

# Lecture 10 - Latin Squares and Rook Polynomials

## Latin Squares

- Definition: Let  $n$  be a positive integer and let  $S$  be a set of  $n$  distinct elements. A Latin square of order  $n$  based in the set  $S$  is an  $n$ -by- $n$  array, each of whose entries is an element of  $S$  such that each of the  $n$  elements of  $S$  occurs exactly once in each row and each column.
- It follows from the pigeonhole principle that we can check in either of two ways whether an  $n$ -by- $n$  array based on a set  $S$  of  $n$  elements is a Latin square.
  - Check that each element of  $S$  occurs at least once in each row and at least once in each column
  - Check that no element of  $S$  occurs more than once in each row and no more than once in each column
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