Problem 1.72. Let M_1 and M_2 be DFAs that have k_1 and k_2 states, respectively, and then let $U = L(M_1) \cup L(M_2)$. **Part a.** Show that if $U \neq \phi$, then U contains some string s, where $|s| < max(k_1, k_2)$.

Proof. Solution Replace this text with the details of your proof or solution. **Part b.** Show that if $U \neq \Sigma^*$, then U excludes some string s, where $|s| < k_1k_2$.

Proof. Solution Replace this text with the details of your proof or solution.