Your name is:

Please circle your recitation:

1)	M2	2-131	Holm	2-181	3-3665	tsh@math
2)	M2	2-132	Dumitriu	2-333	3-7826	dumitriu@math
3)	M3	2-131	Holm	2-181	3-3665	tsh@math
4)	T10	2-132	Ardila	2-333	3-7826	fardila@math
5)	T10	2-131	Czyz	2-342	3-7578	czyz@math
6)	T11	2-131	Bauer	2-229	3-1589	bauer@math
7)	T11	2-132	Ardila	2-333	3-7826	fardila@math
8)	T12	2-132	Czyz	2-342	3-7578	czyz@math
9)	T12	2-131	Bauer	2-229	3-1589	bauer@math
10)	T1	2-132	${\bf Ingerman}$	2-372	3-4344	ingerman@math
11)	T1	2-131	Nave	2-251	3-4097	nave@math
12)	T2	2-132	${\bf Ingerman}$	2-372	3-4344	ingerman@math
13)	T2	1-150	Nave	2-251	3-4097	nave@math

1 (30 pts.) Suppose the matrix A has reduced row echelon form R:

$$A = \left[egin{array}{ccccc} 1 & 2 & 1 & b \ 2 & a & 1 & 8 \ & ({
m row} & 3) \end{array}
ight], \quad R = \left[egin{array}{cccc} 1 & 2 & 0 & 3 \ 0 & 0 & 1 & 2 \ 0 & 0 & 0 & 0 \end{array}
ight]$$

- What can you say immediately about row 3 of A?
 - What are the numbers a and b?
 - (c) Describe all solutions of Rx = 0. Circle the spaces that are the same for A as for R: (row space)(column space)(null space).

- 2 (30 pts.) Find the number c that makes this matrix singular (not invertible):

$$A = \left[\begin{array}{ccc} 1 & 2 & 3 \\ 1 & 5 & 6 \\ 2 & 6 & c \end{array} \right]$$

- (b) If c = 20 what are the column space C(A) and the nullspace N(A)? Describe them in this specific case (not just repeat their definitions). Also describe $C(A^{-1})$ and $N(A^{-1})$ for the inverse matrix!
- With c=20 factor the matrix into A=LU (lower triangular L and upper triangular U).

3 (40 pts.) Suppose A is an m by n matrix of rank r.

If Ax = b has a solution for every right side b, what is the column space of A?

(b) In part (a), what are all equations or inequalities that must hold between the numbers m, n, and r.

c) Give a specific example of a 3 by 2 matrix A of rank 1 with first row [2 5]. Describe the column space C(A) and the nullspace N(A) completely.

Suppose the right side b is the same as the first column in your example (part c). Find the complete solution to Ax = b.