

# Chapter 1

## Base for a Topology

**Definition 1.1.** Let  $(X, \tau)$  be a topological space. Then a class  $\mathcal{B} \subseteq \tau$  is a **base** for the topology  $\tau$  on  $X$  if every member of  $\tau$  can be written as a union of members of  $\mathcal{B}$ . Equivalently,  $U \in \tau$  can be written as  $U = \cup_{B \in \mathcal{B}} B$ .