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PART A: RMSSE between Noiseless and Noisy image

```
load('.../data/assignmentImageDenoisingPhantom.mat');
disp('RRMSE between Noiseless and noisy image');
disp(rrmse(imageNoiseless,imageNoisy));

RRMSE between Noiseless and noisy image
    0.4584
```

PART B: 1. Quadratic prior

```
y=imageNoisy;
x=y;
alpha=1;
 step=0.001;
prev rrmse=100;
obj fun quadratic=[];
while(abs(rrmse(imageNoiseless,x)-prev_rrmse)>0.000001)
                prev_rrmse=rrmse(imageNoiseless,x);
                 grad_prior=2*((x-circshift(x,1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circshift(x,-1,1))+(x-circ
 circshift(x,1,2))+(x-circshift(x,-1,2)));
                grad=2*(1-alpha)*(x-y)+alpha*grad prior;
                x=x-step*grad;
                 %disp(rrmse(imageNoiseless,x));
                 obj_fun_quadratic=[obj_fun_quadratic prev_rrmse];
denoised_quadratic_image=x;
disp('RRMSE for alpha=1:');
disp(rrmse(imageNoiseless,x));
disp('Since alpha=1, 1.2*1 will be outside the limits');
disp('Hence RRMSE(1.2*alpha*)=');
disp(rrmse(imageNoiseless,x));
 RRMSE for alpha=1:
                 0.2279
```

```
Since alpha=1, 1.2*1 will be outside the limits
Hence RRMSE(1.2*alpha*)=
0.2279
```

PART B: 2. Huber prior

```
alpha=1;
gamma=0.007;
disp('alpha_optimum:')
disp(alpha)
disp('gamma_optimum:')
disp(gamma)
x=imageNoiseless;
y=imageNoisy;
[denoised_huber_image,rrmse,obj_fun_huber]=huber(x,y,alpha,gamma);
disp('For alpha=1 and gamma=0.007, RRMSE(alpha*,gamma*)=');
disp(rrmse);
disp('Since alpha=1, 1.2*1 will be outside the limits');
disp('Hence RRMSE(1.2*alpha*,gamma*)=');
disp(rrmse);
disp('For alpha=0.8*1=0.8 and gamma=0.007,
 RRMSE(0.8*alpha*,gamma*)=0.2776');
disp('For alpha=1 and gamma=1.2*0.007=0.0084,
 RRMSE(alpha*,1.2*gamma*)=0.0705');
disp('For alpha=1 and gamma=0.8*0.007=0.0056,
 RRMSE(alpha, 0.8*gamma*) = 0.0651');
disp('Thus values of alpha and gamma are optimum at 1 and 0.007
 respectively');
alpha_optimum:
gamma_optimum:
    0.0070
For alpha=1 and gamma=0.007, RRMSE(alpha*,gamma*)=
    0.0688
Since alpha=1, 1.2*1 will be outside the limits
Hence RRMSE(1.2*alpha*,gamma*)=
    0.0688
For alpha=0.8*1=0.8 and gamma=0.007, RRMSE(0.8*alpha*, gamma*)=0.2776
For alpha=1 and gamma=1.2*0.007=0.0084,
 RRMSE(alpha*,1.2*gamma*)=0.0705
```

PART B: 3. Discontinuity adaptive prior

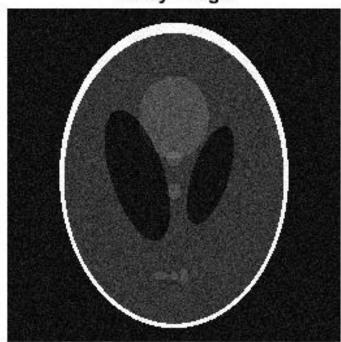
```
alpha=1;
gamma=0.0001;
disp('alpha:')
disp(alpha)
disp('gamma:')
disp(gamma)
x=imageNoiseless;
y=imageNoisy;
[denoised_discontinuity_adaptive_image,rrmse,obj_fun_discontinuity_adaptive]=disco
disp('For alpha=1 and gamma=0.0001, RRMSE(alpha*,gamma*)=');
disp(rrmse);
disp('Since alpha=1, 1.2*1 will be outside the limits');
disp('Hence RRMSE(1.2*alpha*,gamma*)=');
disp(rrmse);
disp('For alpha=0.8*1=0.8 and gamma=0.0001,
 RRMSE(0.8*alpha*,gamma*)=0.4555');
disp('For alpha=1 and gamma=1.2*0.0001=0.0012,
 RRMSE(alpha*,1.2*gamma*)=0.0545');
disp('For alpha=1 and gamma=0.8*0.0001=0.00008,
 RRMSE(alpha, 0.8*gamma*) = 0.0542');
disp('Thus values of alpha and gamma are optimum at 1 and 0.0001
 respectively');
alpha:
     7
gamma:
   1.0000e-04
For alpha=1 and gamma=0.0001, RRMSE(alpha*,gamma*)=
    0.0542
Since alpha=1, 1.2*1 will be outside the limits
Hence RRMSE(1.2*alpha*,gamma*)=
    0.0542
For alpha=0.8*1=0.8 and gamma=0.0001, RRMSE(0.8*alpha*,gamma*)=0.4555
For alpha=1 and gamma=1.2*0.0001=0.0012,
 RRMSE(alpha*,1.2*gamma*)=0.0545
For alpha=1 and gamma=0.8*0.0001=0.00008,
 RRMSE(alpha, 0.8*gamma*)=0.0542
```

Thus values of alpha and gamma are optimum at 1 and 0.0001 respectively

PART C: Image plotting

```
figure; imshow(abs(imageNoisy)); title('Noisy Image');
figure; imshow(imageNoiseless); title('Noiseless Image');
figure;imshow(abs(denoised_quadratic_image)); title('Quadratic MRF Denoised Image');
figure;imshow(abs(denoised_huber_image)); title('Huber MRF Denoised Image');
figure;imshow(abs(denoised_discontinuity_adaptive_image)); title('Discontinuity Adaptive MRF Denoised Image');
```

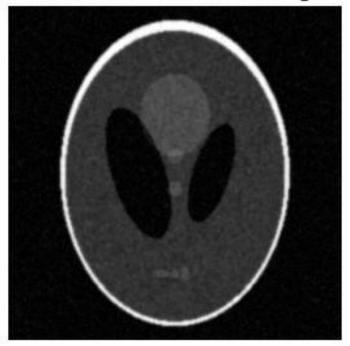




Noiseless Image



Quadratic MRF Denoised Image



Huber MRF Denoised Image



Discontinuity Adaptive MRF Denoised Image

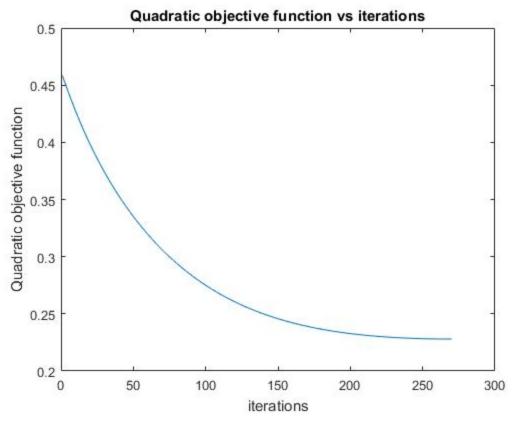


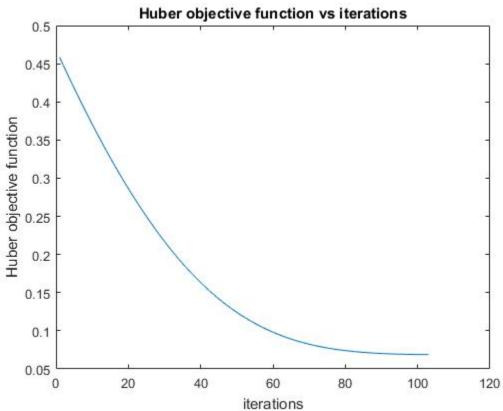
PART D: Objective function vs iteration

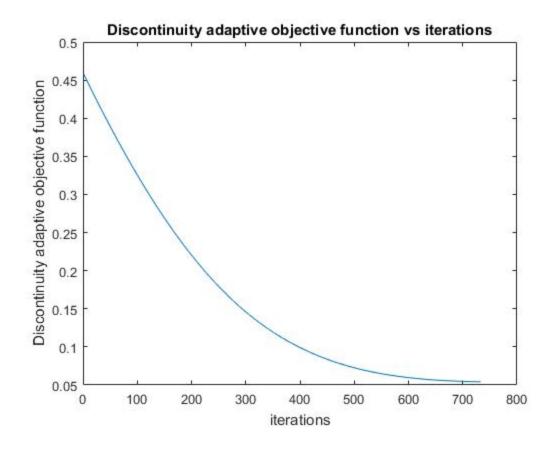
```
figure; plot(obj_fun_quadratic); title('Quadratic objective function
  vs iterations'); xlabel('iterations'); ylabel('Quadratic objective
  function');

figure; plot(obj_fun_huber); title('Huber objective function
  vs iterations'); xlabel('iterations'); ylabel('Huber objective
  function');

figure; plot(obj_fun_discontinuity_adaptive); title('Discontinuity
  adaptive objective function vs iterations'); xlabel('iterations');
  ylabel('Discontinuity adaptive objective function');
```







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