

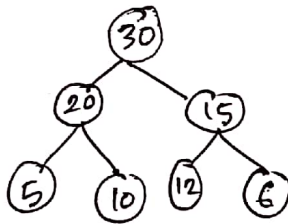
# Binary Heap \*

## Lecture 1

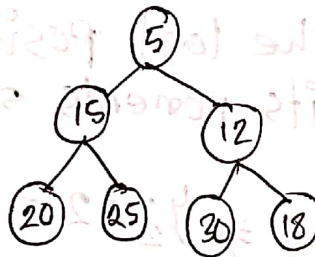
1. What is a Heap
2. Insert in a Heap
3. Deleting from Heap
4. Heap sort
5. Heapify
6. priority Queues

☐ Heap is a complete Binary tree

Max Heap



min Heap



max heap: All the descendents of root is small.

min heap: All the descendents of root is greater

T

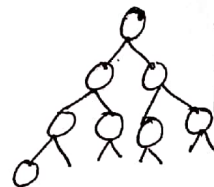
30	20	15	5	10	12	6
1	2	3	4	5	6	7

complete Binary tree  
mean no gap in  
Array

Node at index =  $i$

left child at =  $2*i$

Right child at =  $2*i + 1$



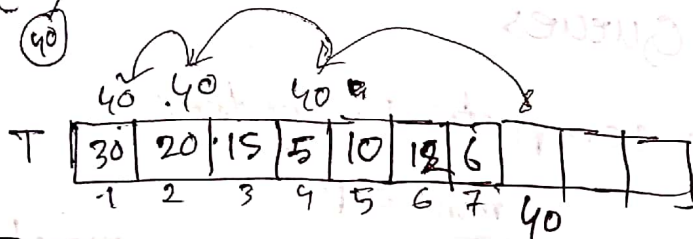
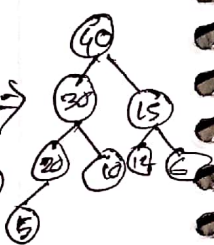
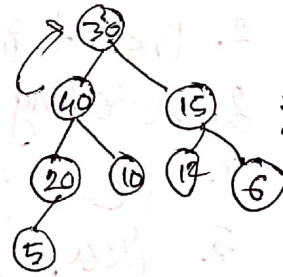
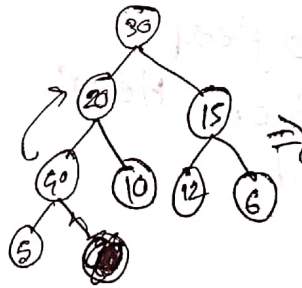
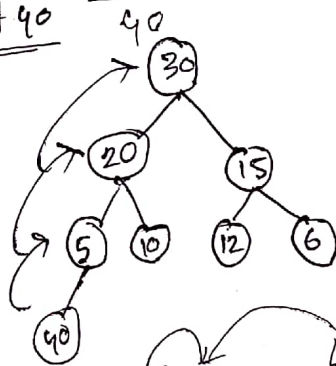
in complete  
Binary tree  
height will be  
 $\log n$  only

# Insert Binary Heap

## Lecture 2

when we insert we insert in the last in array and check and replace in the ~~80~~ Right position

Insert 40 max Heap



40 insert in the last position and check its parents small or greater

$$8/2 = 4 \Rightarrow 4/2 = 2 \Rightarrow 2/2 = 1$$

## Lecture 3

$O(\log n)$

```
void Insert(int A[], int n)
{
    int temp, i = n;
    temp = A[n];
    while (< i > 1 && temp > A[i/2])
    {
        A[i] = A[i/2];
        i = i/2;
    }
    A[i] = temp;
}
```

call

part 1

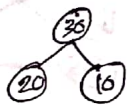
```
void createHeap()
{
    int A[] = {0, 10, 20, 30, 25, 5, 40, 35};
    int i;
    for (i = 2, i <= 7; i++)
    {
        insert(A, i);
    }
}
```

$O(\log n)$

## Lecture 3

## create Heap

30	20	10	40	15	12	25
----	----	----	----	----	----	----



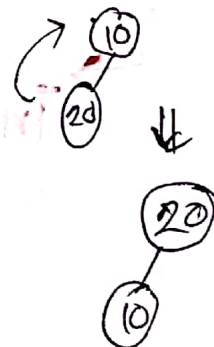
complete Binary tree  
insert Right to left and  
create heap  
This is the Idea

Compare with Parent  
Newly Insert  
Element

10	20	30	25	5
----	----	----	----	---

1. 40

2. Insert 20

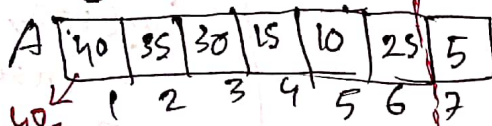
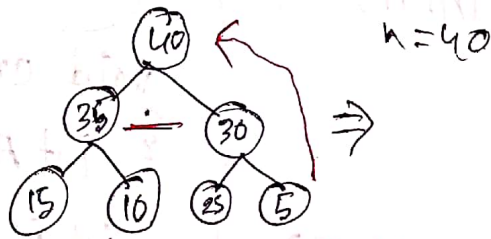


This is Idea create Heap.



# Delete Binary Heap

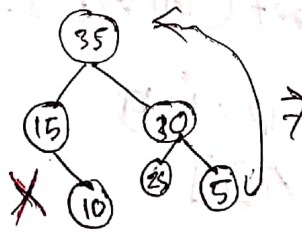
Lecture: 5



**From heap: delete only Root**

you can delete height priority element

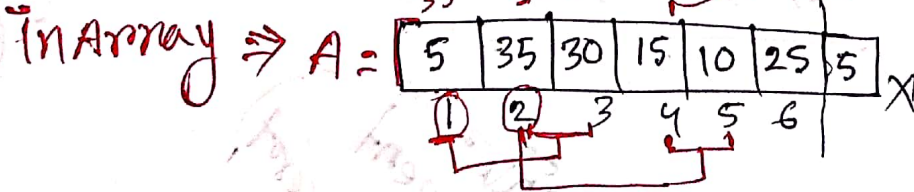
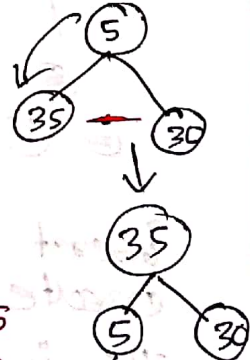
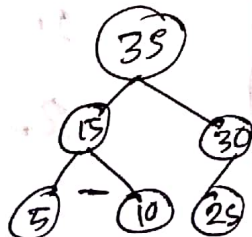
$n=40$



problem

When 40 is gone the Right most element copy in Root

- ① Root delete
- ② copy last element (5) to Root new
- ③ compare Root Both child who is getter (35, 30) change with (5)
- ④ again follow ③ step again and again



```
void Delete(int A[], int n)
```

```
{
    int n, i, j;
    n = A[n];
    A[i] = A[n];
    i = 1, j = 2 * i;
    while (j <= n - 1)
```

```
    if (A[j+1] > A[j])
        j = j + 1; // position change
                    // to child element
                    // 4, 5 like
```

```
    if (A[i] < A[j])
    {
        swap(A[i], A[j]);
        i = j;
        j = 2 * j;
    }
    else
        break;
```

```
} A[n] = n; → store in last Deleted element
```

\*\* When we delete any element from heap.

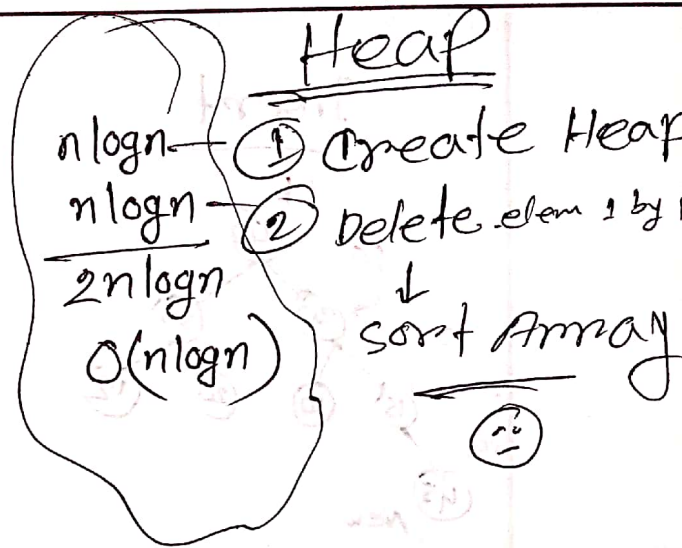
- ① We store in that last
- ② again and again delete then we get ~~for~~ sort array

~~\*\*\*~~

35	10	20	25	15	
----	----	----	----	----	--

 ⇒ 

10	15	20	25	35
----	----	----	----	----

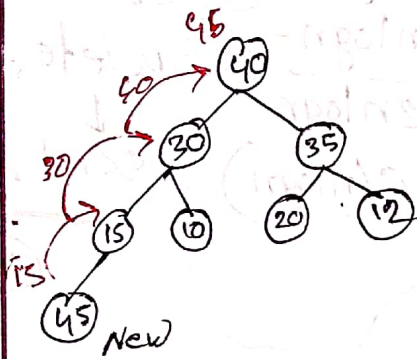




# Lecture 7

## Binary Heap Heapify

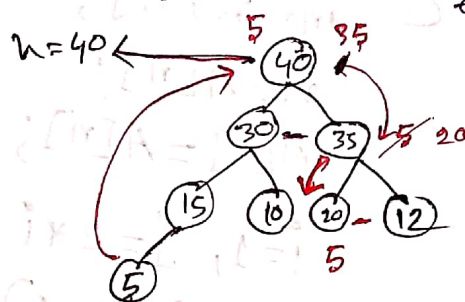
### Insert



upward

Leaf to Root sending element.

### delete



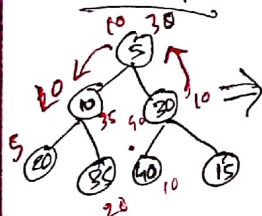
only root element Deleted

- ① send ~~last~~ Last element to Root
- ② compare Root ~~element~~ to children whom is bigger

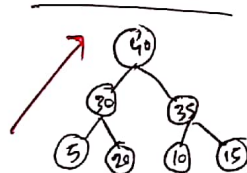
\* Root to leaf sending element

### create Heap

binary Represent



max heap

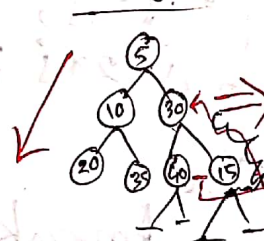


A [5 | 10 | 30 | 20 | 35 | 40 | 15]

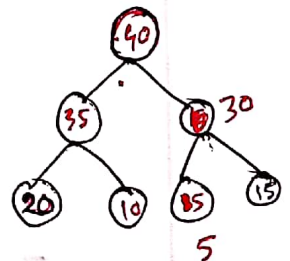
$O(n \log n)$

### Heapify

binary tree



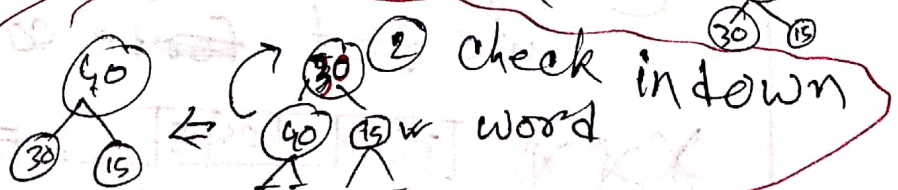
downward



A [5 | 10 | 30 | 20 | 35 | 40 | 15]

$O(n)$

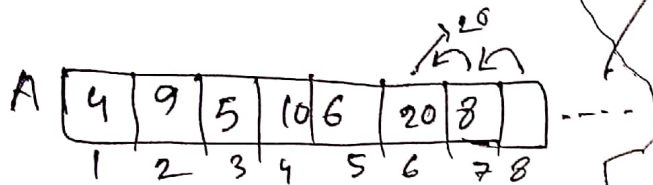
- ① compare leaf bigger send to emidiet Root  
30 → (40-15) → 40



# Binary Heap as Priority queue \*

element  $\Rightarrow$  4, 9, 5, 10, 6, 20, 8, 15, 2, 18

larger the element  
height the priority

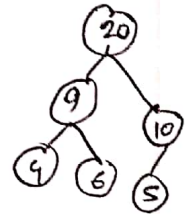


Insert  $O(1)$

Delete  $O(n) \Rightarrow (n+n) = 2n \Rightarrow O(n)$   
↓ search the move

Delete  $\Rightarrow$  search the height  
element and delete  
and move element  
shift

max heap



Insert  $O(\lg n)$

Delete  $O(\lg n)$

\*

Time Reduce