

Report for ABS

- ABS are meant to control the wheel slip in order to maintain the friction coefficient close to the optimal value.
- wheel slip:- Relative motion between a wheel and the surface of the road, during vehicle movement.

Consider vehicle moving in a straight direction under braking conditions.

so for horizontal direction

$$F_f = F_i \quad \text{--- (1)}$$

F_f → Frictional force

F_i → Inertial force

$$F_f = \mu \cdot m \cdot v \cdot g \quad \text{--- (2)}$$

$m \cdot v$ - Total vehicle mass

g - gravitational acceleration

$$F_i = m \cdot v \cdot a_v \quad (a_v - \text{vehicle acceleration})$$

$$\text{where } a_v = \frac{dv}{dt}$$

∴ vehicle acceleration (from (1), (2), (3))

$$\frac{dv}{dt} = \frac{1}{m \cdot v} (\mu \cdot m \cdot v \cdot g)$$

ABS system has to control the wheel slip around an optimal target.

for slip,

$$s = 1 - \frac{\omega_w}{\omega_v}$$

ω_w → equivalent angular speed of the wheel.

$$\mu_v = \frac{V_v}{V_w}$$

V_v (m/s) \rightarrow Vehicle speed

\rightarrow friction coefficient depends on several factors like - wheel slip, vehicle speed, the type of road surface.

For our purpose we are going to take into account only the variation on wheel slip.

Friction Coefficient

Stability zone.	Unstable zone
friction coeff increased with the wheel slip increased	friction coeff decreased with the wheel slip increase

Friction coeff. can be expressed as empirical function, where slip is functional argument.

$$\mu(s) = A \cdot (B \cdot (1 - e^{-C \cdot s}) - D \cdot s)$$

s [-] - wheel slip.

A, B, C, D [-] - empirical coefficients.

Depending upon the value of coeff A, B, C, D empirical formula can be used to represent the friction coefficient for diff road types.

	Type			
	dry	wet	snow	ice
A	0.9	0.7	0.3	0.1
B	1.07	1.07	1.07	1.07
C	0.2773	0.5	0.1773	0.38
D	0.0026	0.003	0.006	0.007

→ wheel model:-

Wheel speed ω_w integrator is initialised. The linear wheel speed V_w is obtained by multiplying the angular speed with wheel radius. distance covered obtained by integrating linear speed.

i/p :- braking force F_b
friction force F_f

o/p :- angular wheel speed ω_w
linear wheel speed V_w
wheel distance d_w

→ Controller

bang-bang type controller reacting on wheel slip feedback. max value at friction coeff. is obtained around slip at 20% (0.2) thus target is 0.2. slip error is the diff. between actual slip & target slip.

Hydraulic system modeled as first order transfer function amplification factor K . time const is

T . o/p is braking forward.

T_b accumulated over time by integrator

i/p → wheel slip $S[-]$

o/p → vehicle speed $V_v [m/s]$.

→ Simulation:-

- Simulation run for 20 sec and results are stored in data inspector.
- When ABS disabled braking force ramps up to maximum value & causes slip. with ABS braking force modulated to maintain optimal slip ratio.
- When ABS deactivated wheel slip climbs to 1 as force increases. When ABS is activated slip is controlled by controlling braking force. When ABS is deactivated wheel locks before coming to complete halt. with ABS active wheel is prevented from locking thus reducing slip.