

Double-Slit Experiment —need more exciting title here, relevant to physics that is demonstrated, particularly light as a wave

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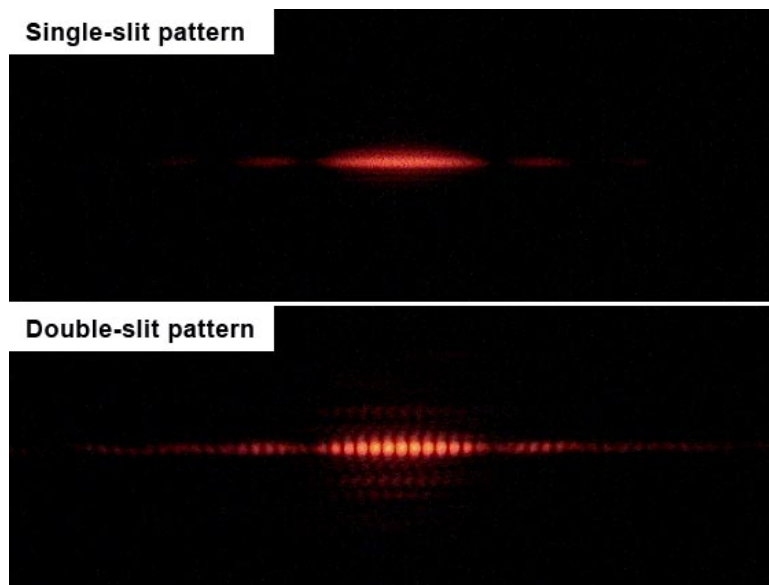


FIG. 1. Single and double-slit interference patterns¹.

Abstract

When two narrow beams of light at the same phase angle are projected on a screen, they interfere and create the fringes of light shown in Fig.1. This phenomenon shows the wave nature of light. Originally done by Young back in 1800, the double-slit experiment was reproduced in this lab with the use of the TWS apparatus with a laser of 670nm in wavelength. The monochromatic light beam was sent from one end of a u-channel through a double-slit to create an interference pattern that was detected by a photodiode at the other end. The observed interference pattern is fitted using Fraunhofer model, which describes far-field diffraction. The amplitude of the double-slit pattern was observed to be the modulated by the single slit diffraction pattern. Reduced χ^2 of the double-slit fit curve is 0.827 and that of the single-slit fit curve is 1.57, both indicating that the data are consistent with the model within our estimate of uncertainty.

[comments on abstract](#)

1. don't include references to figures (or figures) in abstract! Abstract needs to be able to "stand alone." You should move Figure 1 to the introduction.
2. first statement isn't always true. The two beams of light need to have come from the same source, and be coherent. That is, there needs to be a definite and constant phase difference between the two (even if that difference is zero, and they are therefore in phase with each other).
3. first sentence is also misleading. It reads as is you are saying that the projection on the screen causes the interference, which certainly isn't true. The screen is how the variation in light intensity due to wave interference is detected, not how it is caused. Physically, it is because the waves diffracting from each slit spread out, passing through each other. That leads to constructive and destructive interference (peak + peak = bigger peak, valley + valley = deeper valley, peak + valley = flat (null) node). You should include a sentence or two discussing this, so that the reader can understand that the detected interference pattern provides evidence for the wave nature of light.
4. the photodiode measures light intensity, and hence can be used to measure variations in light intensity as a function of some other variable. It doesn't detect interference patterns directly. you had to select different parts of that pattern (by moving a slit across the detector) to

detect the interference pattern.

I. INTRODUCTION

The double-slit experiment, also **known known** as the Young's experiment, explores the wave-like nature of light. **use “experiment — also known as — explores” rather than “experiment, also known as Young's experiment, explores.”** It is important in this experiment for the two sources of light are coherent and have the same phase.**Usage: either “for ... to be” or “that... are.”** **don't have to be same phase, but they do need to have a constant phase difference. Can still get an interference pattern if phase difference is $\pi/2$ instead of zero — the pattern will just have all the double slit interference maxima and minima reversed!** Back in 1801, Thomas Young had difficulty with using common light sources, such as candles and lanterns, to be served as coherent sources of light. Thus instead, Young performed the experiment by filtering sunlight through a pinhole in a window shutter split by a piece of card and projecting it horizontally across the room. Light waves from either side of the card coming through the pinhole can be thus considered coherent sources and the interference pattern was then projected onto a screen from which the wavelength of the light source could be determined using Young's Equation:

$$\lambda = \frac{yd}{mL}$$

This would be a good place to derive equations (1) and (2), since you introduce them without explanation later in your results and analysis section. Include text and a figure that defines your variables.

I'm not sure what the point of the equation above is, since it isn't the equation you use later, and is in fact just a small angle approximation replacing $\sin(\theta)$ with θ . If you think it is helpful, however, then you need to define what the variables mean! How will anyone know what m or d are? YOU would also need a figure. It might be similar to your Figure (2) if you add lines indicating the meanings of L , θ , and y etc, or it might be similar to Figure (5), although that figure doesn't indicate what m is and uses different variables from those in the above equation. For example, it has D equal to what your formula calls L instead of what your formula calls d .

I think this next paragraph about the TWS belongs in the Experiment section

Today, we can do the experiment by using the TWS **what is TWS?** apparatus that includes a monochromatic laser beam at one end (with a wavelength of 670 nm) passing through a

double slit all encapsulated in a tightly sealed does this mean “light-tight”? u-channel. Adjusting the micrometer attached to the detector-slit allows you to gather information regarding the interference pattern that is projected to a photodiode at the other end of the u-channel. what detector slit? It needs defining. A bit wordy possibility — you can do better — might be ‘a slit that can be moved laterally across the detector to pick out individual maxima and minima in the interference pattern ...’

II. EXPERIMENT

In this experiment, the apparatus is set up as shown in Fig. 2. After precise alignment of the laser, the double-slit, the slit-blocker, and the detector-slit, the photodiode is connected to a multimeter which is ultimately connected to the computer. LabView is used to collect data first for the double-slit experiment and for the single-slit experiment.

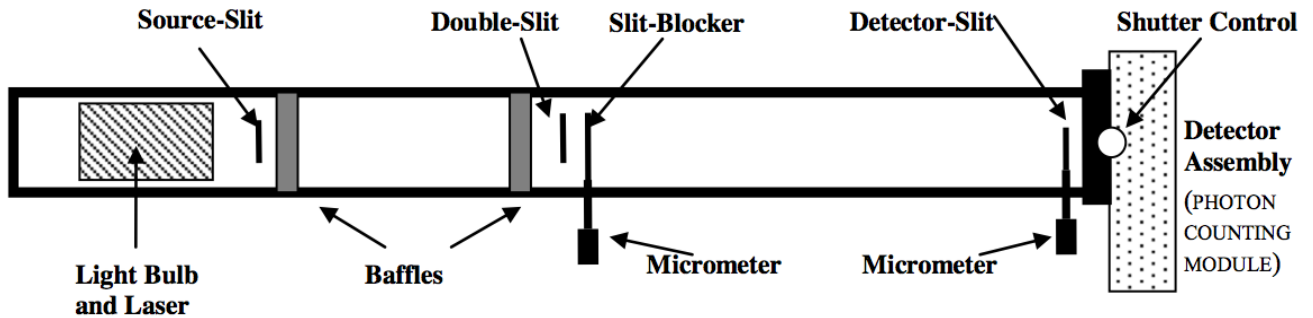


FIG. 2. Schematic of TWS apparatus - not to scale².

All parts are carefully aligned how is this done? did you follow a particular instruction sheet? what is the criteria for alignment? and key positions of the slit-blocker are recorded, so that light from one or two slits could be blocked and form both double-slit and single-slit interference patterns. this is misleading. I think you are using the slit blocker to select between single-slit and double-slit diffraction experiments. Depending on the experiment chosen, you then either see a single-slit interference pattern dependent on the ratio a/λ of the slit width a to the light wavelength λ or a double-slit pattern with a bright-fringe to bright-fringe spacing dependent on the ratio d/λ of the slit spacing d to the light wavelength λ , modulated by a single-slit pattern due to the finite widths of the two slits The shutter

at the end of the U-channel was kept closed, because only the photodiode on the surface of the shutter is used. what does the shutter block? what would be exposed to light if it were open? After the preparation work, the double-slit experiment is first performed. A double-slit of with? slit width approximately 0.1 mm and slit separation 0.406 mm is used. don't yet get a choice of slit separations? if so, "was chosen" or "was used" would be better choices than "is used."

The slit-blocker is set at the position where light from both slits are allowed to pass, and the detector-slit is set at the position of the central maximum. The photodiode outputs a voltage that is proportional to the intensity of the laser beam. The laser beam intensity is constant. Don't you mean something related to the interference pattern that actually varies?

By changing the position of the detector-slit, intensity of the laser light is recorded by LabView as a function of location. same comment: not measuring intensity of laser light, measuring intensity of interference pattern due to constructive and destructive interference of the light waves diffracting from each slit (or slit edge). Don't say exactly that – I'm being wordy and overprecise here Then the experiment is repeated for single-slit when the slit-blocker blocks light from one of the two slits.

III. RESULTS

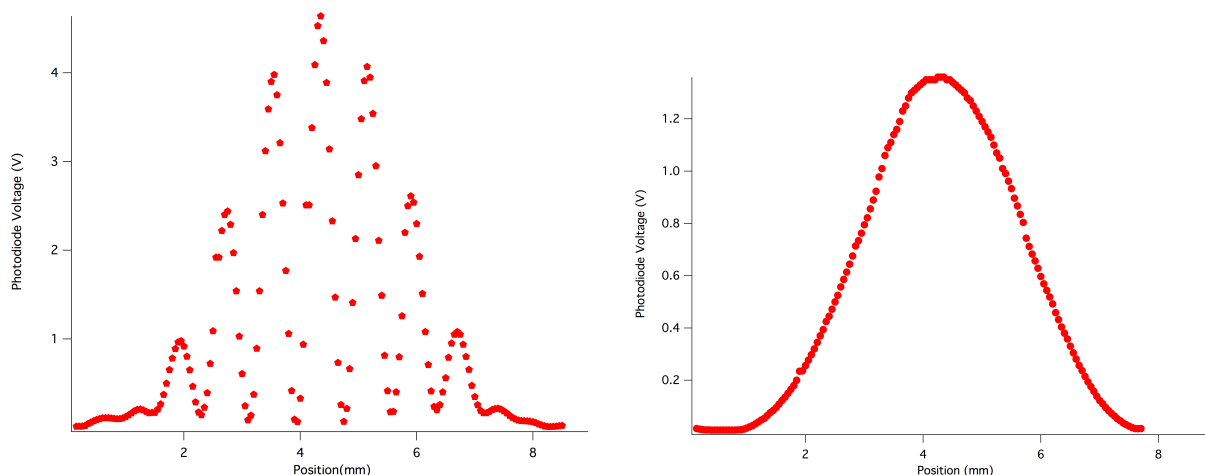


FIG. 3. Recorded data for double (left) and single-slit (right) interference experiments.

The recorded raw data for the double and single-slit experiments are shown in Fig.3. First looking at the double slit experiment, to create the curve of best fit, the Fraunhofer equation is applied to the double-slit intensity:

$$I = I_0 \text{sinc}^2\left(\frac{\pi a}{\lambda} \sin \theta\right) \cos^2\left(\frac{\pi d}{\lambda} \sin \theta\right) \quad (1)$$

there are special commands in LaTeX for trig functions. Please use them.

for example, use `\sin{\theta}` or `\sin(\theta)` or `\sin{\left(d/\lambda\right)}` rather than `sin \theta`

notice how much better the following looks:

$$I = I_0 \text{sinc}^2\left(\frac{\pi a}{\lambda} \sin \theta\right) \cos^2\left(\frac{\pi d}{\lambda} \sin \theta\right)$$

where, since not everyone who is a likely reader of this report would know what sinc is, you should define

$$\text{sinc}(\alpha) \equiv \frac{\sin(\alpha)}{\alpha}$$

Using plotting tools in Igor while applying Eq. 1, we can obtain the plot shown below in Fig. 4. just plotting tools? you didn't also use a non-linear least squares curve fitting routing? Calculation of the error bars will be included in the discussion section.

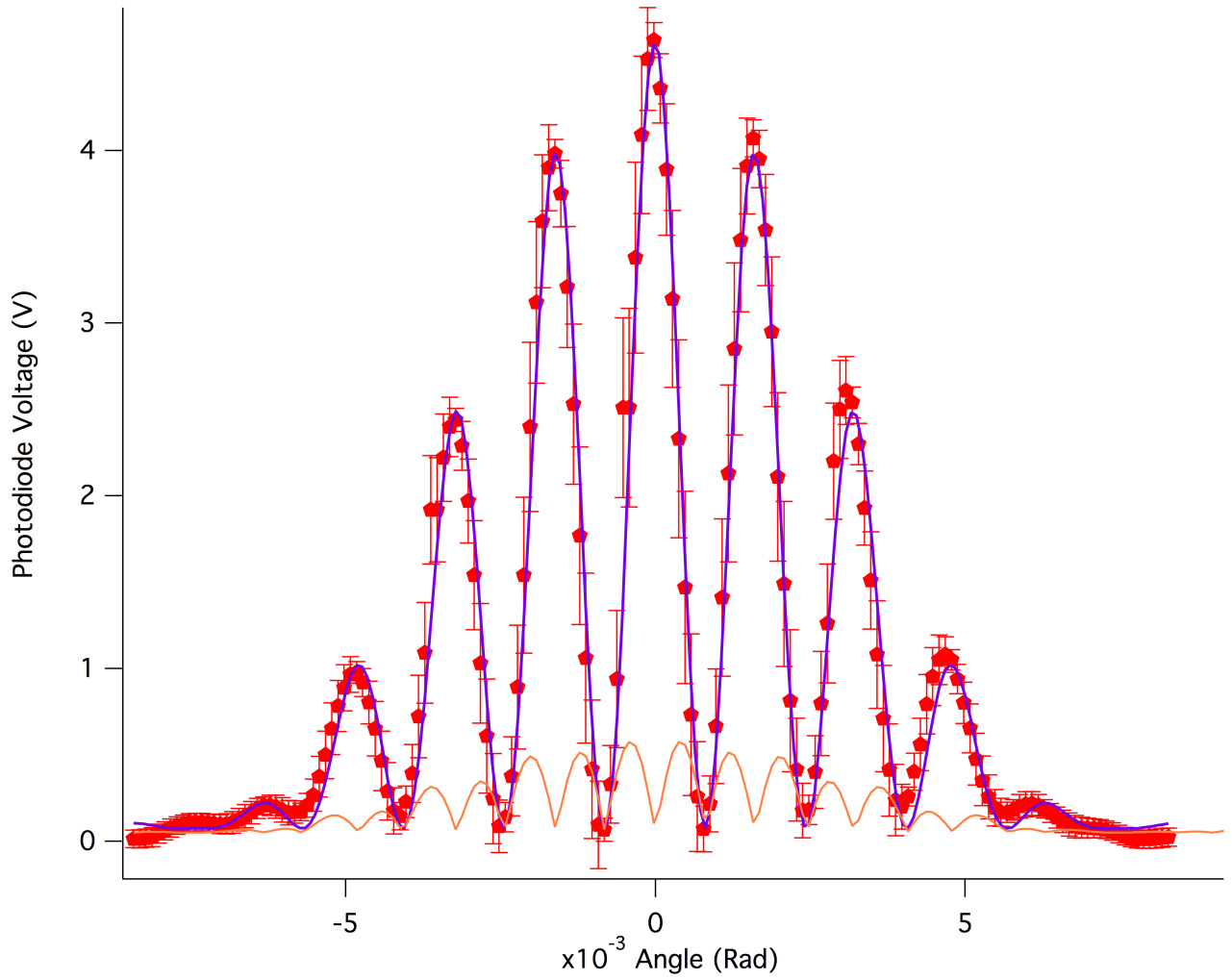


FIG. 4. Plot of raw data, error bars and fit curve of the double-slit experiment. The y-axis is the voltage the photodiode outputs which is proportional to the intensity of light shining on it, and the x-axis is the angle away from the central maximum (Fig. 5). The curve at the bottom of the graph shows the size of error as a function of angle.

The Fraunhofer conditions can be applied once again to create the curve of best fit for the single-slit experiment:

$$I = I_0 \text{sinc}^2\left(\frac{\pi a}{\lambda} \sin\theta\right) \quad (2)$$

see comments above regarding LaTeX commands for functions like sin and sinc, as well as use of larger parentheses

Using plotting tools in Igor while applying Eq.2, we can obtain the plot shown in Fig.6. Calculation of the error bars will be once again included in the discussion section for the

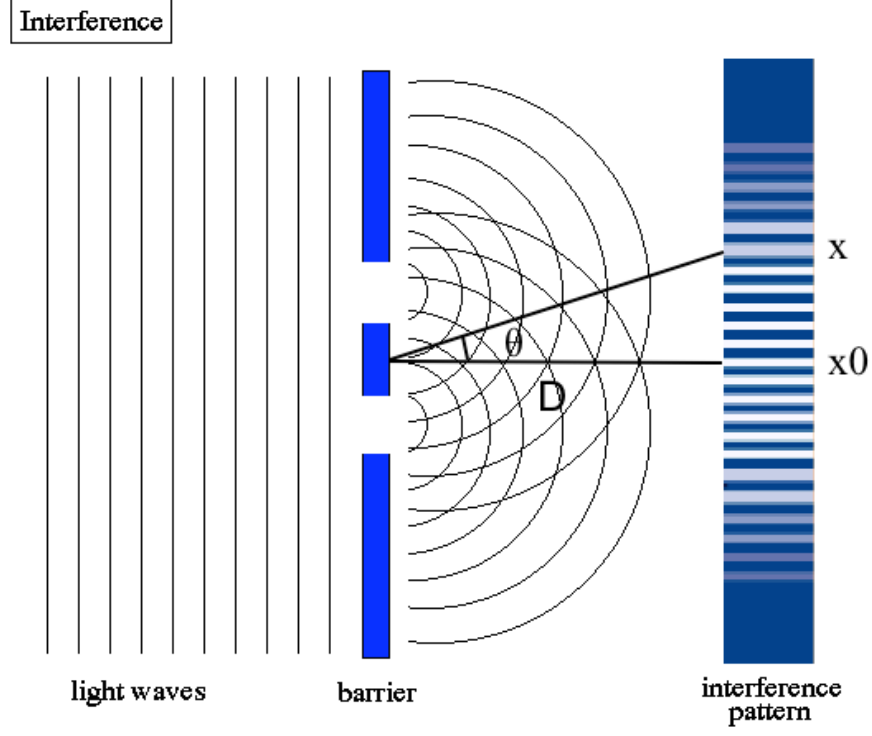


FIG. 5. Calculate angle from position³

TABLE I. Double-slit data. the variables a and d are missing from Figure 5, and in Figure 5 D is mislabeled as the length L from the slits to the detector instead of the distance d between the slits

Name	Symbol	Value	Uncertainties(\pm)
Slit width	a	$88.3 \mu m$	$0.4 \mu m$
Slit separation	d	$426.89 \mu m$	$0.07 \mu m$
Wavelength	λ	0.67 nm	N/A
Max voltage	V_0	4.55 V	0.07 V
Voltage offset	V_{offset}	0.073 V	0.008 V
Theta offset	θ_{offset}	$1\text{E-}05 \text{ rad}$	$8\text{E-}06 \text{ rad}$
Chi Squared	X^2	0.827068	

single slit experiment.

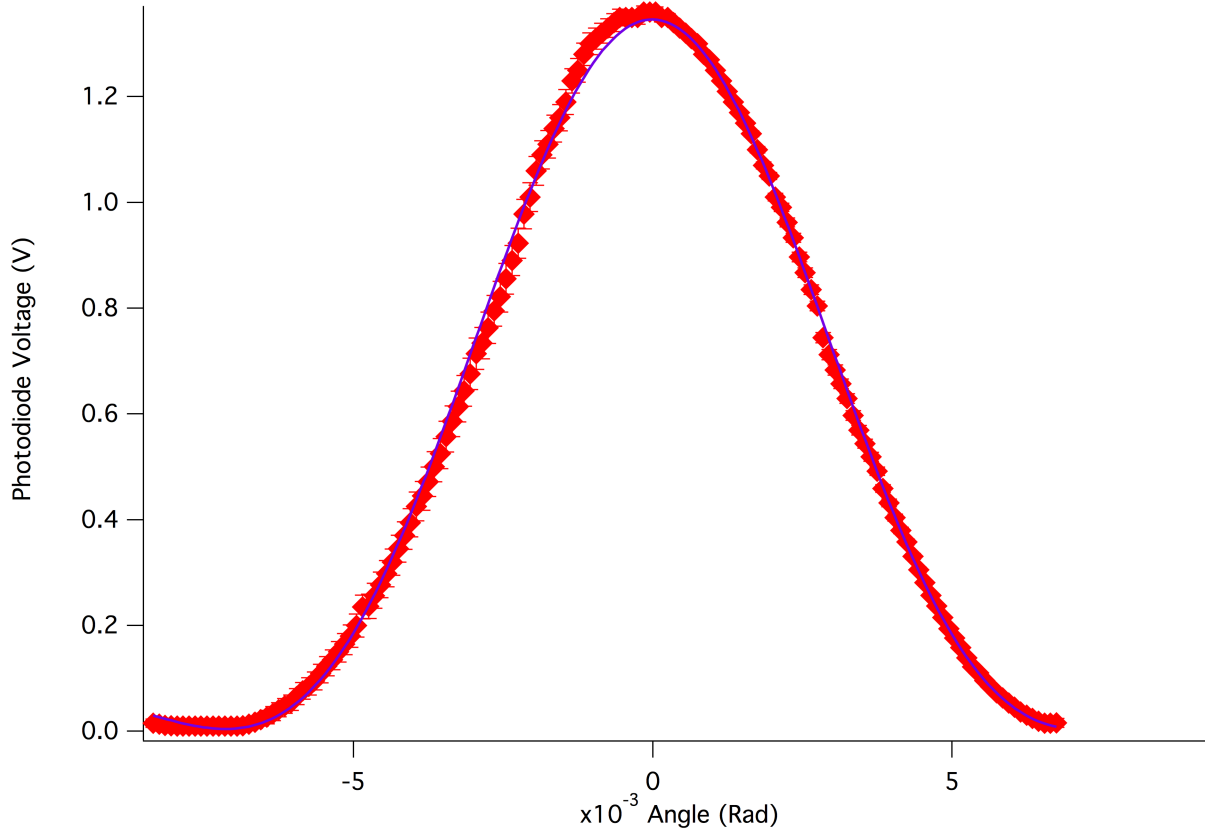


FIG. 6. Plot of raw data, error bars and fit curve of the single-slit experiment. The y-axis is still the output voltage of the photodiode, and the x-axis is the angle away from the central maximum.

IV. DISCUSSION

A. Double-Slit Experiment

The Fraunhofer/Fresnel theory (Eq.1) of interference gives the intensity of light as a function of angle. The photodiode we use to conduct the experiment outputs a voltage proportional to the intensity of light detected ($I = kV$), thus the intensity measurements can be replaced by the voltage readings and the analysis holds for both:

$$V = V_0 \text{sinc}^2\left(\frac{\pi a}{\lambda} \sin(\theta + \theta_{offset})\right) \cos^2\left(\frac{\pi d}{\lambda} \sin(\theta + \theta_{offset})\right) + V_{offset} \quad (3)$$

Several parameters are added to the original Fraunhofer model. V_{offset} is describing the affect of the background light. Although the photodiode is kept in a closed black box, there is a slight amount of background light, which will produce an offset and shift the whole

TABLE II. Single-slit data the variable a is missing from Figure 5. You also haven't yet defined some terms such as the two offsets. To solve this, introduce equation (3) earlier and/or note in this caption that terms are defined in equation (3) and a corrected version of figure 5

Name	Symbol	Value	Uncertainties(\pm)
Slit width	a	$93.9 \mu m$	$0.2 \mu m$
Wavelength	λ	0.67 nm	N/A
Max voltage	V_0	1.350 V	0.002 V
Voltage offset	V_{offset}	0.004 V	0.001 V
Theta offset	θ_{offset}	$1\text{E-}05 \text{ rad}$	$7\text{E-}06 \text{ rad}$
Chi Squared	χ^2	1.56815	

curve up. θ_{offset} describes the systematic error in angle, which is a result of the systematic error in position.

Some other parameters need fitting are slit width and slit separation. Due to manufacturing imperfection, the slit width and slit separation have slightly different values than given by the experiment manual. The wavelength of the laser might also be slightly off, but because equation m contains ratio terms $\frac{\pi a}{\lambda}$ and $\frac{\pi d}{\lambda}$, the numerator and denominator cannot change at the same time. Compared to a and d , λ is less likely to have a greatly different value, so it is held at $0.67 \mu m$. V_0 stands for the voltage measured at the central maximum.

Uncertainty in the variable (angle θ) is determined by applying error propagation. Each step of the detector-slit change is designed to be 0.05 mm on the micrometer, from $x_i = 0.15 \text{ mm}$ to $x_f = 8.35 \text{ mm}$. Angle θ corresponds to the position in radian (Fig. 5) is given by

$$\theta = \frac{\arctan(x - x_0)}{L} \quad (4)$$

L is the distance from the double-slit to the photodiode, is 50 cm given by the experiment manual. x_0 is found to be $4.4 \pm 0.1 \text{ mm}$ given by the Gaussian curve fit to the data set.

I suggest using L instead of D , to avoid confusion with d

However, due to human error in place of the vague and unhelpful term “human error” explain precisely what source of the error, such as “due to my lab partner hugging me each

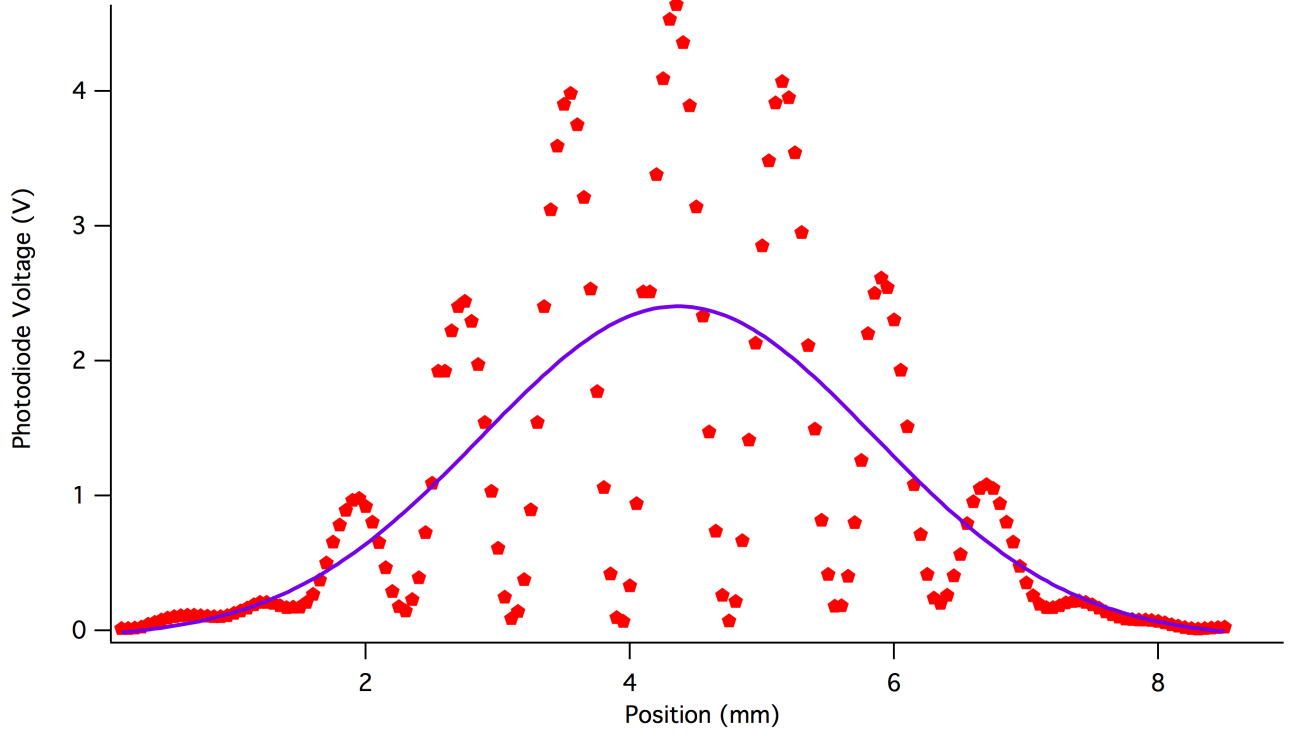


FIG. 7. Gaussian curve fit of double-slit interference is made to find the position where the intensity/output voltage of the photodiode peaks.

time I tried to advance the micrometer” or ”the precision of the micrometer is limited to 0.025 mm” or “since we can only set the micrometer position with a precision of 0.025 mm” or similar , each step is not perfectly 0.05mm, but $0.05 \pm 0.03mm$. Then the error in angle is given by taking derivative of Eq. 4 and multiply θ' by δx , which is 0.03mm.

$$\theta' = \frac{1}{L(1 + (x - x_0)^2)} \quad (5)$$

$$\delta\theta = \theta' \delta x = \frac{\delta x}{L(1 + (x - x_0)^2)} \quad (6)$$

$\delta\theta$ is a function of position x. The same method of taking derivative could be applied to find the error in voltage, but it is rather messy. So a different approach is adopted to find δV , which is to change θ in Eq. 3 by $\delta\theta$ and calculate the resulting change in V, which is then divided by 2.

$$\delta V = \frac{|V(\theta + \delta\theta) - V(\theta - \delta\theta)|}{2} \quad (7)$$

It can be seen that the same $\delta\theta$ has a smaller impact on δV when V' is small, and a bigger impact when V' is big.

The multimeter itself also contributes to the error in angle. We estimate the error in meter readings to be $0.05v$. So the overall δV is

$$\delta V_{total} = \delta V + \delta V_{meter} = \delta V + 0.05v \quad (8)$$

δV is plotted as a function of angle in Fig. 4.

The reduced χ^2 is calculated for the fit curve, yielding a value of 0.827. The value is close to 1, meaning that the fit is good within estimation of error. [and, more importantly, your results are well described by the Fraunhofer model for ? slit diffraction.](#)

B. Single-Slit Experiment

The intensity of light as a function of θ in single-slit experiment is given by the Fraunhofer/Fresnel theory in Eq. 2, which can then be transformed as

$$V = V_0 \cos^2\left(\frac{\pi d}{\lambda} \sin(\theta + \theta_{offset})\right) + V_{offset} \quad (9)$$

Parameters need fitting are slit width (a), slit separation (d), maximal voltage (V_0), offset in voltage (V_{offset}) due to background light, and offset in θ (θ_{offset}) due to systematic error of position.

Uncertainty is determined using the same method. θ is found using Eq. 4 while x goes from $x_i = 0.15mm$ to $x_f = 7.7mm$ with a step size of $0.05mm$. However, the value of x_0 need re-calculating, since the single-slit pattern is slightly shifted than the double-slit pattern. A Gaussian fit is done to the data to determine x_{offset} , which is $4.327 \pm 0.003mm$.

The slit to detector distance L remains $50cm$. Uncertainty in step size is also considered to be $0.03mm$, as in the double-slit experiment. Eq. 5, 6 and 7 are used to determine uncertainty in voltage. In the final step of calculating δV_{total} (Eq. 8), δV_{meter} is changed to

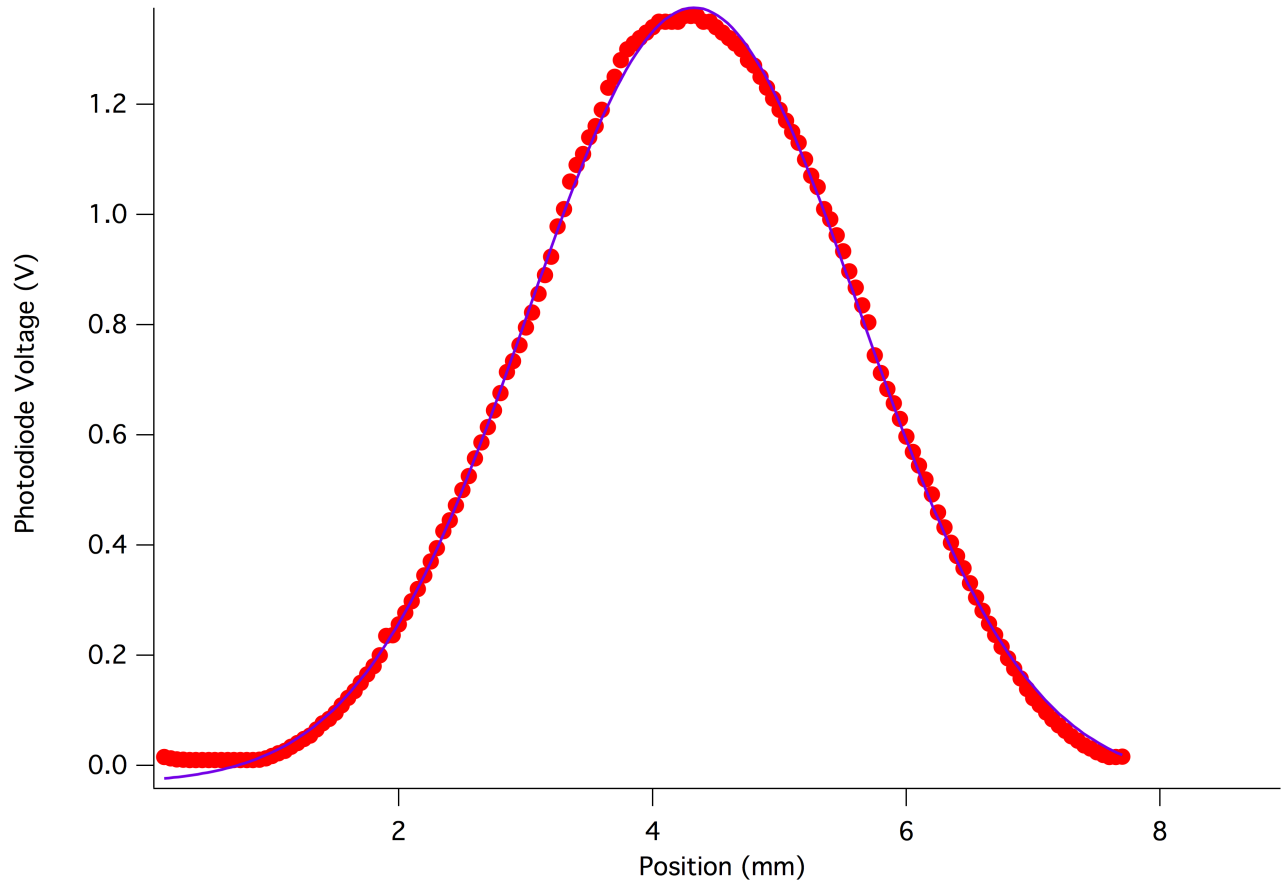


FIG. 8. Gaussian curve fit of single-slit diffraction is made to find the position where intensity/output voltage of the photodiode peaks.

0.01 v , because the single-slit pattern has smaller intensity and thus a fluctuation of smaller scale in voltage.

The reduced χ^2 is 1.56815, which is approximately 1, showing the fit is good within our estimate of error. not quite, but close. what is the probability that the model fits the data, if the reduced chi-square has a value of 1.6? Answer: if 6 or 7 degrees of freedom, then somewhere between 10 and 20 percent. See squires or <http://www.pd.infn.it/lunar-don/didattica/docsper2/TavoleChi2.pdf>, for example. You can see that there is a systematic error in Fig 8 between fit and data as position approaches zero and that the measured peak is slightly assymmetrical, perhaps because the traveling slit in front of the detector is slightly tilted?.

C. Comparison

Looking at parts A and B, we see that the the maximum voltage (V_0) for the double-slit is approximately 4 times the maximum voltage for the single-slit equation. This is because when two central maximums of the two slits are superposed, the amplitude doubles at the central maximum ($\theta = 0$). The intensity is proportional to the amplitude squared:

$$I \propto A^2 \quad 4I \propto (2A)^2$$

This relationship is clearly shown in our experiment:

$$\frac{V_{0,double}}{V_{0,single}} = \frac{A_{0,double}^2}{A_{0,single}^2} = \frac{4.55 \pm 0.07}{1.350 \pm 0.002} = 3.37 \pm 0.06 \approx 4$$

As we can see, the Voltage double slit quadrupled.

I don't think you can claim that a ratio of 3.37 clearly demonstrates that the signal quadrupled. Perhaps the photodiode response is starting to saturate at high intensities, and is no longer linear near the central peak of the two-slit pattern? Perhaps the traveling slit in front of the detector is slightly tilted, and therefore smooths out and (lowers the max value) of the peaks? What you can definitely claim, however, is that you have shown that due to wave inteference, the combined waves have a maximum intensity that is greater than that which would be expected in the absence of wave interference. That is, 3.37 is significantly greater than $1 + 1$, even if it is less than 4.

V. CONCLUSION

The observed interference pattern is fitted using Fraunhofer model, which describes far-field diffraction. The amplitude of the double-slit pattern was observed to be the modulated by the single slit diffraction pattern. Reduced χ^2 of the double-slit fit curve is 0.827 and that of the single-slit fit curve is 1.57.

need something here about how this demonstrates that light behaves as a wave (diffracting and interfering) rather than as a ray, as first demonstrated by Young

ACKNOWLEDGMENTS

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¹ Double Slit Experiment, <http://upload.wikimedia.org/wikipedia/commons/c/c2/Single_slit_and_double_slit2.jpg>.

² TeachSpin Instructions Manual, *Two-Slit interference, One Photon at a Time (TWS1-B), Pulse Counter/Interval Timer (PCIT1)*, 6/2013.

³ Young Two-Slit Experiment, http://abyss.uoregon.edu/~js/21st_century_science/lectures/lec13.html