

POW(x,n) | Binary Exponentiation | Leetcode

Summary

The video presents a detailed explanation of implementing a function to calculate **x raised to the power n** (x^n), covering both brute force and optimized approaches, including handling edge cases such as negative exponents and integer overflow. The content is framed as part of a placement preparation series.

Core Concepts and Problem Statement

- The problem is to compute **power(x, n)** which returns x^n , where:
 - **x** can be any numeric type (integer, double).
 - **n** is an integer (positive, negative, or zero).
 - Important to confirm with the interviewer if **n** can be negative.
 - The function should handle various edge cases, particularly when **n** is negative or at the extreme limits of the integer range.
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Brute Force Approach

- Initialize **answer** as a double with value 1.
- Loop from 1 to **n** (if **n** is positive), multiplying **answer** by **x** in each iteration.
- If **n** is negative:
 - Calculate $x^{|n|}$ using the same loop.
 - Then return $\frac{1}{x^{|n|}}$.
- Edge case:
 - The absolute value of the minimum integer (e.g., -2147483648) cannot be stored in a positive integer variable due to overflow.
 - Use a larger data type such as **long** or **long long** to handle this safely.

- Time complexity: **O(n)**.
 - Space complexity: **O(1)**.
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Optimized Approach: Binary Exponentiation (Exponentiation by Squaring)

- Key insight:

For even powers:

$$x^n = (x \times x)^{n/2}$$

For odd powers:

$$x^n = x \times x^{n-1}$$

- Algorithm steps:
 - If **n** is even:
 - Square **x** (i.e., **x** \Rightarrow **x * x**).
 - Halve **n** (i.e., **n** \Rightarrow **n / 2**).
 - If **n** is odd:
 - Multiply **answer** by **x**.
 - Decrement **n** by 1 to make it even.
 - Stop when **n** reduces to zero.
 - When **n** is negative, convert it to positive (using a **long** to avoid overflow), apply the binary exponentiation, then take the reciprocal (1/**answer**).
 - Time complexity: **O(log n)**.
 - Space complexity: **O(1)**.
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Example Walkthrough: Calculating 2^{10}

Step	Operation	Explanation	Result
1	2^{10}	$2^{2 \times 5} = (2^2)^5$	4^5
2	4^5	4×4^4	4×256
3	4^4	$(4^2)^2 = 16^2$	256
4	16^2	16×16^1	16×16
5	16^1	16×16^0	16×1
6	16^0	Base case: 1	1
7	Calculated $4^4 = 256$	Multiply to get $4^5 = 4 * 256 = 1024$	1024
8	Final result: $2^{10} = 1024$		1024

Code Outline

- Initialize `answer = 1.0`.
- Store a copy of `n` in a larger integer type (`long`) to prevent overflow on negation.
- If `n` is negative, convert `n` to positive.
- Loop while `n > 0` :
 - If `n` is odd, multiply `answer` by `x` and decrement `n` by 1.
 - If `n` is even, square `x` and halve `n`.
- After loop ends:
 - If the original `n` was negative, return `1 / answer`.
 - Otherwise, return `answer`.

Key Insights

- **Handling negative exponents** requires taking the reciprocal after computing the positive power.
- **Integer overflow with negative minimum value** must be managed by using a wider data type (`long` or `long long`).

- **Binary exponentiation optimizes the power calculation** from $O(n)$ to $O(\log n)$ time.
 - The approach works for both integer and floating-point bases.
 - The base case of any number to the power 0 is always 1.
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Summary of Complexity

Approach	Time Complexity	Space Complexity	Notes
Brute force	$O(n)$	$O(1)$	Simple loop, inefficient for large n
Binary Exponentiation	$O(\log n)$	$O(1)$	Efficient, uses divide and conquer

Final Notes

- The video encourages viewers to like and share if they find the explanation helpful.
- Links to additional social platforms and groups are provided for further engagement.
- Future videos will continue exploring problems from the "sd sheet" for placement preparation.

This explanation ensures clarity on the power function implementation, covers edge cases, and provides optimal solutions suitable for technical interviews.

50. Pow(x, n)

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Implement $\text{pow}(x, n)$, which calculates x raised to the power n (i.e. x^n).

Example 1:

Input: $x = 2.00000$, $n = 10$

Output: 1024.00000

Example 2:

Input: $x = 2.10000$, $n = 3$

Output: 9.26100

Handwritten notes for Example 1:

Recursive formula: $x^n = \begin{cases} 1 & -n \\ \underbrace{x \times x}_{\text{ans}} & \text{if } n > 0 \end{cases}$

Calculation for 2^{10} :

$$\begin{aligned} 2^{10} &= (2 \times 2)^5 = (4)^5 = 1024 \quad (2^2)^5 \\ 4^5 &= 4 \times 4^4 = 4 \times 256 \\ 256 &= (4 \times 4)^2 = (16)^2 = 256 \\ 256^1 &= 256 \times (256)^0 \end{aligned}$$

Handwritten notes for Example 2:

Recursive formula: $x^n = \begin{cases} 1 & -n \\ \underbrace{x \times x}_{\text{ans}} & \text{if } n > 0 \end{cases}$

Calculation for 2.1^3 :

$$\begin{aligned} 2^3 &= (2 \times 2)^2 = (4)^2 = 16 \quad (2^2)^2 \\ 4^2 &= 4 \times 4^1 = 4 \times 2 = 8 \\ 2^1 &= (2 \times 2)^0 = 1 \\ 2.1^3 &= 2.1 \times (2.1^2) \end{aligned}$$

Final result: $2.1^3 \rightarrow 9.261$

Code

Recursive Solution

```
class Solution:  
    def rec(self,x,n):  
        if n==0:  
            return 1  
        p=self.rec(x,n//2)  
        return x*p*p if n%2 else p*p  
    def myPow(self,x:float,n:int)→float:  
        ans=self.rec(x,abs(n))  
        if n>0:  
            return ans  
        return 1/ans
```

Iterative Solution

```
class Solution:  
    def iter(self,x,n):  
        ans=1  
        N=n  
        n=abs(n)  
        while n:  
            if n%2:  
                ans=ans*x  
                n=n-1  
            else:  
                x=x*x  
                n=n//2  
        return ans  
    def myPow(self,x:float,n:int)→float:  
        ans=self.iter(x,abs(n))  
        if n>0:  
            return ans  
        return 1/ans
```

