

322. Coin Change

You are given an integer array `coins` representing coins of different denominations and an integer `amount` representing a total amount of money.

Return *the fewest number of coins that you need to make up that amount*. If that amount of money cannot be made up by any combination of the coins, return `-1`.

You may assume that you have an infinite number of each kind of coin.

Example 1:

Input: coins = [1,2,5], amount = 11

Output: 3

Explanation: $11 = 5 + 5 + 1$

Example 2:

Input: coins = [2], amount = 3

Output: -1

Example 3:

Input: coins = [1], amount = 0

Output: 0

Constraints:

- $1 \leq n \leq 12$
- $1 \leq coins_i \leq 2^{31} - 1$
- $0 \leq amount \leq 10^4$

Solution

$$\begin{aligned}
 f(0) &= 0, \\
 f(a) &= \min_{c \in \text{coins}} (1 + f(a - c)) \text{ for } a > 0, \\
 f(a) &= \infty \text{ for } a < 0
 \end{aligned}$$

```

import math
class Solution:
    def rec(self, curr_amount, coins):
        if curr_amount < 0:
            return math.inf
        if curr_amount == 0:
            return 0
        return min([self.rec(curr_amount - coin, coins) + 1 for coin in coins])
    def coinChange(self, coins: List[int], amount: int) → int:
        ans = self.rec(curr_amount = amount, coins = coins)
        return ans if ans != math.inf else -1

```

$$f(a) = \begin{cases} M[a] & a \in M \\ 0 & a = 0 \\ \infty & a < 0 \\ \min_{c \in \text{coins}} (1 + f(a - c)) & \text{otherwise (store in } M[a] \text{)} \end{cases}$$

```

import math
class Solution:
    def mem(self, curr_amount, coins, d):
        if curr_amount < 0:
            return math.inf
        if curr_amount == 0:
            return 0
        if curr_amount not in d:
            d[curr_amount] = min([self.mem(curr_amount - coin, coins, d) +
                                  1 for coin in coins])
        return d[curr_amount]
    def coinChange(self, coins: List[int], amount: int) → int:

```

```

d = {}
ans = self.mem(curr_amount = amount, coins = coins, d = d)
return ans if ans != math.inf else -1

```

$$dp[i] = \min_{c \in \text{coins}, c \leq i} (dp[i - c] + 1), \quad \forall i \in [1, \text{amount}]$$

```

import math
class Solution:
    def tab(self, coins, amount):
        dp = [math.inf for _ in range(amount + 1)]
        dp[0] = 0
        for i in range(1, len(dp)):
            dp[i] = 1 + min([dp[i - coin] for coin in coins if i - coin >= 0],
                            default=math.inf)
        return dp[amount]
    def coinChange(self, coins: List[int], amount: int) → int:
        ans = self.tab(coins = coins, amount = amount)
        return ans if ans != math.inf else -1

```

Overnight

Your task is to calculate how many ways you can get the sum n by rolling the dice. Each roll of the dice produces a result between 1 and 6.

For example, if $n = 3$, the options are:

- $1 + 1 + 1$
- $1 + 2$
- $2 + 1$
- 3

Input

The input is a number, n : target amount.

Printout

Your program should print one integer: how many ways can you get the sum.

Bounds

- $1 \leq n \leq 50$

Example

Input:

```
3
```

Printout:

```
4
```

Solution

$$f(n) = \begin{cases} 1 & n = 0 \\ \sum_{n-d \geq 0} f(n-d) & n > 0 \end{cases}$$

```
n = int(input())
dice = [1,2,3,4,5,6]
def rec(n, dice):
    if n == 0:
        return 1
    return sum([rec(n - d, dice) for d in dice if n - d >= 0])
print(rec(n, dice))
```

$$f(n) = \begin{cases} 1 & n = 0 \\ M[n] & n \in M \\ \sum_{n-d \geq 0} f(n-d) & n \notin M \end{cases}$$

```
n = int(input())
dice = [1,2,3,4,5,6]
def mem(n, dice, M):
    if n == 0:
        return 1
    if n not in M:
        M[n] = sum([mem(n - d, dice, M) for d in dice if n - d >= 0])
    return M[n]
M = {}
print(mem(n, dice, M))
```

$$dp[n] = \begin{cases} 1 & n = 0 \\ \sum_{n-d \geq 0} dp[n-d] & n > 0 \end{cases}$$

```
n = int(input())
dice = [1,2,3,4,5,6]
def tab(n, dice):
    dp = [0 for _ in range(n + 1)]
    dp[0] = 1
    for i in range(1, len(dp)):
        dp[i] = sum([dp[i - d] for d in dice if i-d>=0])
    return dp[n]
print(tab(n, dice))
```