

Today's Agenda :-

Will start at

9:05 PM

- 1) Imp Announcement
- 2) Count of Pairs "ag"
- 3) No of Leaders in an array
- 4) Intro to Subarrays
- 5) Smallest Subarray containing min & max of array

Q1) Given a String s of lowercase characters. Return the count of pairs (i, j) such that $i < j$ & $s[i] = 'a'$ & $s[j] = 'g'$.

Eg Str: "abegag" (0, 5)
(4, 5)
(0, 3)

Eg Str: "acgdgag" i j
0 2
0 4
0 6
5 6 } ans = 4

Eg Str: "bcagggaag" i j
2 3
2 4
2 7
5 7
6 7 } ans = 5

Brute force:-

```

int cnt = 0
for(int i = 0; i < N; i++) {
    if (s[i] == 'a') {
        for(int j = i+1; j < N; j++) {
            if (s[j] == 'g') {
                cnt++;
            }
        }
    }
}

```

$\boxed{i < N-1}$
 str 0 1 2 3 4 5 }
 g g a g a a }
 $\nearrow 0, N-1$
 s[i]

TC: $O(N^2)$
 SC: $O(1)$

Observation :-

For every 'a', we are counting 'g' on right side

Eg

	0	1	2	3	4	5	6	7	8
str:	a	d	g	a	g	a	g	f	g
	\downarrow			\downarrow		\downarrow			
	i=0	—————							cnt = 4
				i=3	—————			cnt = 3	
						i=5	—————		cnt = 2
									<u>ans = 9</u>

\leftarrow Right to left
 maintaining count of g

Eg	a	d	g	a	g	a	g	f	g	ans = 0 cnt_g = 0
	ans = ans + cnt_g		cnt_g = 4	ans = ans + cnt_g	cnt_g = 3	ans = ans + cnt_g ans = 2	cnt_g = 2			cnt_g = cnt_g + 1 cnt_g = 1
	ans = 9			ans = 5						

```
int ans = 0, cnt_g = 0
```

```
for(int i = N-1; i >= 0; i--) {
```

```
    if (str[i] == 'g') {
```

```
        cnt_g++
```

```
    }
```

```
    else if (str[i] == 'a') {
```

```
        ans = ans + cnt_g
```

```
    }
```

```
}
```

```
return ans
```

TC : O(N)
SC : O(1)

a []
[] g

TODO: Try going from left to right

Hint : You have to maintain cnt_a



Q2) Given an array of size N . Count the no of leaders.

Leader: An element strictly greater than all elements on the right side.

Eg $ar[]: \{2, 5, 3, 4, 17, 16\}$ } ans = 2 ✓

Eg $ar[]: \{2, 5, 4, 3, 2, 1\}$ } ans = 5

Eg $ar[]: \{10, 8, 8\}$ } ans = 2 ✓

BF: For every element at i^{th} index, if all elements on right side are less than $ar[i]$, then i^{th} element will be a leader.

```
int leaders = 1
```

```
for (int i = 0; { i <= N-2  
                OR  
                i < N-1 } i++) {  
    bool flag = true  
    for (int j = i+1; j < N; j++) {  
        if (ar[j] > ar[i]) {  
            flag = false, break;  
        }  
    }  
    if (flag == true) { leaders++; }  
}  
return leaders
```

TC: $O(N^2)$

SC: $O(1)$

Optimisation :-

- 1) For every element, we are considering all elements on right
- 2) Scan all elements from $R \rightarrow L$ & maintain track of max till now

i
 $0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7$
 $ar[]: \{ 7 \quad 13 \quad 2 \quad 9 \quad 12 \quad 6 \quad 8 \quad 4 \}$

$last_max = 4$

$cnt = 1$

$i \quad ar[i] \quad last_max \quad \text{count of leaders}$

6 8 ~~4~~ 8 2

5 6 8 2

4 12 ~~8~~ 12 3

3 9 12 3

2 2 12 3

1 13 ~~12~~ 13 4

0 7 13 4

$cnt = 4$

$int \quad leaders = 1$

$int \quad last_max = ar[N-1]$

$for(int \quad i = N-2; \quad i \geq 0; \quad i--) \{$

$if(ar[i] > last_max) \{$

$leaders++$

$last_max = ar[i]$

$\}$

$\}$

$return \quad leaders$

$TC: O(N)$

$SC: O(1)$

Subarray:- Commonly defined as part / section of an array which consist of contiguous elements of array.

Eg :- $arr[] : \{ 1, 5, 2, 3, 6, 8, 4 \}$
 $[5, 2, 3, 6] : [s \ e]$

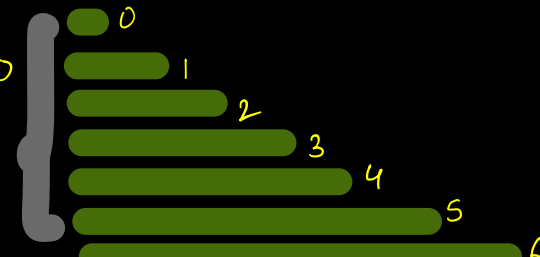
Subarray $[s, e] : l - s + 1 \rightarrow \text{length of subarray}$
 $\hookrightarrow s \leq e$

• $[1, 1]$

- A single element is a subarray : 1 2, 3, 4 ...
- An entire array is also a subarray : N

Eg $arr[] : \{ 4, 2, 10, 3, 12, -2, 15 \}$

Start: 0
 $[4]$
 $[4 \ 2]$



$[4, 2, 10]$

$[4, 2, 10, 3]$

$[4, 2, 10, 3, 12]$

$[4, 2, 10, 3, 12, -2]$

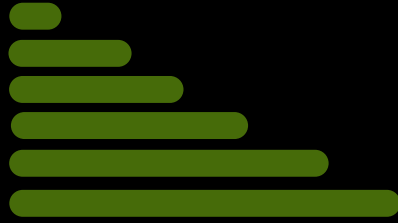
$[4, 2, 10, 3, 12, -2, 15]$

subarrays

starting from 0 : 7

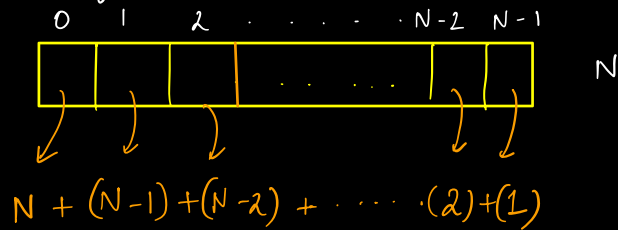
arr[] : { 4, 2, 10, 3, 12, -2, 15 }

Start : 1



} # Subarrays starting from 1: 6

Total No of subarrays for a given array of size N :-



Sum of N Natural Nos

$$\# \text{ of Subarrays} = \frac{N(N+1)}{2}$$

Break for 7 Min

Relax, Have some water !

Contest : Online coding assessment / challenge

↳ 11th Aug (Friday) : 1st Contest }

Syllabus : Arrays + TC }

↳ 9:PM - 10:30PM (90 min) → 3 Coding Ques

10:30 PM - Contest Discussion ✓

- ↓
- 1) Attend session
 - 2) Solve assignments

Q3) Given an array of size N. Return the length of the **smallest subarray** which contains both **maximum & minimum element** of the array.

Eg $arr[] : \{ 2, 2, 6, 4, 5, 1, 5, 2, 6, 4, 1 \}$

$\left. \begin{array}{l} \text{min_ele} = 1 \\ \text{max_ele} = 6 \end{array} \right\} \begin{array}{l} \text{start} \quad \text{end} \\ [8, 10] : \underline{3 \text{ ans}} \end{array}$

$arr[] : \{ 1, 2, 3, 1, 3, 4, 6, 4, 6, 3 \}$

 $[0, 8] : 9$

$\left. \begin{array}{l} \text{min_ele} = 1 \\ \text{max_ele} = 6 \end{array} \right\} \begin{array}{l} \text{start} \quad \text{end} \\ [3, 6] : 6 - 3 + 1 : \boxed{4 = \text{ans}} \end{array}$

Eg : $arr[] : \{ 8, 8, 8, 8, 8 \}$

$\begin{array}{l} \text{min_ele} = 8 \\ \text{max_ele} = 8 \end{array} \quad \begin{array}{l} [0, 0] \checkmark \boxed{\text{len} = 1} \checkmark \\ [1, 1] - \uparrow \\ [2, 2] - \uparrow \end{array}$

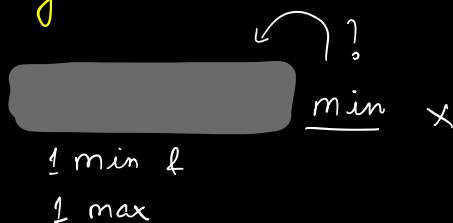
BF: for all subarrays that exist, find the smallest len which contains both min & max.

→ Next class: Subarrays

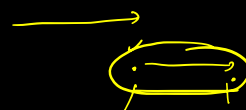
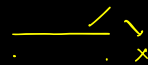
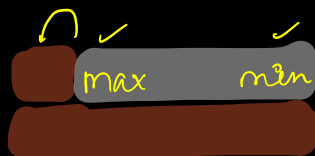
→ TC: $O(N^3)$
SC: $O(1)$

Observations :- Ans subarray

1) final ans subarray should contain 1 min & 1 max



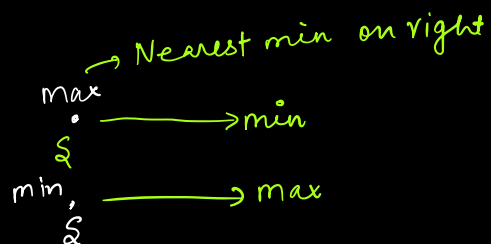
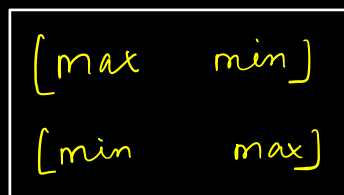
2) Max & Min should be only on corners



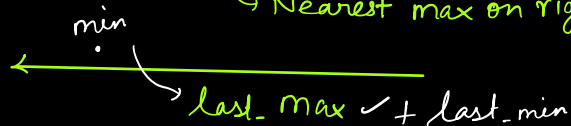
→ ans subarray

3) Case I

Case II



→ Nearest max on right



Eg arr[]: { 2, 2, 6, 4, 5, 1, 5, 2, 6, 4, 1 }

ans = N

min_ele = 1
max_ele = 6
last_min = 5
last_max = 8

0	1	2	3	4	5	6	7	8	9	10
2	2	6	4	5	1	5	2	6	4	1
		last_max = 2 [2, 5]: 4 ans = 3			last_min = 5 [5, 8]: 4 ans = 3			last_max = 8 [8, 10]: 3 ans = 3		
								last_min = 10		

ans = 3

```
int min_ele
int max_ele
int last_min_i = -1
int last_max_i = -1
int ans = N
```

TC: O(N)
SC: O(1)

if (min_ele == max_ele) return 1
// iterate & find min_ele & max_ele of array

for (int i = N-1; i >= 0; i--) {

if (arr[i] == min_ele) {

last_min_i = i

// [i last_max_i] : possible Candidate

if (last_max_i != -1) {

int len = last_max_i - i + 1
if (len < ans) { ans = len }

}

[s e]
e - s + 1

i_{th} → last_max_i
min_ele →

```

if (arr[i] == max_ele) {
    last_max_i = i
    // s e [i ... last_min_i] : possible candidate
    if (last_min_i != -1) {
        int len = last_min_i - i + 1 ✓
        if (len < ans) { ans = len }
    }
}
}
return ans

```

^s ^e
 (ith → last_min_i)
 max_ele

Eg :-

	0	1	2	3	4	5	6	7
L	5	4	3	1	2	6	8	3

i = 3

{ min_ele = 1
 max_ele = 8
 last_max_i = 6
 last_min_i = 3

[1 ... 8]
 [3 6] ✓ [8 ... L]

Eg

arr[] :	0	1	2
	8	8	8

min = 8
 max = 8
 last_max = 1
 last_min = -1

last_min : last_min = 2

Next class :-

Subarrays

Agenda :- 1) Printing all Subarrays

2) Sum of all Subarrays in different ways $\rightarrow O(N)$ ✓

3) Contribution Technique } Very Important ✓

The concepts learned will be used throughout the course,
So requesting all to not miss the session !

Thank You 😊