

ENG 346

Data Structures and Algorithms for Artificial Intelligence

Stacks and Queues

Dr. Mehmet PEKMEZCİ

mpekmezci@gtu.edu.tr

<https://github.com/mehmetpekmezci/GTU-ENG-346>

Abstract Data Types

- High-level description of a collection of data and the operations that can be performed on that data.
- Benefits:
 - Data Structure Abstraction: Behavior of a data structure.
 - Operations: A set of operations that can be performed on the data.
 - Encapsulation: Encapsulate the data and operations into a single unit.
 - Reusability: Reuse in different applications.

ADTs – continued

- **List:** List of elements accessible by positions.
- **Dictionary:** Key-value pairs.
- **Set:** Collection of distinct elements.
- **Stack:** Follows Last-In-First-Out (LIFO) principle.
- **Queue:** Follows First-In-First-Out (FIFO) principle.
- **Graph:** Vertices and using edges.

Stacks

- Insertions and deletions from the same end of the list.
- Follow the last-in first-out scheme

Main Operations	Auxiliary Operations
S.push(item)	item = S.top()
item = S.pop()	len(S)
	S.is_empty()

Stacks – continued

- General Applications
 - Function's call stack
 - Internet Browser history
 - Editor undo/redo
 - ...
- Algorithm design
 - Reverse polish notation
 - ...

Stacks – Example

Operation	Return Value	Stack Contents
S.push(5)	–	[5]
S.push(3)	–	[5, 3]
len(S)	2	[5, 3]
S.pop()	3	[5]
S.is_empty()	False	[5]
S.pop()	5	[]
S.is_empty()	True	[]
S.pop()	“error”	[]
S.push(7)	–	[7]
S.push(9)	–	[7, 9]
S.top()	9	[7, 9]
S.push(4)	–	[7, 9, 4]
len(S)	3	[7, 9, 4]
S.pop()	4	[7, 9]
S.push(6)	–	[7, 9, 6]
S.push(8)	–	[7, 9, 6, 8]
S.pop()	8	[7, 9, 6]

Array-Based Stack Implementation

```
class Stack:
    def __init__(self, size=10):
        pass
    def push(self, data):
        pass
    def pop(self):
        pass
    def is_empty(self):
        pass
    def top(self):
        pass
    def __len__(self):
        pass
    def display(self):
        pass
```

Example – Parenthesis Matching

Algorithm ParenthesisMatching(X, n):

Input: An array X of n tokens, each of which is either a grouping symbol, a variable, an arithmetic operator, or a number

Output: **true** if and only if all the grouping symbols in X match

Let S be an empty stack

for $i=0$ to $n-1$ **do**

if $X[i]$ is an opening grouping symbol **then**

$S.push(X[i])$

else if $X[i]$ is a closing grouping symbol **then**

if $S.is_empty()$ **then**

return false {nothing to match with}

if $S.pop()$ does not match the type of $X[i]$ **then**

return false {wrong type}

if $S.isEmpty()$ **then**

return true {every symbol matched}

else return false {some symbols were never matched}

Reverse Polish Notation

- Mathematical notation: Infix, operators are between operands.
 - E.g.: $2 + 3 * (4 + 7)$
- Polish Notation: Prefix, operators before operands.
 - E.g.: $+ 2 * 3 + 4 7$
- Reverse Polish Notation: Postfix, operators follow operands.
 - E.g.: $2 3 4 7 + * +$

Example – Reverse Polish Notation Calculator



- Using Stack

Queues

- Insertions to the end, deletions from the front of the list.
- Follow the first-in first-out scheme

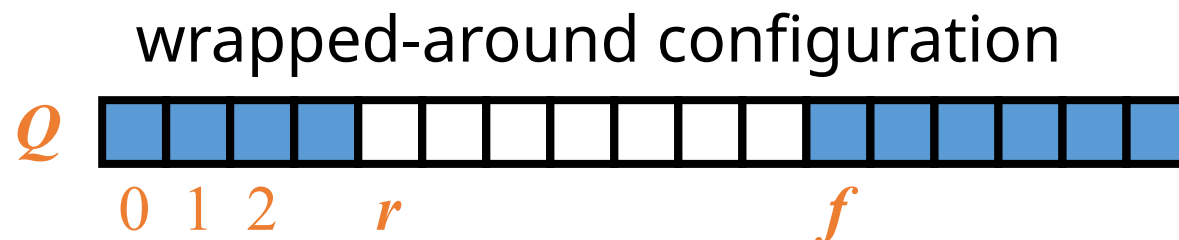
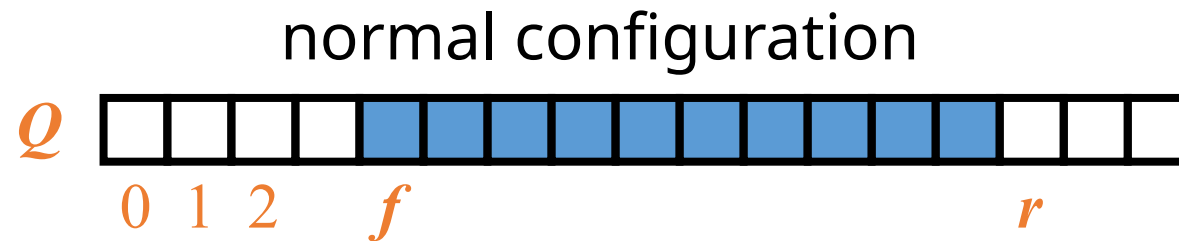
Main Operations	Auxiliary Operations
Q.enqueue(item)	item = Q.first()
item = Q.dequeue()	len(Q)
	Q.is_empty()

Queues – continued

- General Applications
 - Waiting lists
 - Access to shared resources (e.g., printer)
 - Round Robin Scheduler
 - ...
- Algorithm design
 - ...

Array-based Queue Implementation

- Use an array of size N in a circular fashion
- Two variables keep track of the front and rear
 - f index of the front element
 - r index immediately past the rear element
- Array location r is kept empty

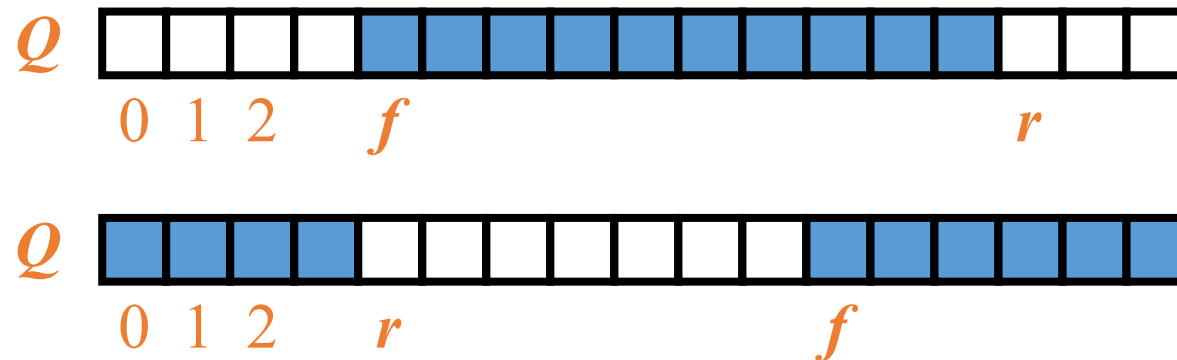


Queue Operations

- We use the modulo operator (remainder of division)

Algorithm *size()*
 return $(N - f + r) \bmod N$

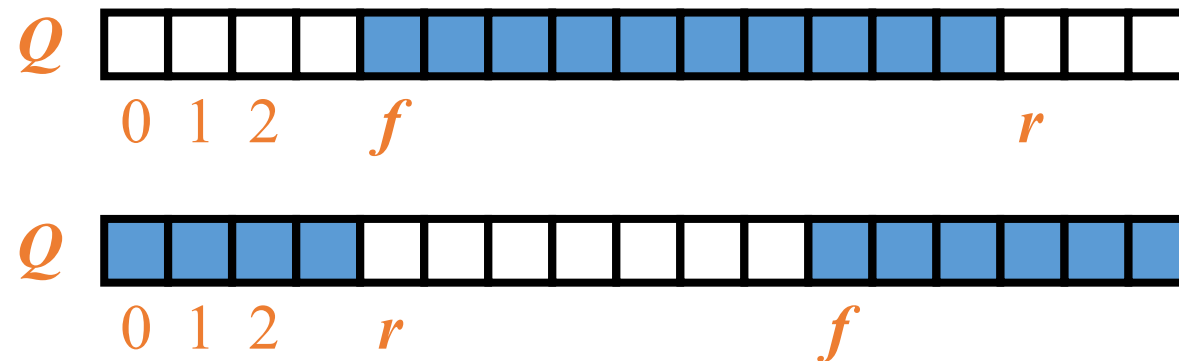
Algorithm *isEmpty()*
 return $(f = r)$



Queue Operations (cont.)

- Operation enqueue throws an exception if the array is full
- This exception is implementation-dependent

Algorithm *enqueue(o)*
if *size()* = $\tilde{N} - 1$ **then**
 throw *FullQueueException*
else
 $Q[r] \Leftarrow o$
 $r \Leftarrow (r + 1) \bmod N$

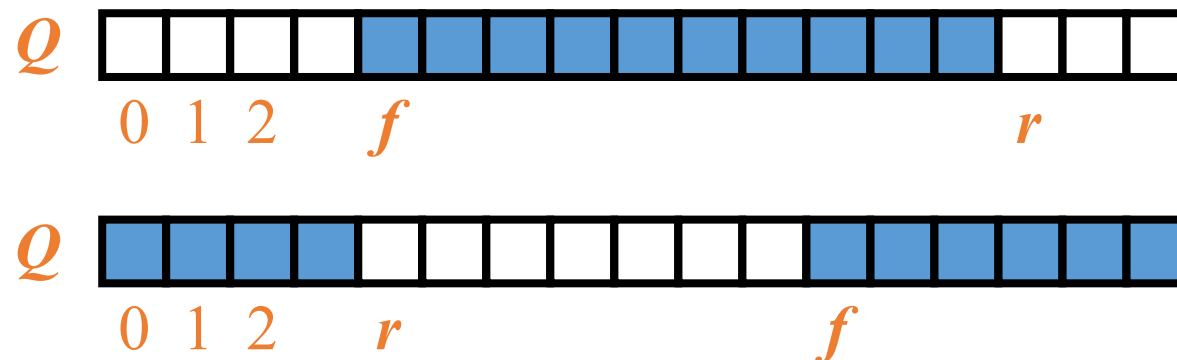


Queue Operations (cont.)

- Operation dequeue throws an exception if the queue is empty
- This exception is specified in the queue ADT

```

Algorithm dequeue()
  if isEmpty() then
    throw EmptyQueueException
  else
     $o \Leftarrow Q[f]$ 
     $f \Leftarrow (f + 1) \bmod N$ 
    return  $o$ 
  
```



Queues – Example

Operation	Return Value	first \leftarrow Q \leftarrow last
Q.enqueue(5)	–	[5]
Q.enqueue(3)	–	[5, 3]
len(Q)	2	[5, 3]
Q.dequeue()	5	[3]
Q.is_empty()	False	[3]
Q.dequeue()	3	[]
Q.is_empty()	True	[]
Q.dequeue()	“error”	[]
Q.enqueue(7)	–	[7]
Q.enqueue(9)	–	[7, 9]
Q.first()	7	[7, 9]
Q.enqueue(4)	–	[7, 9, 4]
len(Q)	3	[7, 9, 4]
Q.dequeue()	7	[9, 4]

Array Based Queue Implementation

```
class Queue:
    def __init__(self, c=10):
        pass
    def is_empty(self):
        pass
    def enqueue(self, data):
        pass
    def dequeue(self):
        pass
    def __len__(self):
        pass
    def display(self):
        pass
    def first(self):
        pass
```