Midterm (100 pts)

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Assigned : November the 10th, 10h30

Duration: 150 minutes

Name-Surname:

1 List Manipulations (35 pts)

Q1. Write below described functions in Haskell without employing Prelude library functions and the list comprehension.

a) (10 pts) rotateN :: Int -> [a] -> [a] takes an integer n and a list [a] of arguments, and right rotates the list n times.

```
rotateN 2 [7,5,1,3,6] == [1,3,6,7,5]

rotateN 4 [7,5,1,3,6] == [6,7,5,1,3]

rotateN 5 [7,5,1,3,6] == [7,5,1,3,6]

rotateN 6 [7,5,1,3,6] == [5,1,3,6,7]
```

b) (10pts) deleteKey :: (Eq a) ⇒ a -> [(a,b)] -> [(a,b)] takes a key (of some Eq class instance type a) with a list of pairs l, and returns a list of pairs that does not contain (k,v) pairs such that key == k.

c) (**15pts**) partition :: (a -> Bool) -> [a] -> ([a],[a]) takes a predicate, p along with a list l, and returns a pair of lists (l1,l2) such that l1 contains members of l satisfying p while l2 contains those that do not satisfy p. Note that in both l1 and l2, elements are supposed to be in the same order with that of l.

2 User Defined Data Types (40 pts)

Q2. Within the context of a type BoolExp of propositional logical formulas, and a type BValuations of Boolean valuations, implement below stated functions in Haskell without employing Prelude functions and list comprehension.

data BoolExp where

```
Prop :: Char
             -> BoolExp
And :: BoolExp -> BoolExp -> BoolExp
Or :: BoolExp -> BoolExp -> BoolExp
Impl :: BoolExp -> BoolExp
Iff :: BoolExp -> BoolExp
Not :: BoolExp -> BoolExp
```

type BValuation = [(Char, Bool)]



Notice.

The proposition And (Prop 'p') (Prop 'q') denotes the logical "and" of propositional formulae p and q $(p \land q)$ while Impl (Prop 'p') (Prop 'q') represents the proposition p "implies" q, namely $p \implies q$. Similarly, Iff (Prop 'p') (Prop 'q') stands for the "double way implication" in between p and q, $p \iff q$.

In a valuation like [('p', True), ('q', False)], the proposition Prop 'p' takes the value of True while Prop 'q' is False.

a) (10 pts) printBoolExp :: BoolExp -> String represents formulae in the string form.

```
"p"
printBoolExp (Prop 'p')
printBoolExp (And (Prop 'p') (Prop 'q'))
                                                                "(p && q)"
printBoolExp (Or (Prop 'p') (Prop 'q'))
                                                                "(p || q)"
printBoolExp (Impl (Prop 'p') (Prop 'q'))
                                                                "(p -> q)"
printBoolExp (Iff (Prop 'p') (Prop 'q'))
                                                                "(p <-> q)"
                                                                "(~p)"
printBoolExp (Not (Prop 'p'))
printBoolExp (And (Prop 'r') (Iff (Prop 'p') (Prop 'q'))) == "(r && (p <-> q))"
```

b) (15 pts) propNames :: BoolExp -> [Char] extracts proposition names out of a given formula where no name duplications allowed. The appearance order also matters.

c) (15 pts) beval :: BValuation -> BoolExp -> Bool evaluates the given formula under a valuation, and returns the Bool value.

3 Untyped λ -Calculus (25 pts)

Q3. β -reduce below untyped λ -terms, as far as possible, employing the normal (leftmost-outermost) reduction order. Clearly demonstrate every single reduction step.

a) (**10 pts**) $((\lambda f. \lambda x. fff x)f)((\lambda f. \lambda x. fff x)f)$

b) (15 pts) $(\lambda u. \lambda w. \lambda f. \lambda x. w f(u f x)) (\lambda f. \lambda x. f f f f f x) (\lambda f. \lambda x. f f f f f f x)$