

**Problem 7.33.** In the following solitaire game, you are given an  $m \times m$  board. On each of its  $m^2$  positions lies either a blue stone, a red stone, or nothing at all. You play by removing stones from the board until each column contains only stones of a single color and each row contains at least one stone. You win if you achieve this objective. Winning may or may not be possible, depending upon the initial configuration. Let  $SOLITAIRE = \{\langle G \rangle \mid G \text{ is a winnable game configuration}\}$ . Prove that  $SOLITAIRE$  is NP-complete.

*Proof.* Try this... Reduce 3COLOR SOLITAIRE - Number of nodes  $v$  in graph  $G$  maps to  $m - v$  x  $v$  gives a grid which resembles an adjacency matrix of  $G$  - Color of stones in a columns gives the color of nodes of  $G$  - blue stone = color 1 - red stone = color 2 - empty column = color 3  $\square$