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# MoFEM: An open source, parallel finite element library – MFront integration

Karol Lewandowski & Łukasz Kaczmarczyk,  
Andrei Shvarts, Ignatios Athanasiadis, Mebratu Wakeni,  
Hoang Nguyen, Daniele Barbera, Christophe-Alexandre  
Chalons-Mouriesse, Adriana Kulikova & Chris Pearce

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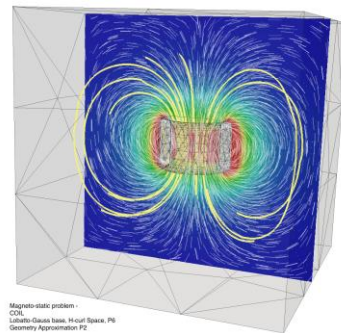
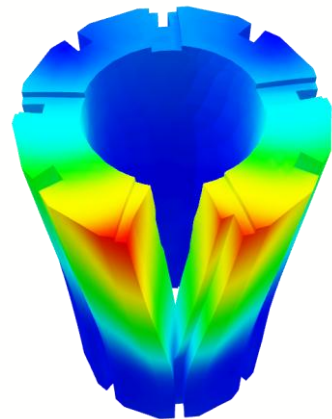




# MoFEM in a nutshell

## Mesh-oriented Finite Element Method:

- C++ open-source library (permitting private user modules)
- Mixing different element types and shapes in one mesh
- Using hierarchical basis functions (*hp*-adaptivity)
- Support for L2, H-div, H-curl, and H1 approximation spaces
- Supporting multi-field and multi-physics problems
- Native support for parallelisation
- Chained with state-of-the-art libraries for managing Topology (MOAB) and Linear Algebra (PETSc) – developed at the Argonne National Laboratory
- Validated and currently used by EDF Energy and Jacobs

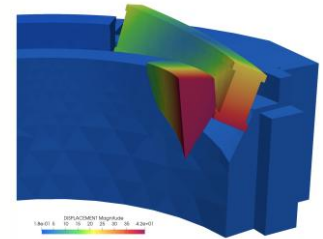
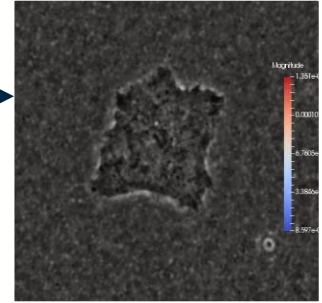
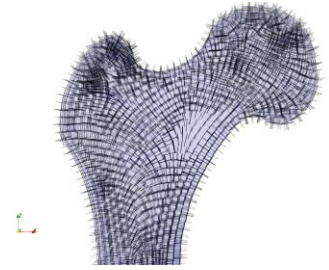


Magneto-static problem  
CQ1  
Lobatto-Gauss base, H-curl Space, P6  
Geometry Approximation P2



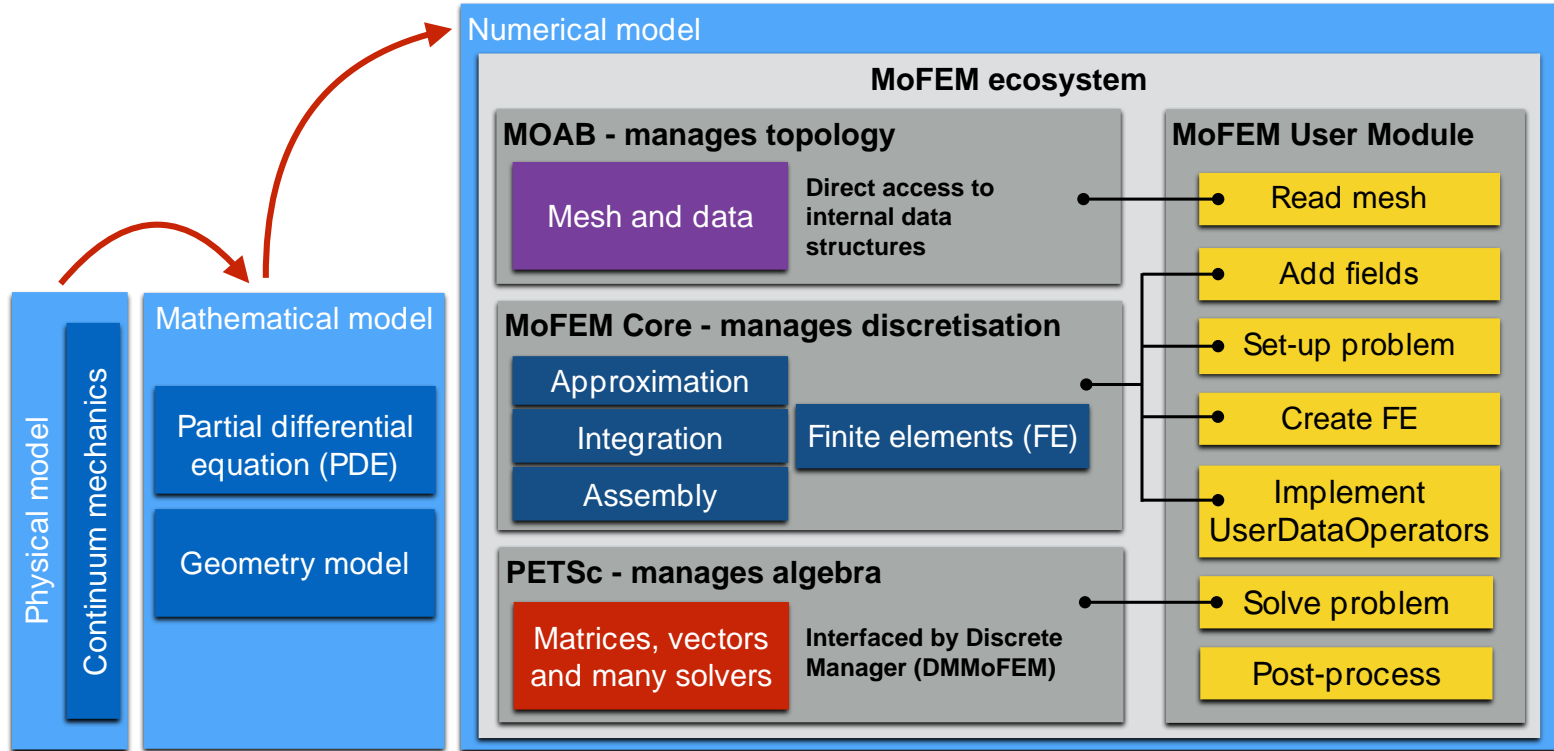
# Design objectives

- Design for research & development
- Solve practical engineering problems
- Allow for rapid development for nonstandard niche problems
- Create competitive advantage for industrial/research partner
- Enabling to break complex problem into small simple parts
- Enabling collaborative work distributed in time and space
- Structure allowing testing small parts separately
- Handling of error and unified logging



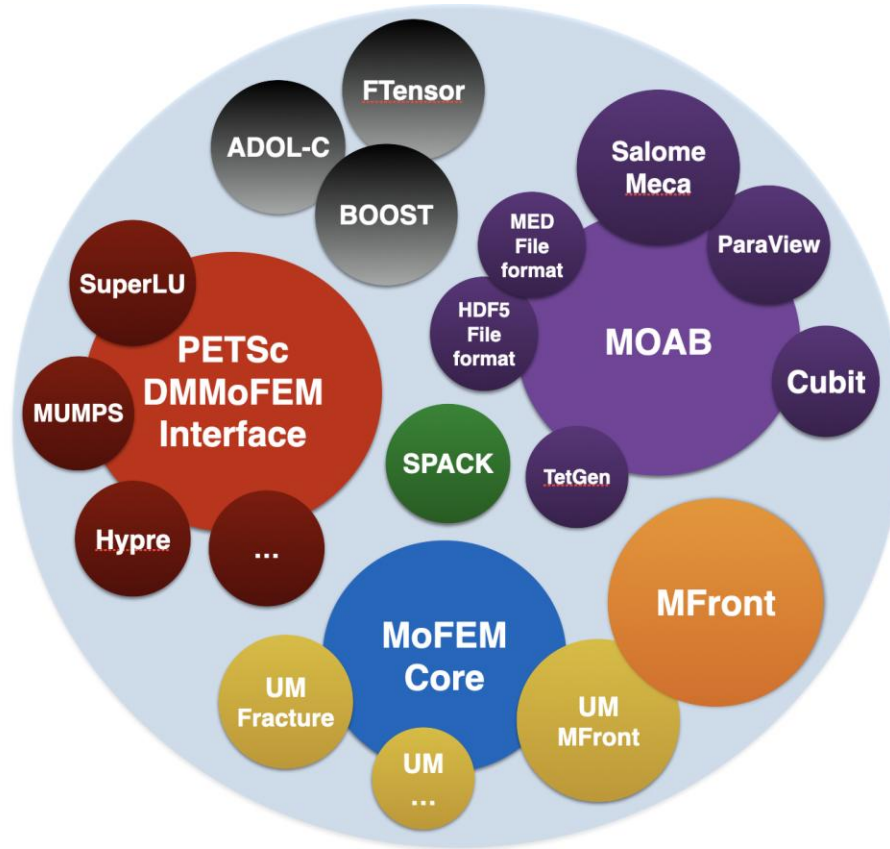


# Basic design of MoFEM





# MoFEM ecosystem





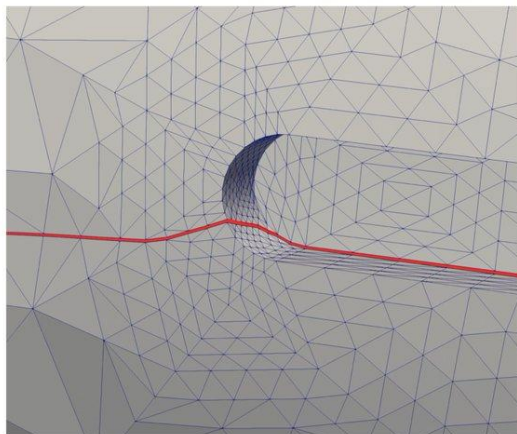
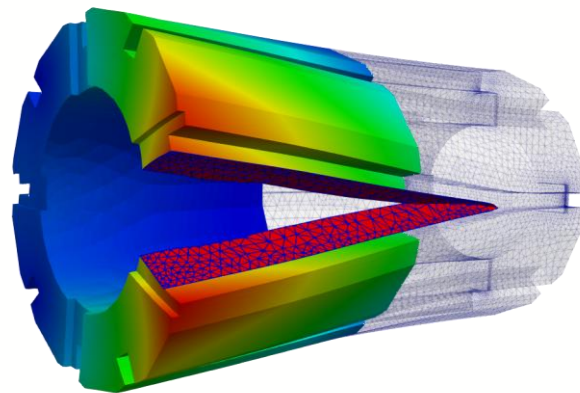


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edfENERGY

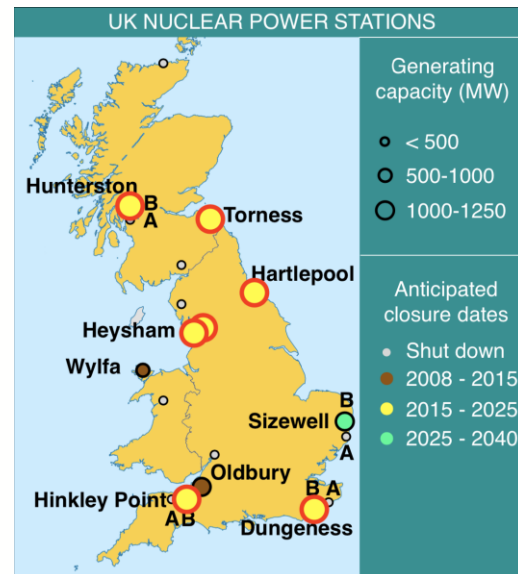
MoFEM is used by EDF/Jacobs Energy to  
**assess structural integrity of nuclear  
reactors in the UK.**



Simulation

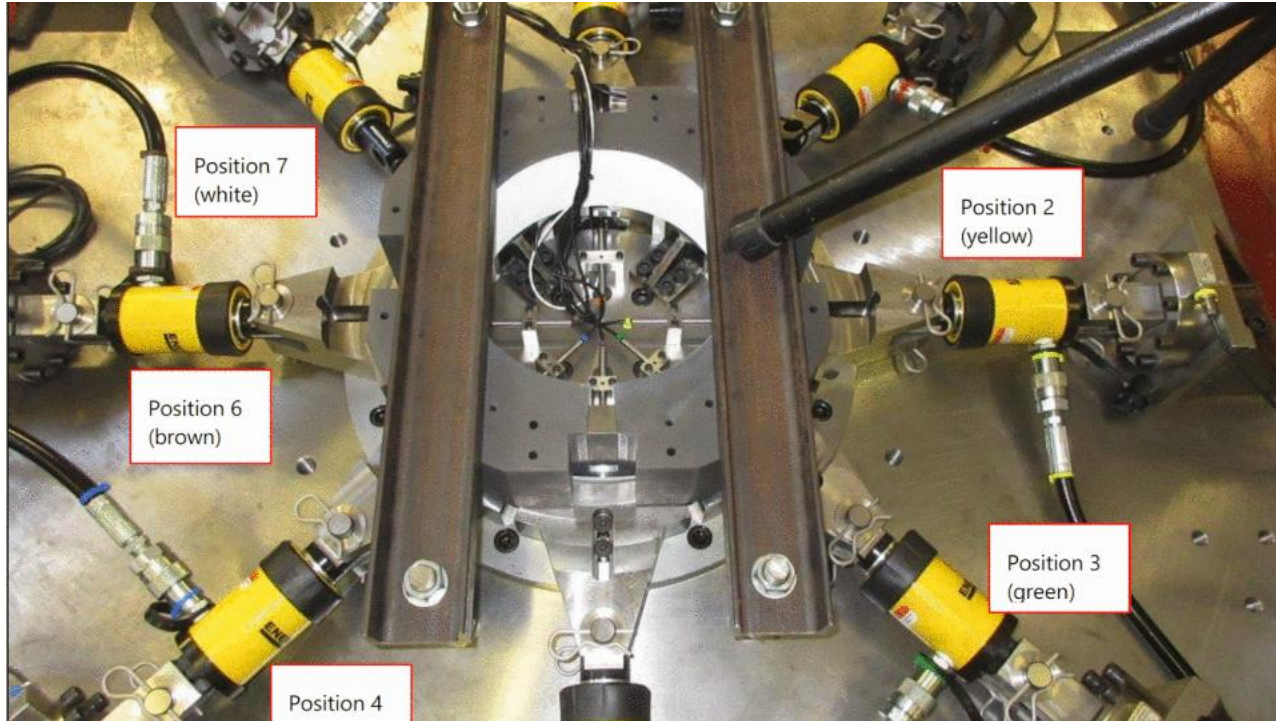


Experiment



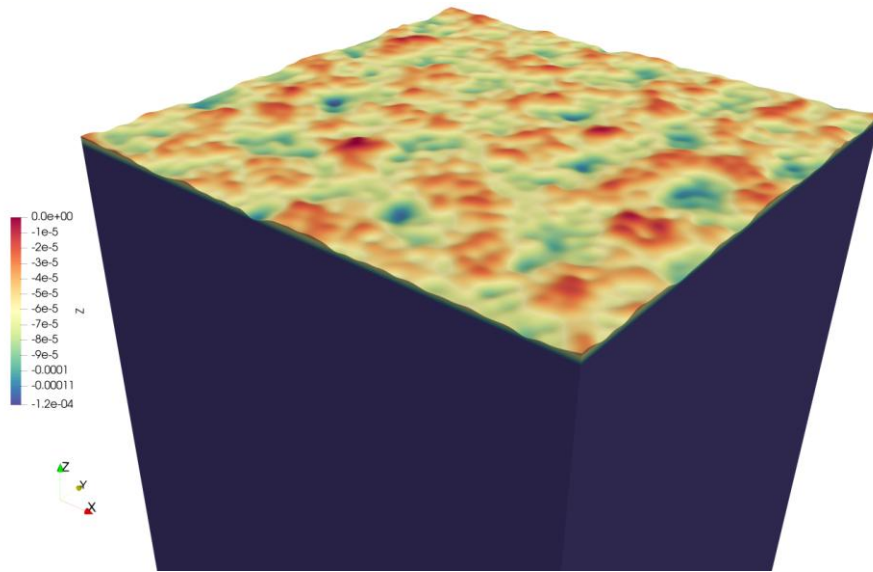


# Comparing rig test and simulation

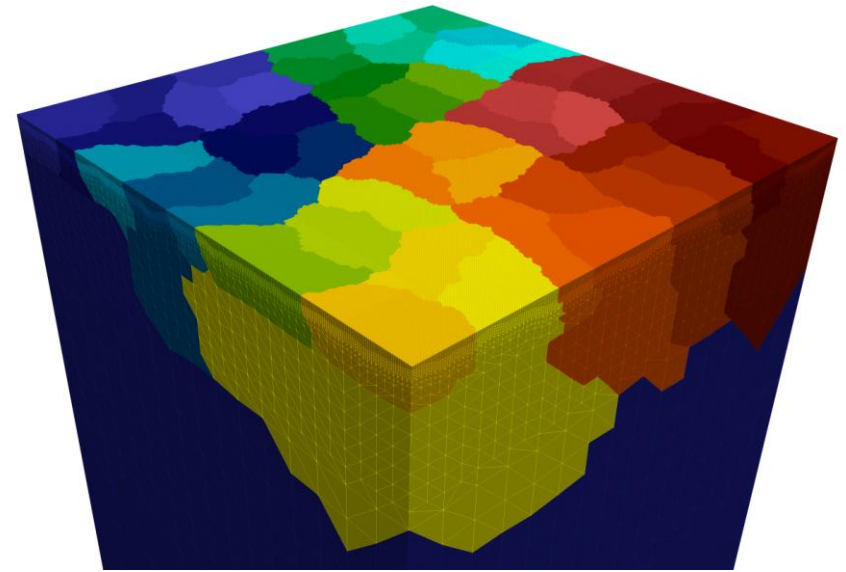




## Rough surface contact: FE mesh



Surface height projected on the mesh

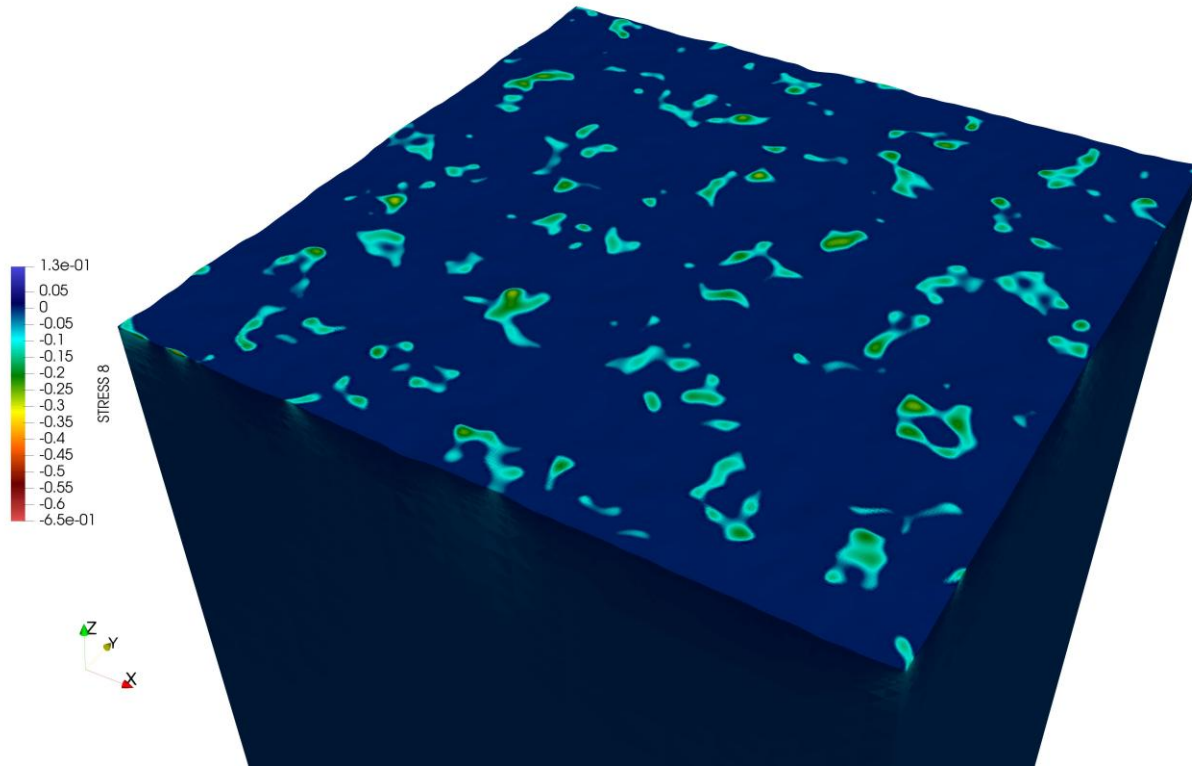


Mesh partitioned into 48 parts



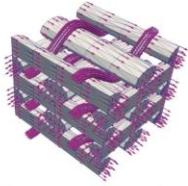


# Rough surface contact: normal traction

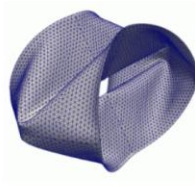




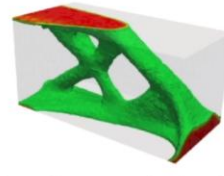
# Examples of user modules



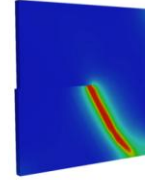
Homogenisation



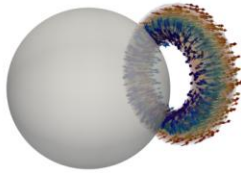
Solid shell



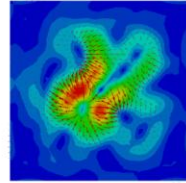
Topology optimisation



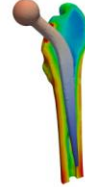
Phase field fracture



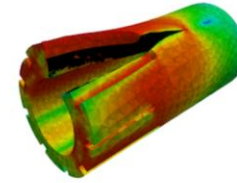
Navier-Stokes flow



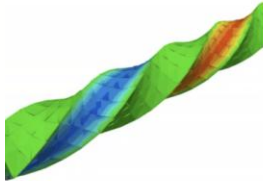
Cell traction microscopy



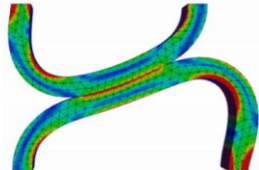
Bone remodelling



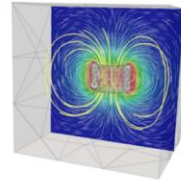
Configurational fracture



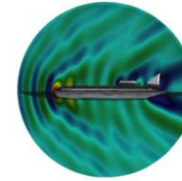
Plasticity



Mortar contact



Magnetostatics

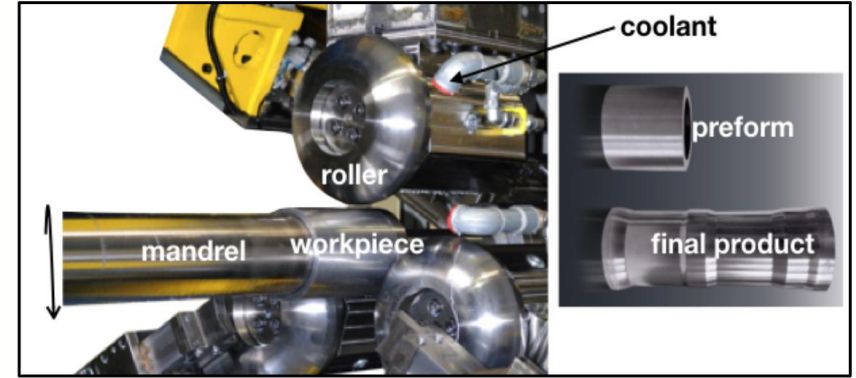


Acoustic wave propagation

# Multifield plasticity

$$\left\{ \begin{array}{ll} \frac{\partial \sigma_{ij}}{\partial x_j} - b_i = 0 & \forall x \in \Omega \\ \varepsilon_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \\ \sigma_{ij} = D_{ijkl} (\varepsilon_{kl} - \varepsilon_{kl}^p) \\ \dot{\varepsilon}_{kl}^p - \dot{\tau} \left( \frac{\partial f}{\partial \sigma_{kl}} \Big|_{(\sigma, \tau)} \right) = 0 \\ f(\sigma, \tau) \leq 0, \dot{\tau} \geq 0, \dot{\tau} f(\sigma, \tau) = 0 \\ u_i = \bar{u}_i & \forall x \in \partial\Omega_u \\ \sigma_{ij} n_j = \bar{t}_i & \forall x \in \partial\Omega_\sigma \\ \Omega_u \cup \Omega_\sigma = \Omega \\ \Omega_u \cap \Omega_\sigma = \emptyset \end{array} \right.$$

## Incremental cold flow forming



$$\left\{ \begin{array}{l} \left( \frac{\partial \delta u_i}{\partial x_j}, \sigma_{ij} \right)_\Omega - (\delta u_i, b_i)_\Omega - (\delta u_i, \bar{t}_i)_{\partial\Omega_\sigma} = 0 \\ (\delta \varepsilon_{kl}^p, D_{ijkl} (\dot{\varepsilon}_{kl}^p - \dot{\tau} A_{kl})) = 0 \\ \left( \delta \tau, c_n \dot{\tau} - \frac{1}{2} \{ c_n \dot{\tau} + (f(\boldsymbol{\sigma}, \tau) - \sigma_y) + \| c_n \dot{\tau} + (f(\boldsymbol{\sigma}, \tau) - \sigma_y) \| \} \right) = 0 \end{array} \right.$$

$$\begin{array}{l} \forall \delta u_i \in H^1(\Omega) \\ \forall \delta \varepsilon_{ij}^p \in L^2(\Omega) \cap \mathcal{S} \\ \forall \delta \tau \in L^2(\Omega) \end{array}$$



# Adding fields

```
//! [Set up problem]
MoFEMErrorCode Example::setupProblem() {
    MoFEMFunctionBegin;
    Simple *simple = mField.getInterface<Simple>();
    // Add field
    CHKERR simple->addDomainField("U", H1, AINSWORTH_LEGENDRE_BASE, 2);
    CHKERR simple->addDomainField("TAU", L2, AINSWORTH_LEGENDRE_BASE, 1);
    CHKERR simple->addDomainField("EP", L2, AINSWORTH_LEGENDRE_BASE, 3);
    CHKERR simple->addBoundaryField("U", H1, AINSWORTH_LEGENDRE_BASE, 2);
    CHKERR simple->setFieldOrder("U", order);
    CHKERR simple->setFieldOrder("TAU", order-1);
    CHKERR simple->setFieldOrder("EP", order-1);
    CHKERR simple->setUp();
    MoFEMFunctionReturn(0);
}
//! [Set up problem]
```

$u$

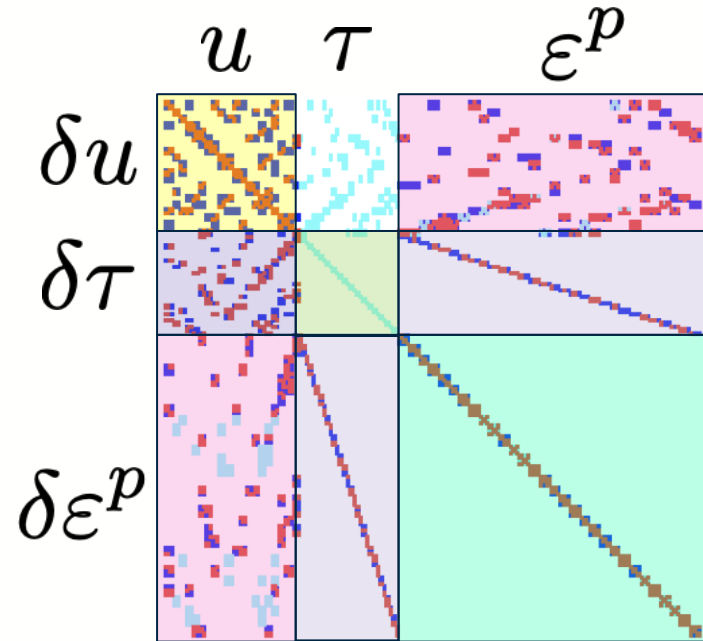
$\tau$

$\varepsilon^p$





# Matrix



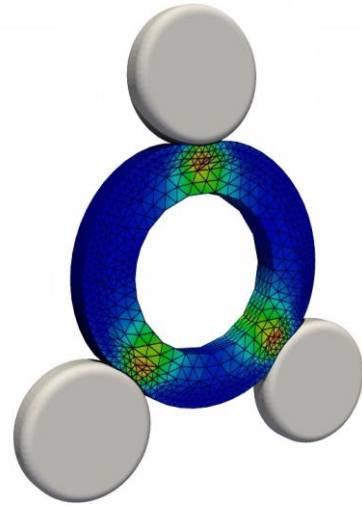
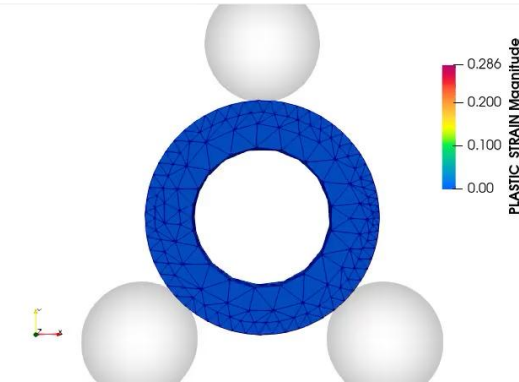
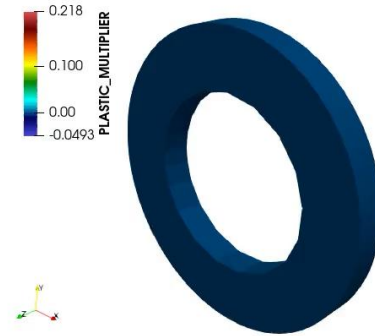
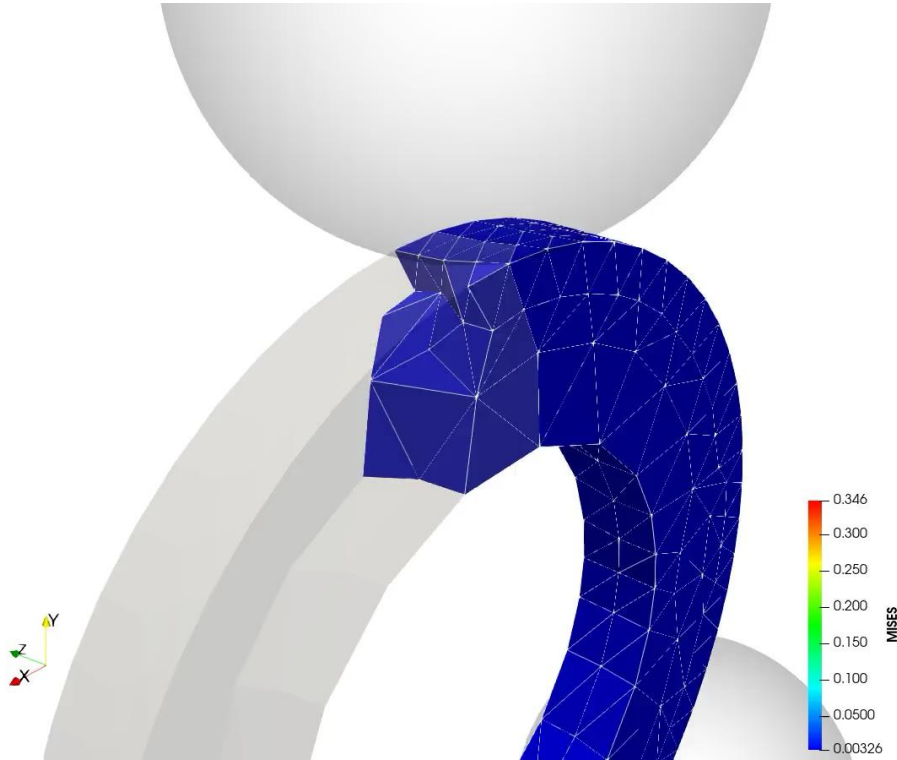
Conservation of linear momentum

Plastic constrains

Flow rule



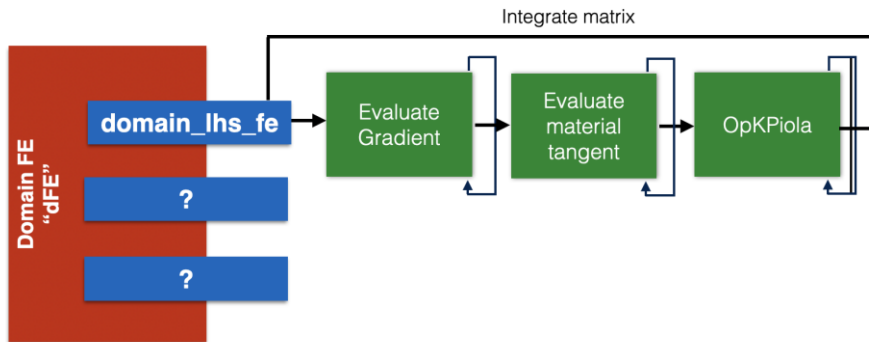
# Multifield plasticity



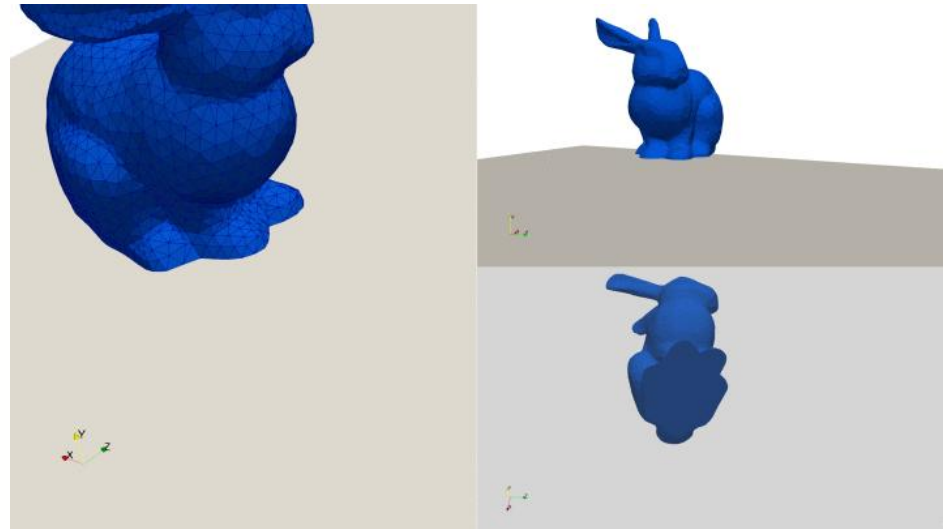


# Form integrators

```
// Only used with Henky/nonlinear material
using OpKPiola = FormsIntegrators<DomainEleOp>::Assembly<PETSC>::BiLinearForm<
    GAUSS>::OpGradTensorGrad<1, SPACE_DIM, SPACE_DIM, 1>;
using OpInternalForcePiola = FormsIntegrators<DomainEleOp>::Assembly<
    PETSC>::LinearForm<GAUSS>::OpGradTimesTensor<1, SPACE_DIM, SPACE_DIM>;
```



[http://mofem.eng.gla.ac.uk/mofem/html/tutorial\\_contact\\_problem.html](http://mofem.eng.gla.ac.uk/mofem/html/tutorial_contact_problem.html)





# MFront integration module installation



Spack

Install spack:

```
git clone https://github.com/lorak41/spack.git
```

Install MoFEM + MFront:

```
spack install mofem-cephas+mgis
```

Download MFront integration module into MoFEM

```
cd $MOFEM_INSTALL_DIR/mofem-cephas/mofem/users_modules
```

```
git clone git@bitbucket.org:karol41/um_mfront_interface.git mfront_interface
```

Configure new user module in your build

```
cd $MOFEM_INSTALL_DIR/users_modules_build
```

```
export MGIS_PATH=$(spack find -l --path mgis | awk 'END{print}' | awk 'NF{ print $NF }')"/lib"
```

```
touch CMakeCache.txt
```

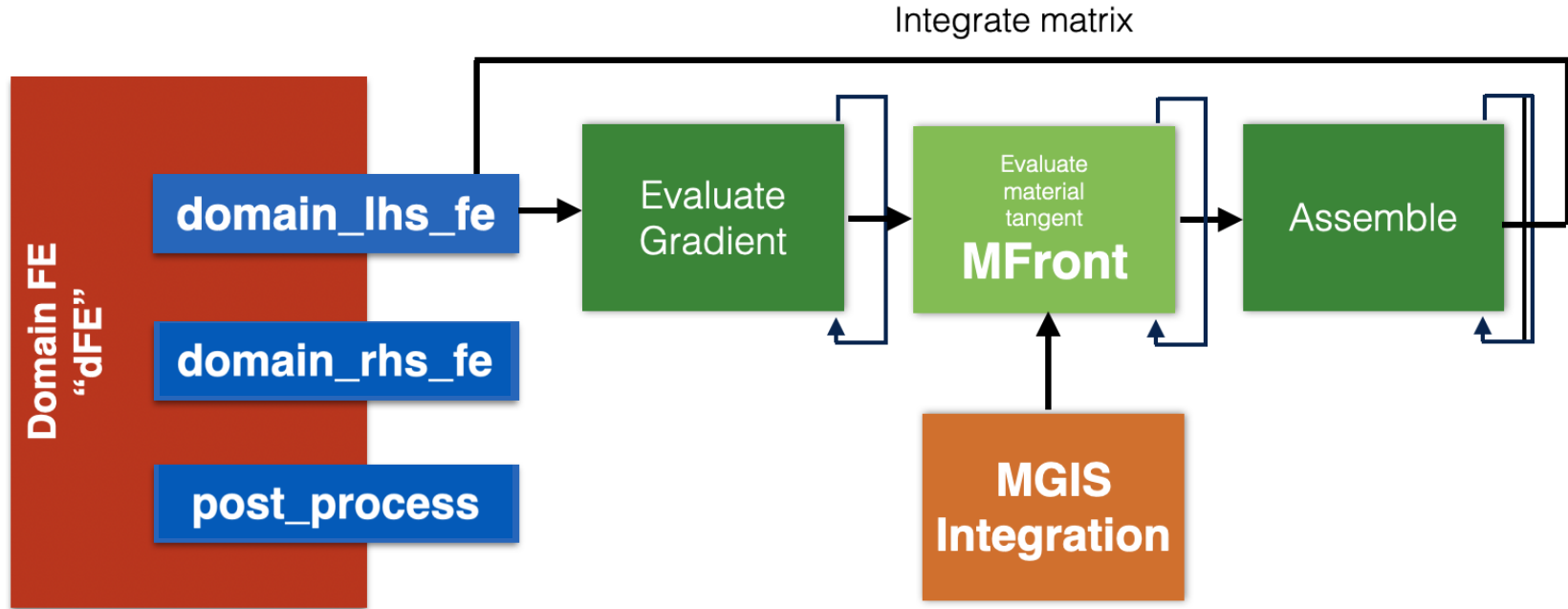
```
./spconfig -DMGIS_PATH=$MGIS_PATH
```

```
make -j4
```





# MFront Integration Pipelines





# MFront integration Pre-processing



Boundary conditions:

Force, pressure, displacement, rotation,  
temperature etc.

Block id: **1**

name: **MATERIAL1**

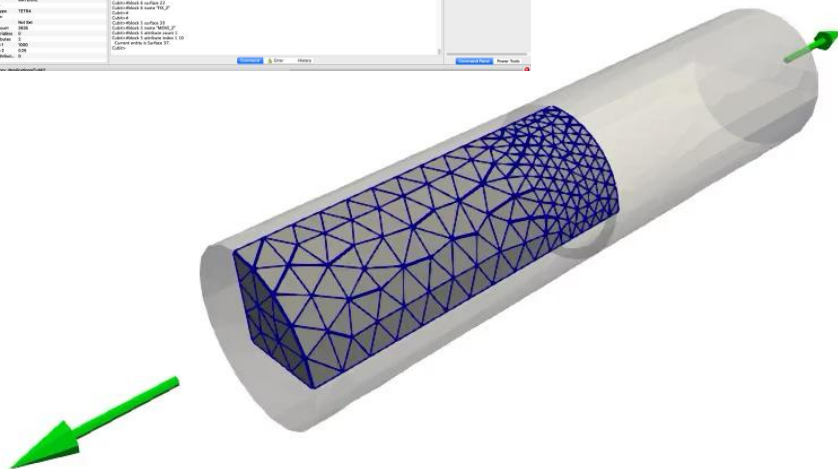
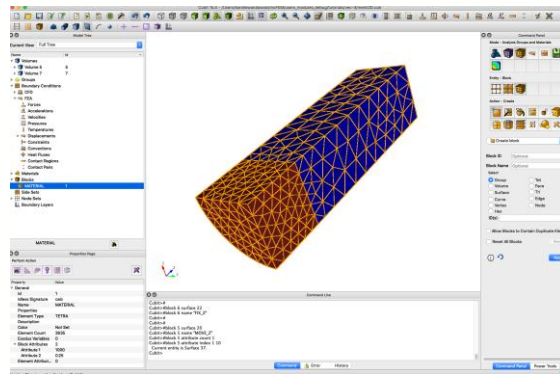
optional:

param 1: 230e6

param 2: 0.3

...

param n:



C. Miehe, N. Apel, M. Lambrecht (2002)

Anisotropic additive plasticity in the logarithmic strain space. Modular kinematic formulation and implementation based on incremental minimization principles for standard materials



# Logarithmic Strain Plasticity Behaviour

```
@DSL Implicit;  
@Behaviour LogarithmicStrainPlasticity;  
@Author Thomas Helfer/Jérémy Bleyer;  
@StrainMeasure Hencky;
```

```
@Algorithm NewtonRaphson;  
@Epsilon 1.e-14;  
@Theta 1;
```

```
@MaterialProperty stress s0;  
s0.setGlossaryName("YieldStress");  
@MaterialProperty stress H0;  
H0.setEntryName("HardeningSlope");  
@MaterialProperty real Rult;  
Rult.setEntryName("UltimateStrength");  
@MaterialProperty real be;  
be.setEntryName("HardeningExponent");
```

```
@Brick StandardElastoViscoPlasticity{  
  stress_potential: "Hooke" {  
    young_modulus: 206913,  
    poisson_ratio: 0.29  
  },  
  inelastic_flow: "Plastic" {  
    criterion: "Mises",  
    isotropic_hardening: "Linear" {R0: s0, H: H0},  
    isotropic_hardening: "Voce" {R0: 0, Rinf: Rult, b: be}  
  }  
};
```



# MFront integration Analysis execution

Command line:

```
./compile_behaviours.sh LogarithmicStrainPlasticityMiehe.mfront
```

```
#!/bin/bash  
mfront --obuild --interface=generic "$@"
```

Saves material library by default into:

src/libBehaviour.so

Run MoFEM/MFront analysis:

```
./mfront_interface -file_name necking_mesh.h5m \  
-block_1 LogarithmicStrainPlasticity \  
-lib_path_1 src/libBehaviour.so \ #not necessary  
-param_1_0 450 -param_1_1 129 \  
-param_1_2 265 -param_1_3 16.93 \  
-load_history load_history.in \  
-order 2 -ts_dt 0.01
```

```
LogarithmicStrainPlasticity behaviour loaded on block 1.  
Finite Strain Kinematics  
Internal variables:  
: ElasticStrain  
: EquivalentPlasticStrain  
External variables:  
: Temperature  
Material properties:  
0 : YieldStrength = 450.  
1 : HardeningSlope = 130.  
2 : UltimateStrength = 265.  
3 : HardeningExponent = 17.
```

Remaining  
parameters:

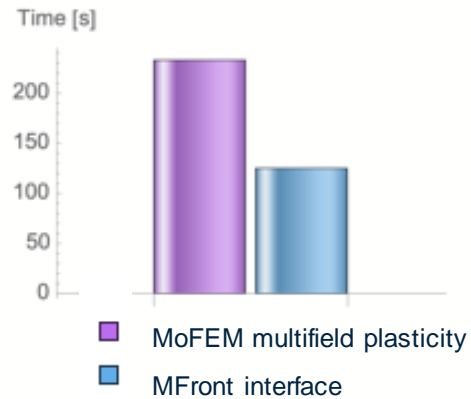
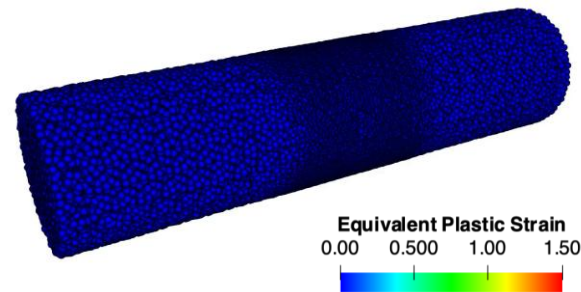
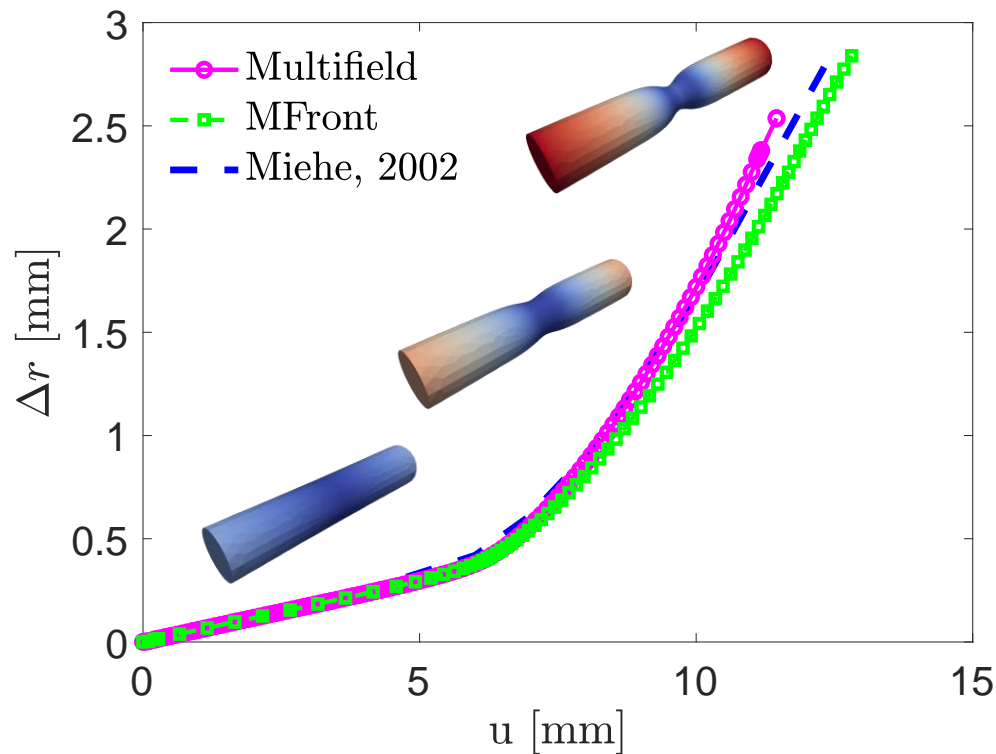


.petscsrc



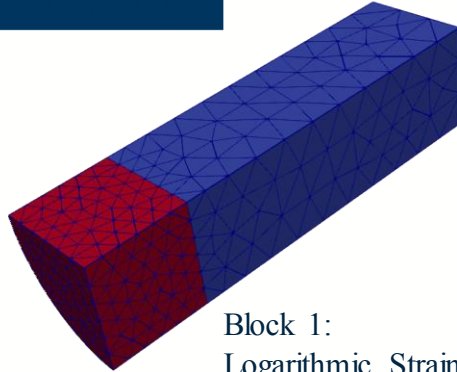


# Example results





# Example with multiple blocks



Block 1:  
Logarithmic Strain  
Plasticity

Block 2:  
SaintVenant Kirchhoff  
Elasticity

Define on the mesh:

Block id: **1**

name: **MATERIAL1\_PLASTIC**

Block id: **2**

name: **MATERIAL2\_ELASTIC**

```
./compile_behaviours.sh LogarithmicStrainPlasticityMiehe.mfront SaintVenantKirchhoffElasticity.mfront
```

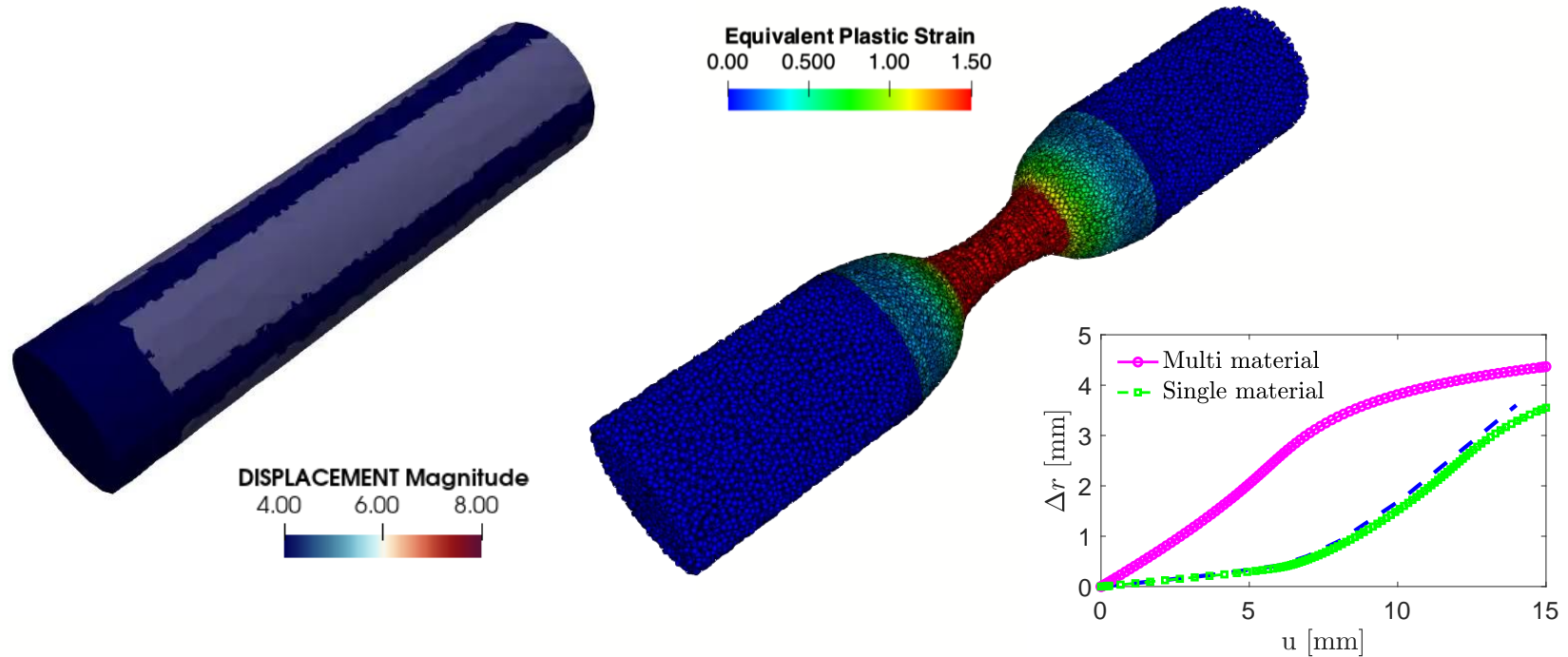
Run MoFEM/MFront analysis:

```
./mfront_interface -file_name necking_mesh2.h5m \  
-block_1 LogarithmicStrainPlasticity \  
-param_1_0 450 -param_1_1 129 -param_1_2 265 -param_1_3 16.93 \  
-block_2 SaintVenantKirchhoffElasticity \  
-param_2_0 2e6 -param_2_1 0.3 \  

```



# Example with multiple blocks



# Summary

## MFront user module:

- Generic, parallel and flexible implementation
- Arbitrary and heterogeneous order of approximation
- Supports both small and large strains behaviours





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**Thank you!**

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