقسيم بر اساس سن.

$$\text{Entropy}(D2\_3) = -\frac{1}{2} * \log_2(\frac{1}{2}) - \frac{1}{2} * \log_2(\frac{1}{2}) = 1$$

Domain(Age) = {Old, Young};

$$\begin{aligned}\text{Entropy}_\text{Age}(D2\_3) &= \frac{1}{2} * (-\frac{1}{1} * \log_2(\frac{1}{1}) - \frac{0}{1} * \log_2(\frac{0}{1})) \\ &\quad + \frac{1}{2} * (-\frac{0}{1} * \log_2(\frac{0}{1}) - \frac{1}{1} * \log_2(\frac{1}{1})) = 0;\end{aligned}$$

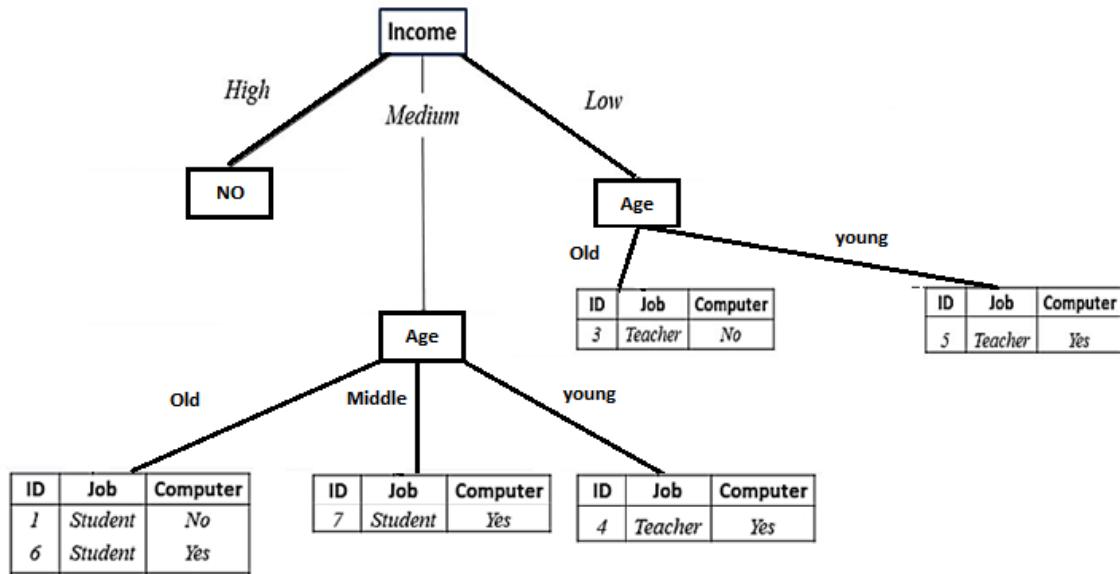
Domain(Job) = {Teacher};

$$\text{Entropy}_\text{Job}(D2\_3) = \frac{1}{2} * (-\frac{1}{2} * \log_2(\frac{1}{2}) - \frac{1}{2} * \log_2(\frac{1}{2})) = 1;$$

$$\text{Entropy}(D2\_3) - \text{Entropy}_\text{Age}(D2\_3) = 1 - 0;$$

$$\text{Entropy}(D2\_3) - \text{Entropy}_\text{Job}(D2\_3) = 1 - 1;$$

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### مرحًّة سوم

$$\text{Entropy}(D3\_1) = -\frac{1}{2} * \log_2(1/2) - \frac{1}{2} * \log_2(1/2) = 1$$

$\text{Domain(Job)} = \{\text{Student}\};$

$$\text{Entropy\_Job}(D3\_1) = 2/2 * (-\frac{1}{2} * \log_2(1/2) - \frac{1}{2} * \log_2(1/2)) = 1;$$

$$\text{Entropy}(D3\_1) - \text{Entropy\_Job}(D3\_1) = 0$$

$$\text{Entropy}(D3\_2) = -1/1 * \log_2(1/1) = 0$$

$$\text{Entropy}(D3\_3) = -1/1 * \log_2(1/1) = 0$$

