

# 1 Text Classification and Feature Selection

## 1.3 $\chi^2$ -Feature selection

$$\chi^2(\text{mathematics,composition}) = \frac{370 * (30 * 340 - 120 * 60)^2}{(30 + 120) * (30 + 60) * (120 + 340) * (60 + 340)} = 13.405797101$$

$$\chi^2(\text{mathematics,gravity}) = \frac{370 * (3 * 367 - 87 * 87)^2}{(3 + 87) * (3 + 87) * (367 + 87) * (376 + 87)} = 9.27139367$$

$$\chi^2(\text{mathematics,differential}) = \frac{370 * (50 * 320 - 40 * 50)^2}{(50 + 40) * (50 + 50) * (320 + 40) * (320 + 50)} = 60.49382716$$

$$\chi^2(\text{mathematics,theory}) = \frac{370 * (7 * 363 - 83 * 23)^2}{(7 + 83) * (7 + 23) * (363 + 83) * (363 + 23)} = 0.317943502$$

$$\chi^2(\text{chemistry,composition}) = \frac{370(43 * 337 - 107 * 7)^2}{(43 + 107) * (43 + 7) * (337 + 107) * (337 + 7)} = 60.995660207$$

$$\chi^2(\text{chemistry,gravity}) = \frac{370 * (-50 * 90)^2}{(370 + 50) * (370 + 90)} = 387810.55900621$$

$$\chi^2(\text{chemistry,differential}) = \frac{370 * (2 * 368 - 48 * 98)^2}{(2 + 48) * (2 + 98) * (368 + 48) * (368 + 98)} = 6.010295147$$

$$\chi^2(\text{chemistry,theory}) = \frac{370 * (5 * 365 - 45 * 25)^2}{(5 + 45) * (5 + 25) * (365 + 45) * (365 + 25)} = 0.755889097$$

$$\chi^2(\text{astronomy,composition}) = \frac{370 * (47 * 323 - 103 * 73)^2}{(47 + 103) * (47 + 73) * (323 + 103) * (323 + 73)} = 7.15333772$$

$$\chi^2(\text{astronomy,gravity}) = \frac{370 * (53 * 317 - 77 * 37)^2}{(53 + 77) * (53 + 37) * (317 + 77) * (317 + 37)} = 44.135628321$$

$$\chi^2(\text{astronomy,differential}) = \frac{370 * (19 * 351 - 111 * 81)^2}{(19 + 111) * (19 + 81) * (351 + 111) * (351 + 81)} = 0.768877373$$

$$\chi^2(\text{astronomy,theory}) = \frac{370 * (11 * 359 - 19 * 119)^2}{(11 + 19) * (11 + 119) * (359 + 19) * (359 + 119)} = 714.906766087$$

$$\chi^2(\text{physics,composition}) = \frac{370 * (30 * 340 - 120 * 70)^2}{(30 + 120) * (30 + 70) * (340 + 120) * (340 + 70)} = 0.412301166$$

$$\chi^2(\text{physics,gravity}) = \frac{370 * (34 * 336 - 56 * 56)^2}{(34 + 56) * (34 + 56) * (336 + 56) * (336 + 56)} = 20.419450743$$

$$\chi^2(\text{physics,differential}) = \frac{370 * (29 * 341 - 71 * 71)^2}{(29 + 71) * (29 + 71) * (341 + 71) * (341 + 71)} = 5.123096239$$

$$\chi^2(\text{physics,theory}) = \frac{370 * (7 * 363 - 23 * 93)^2}{(7 + 23) * (7 + 93) * (363 + 23) * (363 + 93)} = 0.113234933$$

$$\chi^2_{avg}(\text{composition}) = \frac{90}{370} * 13.41 + \frac{50}{370} * 61 + \frac{130}{370} * 7.15 + \frac{100}{370} * 0.41 = 15,221891892$$

This means composition would be a good feature for chemistry

$$\chi^2_{avg}(\text{gravity}) = \frac{90}{370} * 9.27 + \frac{50}{370} * 387810 + \frac{130}{370} * 44.1 + \frac{100}{370} * 20.42 = 2311152,353918919$$

This means gravity would be a good feature for chemistry

$$\chi^2_{avg}(\text{differential}) = \frac{90}{370} * 60.5 + \frac{50}{370} * 6.01 + \frac{130}{370} * 0.77 + \frac{100}{370} * 5.12 = 17,182702703$$

This means differential would be a good feature for mathematics

$$\chi^2_{avg}(\text{theory}) = \frac{90}{370} * 0.32 + \frac{50}{370} * 0.76 + \frac{130}{370} * 714.9 + \frac{100}{370} * 0.11 = 251,391351351$$

This means theory would be a good feature for physics

Since we have no feature above the threshold for astronomy the next best feature would be gravity. This is caused by the really high value caused by 0 cases of gravity in the class chemistry.