



**North South University**  
Department of Electrical & Computer Engineering

**PROJECT REPORT**

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**Faculty:** Dr. S.M. Mahfuz Alam

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**Combinational and Sequential Seven-Segment Display Circuits**

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# Table of Contents

<b>Introduction</b>	3
<b>PHASE ONE: Combinational Part</b>	
<b>Truth Table</b>	4
<b>1<sup>st</sup> Canonical Forms</b>	5
<b>2<sup>nd</sup> Canonical Forms</b>	6
<b>SOP Forms</b>	
Boolean Equations with K-Maps	7
Circuit Diagram	9
<b>POS Forms with K-Maps</b>	
Boolean Equations with K-Maps	10
Circuit Diagram	12
<b>NAND Gate Implementation</b>	
Explanation	13
Boolean Equations	13
Circuit Diagram	14
<b>NOR Gate Implementation</b>	
Explanation	15
Boolean Equations	15
Circuit Diagram	16
<b>Decoder Implementation</b>	
Explanation	17
Circuit Diagram	17
<b>MUX Implementation</b>	
Explanation	18

Circuit Diagram	18
<b>Hardware Implementation</b>	
Choice of Implementation	19
Cost of Implementation	19
 <b>PHASE TWO: Sequential Part</b>	
<b>Preface</b>	20
<b>State Diagram</b>	20
<b>JK Flip-Flop Implementation</b>	
State Table	21
Flip-Flop Equations with K-Maps	21
Circuit Diagram	23
<b>D Flip-Flop Implementation</b>	
State Table	24
Flip-Flop Equations with K-Maps	25
Circuit Diagram	26
<b>T Flip-Flop Implementation</b>	
State Table	27
Flip-Flop Equations with K-Maps	28
Circuit Diagram	29
<b>Hardware Implementation</b>	
Choice of Implementation	30
Cost of Implementation	30
 <b>Limitations</b>	31
 <b>Conclusion</b>	31

# Introduction

The project report serves as a documentation for the logic, design and implementation of the various forms of a seven-segment display circuit. The circuit is expected to generate the sequence 2S-10321DLDD, with each character corresponding to one of 12 different inputs or states.

The project is divided into two parts based on the fundamental circuit logic types: combinational logic, and sequential logic. For each part, numerous alternative designs of the circuit are presented. From among them only one is chosen for the hardware implementation, whereas all of them are implemented using software such as Logisim.

Therefore, as an implication, the purpose of this project is to test, assess and apply the culmination of one's skills and knowledge of digital logic design acquired through the course and lab works.

# PHASE 1: COMBINATIONAL PART

## Truth Table

Ref.	Inputs				Outputs						
	$w$	$x$	$y$	$z$	$A$	$B$	$C$	$D$	$E$	$F$	$G$
0	0	0	0	0	1	1	0	1	1	0	1
1	0	0	0	1	1	0	1	1	0	1	1
2	0	0	1	0	0	0	0	0	0	0	1
3	0	0	1	1	0	1	1	0	0	0	0
4	0	1	0	0	1	1	1	1	1	1	0
5	0	1	0	1	1	1	1	1	0	0	1
6	0	1	1	0	1	1	0	1	1	0	1
7	0	1	1	1	0	1	1	0	0	0	0
8	1	0	0	0	0	1	1	1	1	0	1
9	1	0	0	1	0	0	0	1	1	1	0
10	1	0	1	0	0	1	1	1	1	0	1
11	1	0	1	1	0	1	1	1	1	0	1
12	1	1	0	0	x	x	x	x	x	x	x
13	1	1	0	1	x	x	x	x	x	x	x
14	1	1	1	0	x	x	x	x	x	x	x
15	1	1	1	1	x	x	x	x	x	x	x

## 1<sup>st</sup> Canonical Forms

$$\begin{aligned} A(w, x, y, z) &= \sum (0, 1, 4, 5, 6) \\ &= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}xy\bar{z} \end{aligned}$$

$$\begin{aligned} B(w, x, y, z) &= \sum (0, 3, 4, 5, 6, 7, 8, 10, 11) \\ &= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}xy\bar{z} + \bar{w}xyz + w\bar{x}\bar{y}\bar{z} + w\bar{x}\bar{y}z \\ &\quad + w\bar{x}yz \end{aligned}$$

$$\begin{aligned} C(w, x, y, z) &= \sum (1, 3, 4, 5, 7, 8, 10, 11) \\ &= \bar{w}\bar{x}\bar{y}z + \bar{w}\bar{x}yz + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}xy\bar{z} + w\bar{x}\bar{y}\bar{z} + w\bar{y}x\bar{z} + w\bar{x}yz \end{aligned}$$

$$\begin{aligned} D(w, x, y, z) &= \sum (0, 1, 4, 5, 6, 8, 9, 10, 11) \\ &= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}x\bar{y}\bar{z} + \bar{w}x\bar{y}z + \bar{w}xy\bar{z} + w\bar{x}\bar{y}\bar{z} + w\bar{x}\bar{y}z + w\bar{x}yz \\ &\quad + w\bar{y}xz \end{aligned}$$

$$\begin{aligned} E(w, x, y, z) &= \sum (0, 4, 6, 8, 9, 10, 11) \\ &= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}x\bar{y}\bar{z} + \bar{w}xy\bar{z} + w\bar{x}\bar{y}\bar{z} + w\bar{x}\bar{y}z + w\bar{y}x\bar{z} + w\bar{x}yz \end{aligned}$$

$$F(w, x, y, z) = \sum (1, 4, 9) = \bar{w}\bar{x}\bar{y}z + \bar{w}x\bar{y}\bar{z} + w\bar{x}\bar{y}z$$

$$\begin{aligned} G(w, x, y, z) &= \sum (0, 1, 2, 5, 6, 8, 10, 11) \\ &= \bar{w}\bar{x}\bar{y}\bar{z} + \bar{w}\bar{x}\bar{y}z + \bar{w}\bar{x}y\bar{z} + \bar{w}x\bar{y}z + \bar{w}xy\bar{z} + w\bar{x}\bar{y}\bar{z} + w\bar{x}\bar{y}z + w\bar{x}yz \end{aligned}$$

## 2<sup>nd</sup> Canonical Forms

$$\begin{aligned} A(w, x, y, z) &= \prod (2, 3, 7, 8, 9, 10, 11) \\ &= (w + x + \bar{y} + z)(w + x + \bar{y} + \bar{z})(w + \bar{x} + \bar{y} + \bar{z})(\bar{w} + x + y \\ &\quad + z)(\bar{w} + x + y + \bar{z})(\bar{w} + x + \bar{y} + z)(\bar{w} + x + \bar{y} + \bar{z}) \end{aligned}$$

$$\begin{aligned} B(w, x, y, z) &= \prod (1, 2, 9) \\ &= (w + x + y + \bar{z})(w + x + \bar{y} + z)(\bar{w} + x + y + \bar{z}) \end{aligned}$$

$$\begin{aligned} C(w, x, y, z) &= \prod (0, 2, 6, 9) \\ &= (w + x + y + z)(w + x + \bar{y} + z)(w + \bar{x} + \bar{y} + z)(\bar{w} + x + y + \bar{z}) \end{aligned}$$

$$\begin{aligned} D(w, x, y, z) &= \prod (2, 3, 7) \\ &= (w + x + \bar{y} + z)(w + x + \bar{y} + \bar{z})(w + \bar{x} + \bar{y} + \bar{z}) \end{aligned}$$

$$\begin{aligned} E(w, x, y, z) &= \prod (1, 2, 3, 5, 7) \\ &= (w + x + y + \bar{z})(w + x + \bar{y} + z)(w + x + \bar{y} + \bar{z})(w + \bar{x} + y \\ &\quad + \bar{z})(w + \bar{x} + \bar{y} + \bar{z}) \end{aligned}$$

$$\begin{aligned} F(w, x, y, z) &= \prod (0, 2, 3, 5, 6, 7, 8, 10, 11) \\ &= (w + x + y + z)(w + x + \bar{y} + z)(w + x + \bar{y} + \bar{z})(w + \bar{x} + y \\ &\quad + \bar{z})(w + \bar{x} + \bar{y} + z)(w + \bar{x} + \bar{y} + \bar{z})(\bar{w} + x + y + z)(\bar{w} + x + \bar{y} \\ &\quad + z)(\bar{w} + x + \bar{y} + \bar{z}) \end{aligned}$$

$$\begin{aligned} G(w, x, y, z) &= \prod (3, 4, 7, 9) \\ &= (w + x + \bar{y} + \bar{z})(w + \bar{x} + y + z)(w + \bar{x} + \bar{y} + \bar{z})(\bar{w} + x + y + \bar{z}) \end{aligned}$$

## Sum of Product Forms (SOP)

### Boolean Equations with K-Maps

*A*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	1	1		
	01	1	1		1
	11	x	x	x	x
	10				

$$A(w, x, y, z) = \bar{w}\bar{y} + x\bar{z}$$

*B*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	1		1	
	01	1	1	1	1
	11	x	x	x	x
	10	1		1	1

$$B(w, x, y, z) = x + w\bar{z} + yz + \bar{y}\bar{z}$$

*C*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00		1	1	
	01	1	1	1	
	11	x	x	x	x
	10	1		1	1

$$C(w, x, y, z) = wy + w\bar{z} + \bar{w}z + x\bar{y}$$

*D*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	1	1		
	01	1	1		1
	11	x	x	x	x
	10	1	1	1	1

$$D(w, x, y, z) = w + \bar{y} + x\bar{z}$$



*E*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	1			
	01	1			1
	11	x	x	x	x
	10	1	1	1	1

$$E(w, x, y, z) = w + x\bar{z} + \bar{y}z$$

*F*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00		1		
	01	1			
	11	x	x	x	x
	10		1		

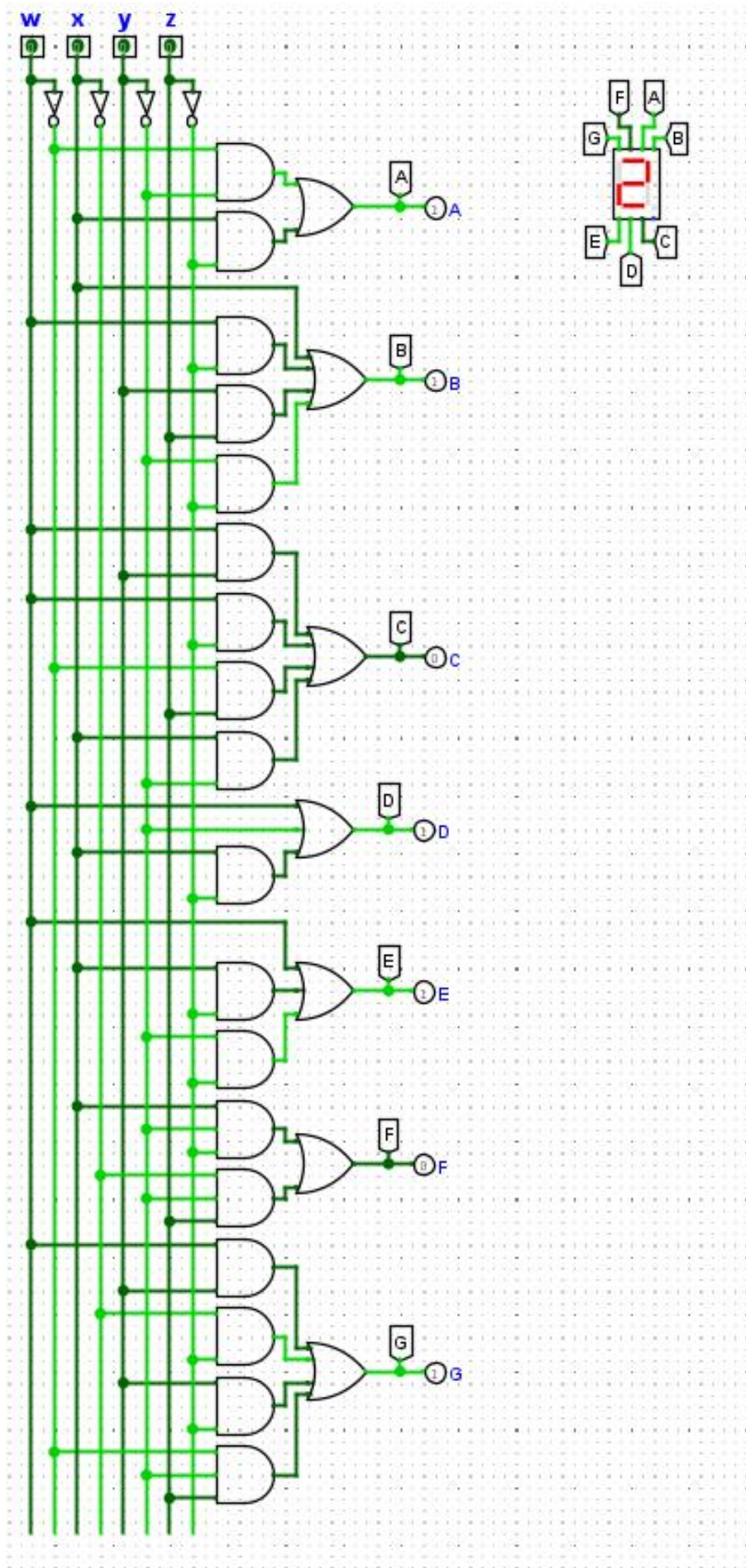
$$F(w, x, y, z) = x\bar{y}z + \bar{x}\bar{y}z$$

*G*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	1	1		1
	01		1		1
	11	x	x	x	x
	0	1		1	1

$$G(w, x, y, z) = wy + \bar{x}\bar{z} + y\bar{z} + \bar{w}\bar{y}z$$

## Circuit Diagram



## Product of Sum Forms (POS)

### Boolean Equations with K-Maps

*A*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00			0	0
	01			0	
	11	x	x	x	x
	10	0	0	0	0

$$A(w, x, y, z) = \bar{w}(x + \bar{y})(\bar{y} + \bar{z})$$

*B*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00		0		0
	01				
	11	x	x	x	x
	10		0		

$$B(w, x, y, z) = (x + y + \bar{z})(w + x + \bar{y} + z)$$

*C*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00	0			0
	01				0
	11	x	x	x	x
	10		0		

$$C(w, x, y, z) = (w + x + z)(w + \bar{y} + z)(\bar{w} + y + \bar{z})$$

*D*

		<i>yz</i>			
		00	01	11	10
<i>wx</i>	00			0	0
	01			0	
	11	x	x	x	x
	10				

$$D(w, x, y, z) = (w + x + \bar{y})(w + \bar{y} + \bar{z})$$

$E$

		$yz$			
		00	01	11	10
$wx$	00		0	0	0
	01		0	0	
	11	x	x	x	x
	10				

$$E(w, x, y, z) = (w + \bar{z})(w + x + \bar{y})$$

$F$

		$yz$			
		00	01	11	10
$wx$	00	0		0	0
	01		0	0	0
	11	x	x	x	x
	10	0		0	0

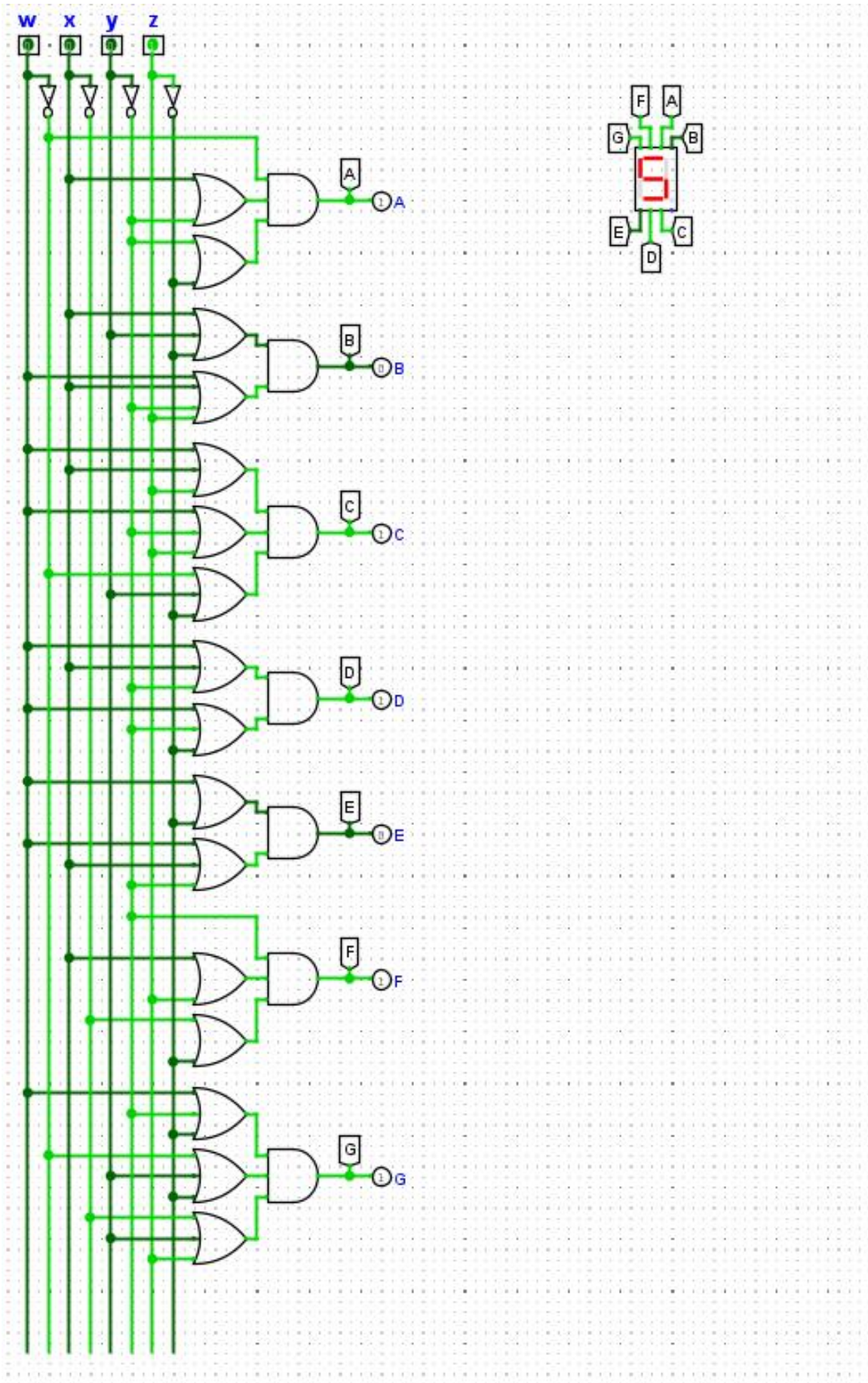
$$F(w, x, y, z) = \bar{y}(x + z)(\bar{x} + \bar{z})$$

$G$

		$yz$			
		00	01	11	10
$wx$	00			0	
	01	0		0	
	11	x	x	x	x
	10		0		

$$G(w, x, y, z) = (w + \bar{y} + \bar{z})(\bar{w} + y + \bar{z})(\bar{x} + y + z)$$

## Circuit Diagram



## NAND Gate Implementation

### Explanation

One way to figure out an implementation of the seven-segment display circuit using only NAND gates is by transformation each output function in SOP form so that the only operators involved are the NOT and AND operators (which are combined to represent the NAND operator). Then, on the basis of these alternative expressions the circuit is built.

### Boolean Equations

$$A(w, x, y, z) = \bar{w}\bar{y} + x\bar{z} = \overline{\overline{\bar{w}\bar{y} + x\bar{z}}} = \overline{\bar{w}\bar{y}} \overline{x\bar{z}}$$

$$B(w, x, y, z) = x + w\bar{z} + yz + \bar{y}\bar{z} = \overline{\overline{x + w\bar{z} + yz + \bar{y}\bar{z}}} = \overline{\bar{x} \bar{w}\bar{z} \bar{y}\bar{z}}$$

$$C(w, x, y, z) = wy + w\bar{z} + \bar{w}z + x\bar{y} = \overline{\overline{wy + w\bar{z} + \bar{w}z + x\bar{y}}} = \overline{\bar{w}\bar{y}} \overline{\bar{w}\bar{z}} \overline{\bar{w}z} \overline{x\bar{y}}$$

$$D(w, x, y, z) = w + \bar{y} + x\bar{z} = \overline{\overline{w + \bar{y} + x\bar{z}}} = \overline{\bar{w} \bar{y} \bar{x}\bar{z}}$$

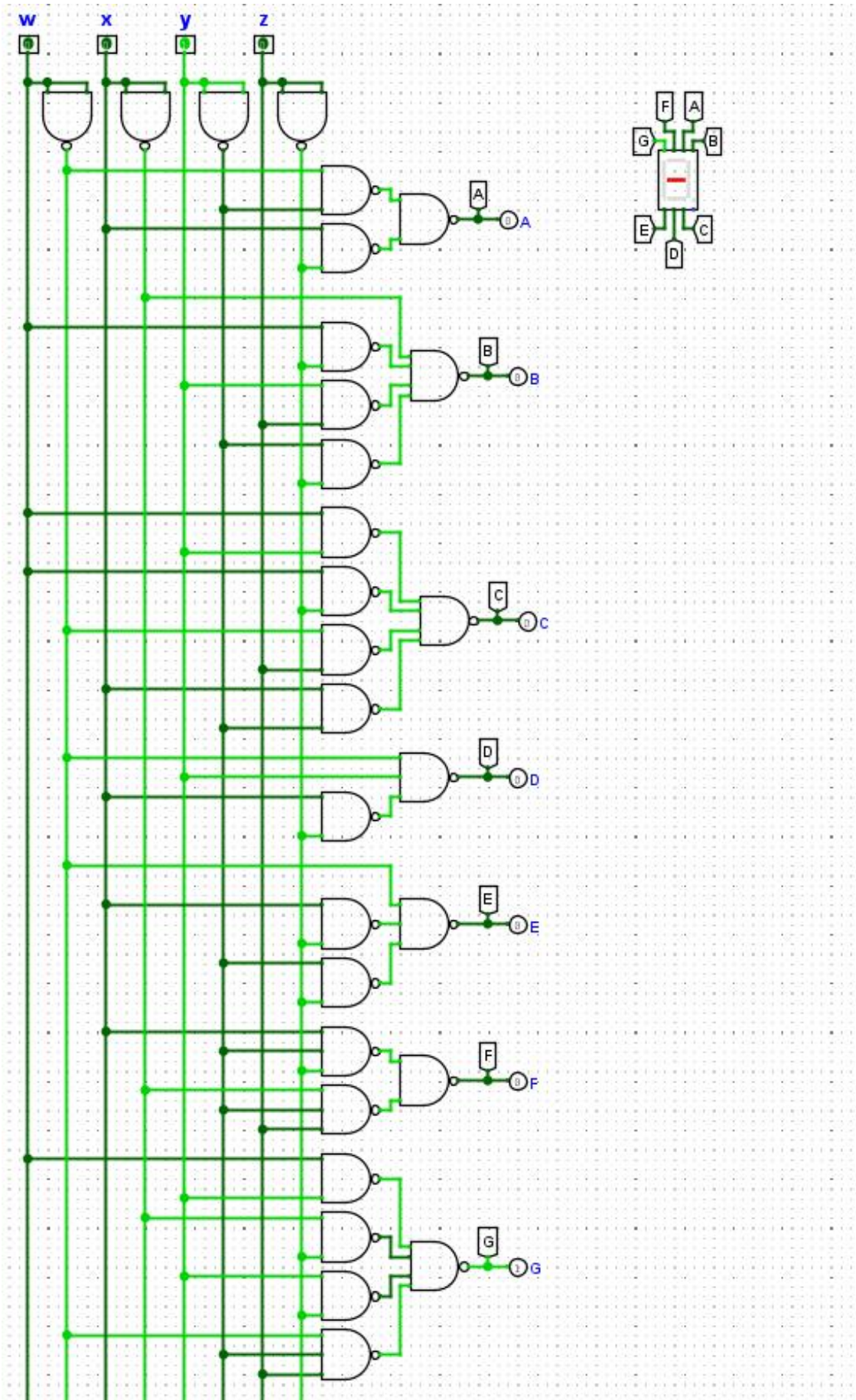
$$E(w, x, y, z) = w + x\bar{z} + \bar{y}\bar{z} = \overline{\overline{w + x\bar{z} + \bar{y}\bar{z}}} = \overline{\bar{w} \bar{x}\bar{z} \bar{y}\bar{z}}$$

$$F(w, x, y, z) = x\bar{y}\bar{z} + \bar{x}\bar{y}z = \overline{\overline{x\bar{y}\bar{z} + \bar{x}\bar{y}z}} = \overline{\bar{x}\bar{y}\bar{z}} \overline{\bar{x}\bar{y}z}$$

$$G(w, x, y, z) = wy + \bar{x}\bar{z} + y\bar{z} + \bar{w}\bar{y}z = \overline{\overline{wy + \bar{x}\bar{z} + y\bar{z} + \bar{w}\bar{y}z}} = \overline{\bar{w}\bar{y}} \overline{\bar{x}\bar{z}} \overline{y\bar{z}} \overline{\bar{w}\bar{y}z}$$



## Circuit Diagram



## NOR Gate Implementation

### Explanation

One way to figure out an implementation of the seven-segment display circuit using only NOR gates is by transformation each output function in POS form so that the only operators involved are the NOT and OR operators (which are combined to represent the NOR operator). Then, on the basis of these alternative expressions the circuit is built.

### Boolean Expressions

$$A(w, x, y, z) = \bar{w}(x + \bar{y})(\bar{y} + \bar{z}) = \overline{\overline{\bar{w}(x + \bar{y})(\bar{y} + \bar{z})}} = \overline{w + (x + \bar{y}) + (\bar{y} + \bar{z})}$$

$$\begin{aligned} B(w, x, y, z) &= (x + y + \bar{z})(w + x + \bar{y} + z) = \overline{\overline{(x + y + \bar{z})(w + x + \bar{y} + z)}} \\ &= \overline{(x + y + \bar{z}) + (w + x + \bar{y} + z)} \end{aligned}$$

$$\begin{aligned} C(w, x, y, z) &= (w + x + z)(w + \bar{y} + z)(\bar{w} + y + \bar{z}) \\ &= \overline{\overline{(w + x + z)(w + \bar{y} + z)(\bar{w} + y + \bar{z})}} \\ &= \overline{(w + x + z) + (w + \bar{y} + z) + (\bar{w} + y + \bar{z})} \end{aligned}$$

$$\begin{aligned} D(w, x, y, z) &= (w + x + \bar{y})(w + \bar{y} + \bar{z}) = \overline{\overline{(w + x + \bar{y})(w + \bar{y} + \bar{z})}} \\ &= \overline{(w + x + \bar{y}) + (w + \bar{y} + \bar{z})} \end{aligned}$$

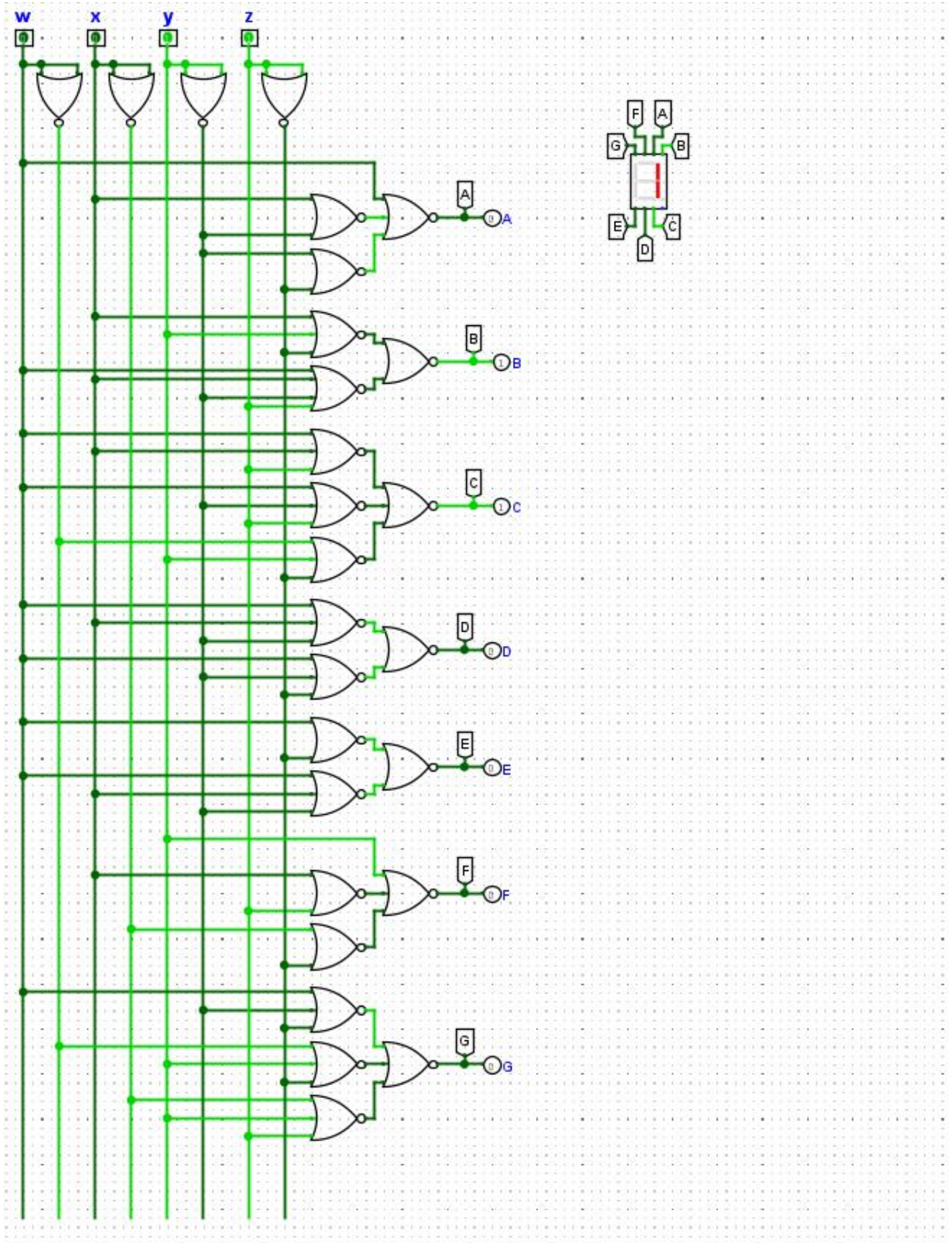
$$\begin{aligned} E(w, x, y, z) &= (w + \bar{z})(w + x + \bar{y}) = \overline{\overline{(w + \bar{z})(w + x + \bar{y})}} \\ &= \overline{(w + \bar{z}) + (w + x + \bar{y})} \end{aligned}$$

$$F(w, x, y, z) = \bar{y}(x + z)(\bar{x} + \bar{z}) = \overline{\overline{\bar{y}(x + z)(\bar{x} + \bar{z})}} = \overline{y + (x + z) + (\bar{x} + \bar{z})}$$

$$\begin{aligned} G(w, x, y, z) &= (w + \bar{y} + \bar{z})(\bar{w} + y + \bar{z})(\bar{x} + y + z) \\ &= \overline{\overline{(w + \bar{y} + \bar{z})(\bar{w} + y + \bar{z})(\bar{x} + y + z)}} \\ &= \overline{(w + \bar{y} + \bar{z}) + (\bar{w} + y + \bar{z}) + (\bar{x} + y + z)} \end{aligned}$$



## Circuit Diagram

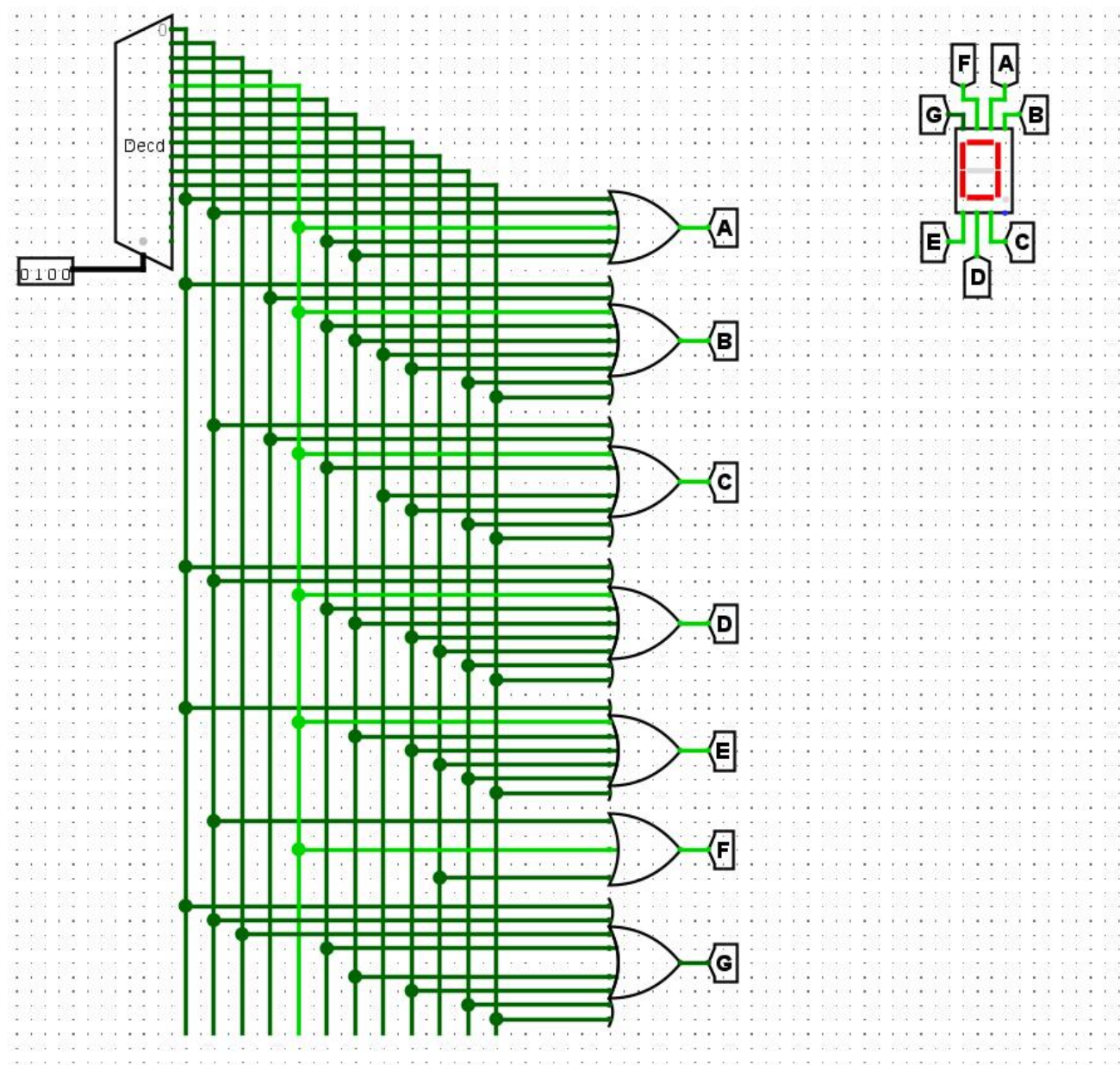


## Decoder Implementation

### Explanation

In constructing a seven-segment display circuit with an active-high 4-to-16 line decoder, the output activated by a specific select input combination serves the purpose of illuminating the segments essential for forming the related character. Each segment is turned on for more than one binary code, so the input to it is controlled by a multi-input OR gate that connects all the decoder outputs activated by the corresponding binary input combinations. Note that the decoder outputs for inputs 1100 to 1111 are not driven to any of the segments.

### Circuit Diagram



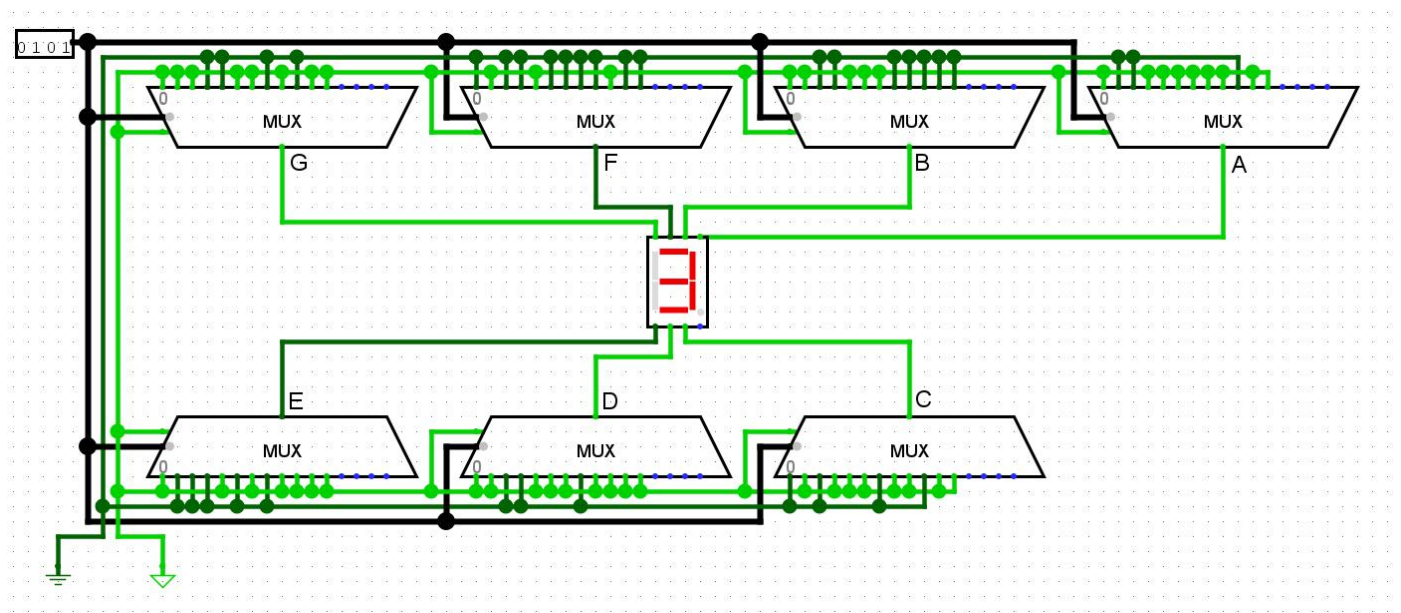


## MUX Implementation

### Explanation

Linked to each segment of the display is the output of a 16-to-1 multiplexer. Each data input of the MUX is connected to either the power supply (HIGH) or ground (LOW), depending on whether or not it activates the segment due to a certain combination of selection bits. This means that the data inputs directly evaluate to the output of the function, which is consistent with the truth table. However, as a consequence of this fact, all the multiplexers share the characteristics that the data inputs from  $I_{12}$  to  $I_{15}$  do not provide any relevant information, representing the don't care conditions.

### Circuit Diagram



## Hardware Implementation

### Choice of Implementation

The choice of implementation depends on four factors to varying degrees: cost, complexity, and availability of materials. The MUX and decoder implementations were ignored, since the required ICs are difficult to come by. Moreover, using multiplexers and decoders with lesser input/output lines vastly complicates the circuit design by greatly increasing the number of connections. Among the rest of the implementations, the SOP form and the NAND gate ones stand out as optimal due to the fact that they require the least number of gates, thus minimizing cost and complexity of the circuit. However, the former of the two was chosen due to following reasons: (a) multi-input AND and OR gates can be more easily decomposed into a collection of interconnected two-input gates (b) as a result, repeated terms between equations (e.g.  $x\bar{z}$  in  $D$  and  $E$ ) would only need to be implemented once and shared among the corresponding circuit segments. Thus, the circuit can be further simplified using only ICs containing gates with no more than two inputs, reducing costs.

The materials for hardware implementation is listed in the following section.

### Cost of Implementation

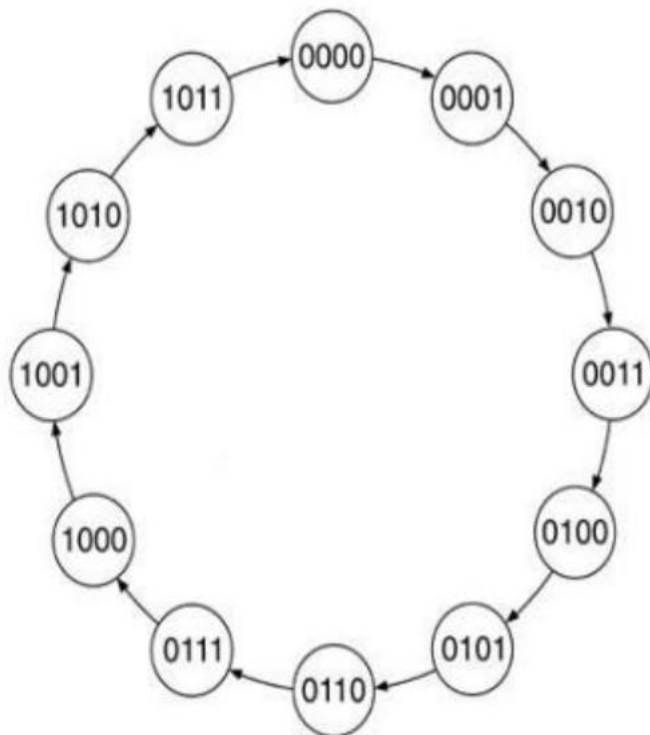
Index	Name	Cost Per Unit	Quantity	Total Cost
1	Breadboard (Large)	140	3	420
2	Male-to-Male Connectors x40	120	3	360
3	9V Battery	80	1	80
4	Battery Connector	15	1	15
5	5V Voltage Regulator	20	1	20
6	Seven Segment Display (Common Cathode)	15	1	15
7	Push Down Switch	15	4	60
8	IC 7404 Hex Inverters NOT Gates	30	1	30
9	IC 7408 Quad Two-Input AND Gates	30	4	120
10	IC 7432 Quad Two-Input OR Gates	30	4	120
<b>CUMULATIVE TOTAL</b>				<b>1240</b>

# PHASE 2: SEQUENTIAL PART

## Preface

As a sequential circuit, the seven-segment display should display each character in sequence between constant time intervals. This can be achieved in many ways. In this project, we have decided to design a synchronous MOD 12 up-counter, using the JK, D, and T flip-flops, that counts from 0000 to 1011 incrementally with every clock pulse. This means, the counter circuit requires 4 flip-flops, representing the bits of the binary code. The output of each flip-flop is then directed to the corresponding input of the SOP form of the combinational circuit connected to the seven-segment display. In this way, the characters in the sequence are displayed one-by-one as long as the counter is powered or the clock pulses are delivered.

## State Diagram



# JK Flip-Flop Implementation

## State Table

Present State				Next State				Flip Flop Inputs							
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$	$J_3$	$K_3$	$J_2$	$K_2$	$J_1$	$K_1$	$J_0$	$K_0$
0	0	0	0	0	0	0	1	0	x	0	x	0	x	1	x
0	0	0	1	0	0	1	0	0	x	0	x	1	x	x	1
0	0	1	0	0	0	1	1	0	x	0	x	x	0	1	x
0	0	1	1	0	1	0	0	0	x	1	x	x	1	x	1
0	1	0	0	0	1	0	1	0	x	x	0	0	x	1	x
0	1	0	1	0	1	1	0	0	x	x	0	1	x	x	1
0	1	1	0	0	1	1	1	0	x	x	0	x	0	1	x
0	1	1	1	1	0	0	0	1	x	x	1	x	1	x	1
1	0	0	0	1	0	0	1	x	0	0	x	0	x	1	x
1	0	0	1	1	0	1	0	x	0	0	x	1	x	x	1
1	0	1	0	1	0	1	1	x	0	0	x	x	0	1	x
1	0	1	1	0	0	0	0	x	1	0	x	x	1	x	1
1	1	0	0	x	x	x	x	x	x	x	x	x	x	x	x
1	1	0	1	x	x	x	x	x	x	x	x	x	x	x	x
1	1	1	0	x	x	x	x	x	x	x	x	x	x	x	x

## Flip-Flop Input Equations with K-Maps

$J_3$

$Q_1Q_0$

	00	01	11	10
$Q_3Q_2$ 00				
01			1	
11	x	x	x	x
10	x	x	x	x

$$J_3(Q_3, Q_2, Q_1, Q_0) = Q_2Q_1Q_0$$

$K_3$

$Q_1Q_0$

	00	01	11	10
$Q_3Q_2$ 00	x	x	x	x
01	x	x	x	x
11	x	x	x	x
10			1	

$$K_3(Q_3, Q_2, Q_1, Q_0) = Q_1Q_0$$

$J_2$

$Q_1Q_0$

$K_2$

$Q_1Q_0$

		00	01	11	10
$Q_3\bar{Q}_2$	00			1	
	01	x	x	x	x
	11	x	x	x	x
	10				

$$J_2(Q_3, Q_2, Q_1, Q_0) = \bar{Q}_3 Q_1 Q_0$$

		00	01	11	10
$Q_3\bar{Q}_2$	00	x	x	x	x
	01			1	
	11	x	x	x	x
	10	x	x	x	x

$$K_2(Q_3, Q_2, Q_1, Q_0) = Q_1 Q_0$$

		$Q_1 Q_0$			
		00	01	11	10
$Q_3\bar{Q}_2$	00		1	x	x
	01		1	x	x
	11	x	x	x	x
	10		1	x	x

$$J_1(Q_3, Q_2, Q_1, Q_0) = Q_0$$

		$Q_1 Q_0$			
		00	01	11	10
$Q_3\bar{Q}_2$	00	x	x	1	
	01	x	x	1	
	11	x	x	x	x
	10	x	x	1	

$$K_1(Q_3, Q_2, Q_1, Q_0) = Q_0$$

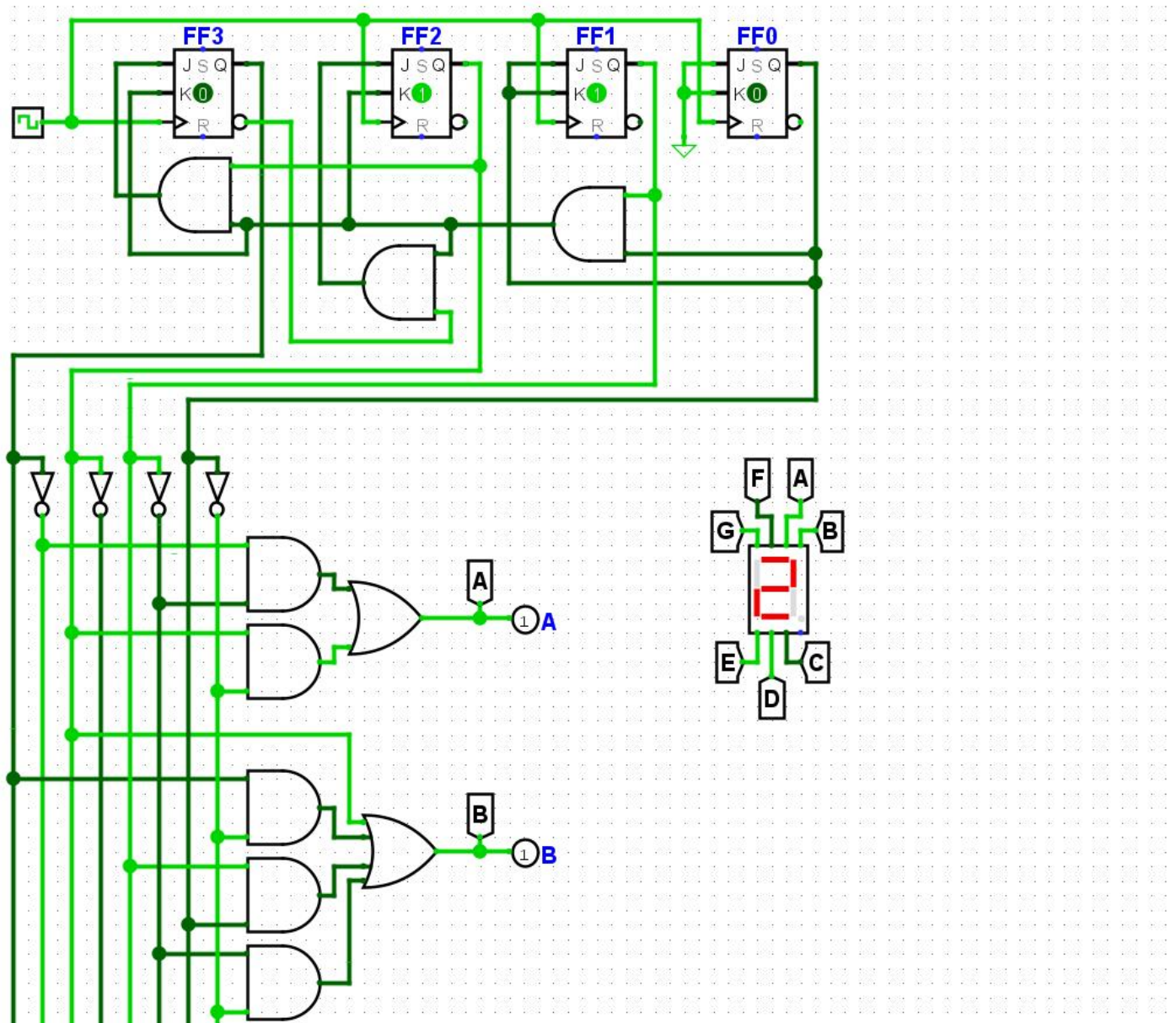
		$Q_1 Q_0$			
		00	01	11	10
$Q_3\bar{Q}_2$	00	1	x	x	1
	01	1	x	x	1
	11	x	x	x	x
	10	1	x	x	1

$$J_0(Q_3, Q_2, Q_1, Q_0) = 1$$

		$Q_1 Q_0$			
		00	01	11	10
$Q_3\bar{Q}_2$	00	x	1	1	x
	01	x	1	1	x
	11	x	x	x	x
	10	x	1	1	x

$$K_0(Q_3, Q_2, Q_1, Q_0) = 1$$

## Circuit Diagram





## D Flip-Flop Implementation

State Table

Present State				Next State				Flip Flop Inputs			
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$	$D_3$	$D_2$	$D_1$	$D_0$
0	0	0	0	0	0	0	1	0	0	0	1
0	0	0	1	0	0	1	0	0	0	1	0
0	0	1	0	0	0	1	1	0	0	1	1
0	0	1	1	0	1	0	0	0	1	0	0
0	1	0	0	0	1	0	1	0	1	0	1
0	1	0	1	0	1	1	0	0	1	1	0
0	1	1	0	0	1	1	1	0	1	1	1
0	1	1	1	1	0	0	0	1	0	0	0
1	0	0	0	1	0	0	1	1	0	0	1
1	0	0	1	1	0	1	0	1	0	1	0
1	0	1	0	1	0	1	1	1	0	1	1
1	0	1	1	0	0	0	0	0	0	0	0
1	1	0	0	x	x	x	x	x	x	x	x
1	1	0	1	x	x	x	x	x	x	x	x
1	1	1	0	x	x	x	x	x	x	x	x
1	1	1	1	x	x	x	x	x	x	x	x

## Flip-Flop Input Equations with K-Maps

$D_3$

	$Q_1Q_0$			
	00	01	11	10
$Q_3\bar{Q}_2$	00			
	01		1	
	11	x	x	x
	10	1	1	1

$$\begin{aligned}
 D_3 (Q_3, Q_2, Q_1, Q_0) &= Q_3\bar{Q}_1 + Q_3\bar{Q}_0 + Q_2Q_1Q_0 \\
 &= Q_3(\bar{Q}_1 + \bar{Q}_0) + Q_2Q_1Q_0
 \end{aligned}$$

$D_2$

	$Q_1Q_0$			
	00	01	11	10
$Q_3\bar{Q}_2$	00		1	
	01	1	1	1
	11	x	x	x
	10			

$$\begin{aligned}
 D_2 (Q_3, Q_2, Q_1, Q_0) &= Q_2\bar{Q}_1 + Q_2\bar{Q}_0 + \bar{Q}_3\bar{Q}_2Q_1Q_0 \\
 &= Q_2(\bar{Q}_1 + \bar{Q}_0) + \bar{Q}_3\bar{Q}_2Q_1Q_0
 \end{aligned}$$

$D_1$

	$Q_1Q_0$			
	00	01	11	10
$Q_3\bar{Q}_2$	00	1		1
	01	1		1
	11	x	x	x
	10	1		1

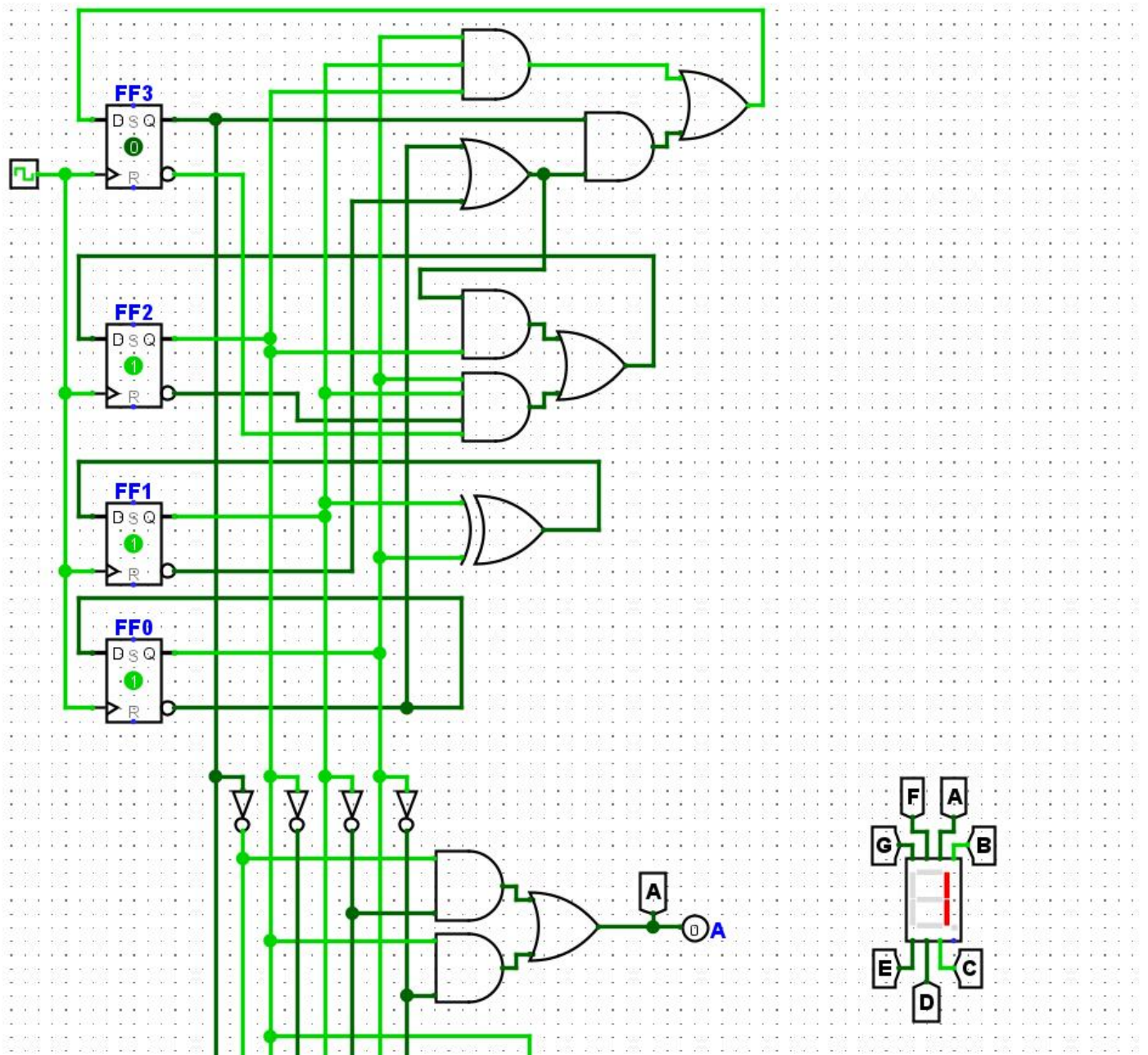
$$\begin{aligned}
 D_1 (Q_3, Q_2, Q_1, Q_0) &= \bar{Q}_1Q_0 + Q_1\bar{Q}_0 \\
 &= Q_1 \oplus Q_0
 \end{aligned}$$

$D_0$

	$Q_1Q_0$			
	00	01	11	10
$Q_3\bar{Q}_2$	00	1		1
	01	1		1
	11	x	x	x
	10	1		1

$$D_0 (Q_3, Q_2, Q_1, Q_0) = \bar{Q}_0$$

# Circuit Diagram



## T Flip-Flop Implementation

State Table

Present State				Next State				Flip Flop Inputs			
$Q_3$	$Q_2$	$Q_1$	$Q_0$	$Q_3$	$Q_2$	$Q_1$	$Q_0$	$T_3$	$T_2$	$T_1$	$T_0$
0	0	0	0	0	0	0	1	0	0	0	1
0	0	0	1	0	0	1	0	0	0	1	1
0	0	1	0	0	0	1	1	0	0	0	1
0	0	1	1	0	1	0	0	0	1	1	1
0	1	0	0	0	1	0	1	0	0	0	1
0	1	0	1	0	1	1	0	0	0	1	1
0	1	1	0	0	1	1	1	0	0	0	1
0	1	1	1	1	0	0	0	1	1	1	1
1	0	0	0	1	0	0	1	0	0	0	1
1	0	0	1	1	0	1	0	0	0	1	1
1	0	1	0	1	0	1	1	0	0	0	1
1	0	1	1	0	0	0	0	1	0	1	1
1	1	0	0	x	x	x	x	x	x	x	x
1	1	0	1	x	x	x	x	x	x	x	x
1	1	1	0	x	x	x	x	x	x	x	x
1	1	1	1	x	x	x	x	x	x	x	x

## Flip-Flop Input Equations with K-Maps

$T_3$

	$Q_1Q_0$			
	00	01	11	10
$Q_3Q_2$	00			
	01		1	
	11	x	x	x
	10		1	

$$\begin{aligned}
 T_3(Q_3, Q_2, Q_1, Q_0) &= Q_3Q_1Q_0 + Q_2Q_1Q_0 \\
 &= Q_1Q_0(Q_3 + Q_2)
 \end{aligned}$$

$T_2$

	$Q_1Q_0$			
	00	01	11	10
$Q_3Q_2$	00		1	
	01		1	
	11	x	x	x
	10			

$$T_2(Q_3, Q_2, Q_1, Q_0) = \overline{Q_3}Q_1Q_0$$

$T_3$

	$Q_1Q_0$			
	00	01	11	10
$Q_3Q_2$	00	1	1	
	01	1	1	
	11	x	x	x
	10	1	1	

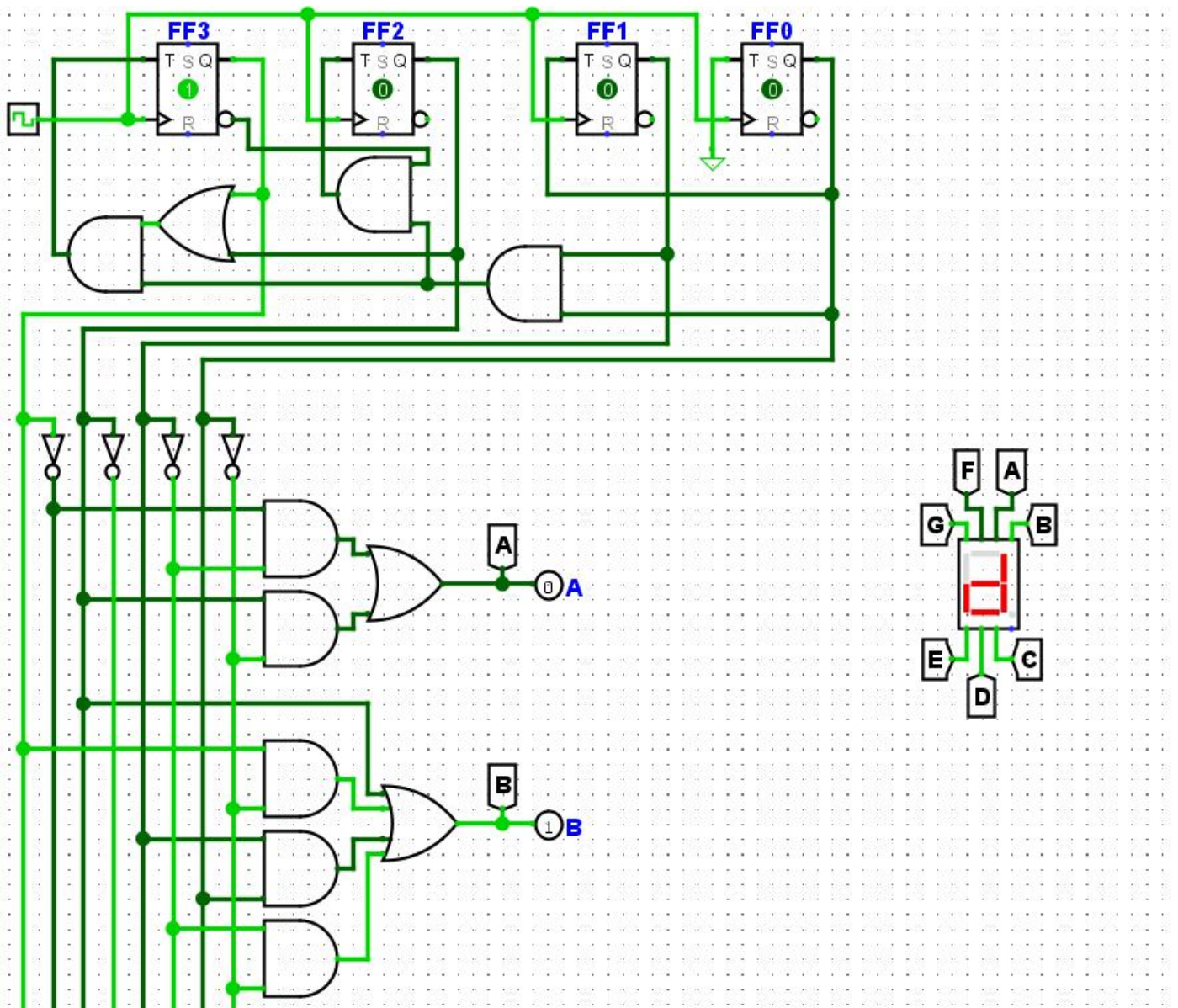
$$T_1(Q_3, Q_2, Q_1, Q_0) = Q_0$$

$T_2$

	$Q_1Q_0$			
	00	01	11	10
$Q_3Q_2$	00	1	1	1
	01	1	1	1
	11	x	x	x
	10	1	1	1

$$T_0(Q_3, Q_2, Q_1, Q_0) = 1$$

## Circuit Diagram



## **Hardware Implementation**

### **Choice of Implementation**

Based on the same factors used to select for the hardware implementation of the combinational circuit, we choose to implement the sequential circuit using JK flip-flops as the counter uses the least number of gates in addition to the 4 flip-flops.

The materials for hardware implementation is listed in the following section.

### **Cost of Implementation**

<b>Index</b>	<b>Name</b>	<b>Cost Per Unit</b>	<b>Quantity</b>	<b>Total Cost</b>
1	Breadboard (Large)	140	1	140
2	Male-to-Male Connectors x40	120	1	120
3	IC 74107 Dual JK Flip-Flops	40	2	80
4	4-pin Push Button Switch	10	1	10
5	IC 7408 Quad Two-Input AND Gates	30	1	30
6	Combinational Part	1240	1	1240
<b>CUMULATIVE TOTAL</b>				<b>1620</b>

# Limitations

Over the course of the project, few hurdles were encountered, especially with regards to the hardware implementations of the seven segment display.

- The initial build of the combinational part provided incorrect outputs to different inputs. Therefore, the circuit had to be rebuilt and tested function by function to ensure that the final result was correct. Employing this step-by-step approach of verifying outputs towards completion would have reduced the time and effort taken.
- For the sequential part, the primary issue lay in deciding and implementing a mechanism for sending clock pulses to the flip-flops. We settled for a push-button switch mechanism that transitions a clock signal from HIGH to LOW on activation. At first, there were some inconsistencies in how characters appeared on the display, but by connecting a resistor between the switch and the VCC, it ensured that the transitions were smooth and stable. Nevertheless, the circuit would have benefited greatly by integrating a clock generator, that could have been built using a 555 Timer IC.

# Conclusion

The project encompassing this report, the software implementations, and the hardware implementations compels students to involve themselves independently of any supervisor in the process of designing, developing, and implementing a digital system. In this manner, students get to evaluate their own capabilities and learn how to collaborate and leverage each other's strengths in order to deliver a complete and purposeful product. By overcoming the challenges and pitfalls along the way, the team gains practical insights that may enable them to become better digital designers and engineers as they apply themselves across the various fields that require competent hands offering fresh perspectives. Although the construction of a seven-segment display circuit in both its combinational and sequential forms has become one of the most common undertaking as a project in digital logic design, it is nonetheless the rudimentary leap that one might need to excel in the discipline.