

# Latent Class Modeling in R

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# Talk Outline

- ▶ Introduction
- ▶ What are Mixture Models?
- ▶ Latent Classes Species
- ▶ poLCA on Portugese Bank Marketing Dataset
  - ▶ Preparing the Data
  - ▶ Formulating the Models
  - ▶ Finding the Right One
- ▶ Using the Model
- ▶ Further on w depmixS4
- ▶ Conclusion Q & A

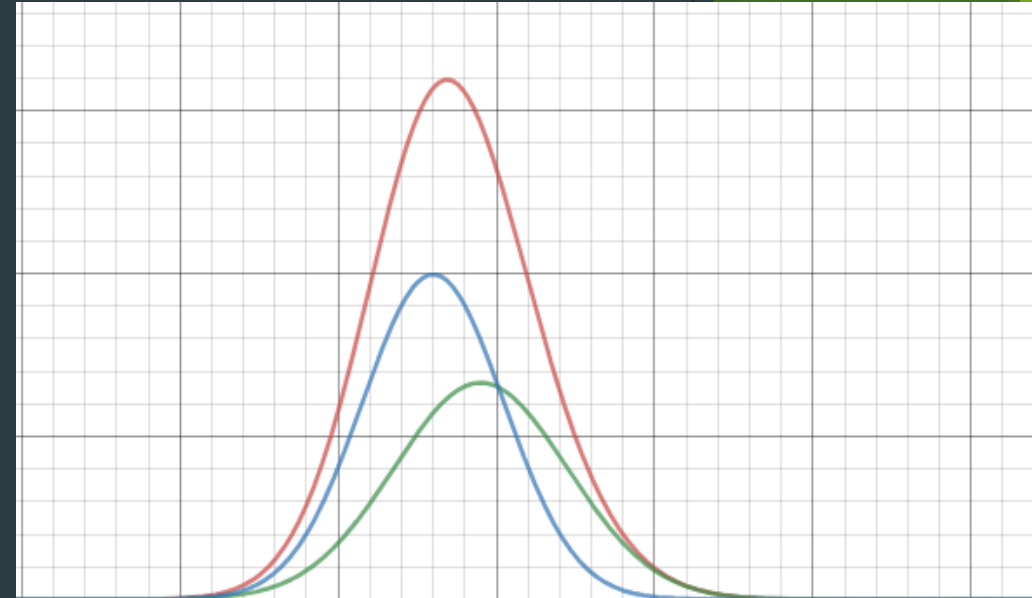
Note: A bit of Bayesian Statistics but don't be scared


# Introduction

- ▶ Latent Class Models are part of the family of Mixture Models (MM).
- ▶ Latent implies “hiddenness”, “concealed”, “unmanifested”, notion of “undisclosed” or “unobserved”
- ▶ In this talk we will focus on one - the Latent Class Analysis (LCA)
- ▶ It is generally a **segmentation** technique but since it is probabilistic (it is MM after all) it can be used for **prediction** too.
- ▶ Does not use distances for similarities *but uses membership probabilities estimated directly from the model.*
- ▶ Where has it been used for:
  - ▶ Health Sciences
  - ▶ Behavioral/Political Sciences
  - ▶ Economics/Econometrics
  - ▶ Marketing Sciences (**heavily used**)
    - ▶ Segmentation w/ Customer Lifetime Values, Recency/Frequency
- ▶ It has sister models w similar names that is why it gets confusing in the literature.


# What are Mixture Models?

- Assume we are studying the heights of people in a city like Melbourne.
- We get their heights and found out that their height distribution looks like the one on **RED**. This is what we see as the result of our data gathering.
- Unknown to us is that there are **male** and **female** heights that are causing that total sample height distribution to behave that way.
- The job of a MM is to find those HIDDEN hence, LATENT variables that are causing the **RED** to behave that way.
- These LATENT variables are the Classes LCA will discover!
- THAT IS GOOD ISN'T IT?




1 

$$y = \exp\left(-\frac{(x-5.9)^2}{2(.3)}\right)\left(\frac{1}{.3(\sqrt{2\pi})}\right) + \exp\left(-\frac{(x-5.6)^2}{2(.2)}\right)\left(\frac{1}{.2(\sqrt{2\pi})}\right)$$

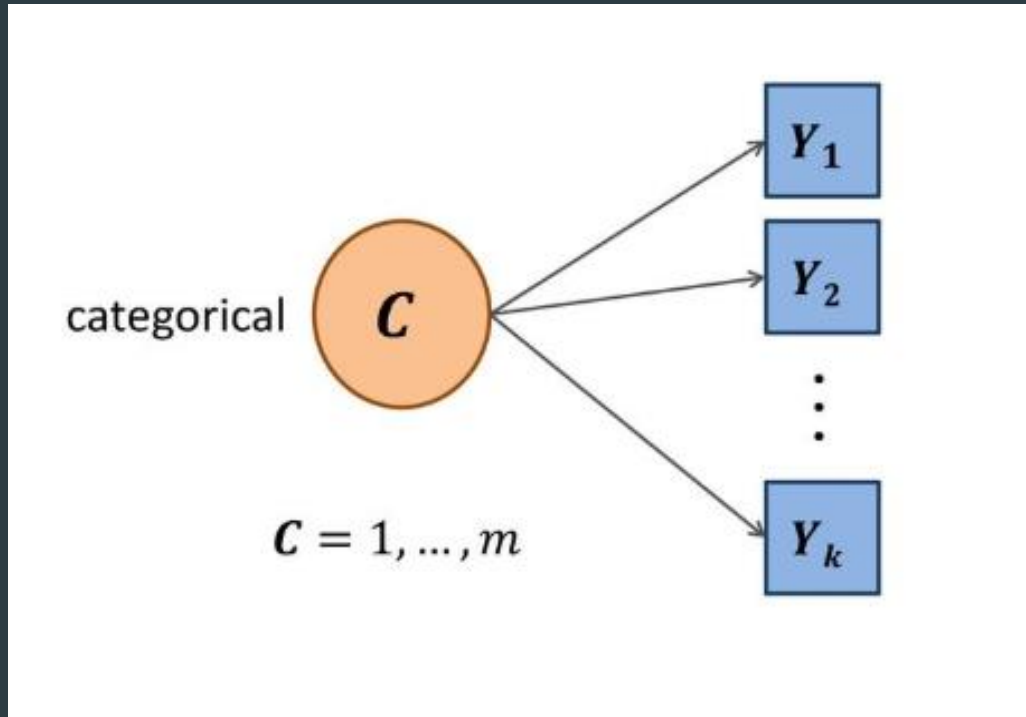
2 

$$y_m = \exp\left(-\frac{(x-5.9)^2}{2(.3)}\right)\left(\frac{1}{.3(\sqrt{2\pi})}\right)$$

3 

$$y_f = \exp\left(-\frac{(x-5.6)^2}{2(.2)}\right)\left(\frac{1}{.2(\sqrt{2\pi})}\right)$$

# VISUALIZING LATENT CLASSES



$Y_i = \text{Categorical Variables}$

$C = \text{Latent Classes} - \text{suspected categorical variables influencing the } Y_i$

# Latent Concepts and its Species

- We need known category variables in our dataset
  - ▶ Sometimes called **indicators**
  - ▶ Sometimes called **manifest variables**
- **Covariates** - these are variables that can secondarily affect the values of our indicators
- **Latent Class** - hidden or unknown variables, which should be named later
- HOW THEY ALL RELATE :

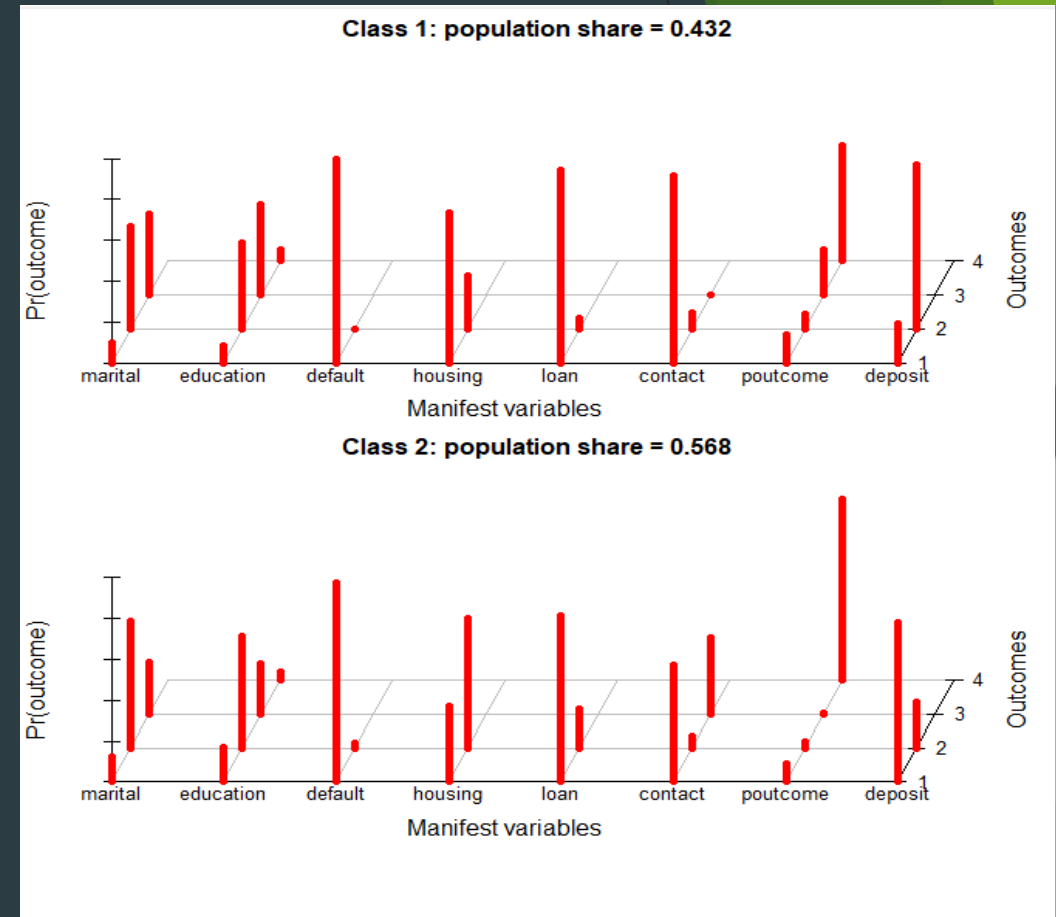
Indicator variables	Latent variable(s)	
	<i>Discrete</i>	<i>Continuous</i>
<i>Discrete</i>	<b>Latent Class Analysis</b>	Latent Trait Analysis
<i>Continuous</i>	Latent Profile Analysis	Factor Analysis

# LCA in R

- ▶ MCLUST - Model based Clustering
- ▶ poLCA - Polytomous LCA - Many Valued Category Variables
- ▶ LCCA - Latent Class Causal Analysis
- ▶ randomLCA - Random Effects LCA
- ▶ BayesLCA - Bayesian LCA
- ▶ depmixS4 - Dependent Mixture Models - Hidden Markov Models of GLMs and Other Distributions in S4

# poLCA R Package

- It means the manifest variables have multi-level factor values or category levels - so multi-nominal vs binomial
- Has no modeling assumptions ie does not rely on knowledge of the distribution of the variables
- $P(Y_i|C_j)$  - given the data came from Class J what is the probability of  $Y_i$  obtaining a certain value?
- Supports latent class “regression” for class membership prediction
- No need for Principal Component Analysis then Linear Discriminant Analysis.
- Offers goodness of fit tests information





# The Portugese Bank Dataset for Marketing

<https://archive.ics.uci.edu/ml/datasets/Bank+Marketing> (modified Kaggle version)

Input variables:

# bank client data:

1 - age (numeric)

2 - job : type of job (categorical: 'admin.', 'blue-collar', 'entrepreneur', 'housemaid', 'management', 'retired', 'self-employed', 'services', 'student', 'technician', 'unemployed', 'unknown')

3 - marital : marital status (categorical: 'divorced', 'married', 'single', 'unknown'; note: 'divorced' means divorced or widowed)

4 - education (categorical: 'basic.4y', 'basic.6y', 'basic.9y', 'high.school', 'illiterate', 'professional.course', 'university.degree', 'unknown')

5 - default: has credit in default? (categorical: 'no', 'yes', 'unknown')

6 - housing: has housing loan? (categorical: 'no', 'yes', 'unknown')

7 - loan: has personal loan? (categorical: 'no', 'yes', 'unknown')

# related with the last contact of the current campaign:

8 - contact: contact communication type (categorical: 'cellular', 'telephone')

9 - month: last contact month of year (categorical: 'jan', 'feb', 'mar', ..., 'nov', 'dec')

10 - day\_of\_week: last contact day of the week (categorical: 'mon', 'tue', 'wed', 'thu', 'fri')

11 - duration: last contact duration, in seconds (numeric). Important note: this attribute highly affects the output target (e.g., if duration=0 then y='no'). Yet, the duration is not known before the call and should be discarded if the intention is to have a realistic predictive model.

# other attributes:

12 - campaign: number of contacts performed during this campaign and for this client (numeric, includes last contact)

13 - pdays: number of days that passed by after the client was last contacted from a previous campaign (numeric; 999 means client was not previously contacted)

14 - previous: number of contacts performed before this campaign and for this client (numeric)

15 - poutcome: outcome of the previous marketing campaign (categorical: 'failure', 'nonexistent', 'success')

# social and economic context attributes

16 - emp.var.rate: employment variation rate - quarterly indicator (numeric)

17 - cons.price.idx: consumer price index - monthly indicator (numeric)

18 - cons.conf.idx: consumer confidence index - monthly indicator (numeric)

19 - euribor3m: euribor 3 month rate - daily indicator (numeric)

20 - nr.employed: number of employees - quarterly indicator (numeric)

Output variable (desired target):

21 - y - has the client subscribed a term deposit? (binary: 'yes', 'no')

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# The Portuguese Bank Dataset for Marketing

## poLCA Modeling Context

- ▶ The data is related with direct marketing campaigns of a Portuguese banking institution. The marketing campaigns were based on phone calls. Often, more than one contact to the same client was required, in order to access if the product (bank term deposit) would be ('yes') or not ('no') subscribed.
- ▶ **Q : We want to know the types of people who say YES/NO to the term deposit deal.**
- ▶ poLCA can only consider **Category/Factor Manifest Variables/Features/Attributes**. For our case study we are going to examine the following
- ▶ Marital - divorced/married/single - marital status
- ▶ Education - primary/secondary/tertiary/unknown - highest level of education
- ▶ Default - yes/no - did the person have a credit in default?
- ▶ Housing - yes/no - does the person have a housing loan?
- ▶ Loan - yes/no - does the person have a personal loan?
- ▶ Contact - cellular/telephone/unknown - how the person got contacted
- ▶ Poutcome - failure/other/success/unknown
- ▶ Deposit - yes/no - the response to the current marketing campaign - did the person subscribe to the term deposit?

# The Code

```
[~] = =PortuBank.R
#####
### Code: PortuBank.R
### Author: L P Cruz https://unpocologico.wordpress.com/
### Input : Portugese Bank Marketing Data Set;
###          https://archive.ics.uci.edu/ml/datasets/Bank+Marketing
### Process: Apply poLCA Latent Class Modeling
### Output : Model reports for varying class counts
#####
### Begin
### Load libraries to use
require(poLCA)

setwd("c:/Users/lcruz/MelBuRn")

### Read the source dataset

PortuBank <- read.csv("bank.csv")

### Wrangle the data
### Pick up the categorical features to use

MyBankData <- PortuBank[, c(3,4,5,7,8,9,16,17)]

### define an initial simple model
f <- cbind(marital,education,default,housing,loan,contact,poutcome,deposit)~1

### Execute the model
print("Model F")
modFpoLCA<-poLCA(f, MyBankData, nclass = 2, na.rm=FALSE, graphs = TRUE)

### define another elaborate model

print("Model H 50000")
modHpoLCA_10<-poLCA(h, MyBankData, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )

###
### End
```

Notice the simplicity of the steps.

Thanks to R, ML codes tend to be short.

Short codes have less moving parts subject to breakages

# Sample Model Report

```
### define an initial simple model
f <- cbind(marital,education,default,housing,loan,contact,poutcome,deposit)~1

### Execute the model
print("Model F")
modFpolCA<-polCA(f, MyBankData, nclass = 2, na.rm=FALSE, graphs = TRUE)
```

*We get conditional probabilities*

$$P(\text{default} = \text{yes} | \text{class} = 1) = 0.0260$$

$$P(\text{deposit} = \text{yes} | \text{class} = 1) = 0.2222$$

```
modFpolCA<-polCA(f, MyBankData, nclass = 2, na.rm=FALSE, graphs = TRUE)
Conditional item response (column) probabilities,
by outcome variable, for each class (row)
$marital
      divorced married single
class 1:  0.1262   0.6201 0.2536
class 2:  0.1022   0.5018 0.3960
$education
      primary secondary tertiary unknown
class 1:  0.1719   0.5453   0.2454  0.0374
class 2:  0.0852   0.4188   0.4422  0.0538
$default
      no    yes
class 1: 0.9740 0.0260
class 2: 0.9993 0.0007
$housing
      no    yes
class 1: 0.3679 0.6321
class 2: 0.7357 0.2643
$loan
      no    yes
class 1: 0.8118 0.1882
class 2: 0.9445 0.0555
$contact
      cellular telephone unknown
class 1:  0.5715   0.0593  0.3692
class 2:  0.9162   0.0825  0.0013
$poutcome
      failure other success unknown
class 1:  0.0892 0.0272  0.0011  0.8825
class 2:  0.1374 0.0756  0.2205  0.5665
$deposit
      no    yes
class 1: 0.7778 0.2222
class 2: 0.1956 0.8044
```

# Detecting a Suitable Model

1. When Estimated Class  $\approx$  Predicted Class  $\Rightarrow$  Good Indication
2. We want the AIC, BIC,  $G^2$  and  $\chi^2$  to be small
3. The ideal situation - all of #1 and #2 are satisfied
4. If mixed, still useful specially when #2 is met
5. Tuning - try varying the class numbers, number of repetitions, maximum iterations

## $\chi^2$ Chi-Square Test for model goodness of fit

$H_0$  the expected = predicted values  
df= 29,  $\chi^2 = 5094.074$

```
Estimated class population shares
0.5677 0.4323
```

```
Predicted class memberships (by modal posterior prob.)
0.5798 0.4202
```

```
=====
Fit for 2 latent classes:
=====
```

```
number of observations: 11162
number of estimated parameters: 29
residual degrees of freedom: 2274
maximum log-likelihood: -59388.76
```

```
AIC(2): 118835.5
BIC(2): 119047.8
G^2(2): 3368.434 (Likelihood ratio/deviance statistic)
X^2(2): 5094.074 (Chi-square goodness of fit)
```

$H_0$  the expected = predicted values  
 $df = 29$ ,  $\chi^2 = 5094.074$

At this result we are rejecting  $H_0$  at  $\alpha = 0.5$ . We are way far to the right

Therefore, this suggests we should try and do better with our model

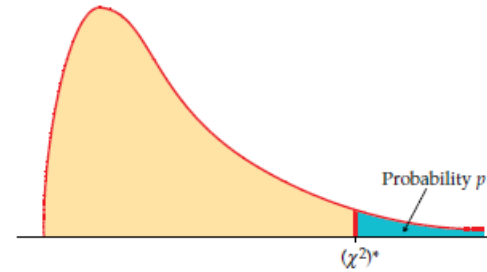


Table entry for  $p$  is the critical value  $(\chi^2)^*$  with probability  $p$  lying to its right.

**TABLE F**  
 $\chi^2$  distribution critical values

df	Tail probability $p$											
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.32	1.64	2.07	2.71	3.84	5.02	5.41	6.63	7.88	9.14	10.83	12.12
2	2.77	3.22	3.79	4.61	5.99	7.38	7.82	9.21	10.60	11.98	13.82	15.20
3	4.11	4.64	5.32	6.25	7.81	9.35	9.84	11.34	12.84	14.32	16.27	17.73
4	5.39	5.99	6.74	7.78	9.49	11.14	11.67	13.28	14.86	16.42	18.47	20.00
5	6.63	7.29	8.12	9.24	11.07	12.83	13.39	15.09	16.75	18.39	20.51	22.11
6	7.84	8.56	9.45	10.64	12.59	14.45	15.03	16.81	18.55	20.25	22.46	24.10
7	9.04	9.80	10.75	12.02	14.07	16.01	16.62	18.48	20.28	22.04	24.32	26.02
8	10.22	11.03	12.03	13.36	15.51	17.53	18.17	20.09	21.95	23.77	26.12	27.87
9	11.39	12.24	13.29	14.68	16.92	19.02	19.68	21.67	23.59	25.46	27.88	29.67
10	12.55	13.44	14.53	15.99	18.31	20.48	21.16	23.21	25.19	27.11	29.59	31.42
11	13.70	14.63	15.77	17.28	19.68	21.92	22.62	24.72	26.76	28.73	31.26	33.14
12	14.85	15.81	16.99	18.55	21.03	23.34	24.05	26.22	28.30	30.32	32.91	34.82
13	15.98	16.98	18.20	19.81	22.36	24.74	25.47	27.69	29.82	31.88	34.53	36.48
14	17.12	18.15	19.41	21.06	23.68	26.12	26.87	29.14	31.32	33.43	36.12	38.11
15	18.25	19.31	20.60	22.31	25.00	27.49	28.26	30.58	32.80	34.95	37.70	39.72
16	19.37	20.47	21.79	23.54	26.30	28.85	29.63	32.00	34.27	36.46	39.25	41.31
17	20.49	21.61	22.98	24.77	27.59	30.19	31.00	33.41	35.72	37.95	40.79	42.88
18	21.60	22.76	24.16	25.99	28.87	31.53	32.35	34.81	37.16	39.42	42.31	44.43
19	22.72	23.90	25.33	27.20	30.14	32.85	33.69	36.19	38.58	40.88	43.82	45.97
20	23.83	25.04	26.50	28.41	31.41	34.17	35.02	37.57	40.00	42.34	45.31	47.50
21	24.93	26.17	27.66	29.62	32.67	35.48	36.34	38.93	41.40	43.78	46.80	49.01
22	26.04	27.30	28.82	30.81	33.92	36.78	37.66	40.29	42.80	45.20	48.27	50.51
23	27.14	28.43	29.98	32.01	35.17	38.08	38.97	41.64	44.18	46.62	49.73	52.00
24	28.24	29.55	31.13	33.20	36.42	39.36	40.27	42.98	45.56	48.03	51.18	53.48
25	29.34	30.68	32.28	34.38	37.65	40.65	41.57	44.31	46.93	49.44	52.62	54.95
26	30.43	31.79	33.43	35.56	38.89	41.92	42.86	45.64	48.29	50.83	54.05	56.41
27	31.53	32.91	34.57	36.74	40.11	43.19	44.14	46.96	49.64	52.22	55.48	57.86
28	32.62	34.03	35.71	37.92	41.34	44.46	45.42	48.28	50.99	53.59	56.89	59.30
29	33.71	35.14	36.85	39.09	42.56	45.72	46.69	49.59	52.34	54.97	58.30	60.73
30	34.80	36.25	37.99	40.26	43.77	46.98	47.96	50.89	53.67	56.33	59.70	62.16
40	45.62	47.27	49.24	51.81	55.76	59.34	60.44	63.69	66.77	69.70	73.40	76.09
50	56.33	58.16	60.35	63.17	67.50	71.42	72.61	76.15	79.49	82.66	86.66	89.56
60	66.98	68.97	71.34	74.40	79.08	83.30	84.58	88.38	91.95	95.34	99.61	102.7
80	88.13	90.41	93.11	96.58	101.9	106.6	108.1	112.3	116.3	120.1	124.8	128.3
100	109.1	111.7	114.7	118.5	124.3	129.6	131.1	135.8	140.2	144.3	149.4	153.2



# Modified Model

```
### define another elaborate model
h <- cbind(default, housing, loan, contact, poutcome, deposit)~1

### Execute the model

print("Model H 50000")
modHpolCA_10<-polCA(h, MyBankData, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )
[]
```

- We have good estimate and predicted w Classes 3 & 4
- We have acceptable numbers also for Classes 1 & 2
- We have bad numbers for Classes 5 & 6
- We got good numbers AIC, BIC,  $G^2$  and  $\chi^2$
- As can be seen we have  $p = 0.13 > \alpha = 0.05$ , so we are accepting the hypothesis that the observed are not significantly different from the expected values - there is a good fit

```
Estimated class population shares
0.1383 0.1543 0.2802 0.2059 0.1591 0.0622
Predicted class memberships (by modal posterior prob.)
0.1141 0.1020 0.2859 0.2089 0.2677 0.0213

=====
Fit for 6 latent classes:
=====
number of observations: 11162
number of estimated parameters: 59
residual degrees of freedom: 132
maximum log-likelihood: -35910.4

AIC(6): 71938.8
BIC(6): 72370.69
G^2(6): 65.67256 (Likelihood ratio/deviance statistic)
X^2(6): 71.30884 (Chi-square goodness of fit)
```

Chi-Square: **71.30884**

Degrees of Freedom: **59**

p: **0.1307**

# Qualitative Analysis

- Q: What kind of people say YES to the offer?
- A: Class 2 & 5 people are likely to say YES to the offer
- Q: What are their characteristics?
  - Never had credits in default
  - No housing loan
  - No personal loan
  - Contacted by Cell phone
  - Undetermined reaction to previous campaign

Q. If the person said YES before how likely is the person to say YES again

```
> modpoc10<-poc10(mybankdata, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )
Model 1: llik = -35919.79 ... best llik = -35919.79
Model 2: llik = -35919.79 ... best llik = -35919.79
Model 3: llik = -35910.4 ... best llik = -35910.4
Model 4: llik = -35910.4 ... best llik = -35910.4
Model 5: llik = -35910.4 ... best llik = -35910.4
Conditional item response (column) probabilities,
by outcome variable, for each class (row)

$default
      no    yes
class 1: 0.9870 0.0130
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.9779 0.0221
class 5: 1.0000 0.0000
class 6: 0.8602 0.1398

$housing
      no    yes
class 1: 0.0000 1.0000
class 2: 0.5164 0.4836
class 3: 0.6826 0.3174
class 4: 0.2665 0.7335
class 5: 1.0000 0.0000
class 6: 0.6743 0.3257

$loan
      no    yes
class 1: 0.8001 0.1999
class 2: 0.9206 0.0794
class 3: 0.8700 0.1300
class 4: 0.8683 0.1317
class 5: 1.0000 0.0000
class 6: 0.5601 0.4399

$contact
      cellular telephone unknown
class 1: 0.9615 0.0385 0.0000
class 2: 0.9606 0.0301 0.0094
class 3: 0.8775 0.1198 0.0027
class 4: 0.0000 0.0163 0.9837
class 5: 0.8710 0.1290 0.0000
class 6: 0.8814 0.0312 0.0874

$outcome
      failure other success unknown
class 1: 0.3432 0.1069 0.0054 0.5445
class 2: 0.1354 0.0625 0.3084 0.4937
class 3: 0.0869 0.0428 0.0160 0.8543
class 4: 0.0000 0.0020 0.0014 0.9966
class 5: 0.0984 0.0709 0.2693 0.5614
class 6: 0.0265 0.0000 0.0000 0.9735
```

\$deposit		no	yes
class 1:	0.6966	0.3034	
class 2:	0.0513	0.9487	
class 3:	0.7616	0.2384	
class 4:	0.7823	0.2177	
class 5:	0.0401	0.9599	
class 6:	0.6605	0.3395	



# Quantitative Analysis

Q. If the person said YES before, how likely is the person to say YES again

$$P(\text{deposit} = \text{YES} | \text{poutcome} = \text{success}) = ?$$

A. We apply Conditional Probs & Bayes' Theorem

$$\begin{aligned} & P(\text{deposit} = \text{YES} | \text{poutcome} = \text{success}) \\ &= \frac{P(\text{deposit} = \text{YES} \cap \text{poutcome} = \text{success})}{P(\text{poutcome} = \text{success})} \\ &= \frac{P(\text{deposit} = \text{YES} \cap \text{poutcome} = \text{success} | \text{class} = 1)}{P(\text{poutcome} = \text{success})} + \dots + \frac{P(\text{deposit} = \text{YES} \cap \text{poutcome} = \text{success} | \text{class} = 6)}{P(\text{poutcome} = \text{success})} \\ &= \frac{(0.3034) \times (0.0054) \times (0.1383) + \dots + (0.3395) \times (0.0000) \times (0.0622)}{(0.0054) \times (0.1383) + \dots + (0.0000) \times (0.0622)} \\ &= \frac{0.087631}{0.095203} = 0.920459 \end{aligned}$$

Therefore 92% chance, we should come back to those who subscribed before and remarket to them.

<https://www.linkedin.com/in/l-p-cruz-phd/>  
<https://unpocologico.wordpress.com/>

```
> modelpoutc10 <- poutc10, mybankdata, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )
Model 1: llik = -35919.79 ... best llik = -35919.79
Model 2: llik = -35919.79 ... best llik = -35919.79
Model 3: llik = -35910.4 ... best llik = -35910.4
Model 4: llik = -35910.4 ... best llik = -35910.4
Model 5: llik = -35910.4 ... best llik = -35910.4
Conditional item response (column) probabilities,
by outcome variable, for each class (row)
```

```
$default
      no    yes
class 1: 0.9870 0.0130
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.9779 0.0221
class 5: 1.0000 0.0000
class 6: 0.8602 0.1398
```

```
$housing
      no    yes
class 1: 0.0000 1.0000
class 2: 0.5164 0.4836
class 3: 0.6826 0.3174
class 4: 0.2665 0.7335
class 5: 1.0000 0.0000
class 6: 0.6743 0.3257
```

```
$loan
      no    yes
class 1: 0.8001 0.1999
class 2: 0.9206 0.0794
class 3: 0.8700 0.1300
class 4: 0.8683 0.1317
class 5: 1.0000 0.0000
class 6: 0.5601 0.4399
```

```
$contact
      cellular telephone unknown
class 1: 0.9615 0.0385 0.0000
class 2: 0.9606 0.0301 0.0094
class 3: 0.8775 0.1198 0.0027
class 4: 0.0000 0.0163 0.9837
class 5: 0.8710 0.1290 0.0000
class 6: 0.8814 0.0312 0.0874
```

```
$poutcome
      failure other success unknown
class 1: 0.3432 0.1069 0.0054 0.5445
class 2: 0.1354 0.0625 0.3084 0.4937
class 3: 0.0869 0.0428 0.0160 0.8543
class 4: 0.0000 0.0020 0.0014 0.9966
class 5: 0.0984 0.0709 0.2693 0.5614
class 6: 0.0265 0.0000 0.0000 0.9735
```

	no	yes
class 1:	0.6966	0.3034
class 2:	0.0513	0.9487
class 3:	0.7616	0.2384
class 4:	0.7823	0.2177
class 5:	0.0401	0.9599
class 6:	0.6605	0.3395

# Prediction

- Because of Conditional Probs & Bayes Theorem, we can make predictions if a client will buy or not based on how more or how less of information we have about the client.
- For example, we can ask the question, what is the probability this person whom I know who does not have a housing loan and no personal loan will say YES to the deal?
- Even if these are the only information we know we can still proceed, this is asking
- $P(\text{deposit} = \text{YES} | \text{housing} = \text{YES}, \text{loan} = \text{YES})$
- Likewise since we have  $P(\text{default} = \text{YES} | \text{class} = 1)$ , by Bayes, we can have  $P(\text{class} = 1 | \text{default} = \text{YES})$
- This is the nice thing about Bayesianism, you can proceed even if you do not have all the information on a customer.

# Naming the Classes

- The difficult part of Latent Class Modeling, the interpretation of the Classes or how to name them
- Some quick rules of thumb:
  - The latent probabilities vary for a manifest variable
  - Then also, they are closer to 0 or 1
- Examples, Class 1 are people w no defaults but has housing loan and no personal loan uses cell phone with no known previous outcome.
- How should we name this class? Lots of possibilities here, and we can make it descriptive
- Note: This gives us a notional profile of a customer.

```
> modnpotca_10<-poLCA(m, myBankData, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )
Model 1: llik = -35919.79 ... best llik = -35919.79
Model 2: llik = -35919.79 ... best llik = -35919.79
Model 3: llik = -35910.4 ... best llik = -35910.4
Model 4: llik = -35910.4 ... best llik = -35910.4
Model 5: llik = -35910.4 ... best llik = -35910.4
Conditional item response (column) probabilities,
by outcome variable, for each class (row)

$default
      no    yes
class 1: 0.9870 0.0130
class 2: 1.0000 0.0000
class 3: 1.0000 0.0000
class 4: 0.9779 0.0221
class 5: 1.0000 0.0000
class 6: 0.8602 0.1398

$housing
      no    yes
class 1: 0.0000 1.0000
class 2: 0.5164 0.4836
class 3: 0.6826 0.3174
class 4: 0.2665 0.7335
class 5: 1.0000 0.0000
class 6: 0.6743 0.3257

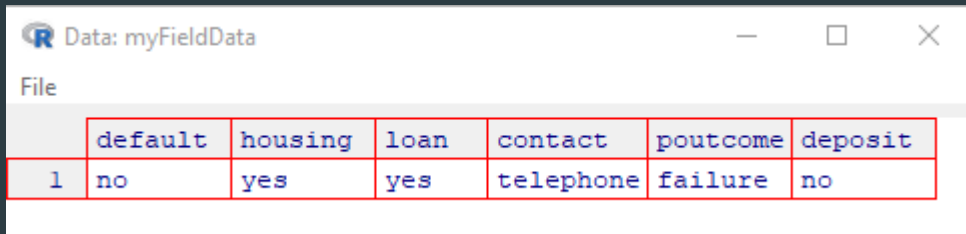
$loan
      no    yes
class 1: 0.8001 0.1999
class 2: 0.9206 0.0794
class 3: 0.8700 0.1300
class 4: 0.8683 0.1317
class 5: 1.0000 0.0000
class 6: 0.5601 0.4399

$contact
      cellular telephone unknown
class 1:   0.9615      0.0385  0.0000
class 2:   0.9606      0.0301  0.0094
class 3:   0.8775      0.1198  0.0027
class 4:   0.0000      0.0163  0.9837
class 5:   0.8710      0.1290  0.0000
class 6:   0.8814      0.0312  0.0874

$spoutcome
      failure other success unknown
class 1:  0.3432 0.1069  0.0054  0.5445
class 2:  0.1354 0.0625  0.3084  0.4937
class 3:  0.0869 0.0428  0.0160  0.8543
class 4:  0.0000 0.0020  0.0014  0.9966
class 5:  0.0984 0.0709  0.2693  0.5614
class 6:  0.0265 0.0000  0.0000  0.9735
```

# Can we predict which Class a data belongs?

- Yes, there are two ways.
- We can use the `predclass` or `posterior` functions of `polCA`
- You give it a Y combination and it will produce back a C.
- Assume we have, a person, w default = NO, housing = YES, loan = YES, contact = TELEPHONE, poutcome = FAILURE, desposit = NO



	default	housing	loan	contact	poutcome	deposit
1	no	yes	yes	telephone	failure	no

```
merge(myFieldData, unique(cbind(MyBankData[, 3:8], modHpo1CA_10$predclass)))  
default housing loan contact poutcome deposit modHpo1CA_10$predclass  
no yes yes telephone failure no 1  
View(myFieldData)
```

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<https://unpocologico.wordpress.com/>

```
> modHpo1CA_10 <- polCA(m, MyBankData, nclass = 6, na.rm=FALSE, maxiter = 50000, nrep=5 )  
Model 1: llik = -35919.79 ... best llik = -35919.79  
Model 2: llik = -35919.79 ... best llik = -35919.79  
Model 3: llik = -35910.4 ... best llik = -35910.4  
Model 4: llik = -35910.4 ... best llik = -35910.4  
Model 5: llik = -35910.4 ... best llik = -35910.4  
Conditional item response (column) probabilities,  
by outcome variable, for each class (row)  
  
$default  
      no    yes  
class 1: 0.9870 0.0130  
class 2: 1.0000 0.0000  
class 3: 1.0000 0.0000  
class 4: 0.9779 0.0221  
class 5: 1.0000 0.0000  
class 6: 0.8602 0.1398  
  
$housing  
      no    yes  
class 1: 0.0000 1.0000  
class 2: 0.5164 0.4836  
class 3: 0.6826 0.3174  
class 4: 0.2665 0.7335  
class 5: 1.0000 0.0000  
class 6: 0.6743 0.3257  
  
$loan  
      no    yes  
class 1: 0.8001 0.1999  
class 2: 0.9206 0.0794  
class 3: 0.8700 0.1300  
class 4: 0.8683 0.1317  
class 5: 1.0000 0.0000  
class 6: 0.5601 0.4399  
  
$contact  
      cellular telephone unknown  
class 1: 0.9615 0.0385 0.0000  
class 2: 0.9606 0.0301 0.0094  
class 3: 0.8775 0.1198 0.0027  
class 4: 0.0000 0.0163 0.9837  
class 5: 0.8710 0.1290 0.0000  
class 6: 0.8814 0.0312 0.0874  
  
$poutcome  
      failure other success unknown  
class 1: 0.3432 0.1069 0.0054 0.5445  
class 2: 0.1354 0.0625 0.3084 0.4937  
class 3: 0.0869 0.0428 0.0160 0.8543  
class 4: 0.0000 0.0020 0.0014 0.9966  
class 5: 0.0984 0.0709 0.2693 0.5614  
class 6: 0.0265 0.0000 0.0000 0.9735
```

# Further On

- depmixS4 - you might try this out if you have a combination of continuous and discrete manifest variables to study
- Accommodates mixed multivariate data
- However, not as extensive report but is offered for extension

# Conclusion

- We talked about mixture models
- We covered the varied ideas on latent classes
- We demonstrated using one technique - poLCA
- We used this to attack a marketing dataset
- We defined how to spot a fitting model
- How to predict using poLCA
- How to cluster using poLCA
- The way ahead

Thank you for coming & having me  
Questions or Comments - Welcome

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