

CSE 331-Computer Organization HW3

32-bit Multiplier

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1801042630

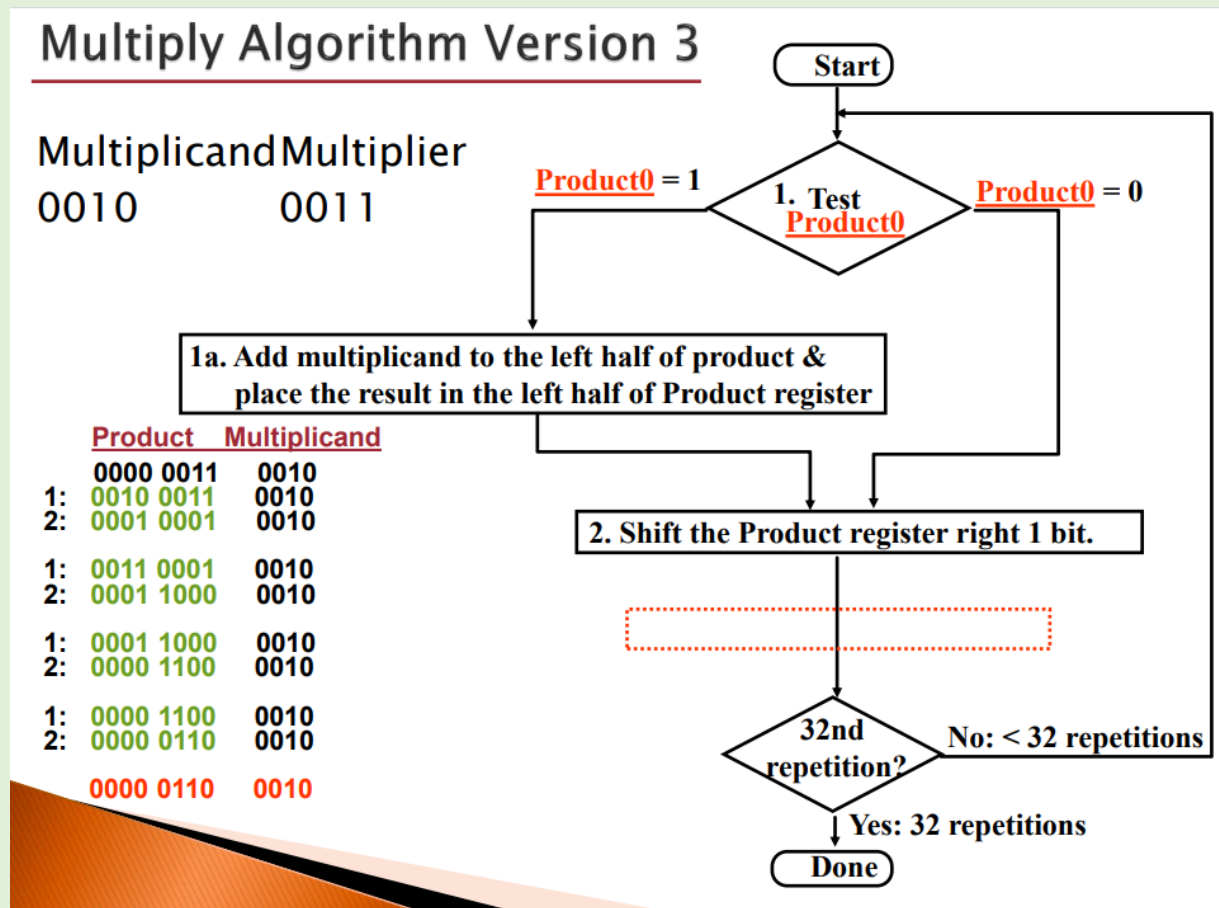
(all the required circuits are in the mult32.circ file)

Following circuits are implemented to the project;

- 1 Arithmetic-Logic Unit(Datapath)
- 1 Control Unit
- 1 Signal Generator
- 1 Synchroniser for Buttons
- 1 one-bit Shifter
- 1 one-bit Adder
- 1 32-bit Adder
- 1 Main circuit named as Multiplier_(main)

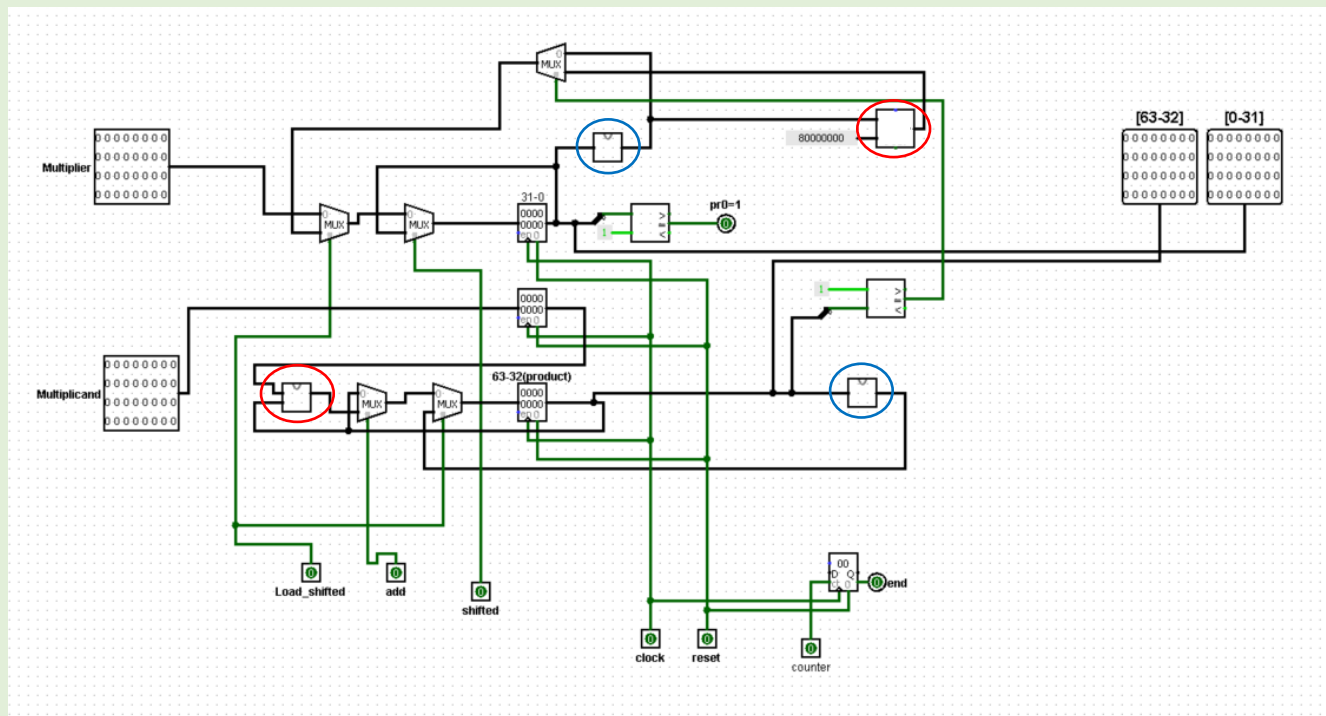
The Algorithm:

The algorithm, which is seen in lecture 5, is used.



Datapath(ALU):

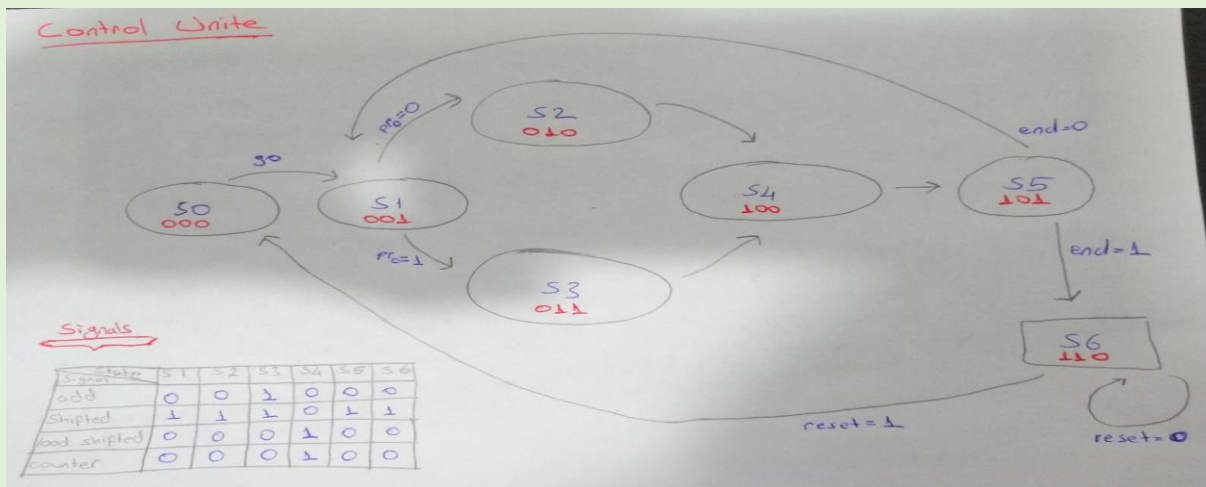
Datapath is the circuit which provides to make required calculations and generate signals for any algorithm.



- Red circle shows the designed 32-bit adder. (as bonus)
- Blue circles show the designed 1-bit shifter. (as bonus)
- All the inputs (except clock) are taken from the control unit.
- All the outputs ("Pr0" and "end") are received to the control unit for controlling the state transitions.
- If pr0=1 adding operation will be performed for 64 bit product. Then it will be shifted.
- If pr0=0 adding operation will NOT be performed. Only the 64 bit product will be shifted.
- Since Logisim does not support 64 bit components, 2x32 bit outputs are used. If 32th bit of the product is 1, [31-0] of the product will be added by 0x80000000 (10000000000000000000000000000000) to make the MSB of first part of the product 1.

Control Unit(FSM):

- The state diagram, truth table, boolean equations and designed circuits are shown below.



Truth Table

clears all the registers and resets the game.

if reset=0

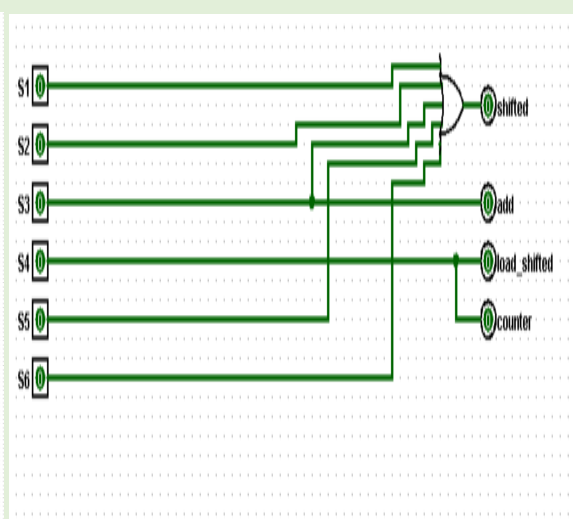
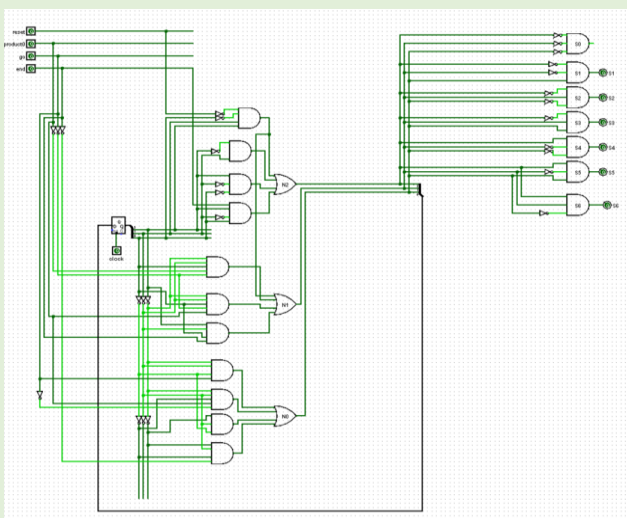
if reset=1

INPUTS							OUTPUTS		
S2	S1	S0	go	pg	end		N2	N1	N0
0	0	0	0	x	x		0	0	0
0	0	0	1	x	x		0	0	1
0	0	1	0	0	x		0	1	0
0	0	1	0	1	x		0	1	1
0	1	0	x	x	x		1	0	0
0	1	1	x	x	x		1	0	0
1	0	0	x	x	x		1	0	1
1	0	1	x	x	0		0	0	1
1	0	1	x	x	1		1	1	0
1	1	0	x	x	x		1	1	0
1	1	0	x	x	x		0	0	0

Boolean Expressions:

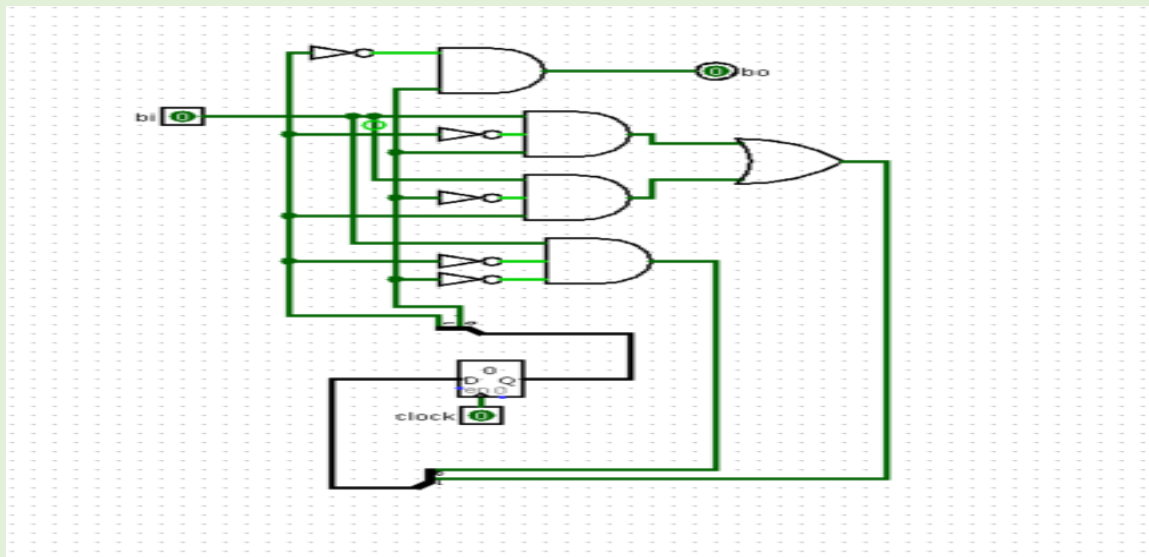
$$N2 = S_2' S_1' + S_2' S_1 S_0' + S_2 S_1 S_0' \text{end} + \text{reset}' \cdot S_2 S_1 S_0'$$

$$N1 = S_2' S_1 S_0 \text{pg}' + S_2 S_1 S_0 \text{pg}' + S_2 S_1 S_0 \text{end} + \text{reset}' \cdot S_2 S_1 S_0'$$

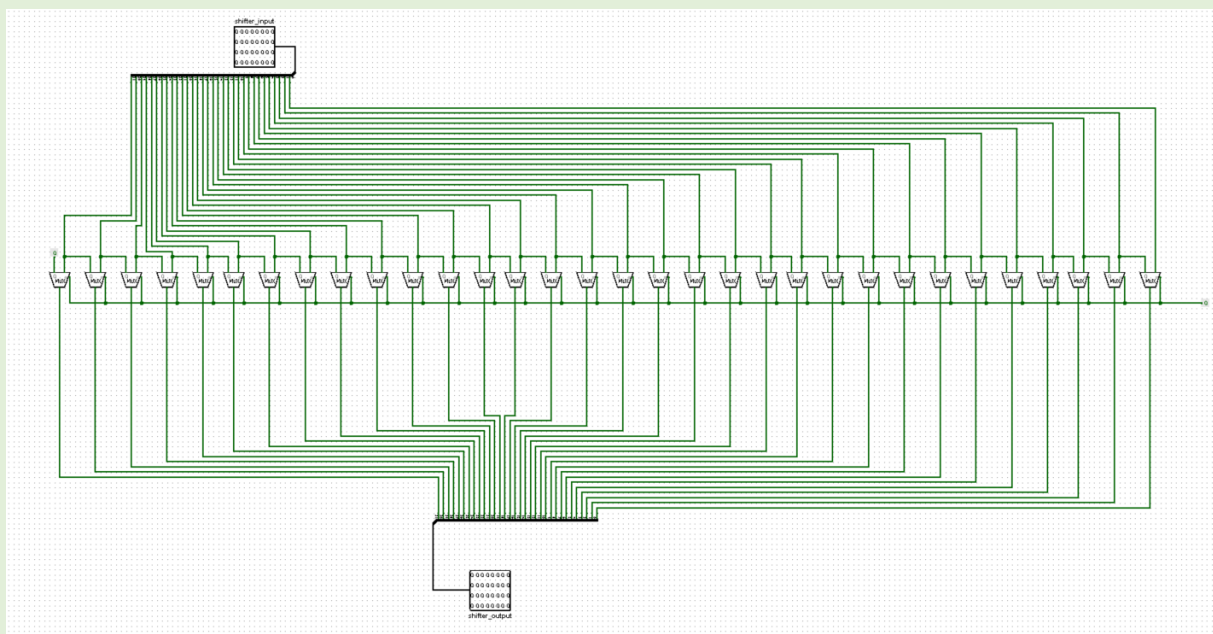
$$N0 = S_2' S_1 S_0 \text{go} + S_2 S_1 S_0 \text{pg}' + S_2 S_1 S_0 \text{end}' + S_2 S_1 S_0 \text{end}'$$


Synchroniser:

- Synchroniser provides to push button for once even it is kept pushed. The synchroniser is already design by me in the Logic Circuits assignments.

**1-bit Shifter:**

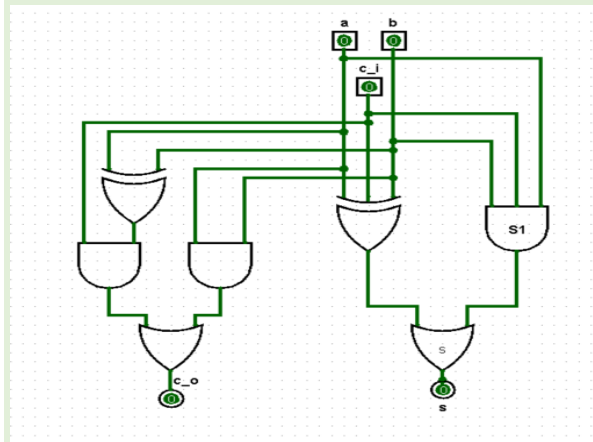
- The designed shifter provides to shift the input number for 1 bit. The constant 0 is for choosing the correct input of multiplexer's. It can be changed as an input but if it is changed, the multiplexers inputs must be switched.



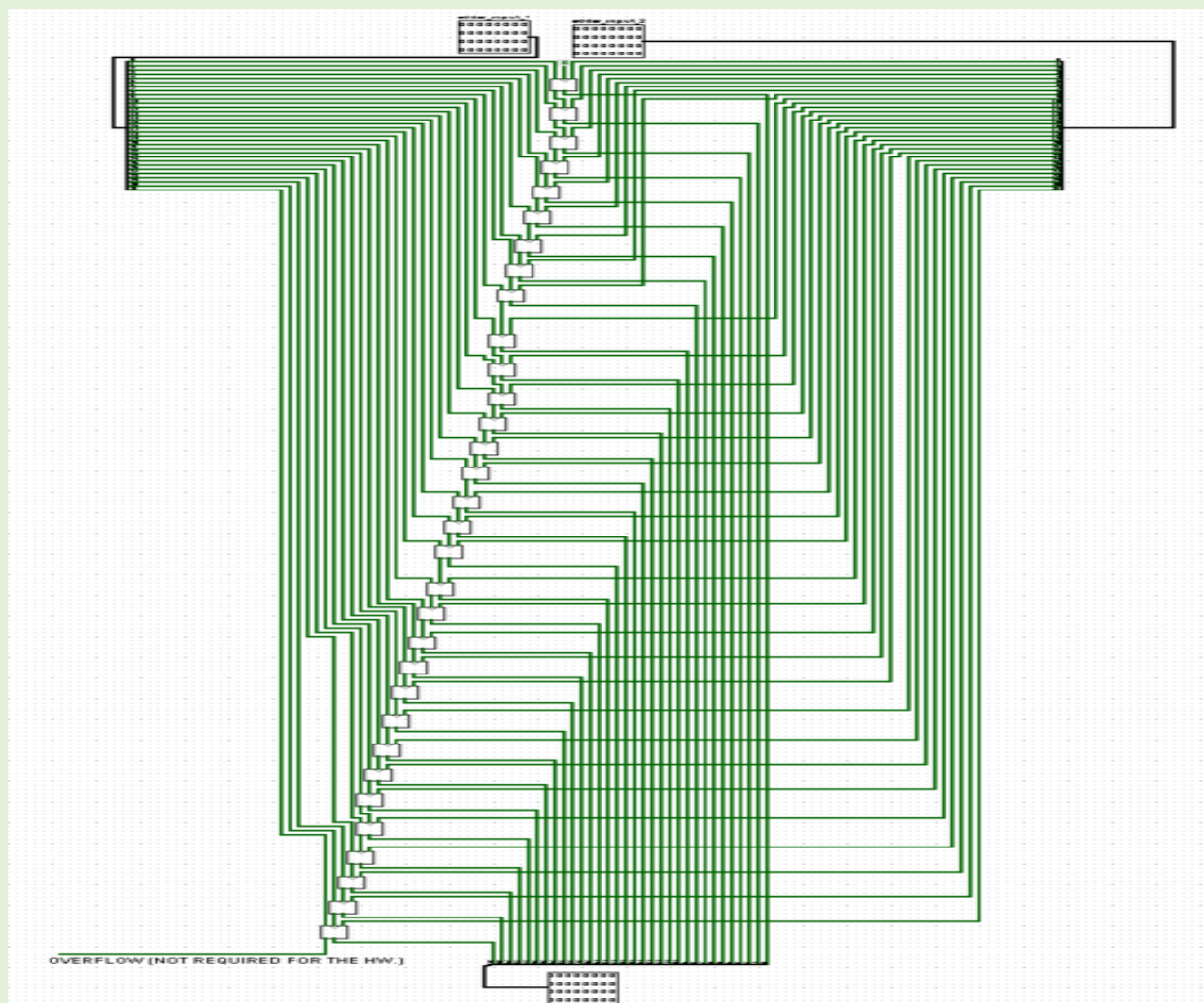
1-bit Adder:

- The truth table, which is seen in lecture 4, is used with some modifications.

a_i	b_i	c_i	c_{i+1}	s_i
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

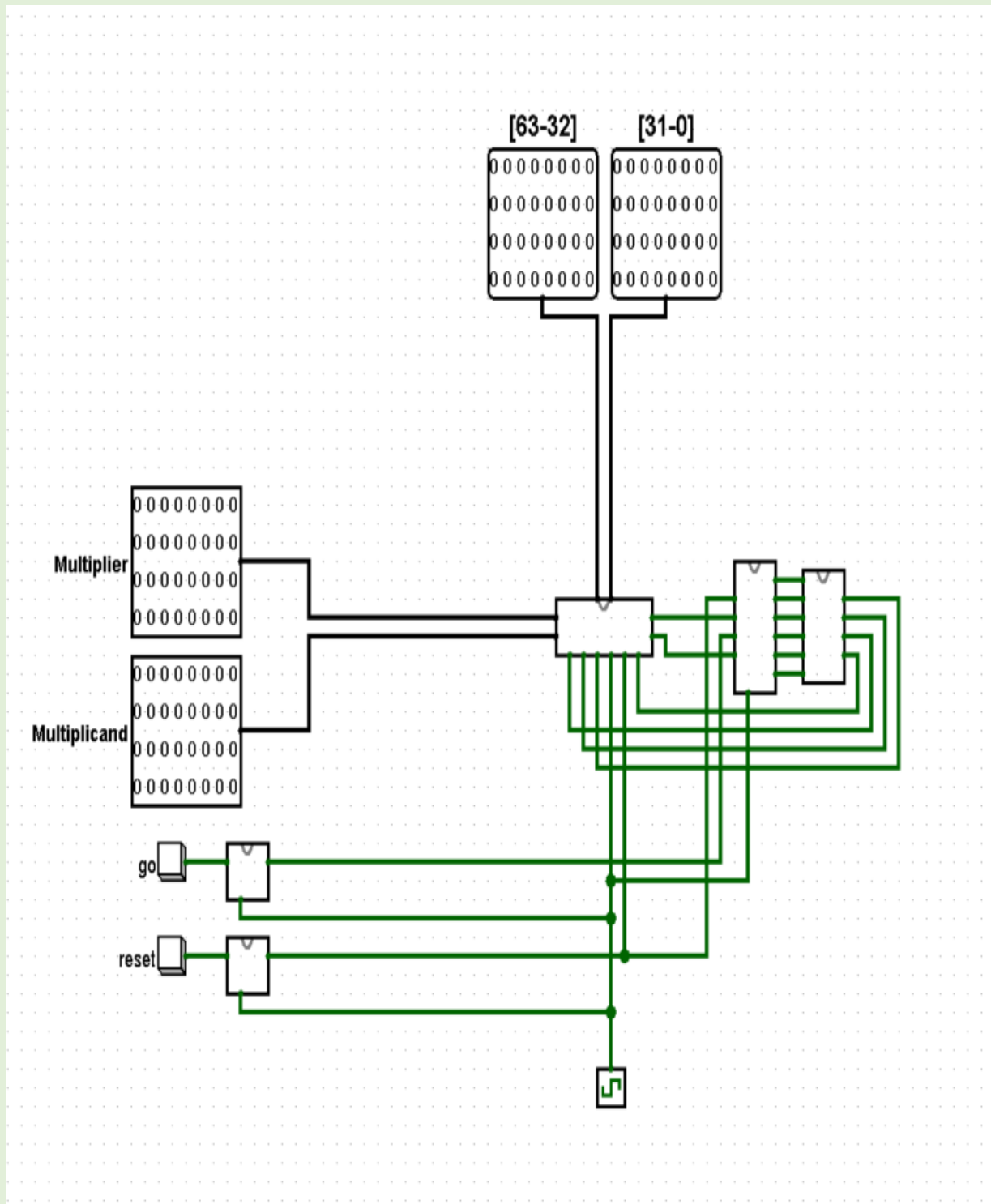
**32-bit Adder:**

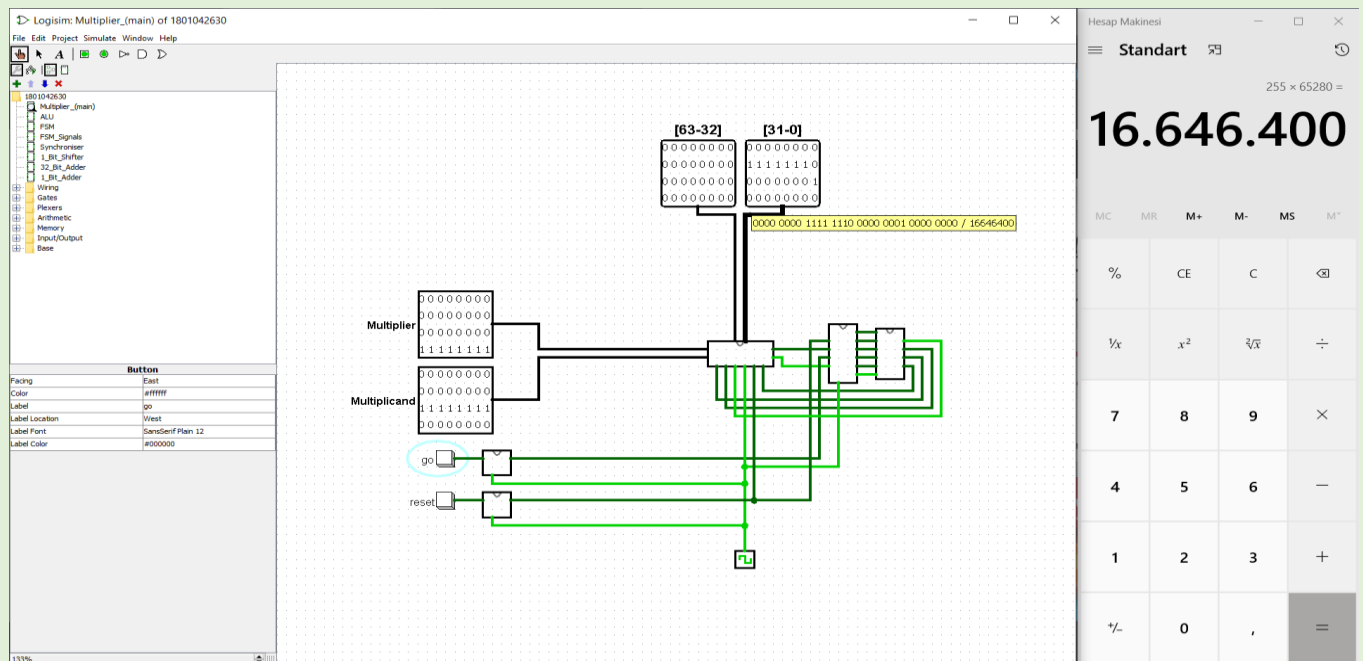
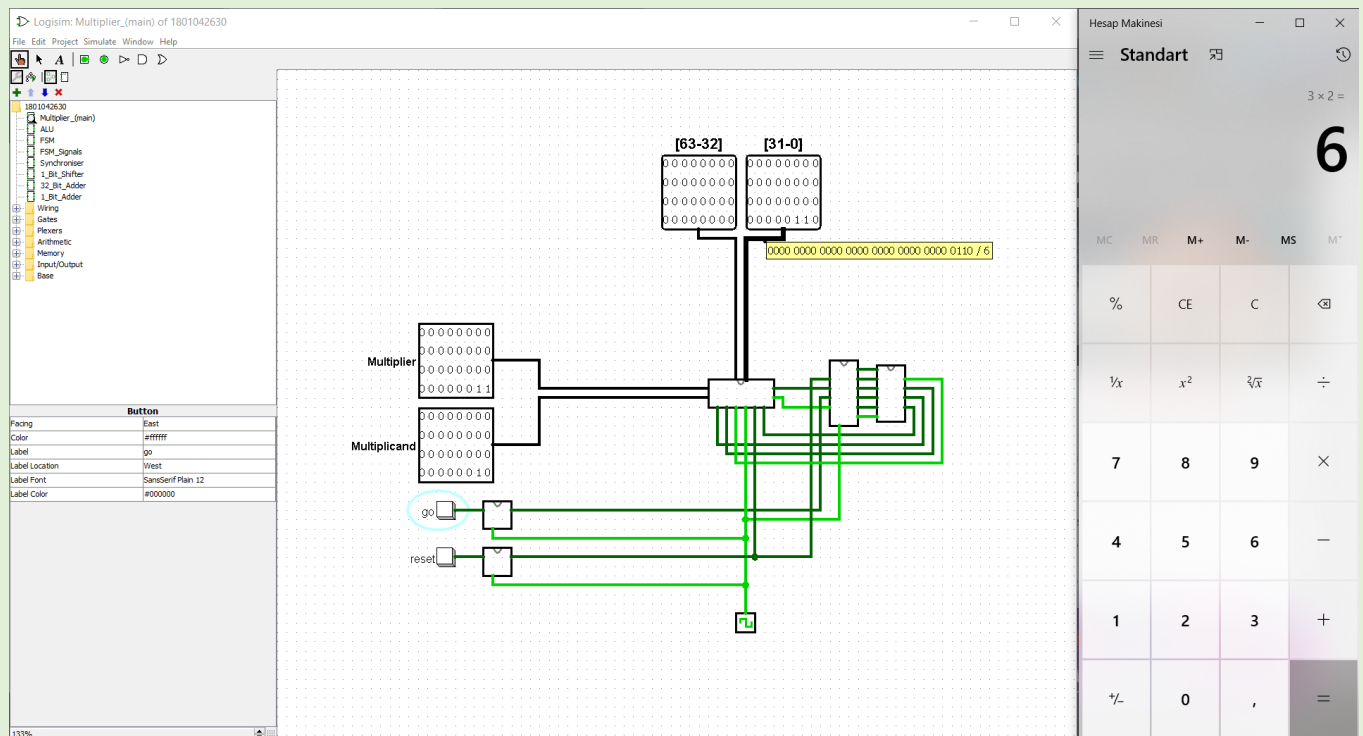
- 32 bit adder is composed of 32x1-bit adder. Adder's carry in values and carry out values are connected to each other. The MSB's carry out bit can show the overflow but it is not required to show it for this project. The template is shown in the circuit below.



The Main:

- Here is an indigenous and national multiplier :))



Test Cases:

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Logisim: Multiplier_(main) of 1801042630

File Edit Project Simulate Window Help

1801042630

- Multiplier_(main)
- ALU
- FSM
- FSM_Signals
- Synchroniser
- 1_Bit_Shifter
- 32_Bit_Adder
- 1_Bit_Adder
- Wiring
- Gates
- Plexers
- Arithmetic
- Memory
- Input/Output
- Base

Button

Facing	East
Color	#ffffff
Label	go
Label Location	West
Label Font	SansSerif Plain 12
Label Color	#000000

Multiplier

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

Multiplicand

0 1 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

go

reset

[63-32]

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

[31-0]

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0000 0000 0000 0000 0000 0000 0000 0001 / 1

Hesap Makinesi

Standard

1073741824 × 4 =

4.294.967.296

MC	MR	M+	M-	MS	M*
%	CE	C	<		
1/x	x ²	√x	÷		
7	8	9	×		
4	5	6	-		
1	2	3	+		
+/-	0	,	=		

Logisim: Multiplier_(main) of 1801042630

File Edit Project Simulate Window Help

1801042630

- Multiplier_(main)
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- 1_Bit_Adder
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- Base

Pin

Facing	East
Output?	No
Data Bits	32
Three-state?	No
Pull Behavior	Unchanged
Label	Multiplicand
Label Location	West
Label Font	SansSerif Bold 12

Multiplier

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 1 1 1 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

Multiplicand

0 1 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

go

reset

[63-32]

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

[31-0]

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0 0 0 0 0 0 0 0

0000 0000 0000 0000 0000 0000 0000 0111 / 7

Hesap Makinesi

Standard

1073741824 × 28 =

30.064.771.072

MC	MR	M+	M-	MS	M*
%	CE	C	<		
1/x	x ²	√x	÷		
7	8	9	×		
4	5	6	-		
1	2	3	+		
+/-	0	,	=		

CSE 331-Computer Organization Assignment3

Logisim: Multiplier_(main) of 1801042630

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Button	
Facing	East
Color	#ffffff
Label	go
Label Location	West
Label Font	SansSerif Plain 12
Label Color	#000000

133%

Multiplier

Multiplicand

go

reset

64

[63-32] [31-0]

0000 0000 0000 0000 0000 0000 1111 1000 0001 / 3969

Hesap Makinesi

Standart

63 × 63 =

3.969

MC	MR	M+	M-	MS	M*
%	CE	C	<		
1/x	x ²	√x	÷		
7	8	9	×		
4	5	6	-		
1	2	3	+		
+/-	0	,	=		

Logisim: Multiplier_(main) of 1801042630

File Edit Project Simulate Window Help

1801042630

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- ALU
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Button	
Facing	East
Color	#ffffff
Label	go
Label Location	West
Label Font	SansSerif Plain 12
Label Color	#000000

133%

Multiplier

Multiplicand

go

reset

64

[63-32] [31-0]

0000 1100 0111 1010 1111 0110 1111 1101 / 209385213

Hesap Makinesi

Standart

3 × 69795071 =

209.385.213

MC	MR	M+	M-	MS	M*
%	CE	C	<		
1/x	x ²	√x	÷		
7	8	9	×		
4	5	6	-		
1	2	3	+		
+/-	0	,	=		