

مرحله اول

$$\text{Entropy}(D1) = -4/10 * \log_2(4/10) - 6/10 * \log_2(6/10) = 0.9710$$

$$\text{Domain}(\text{Age}) = \{\text{Old}, \text{Middle}, \text{Young}\};$$

$$\begin{aligned} \text{Entropy_Age}(D1) &= 4/10 * (-3/4 * \log_2(3/4) - 1/3 * \log_2(1/3)) \\ &+ 3/10 * (-2/3 * \log_2(2/3) - 1/3 * \log_2(1/3)) \\ &+ 3/10 * (-1/3 * \log_2(1/3) - 2/3 * \log_2(2/3)) = 0.8868; \end{aligned}$$

$$\text{Domain}(\text{Income}) = \{\text{High}, \text{Medium}, \text{Low}\};$$

$$\begin{aligned} \text{Entropy_Income}(D1) &= 4/10 * (-4/4 * \log_2(4/4) - 0/4 * \log_2(0/4)) \\ &+ 4/10 * (-1/4 * \log_2(1/4) - 3/4 * \log_2(3/4)) \\ &+ 2/10 * (-1/2 * \log_2(1/2) - 1/2 * \log_2(1/2)) = 0.5245; \end{aligned}$$

$$\text{Domain}(\text{Job}) = \{\text{Teacher}, \text{Student}\};$$

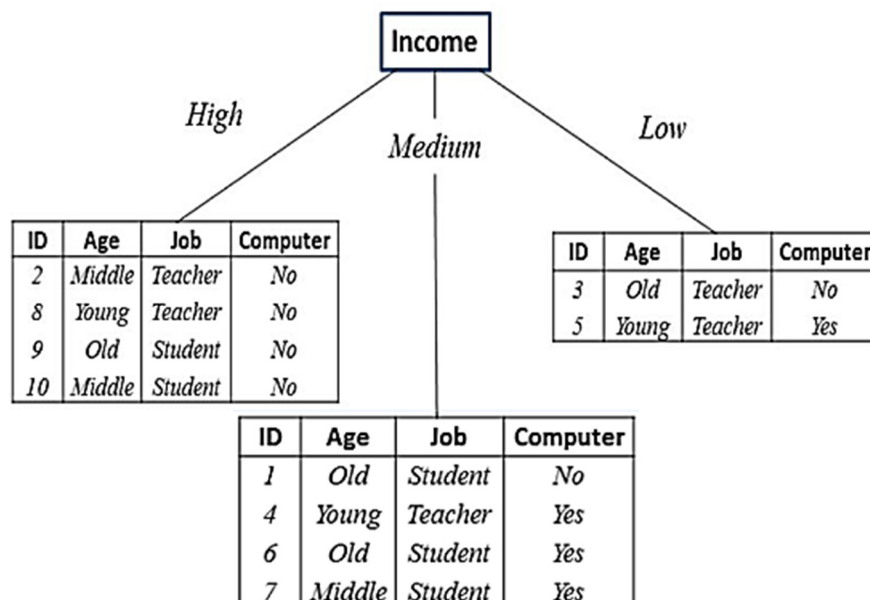
$$\begin{aligned} \text{Entropy_Job}(D1) &= 5/10 * (-3/5 * \log_2(3/5) - 2/5 * \log_2(2/5)) \\ &+ 5/10 * (-3/5 * \log_2(3/5) - 2/5 * \log_2(2/5)) = 0.9710; \end{aligned}$$

$$\text{Entropy}(D1) - \text{Entropy_Age}(D1) = 0.9710 - 0.8868;$$

$$\text{Entropy}(D1) - \text{Entropy_Income}(D1) = 0.9710 - 0.5245;$$

$$\text{Entropy}(D1) - \text{Entropy_Job}(D1) = 0.9710 - 0.9710;$$

تقسیم بر اساس دریافتی.



مرحلة دوم

$$\text{Entropy}(D2_1) = -4/4 * \log_2(4/4) = 0$$

$$\text{Entropy}(D2_2) = -1/4 * \log_2(1/4) - 3/4 * \log_2(3/4) = 0.8113$$

$$\text{Domain}(\text{Age}) = \{\text{Old}, \text{Middle}, \text{Young}\};$$

$$\begin{aligned}\text{Entropy_Age}(D2_2) &= 2/4 * (-1/2 * \log_2(1/2) - 1/2 * \log_2(1/2)) \\ &+ 1/4 * (-0/1 * \log_2(0/1) - 1/1 * \log_2(1/1)) \\ &+ 1/4 * (-0/1 * \log_2(0/1) - 1/1 * \log_2(1/1)) = 0.5000;\end{aligned}$$

$$\text{Domain}(\text{Job}) = \{\text{Teacher}, \text{Student}\};$$

$$\begin{aligned}\text{Entropy_Job}(D2_2) &= 1/4 * (-0/1 * \log_2(0/1) - 1/1 * \log_2(1/1)) \\ &+ 3/4 * (-1/3 * \log_2(1/3) - 2/3 * \log_2(2/3)) = 0.6887;\end{aligned}$$

$$\text{Entropy}(D2_2) - \text{Entropy_Age}(D2_2) = 0.8113 - 0.5000;$$

$$\text{Entropy}(D2_2) - \text{Entropy_Job}(D2_2) = 0.8113 - 0.6887;$$

تقسيم بر اساس سن.

$$\text{Entropy}(D2_3) = -1/2 * \log_2(1/2) - 1/2 * \log_2(1/2) = 1$$

$$\text{Domain}(\text{Age}) = \{\text{Old}, \text{Young}\};$$

$$\begin{aligned}\text{Entropy_Age}(D2_3) &= 1/2 * (-1/1 * \log_2(1/1) - 0/1 * \log_2(0/1)) \\ &+ 1/2 * (-0/1 * \log_2(0/1) - 1/1 * \log_2(1/1)) = 0;\end{aligned}$$

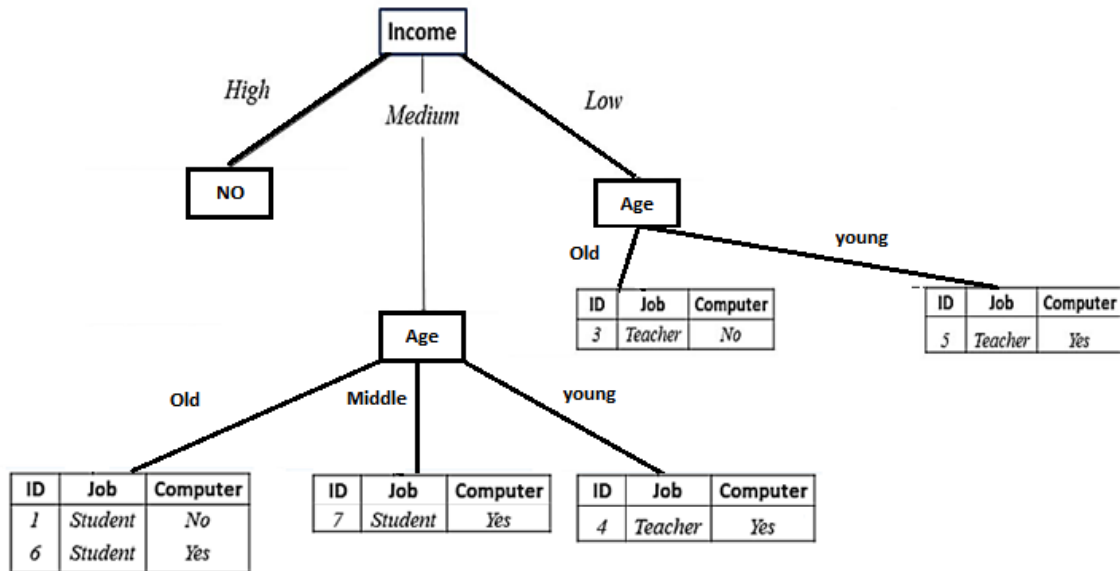
$$\text{Domain}(\text{Job}) = \{\text{Teacher}\};$$

$$\text{Entropy_Job}(D2_3) = 2/2 * (-1/2 * \log_2(1/2) - 1/2 * \log_2(1/2)) = 1;$$

$$\text{Entropy}(D2_3) - \text{Entropy_Age}(D2_3) = 1 - 0;$$

$$\text{Entropy}(D2_3) - \text{Entropy_Job}(D2_3) = 1 - 1;$$

تقسيم بر اساس سن.



مرحلة سوم

$$\text{Entropy}(D3_1) = -1/2 * \log_2(1/2) - 1/2 * \log_2(1/2) = 1$$

$$\text{Domain}(\text{Job}) = \{\text{Student}\};$$

$$\text{Entropy_Job}(D3_1) = 2/2 * (-1/2 * \log_2(1/2) - 1/2 * \log_2(1/2)) = 1;$$

$$\text{Entropy}(D3_1) - \text{Entropy_Job}(D3_1) = 0$$

$$\text{Entropy}(D3_2) = -1/1 * \log_2(1/1) = 0$$

$$\text{Entropy}(D3_3) = -1/1 * \log_2(1/1) = 0$$

