

Chapter 5

Reduction of Multiple Subsystems

Figure 5.1

The space shuttle consists of multiple subsystems. Can you identify those that are control systems, or parts of control systems?

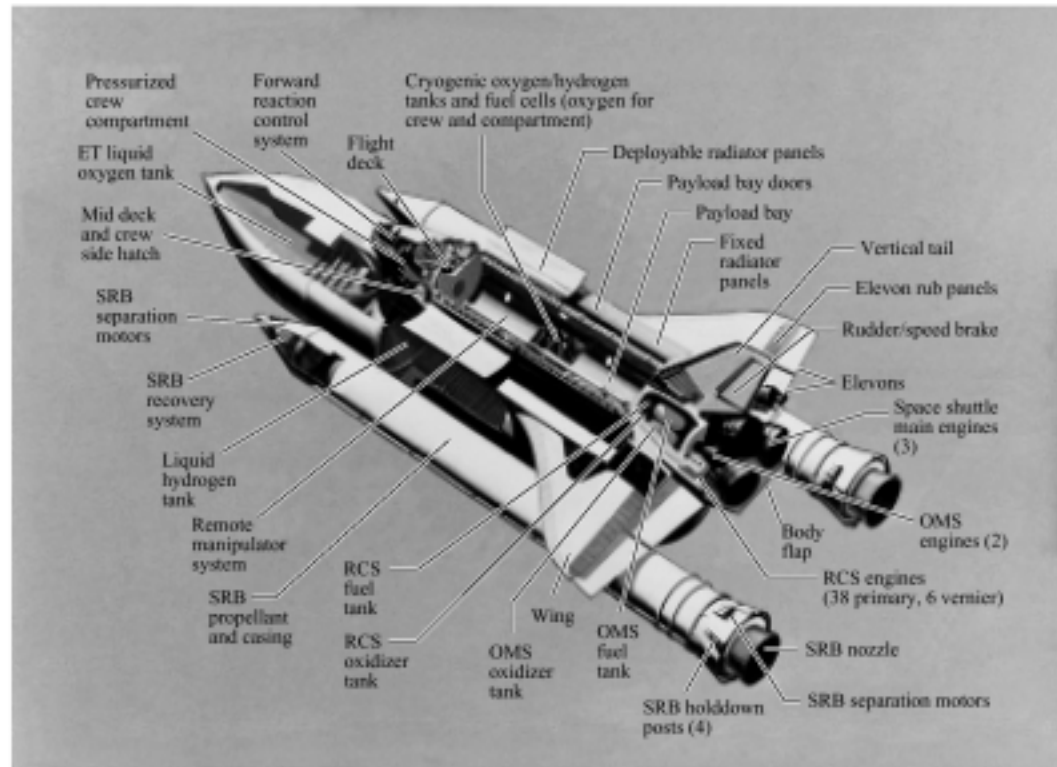


Figure 5.2

Components of a
block diagram for a
linear, time-invariant
system

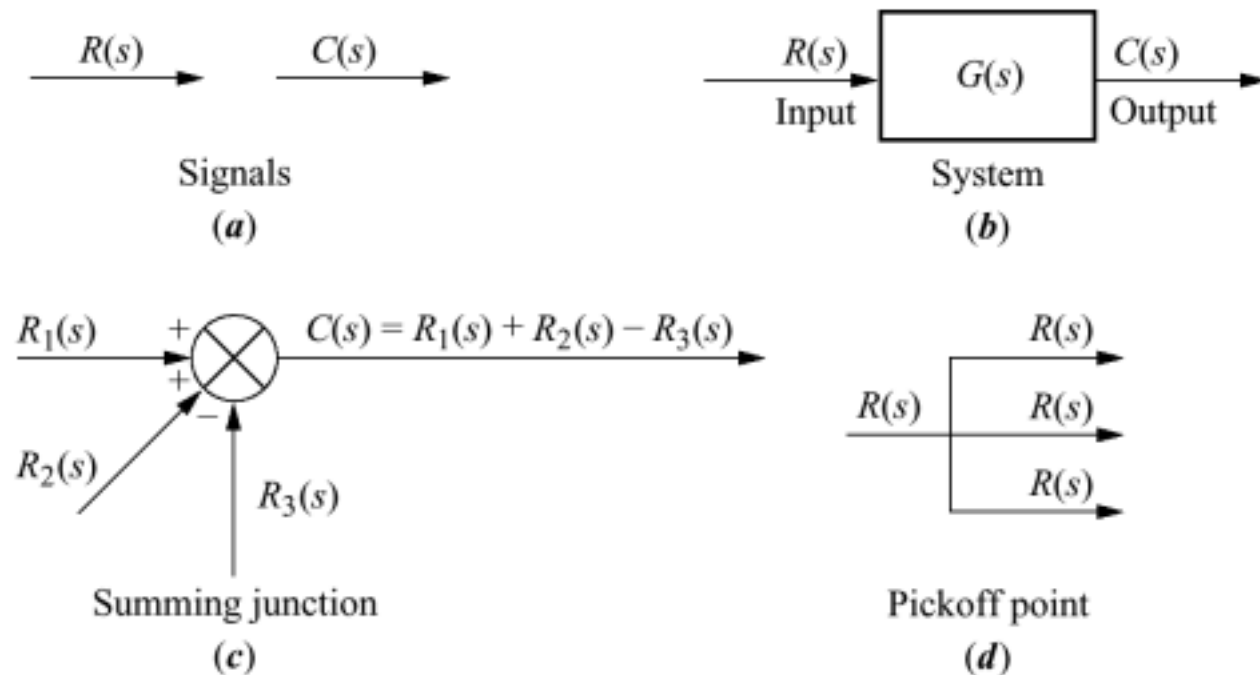


Figure 5.3

- a.** Cascaded
subsystems;
b. equivalent transfer
function

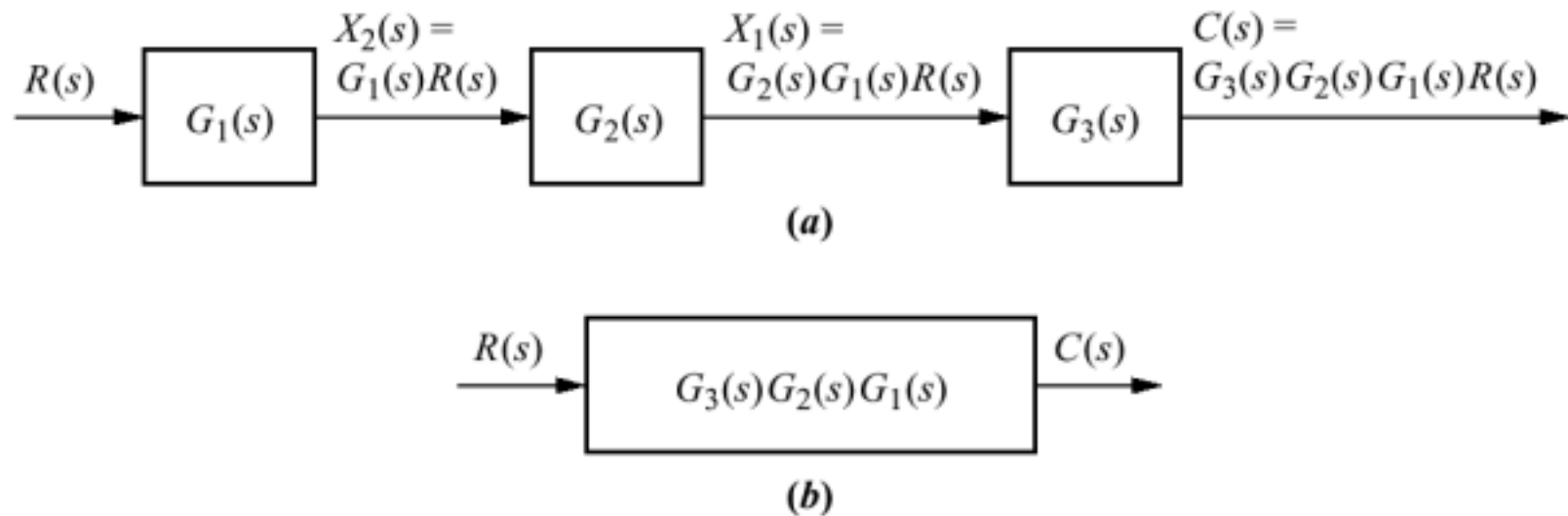


Figure 5.4
Loading in cascaded
systems

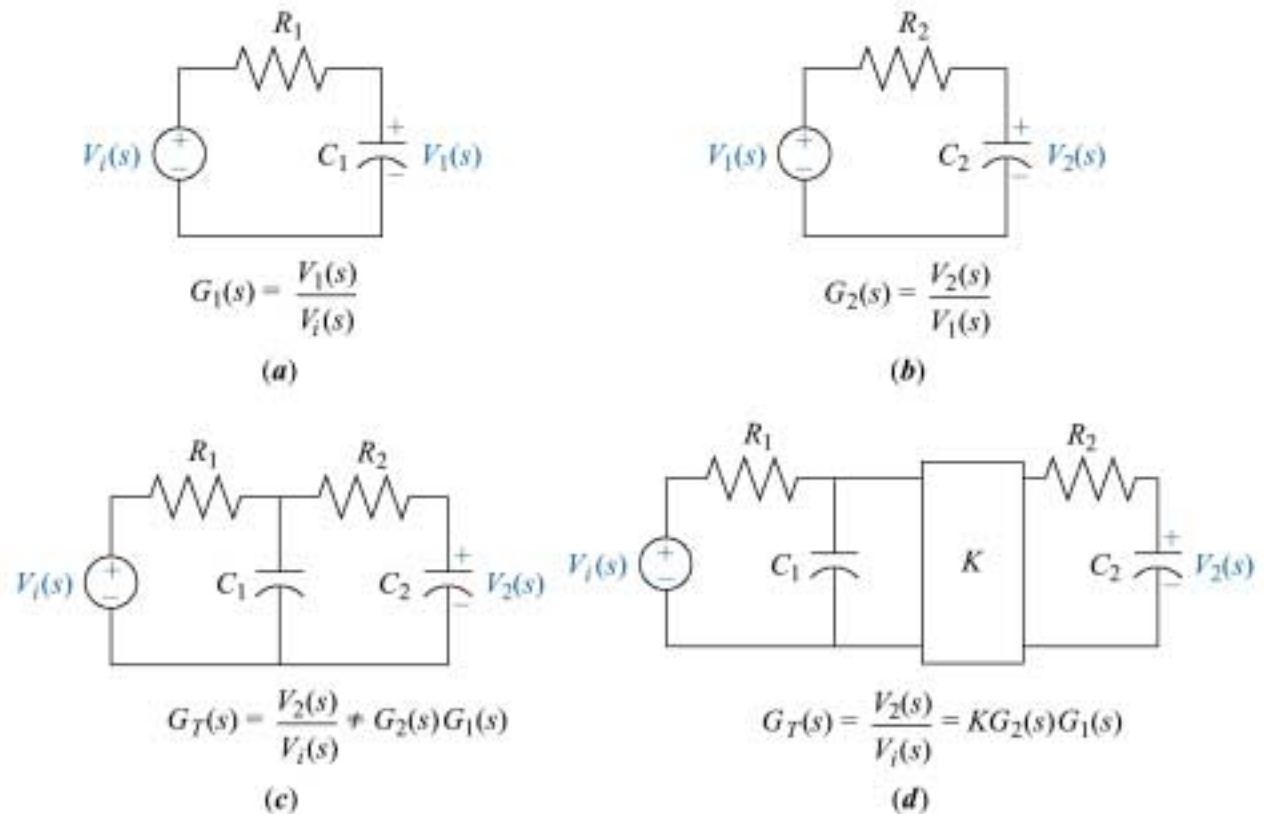


Figure 5.5
a. Parallel
 subsystems;
b. equivalent
 transfer
 function

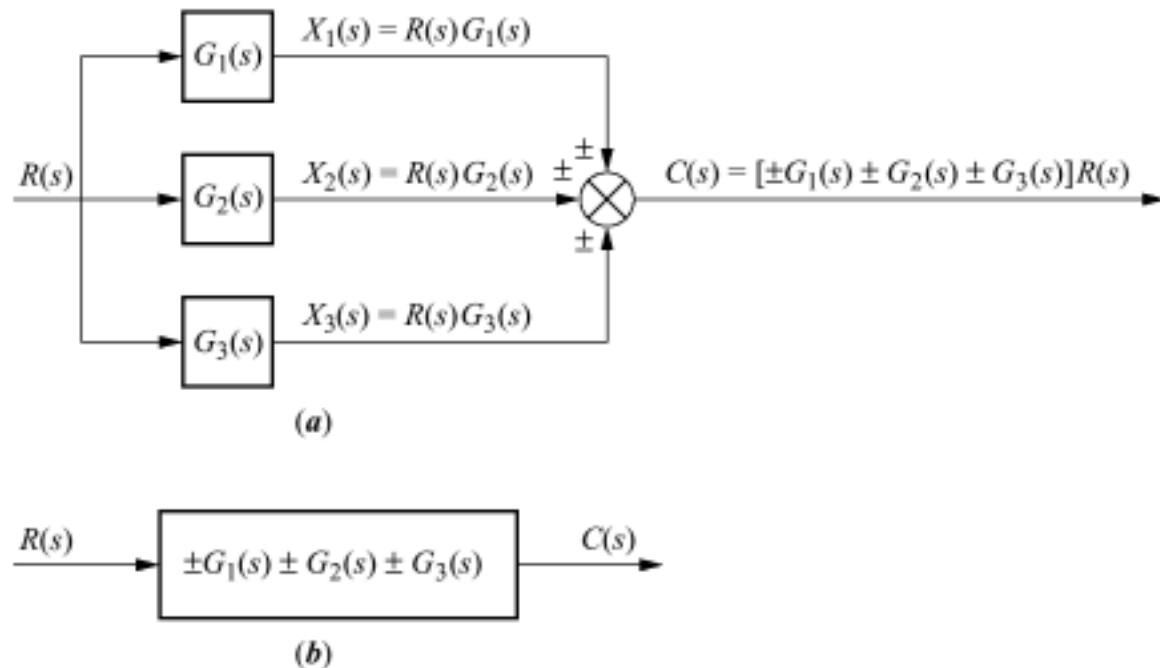


Figure 5.6

- a.** Feedback control system;
- b.** simplified model;
- c.** equivalent transfer function

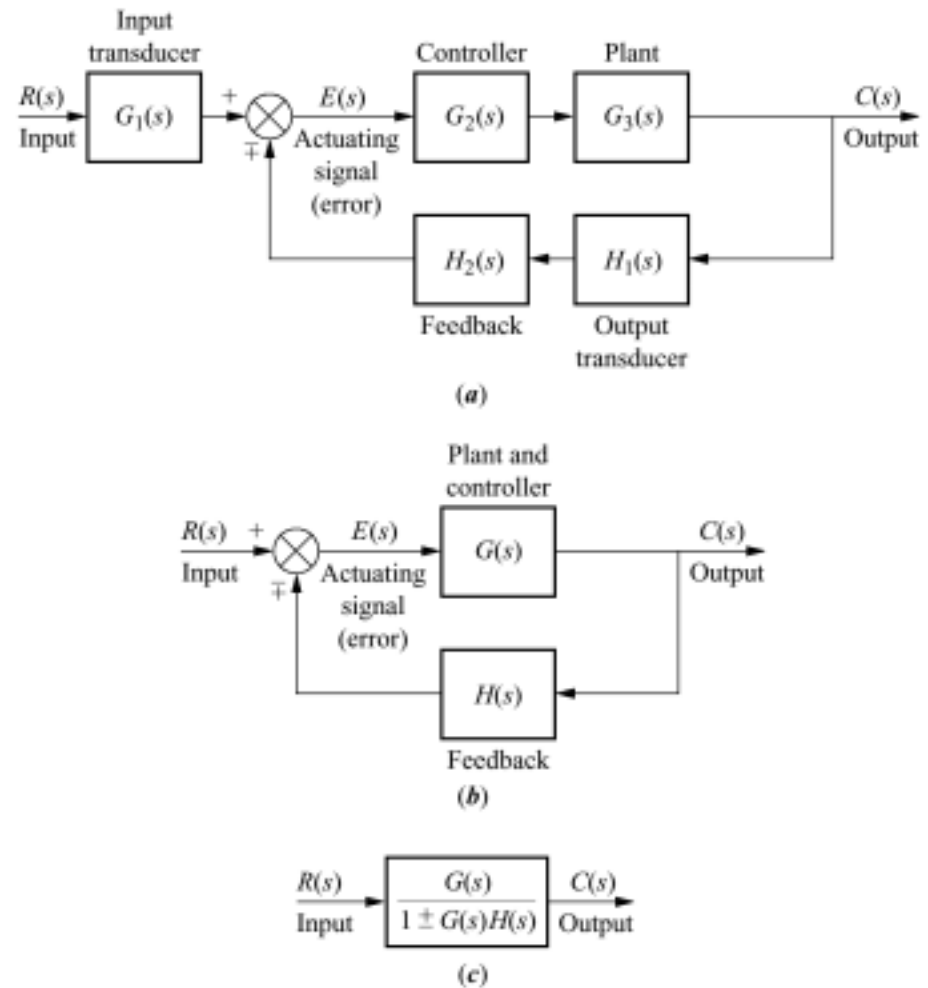


Figure 5.7

Block diagram algebra for summing junctions—equivalent forms for moving a block

- a.** to the left past a summing junction;
- b.** to the right past a summing junction

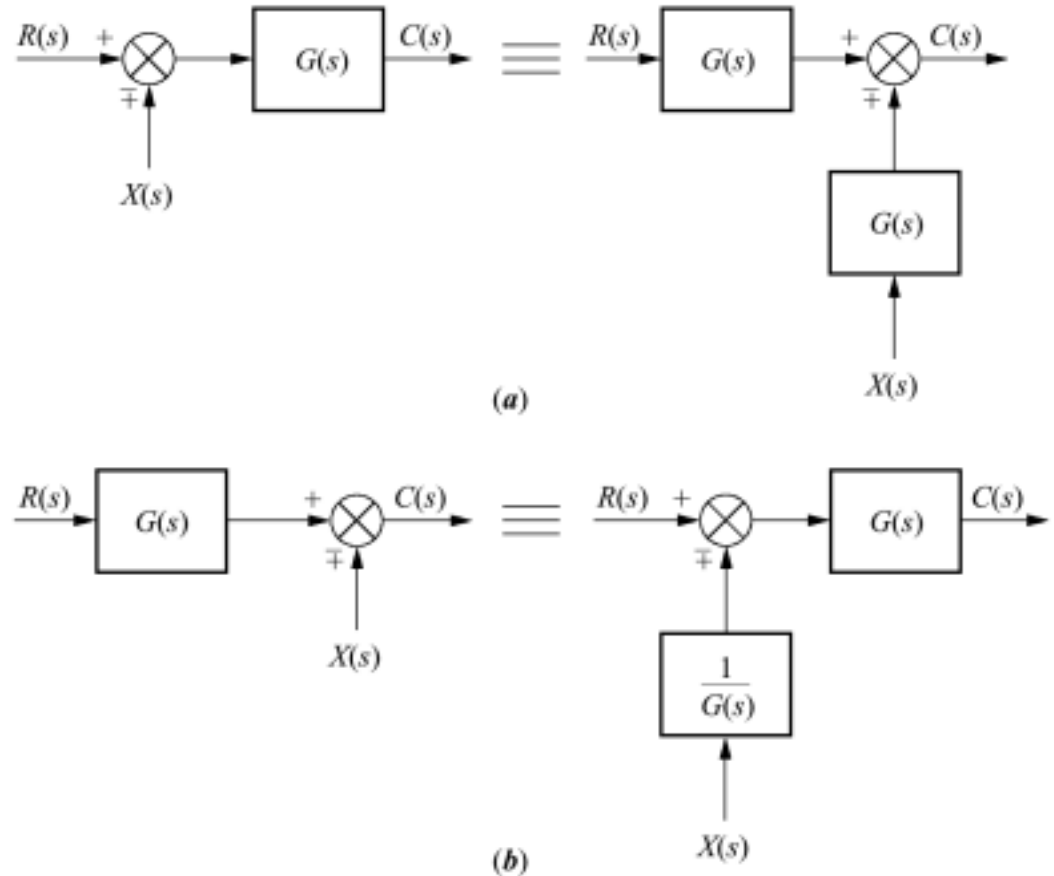


Figure 5.8

Block diagram algebra for pickoff points—equivalent forms for moving a block

- a.** to the left past a pickoff point;
- b.** to the right past a pickoff point

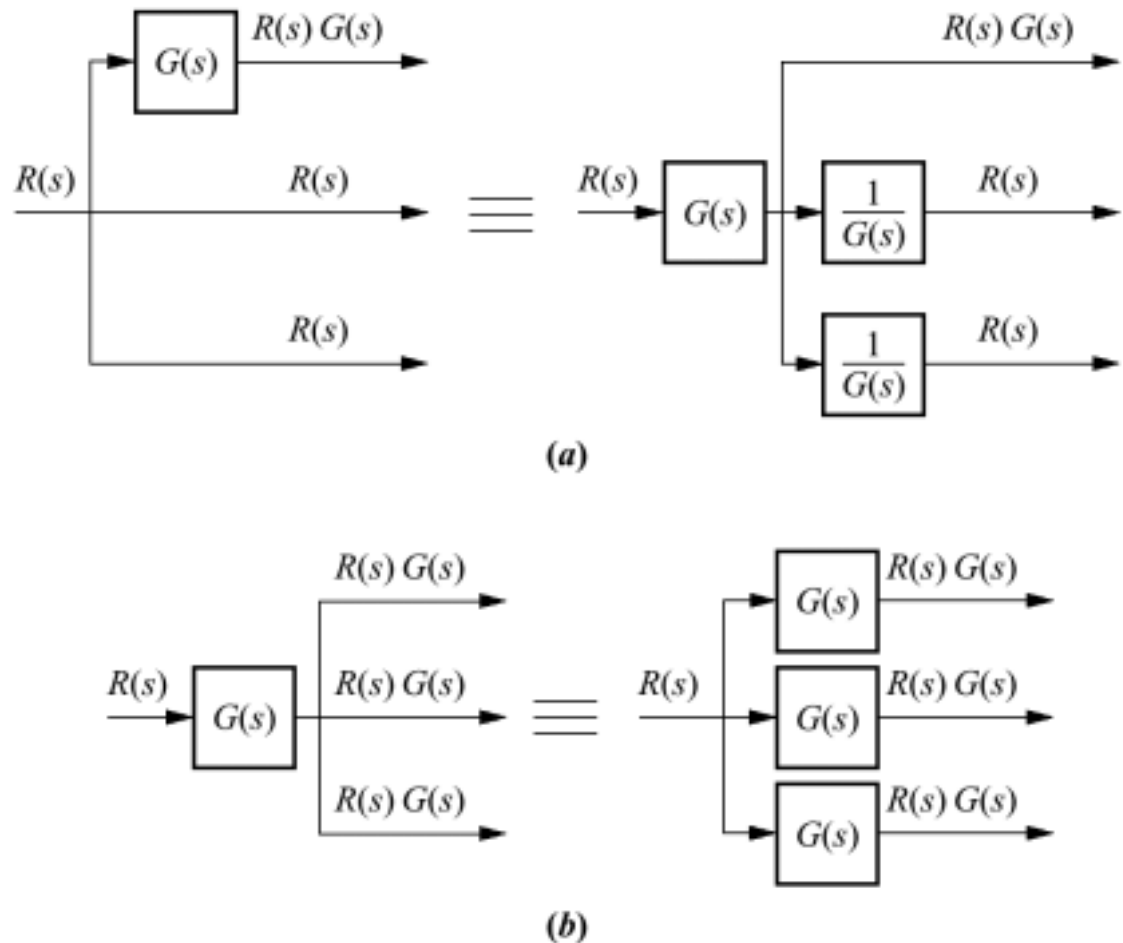


Figure 5.9
Block diagram
for Example 5.1

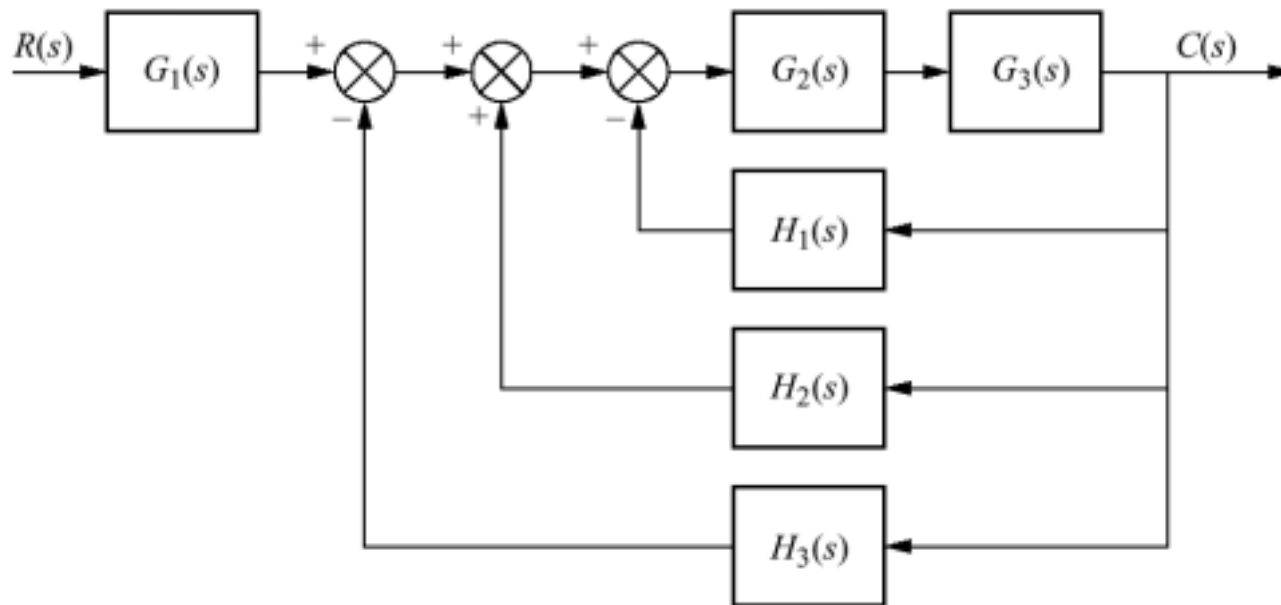


Figure 5.10

Steps in solving
Example 5.1:

a. collapse summing
junctions;

b. form equivalent
cascaded system
in the forward path
and equivalent
parallel system in the
feedback path;

c. form equivalent
feedback system and
multiply by cascaded
 $G_1(s)$

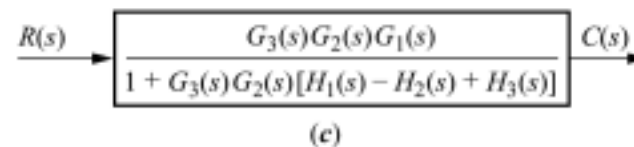
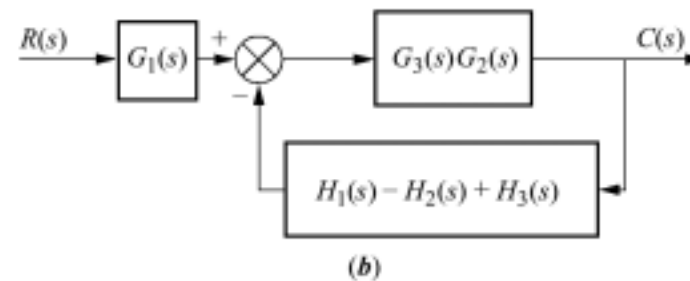
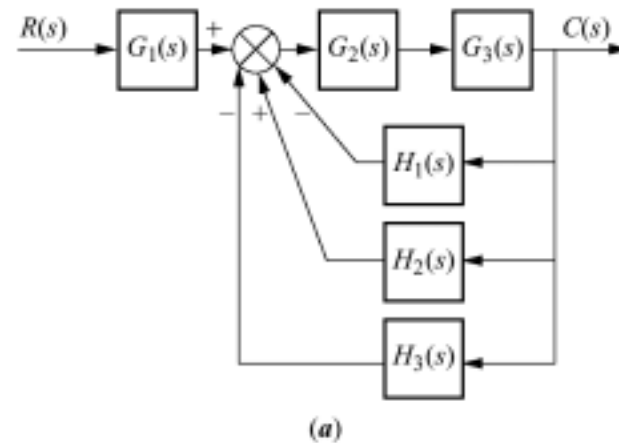


Figure 5.11
Block diagram for
Example 5.2

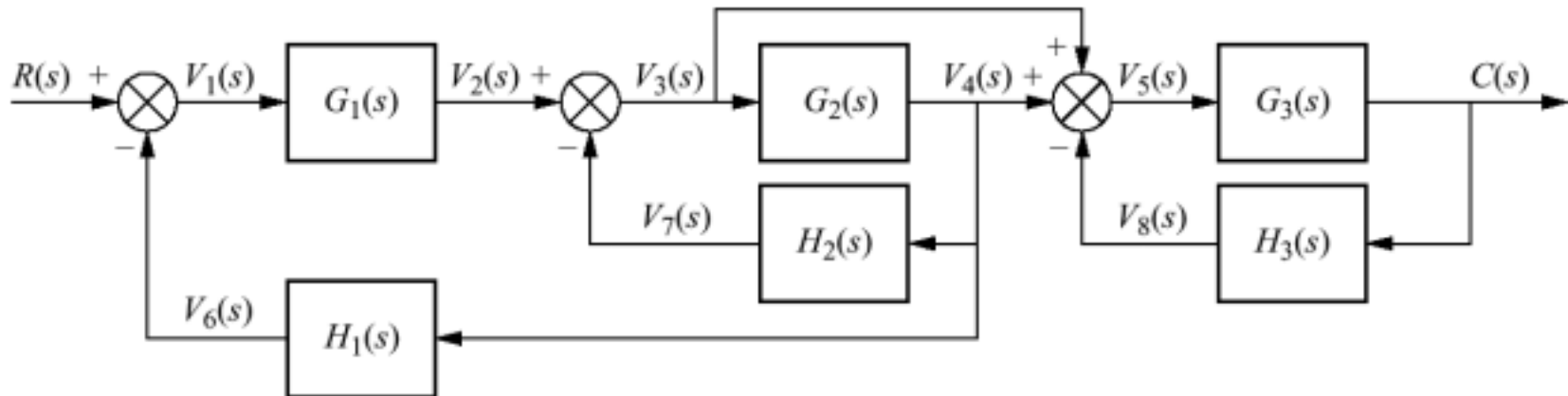


Figure 5.12
Steps in the
block diagram
reduction for
Example 5.2

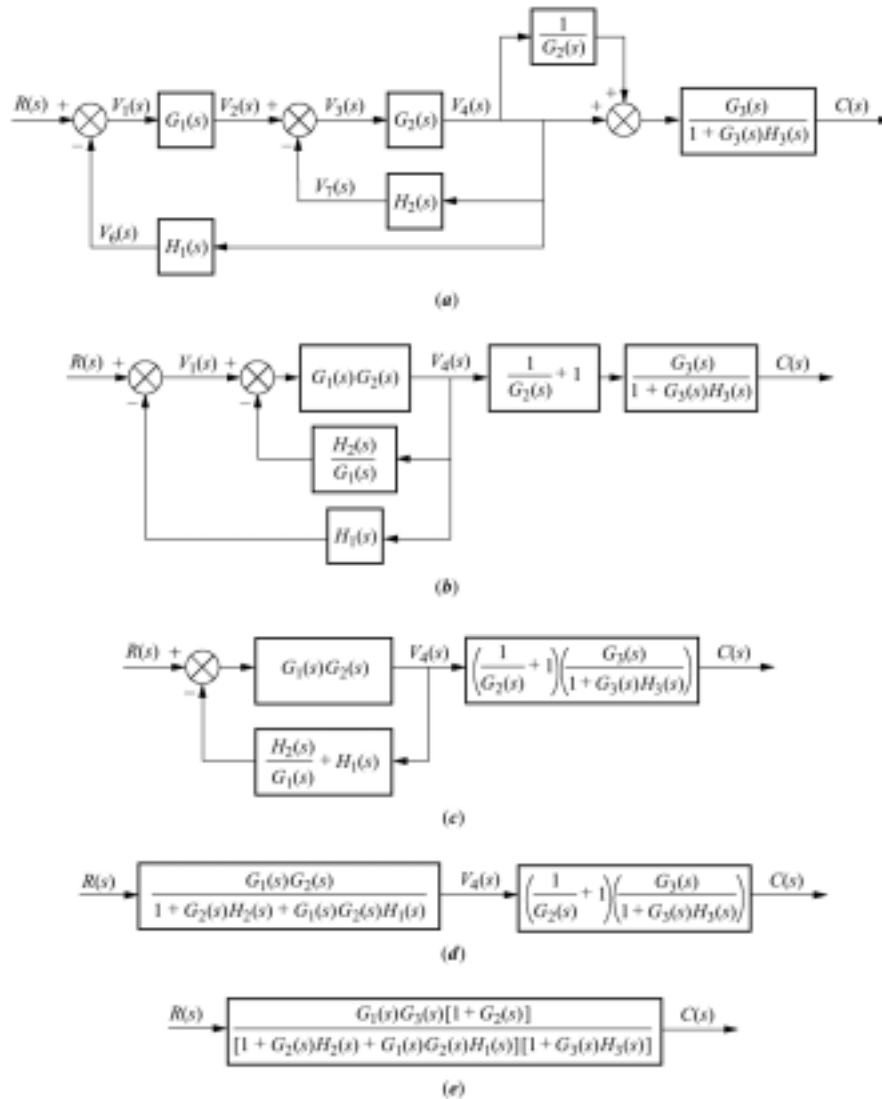


Figure 5.13
Block diagram for
Skill-Assessment
Exercise 5.1

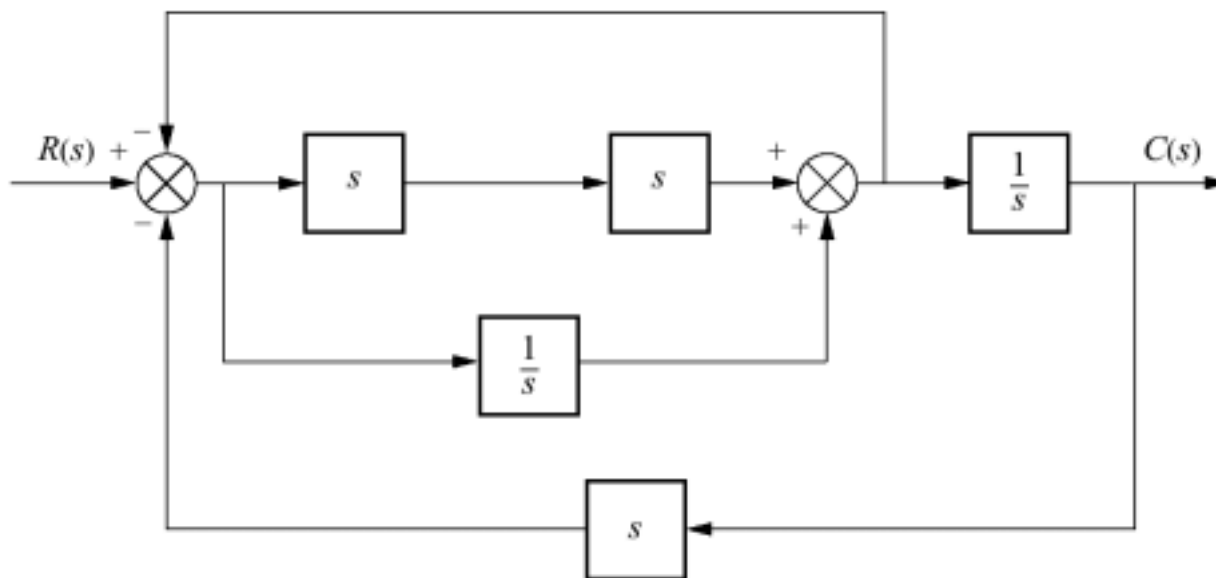


Figure 5.14
Second-order
feedback control
system

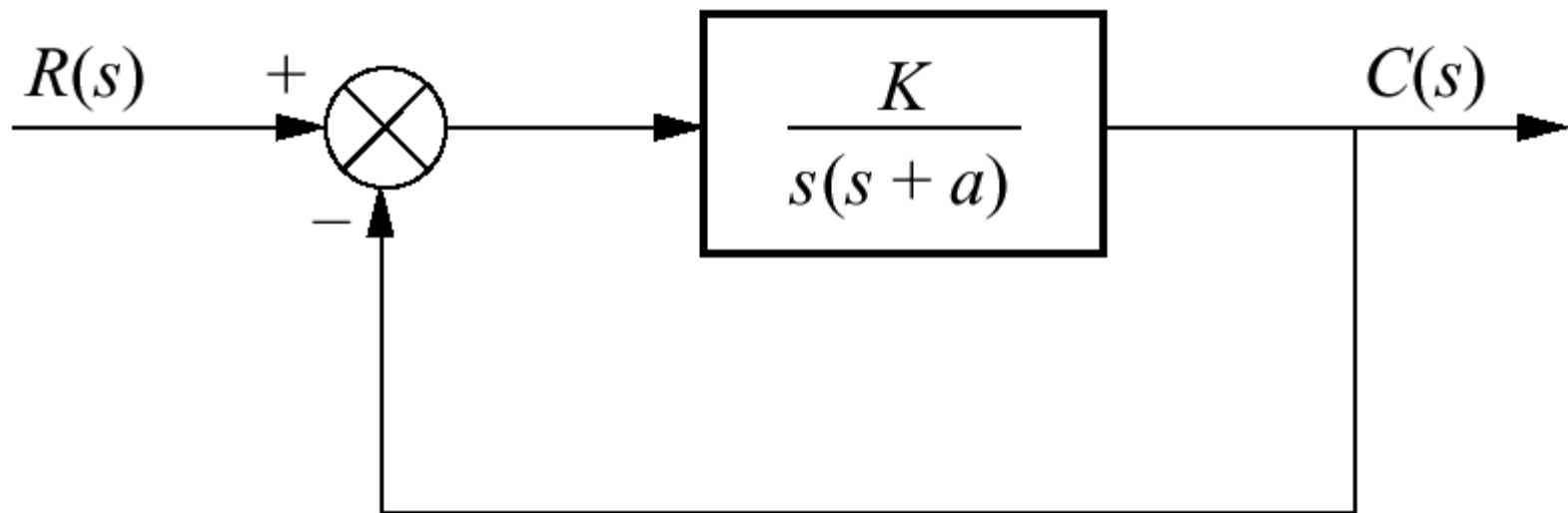


Figure 5.15
Feedback system for
Example 5.3

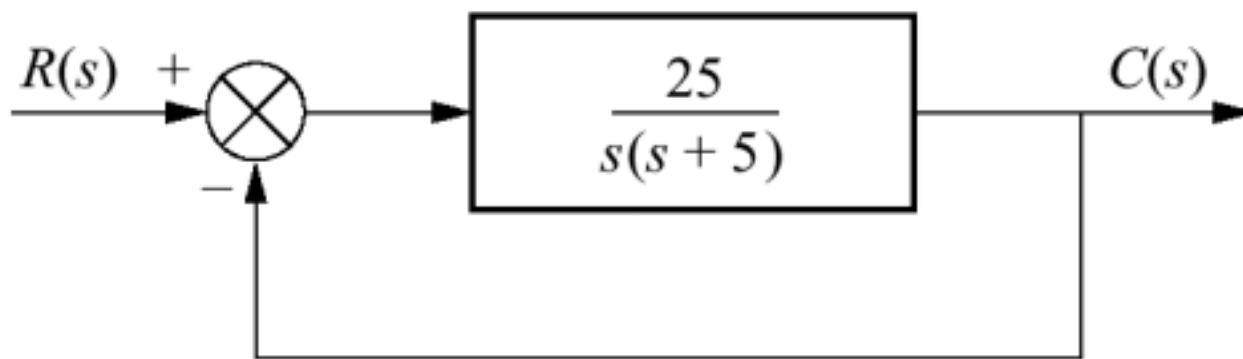


Figure 5.16
Feedback system for
Example 5.4

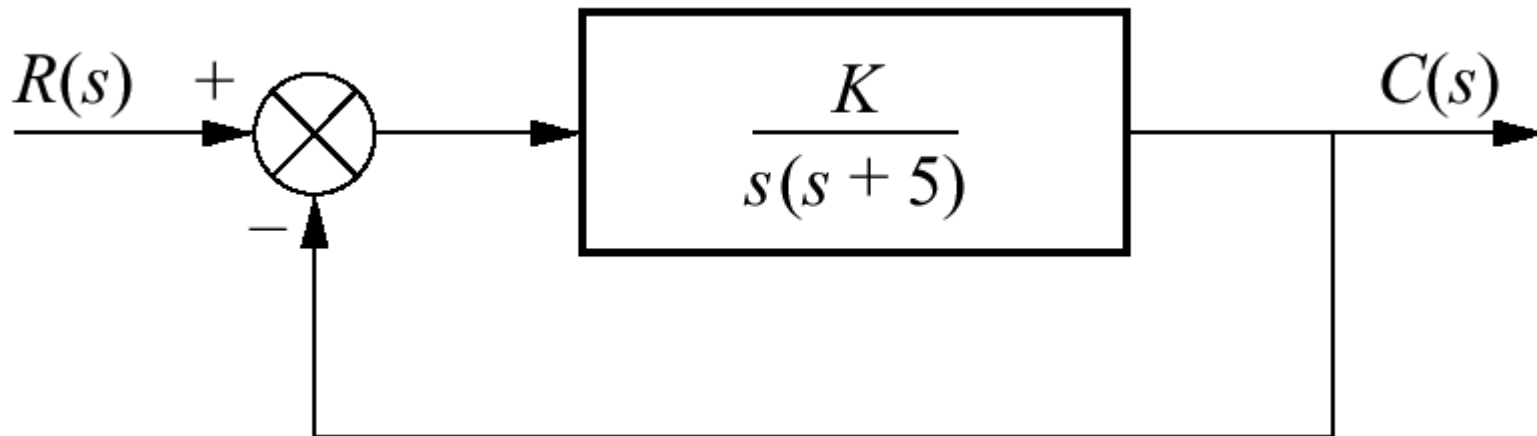


Figure 5.17

Signal-flow graph
components:

a. system;

b. signal;

c. interconnection of
systems and signals

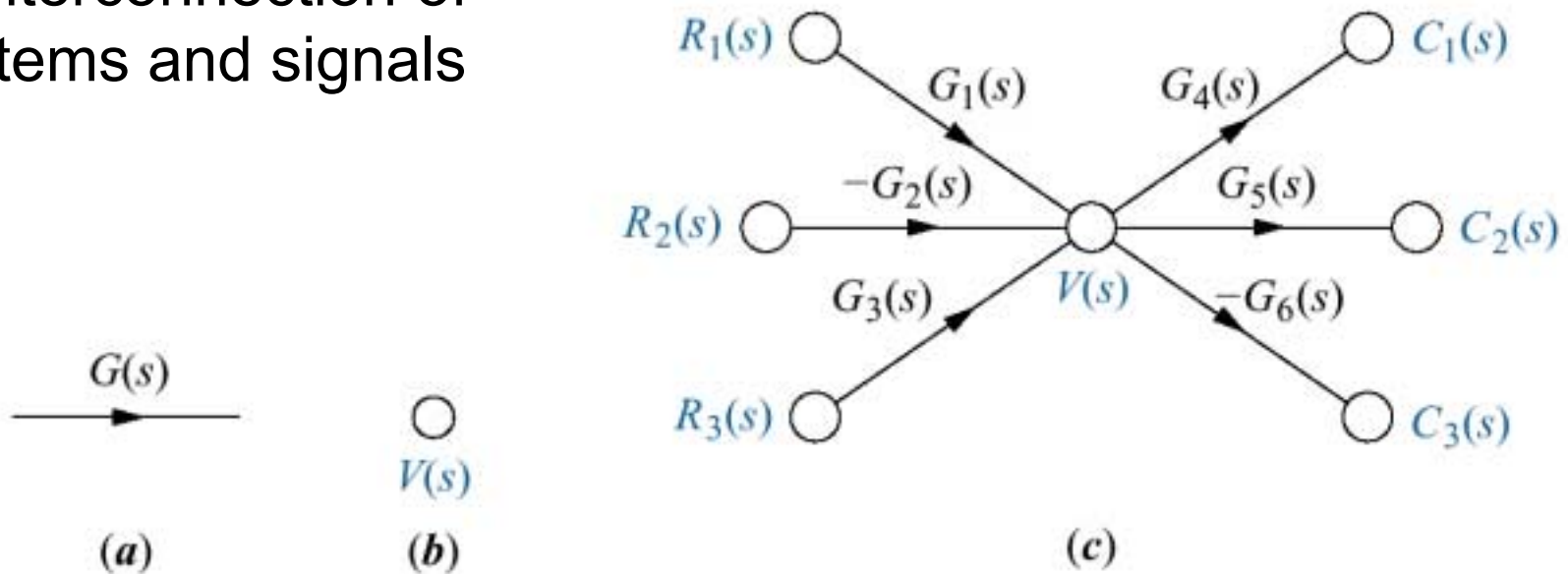


Figure 5.18

Building signal-flow graphs:

a. cascaded system nodes (from Figure 5.3(a));

b. cascaded system signal-flow graph;

c. parallel system nodes (from Figure 5.5(a));

d. parallel system signal-flow graph;

e. feedback system nodes (from Figure 5.6(b));

f. feedback system signal-flow graph

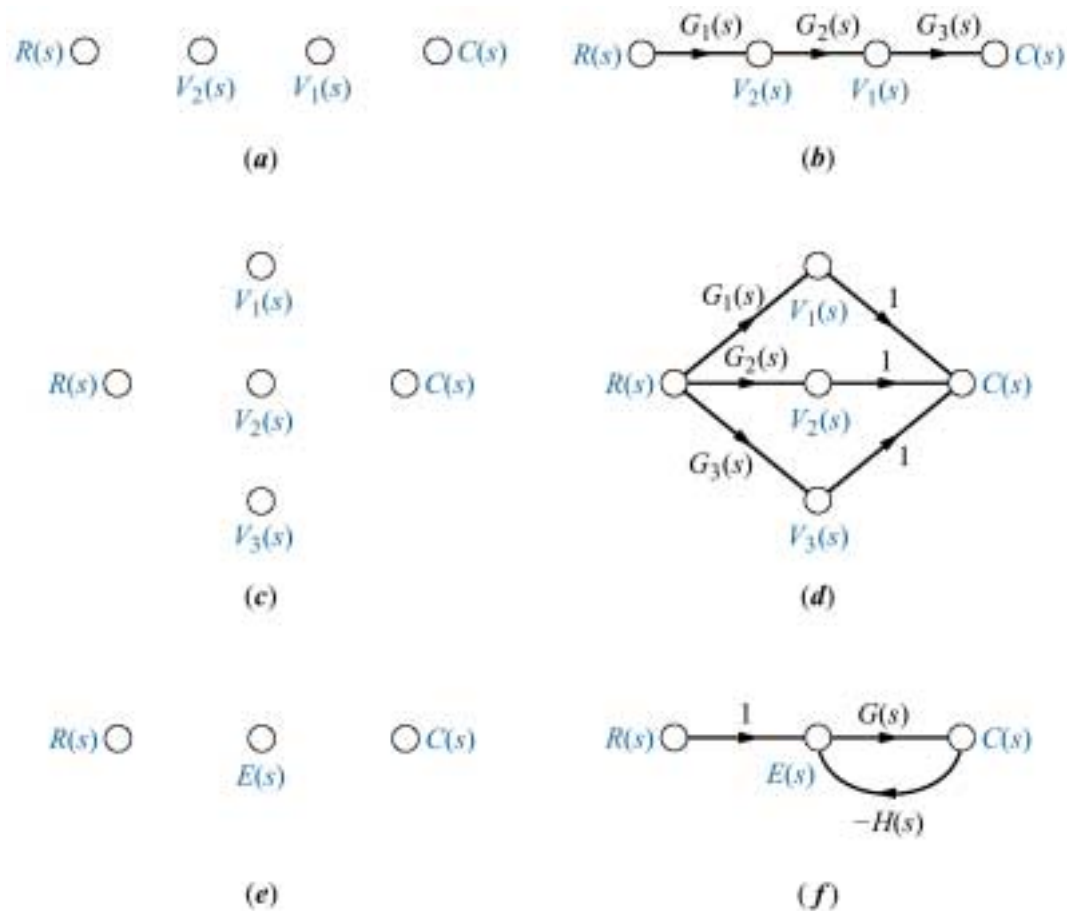


Figure 5.19

Signal-flow graph
development:

- a. signal nodes;
- b. signal-flow graph;
- c. simplified signal-flow graph

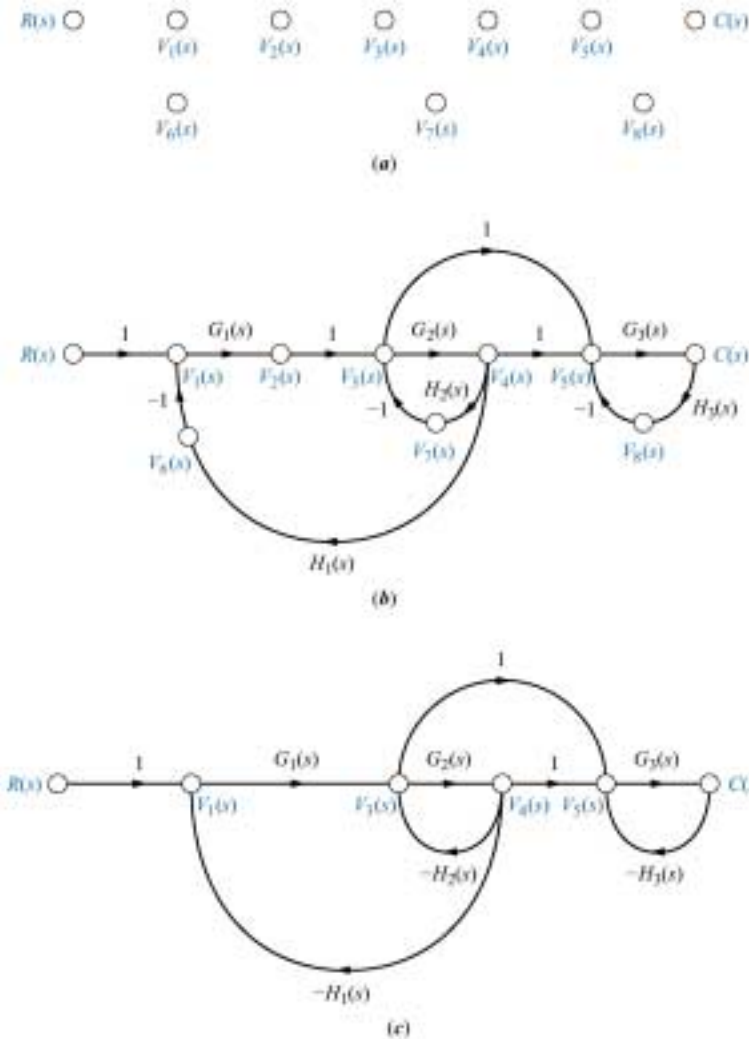


Figure 5.20
Signal-flow graph
for demonstrating
Mason's rule

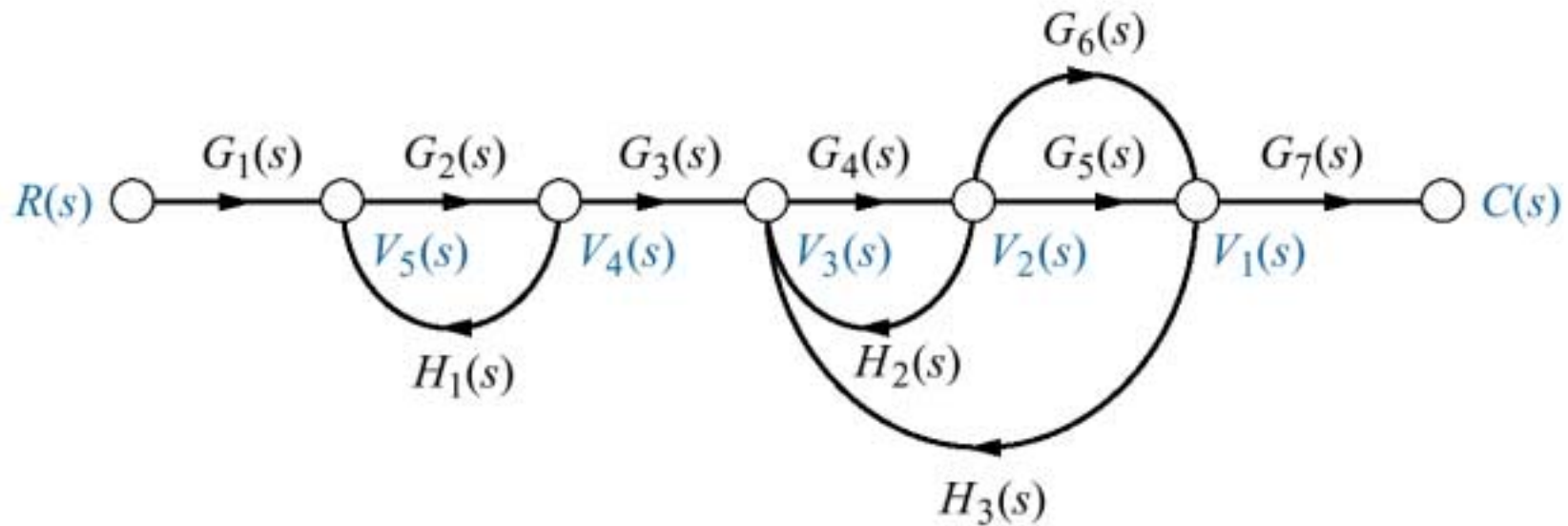


Figure 5.21
Signal-flow graph for
Example 5.7

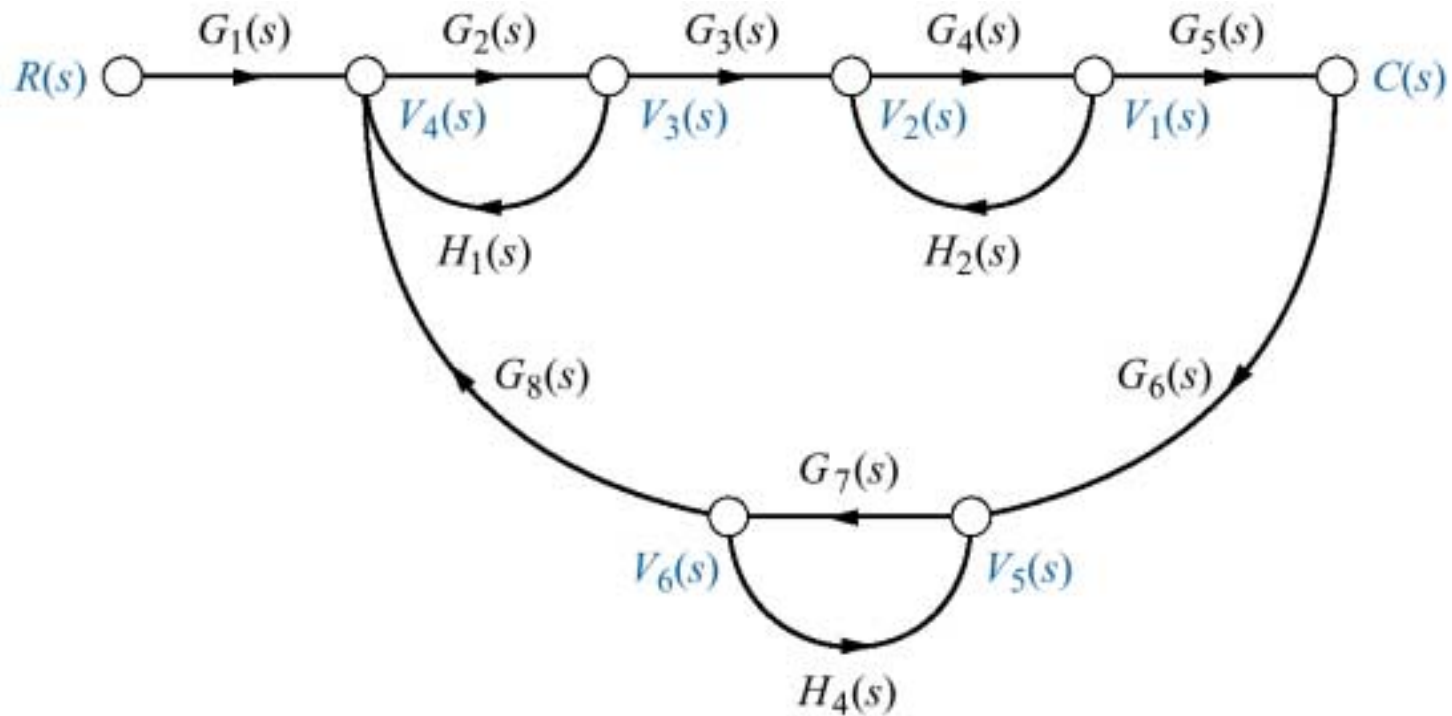


Figure 5.22

Stages of development of a signal-flow graph for the system of Eqs. 5.36:

- a. place nodes;
- b. interconnect state variables and derivatives;
- c. form dx_1/dt ;
- d. form dx_2/dt (figure continues)

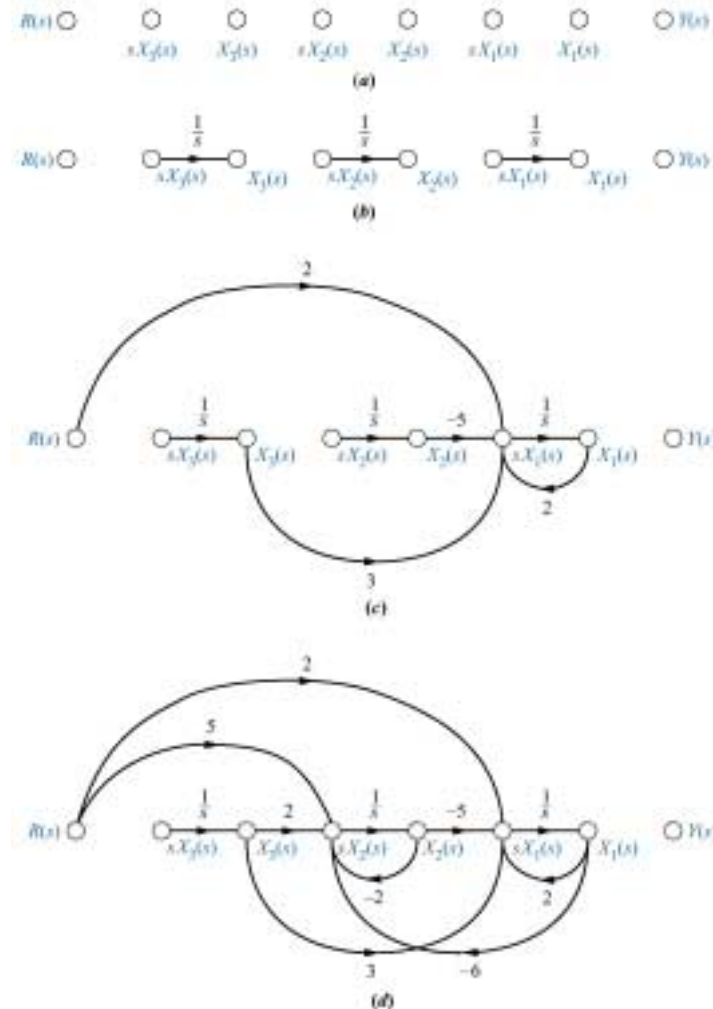


Figure 5.22
(continued)
e. form dx_3/dt ;
f. form output

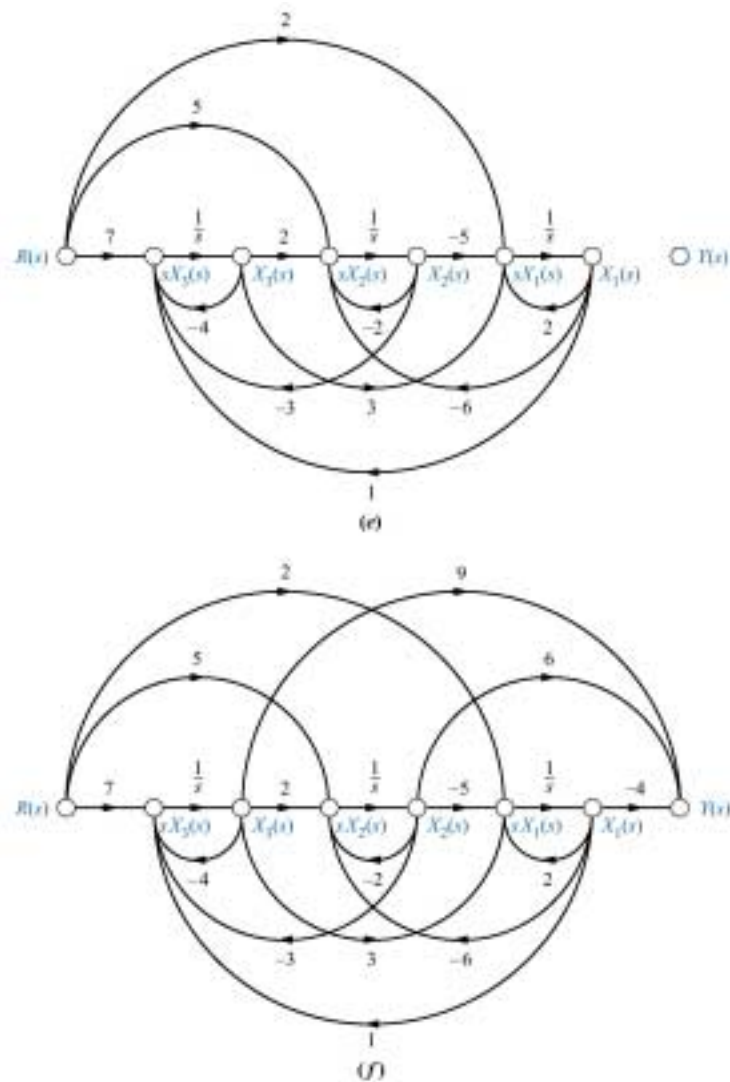


Figure 5.23

Representation of
Figure 3.10 system as
cascaded first-order
systems

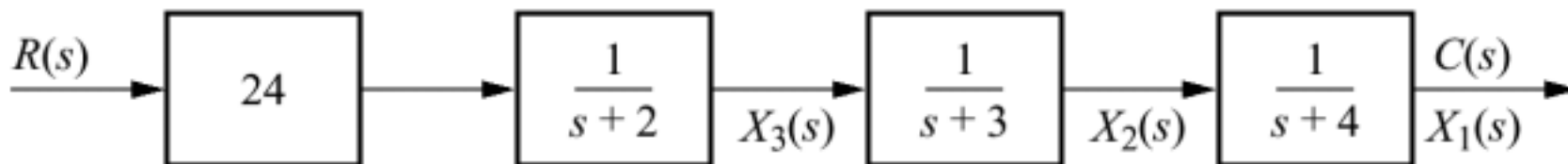


Figure 5.24

a. First-order subsystem;
b. signal-flow graph for Figure 5.23 system

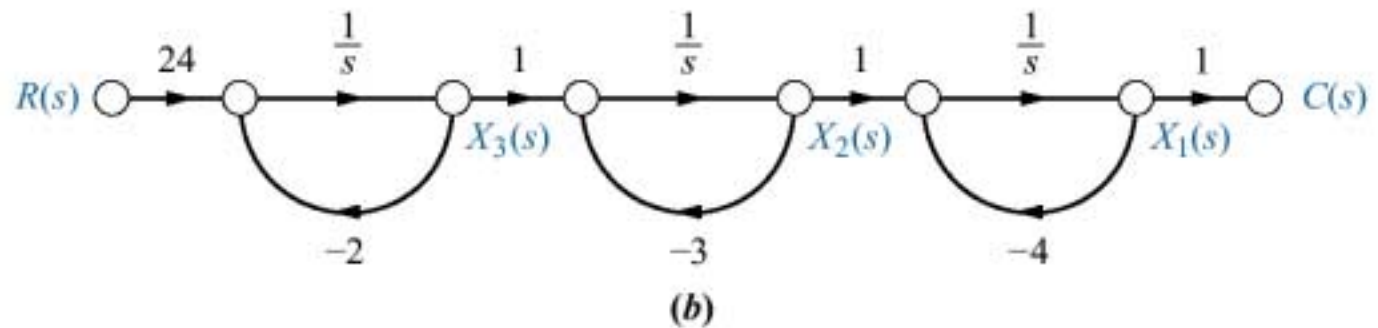
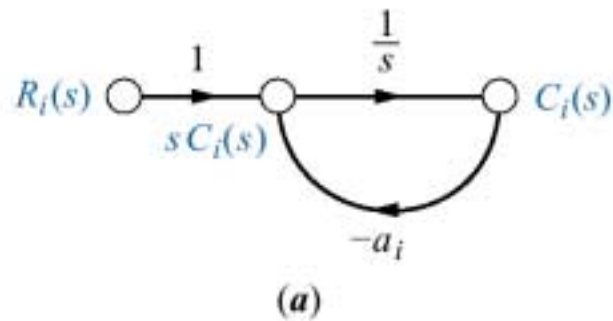


Figure 5.25
Signal-flow
representation
of Eq. (5.45)

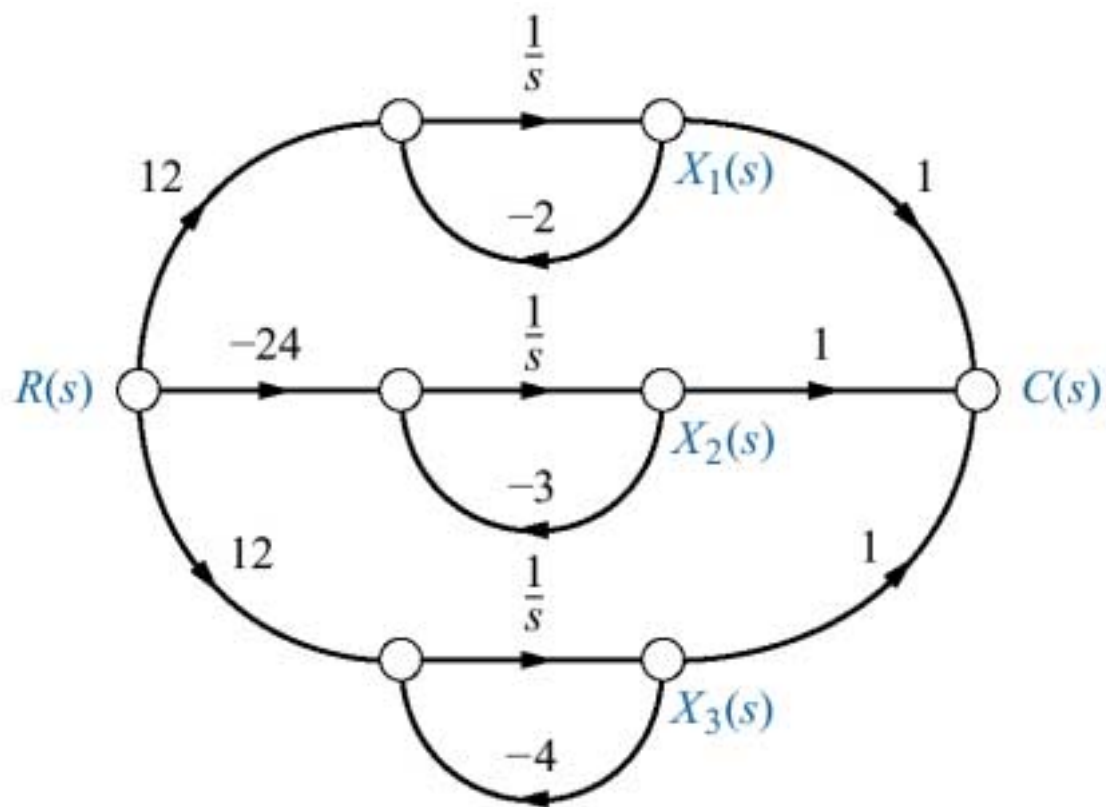


Figure 5.26
Signal-flow
representation
of Eq. (5.52)

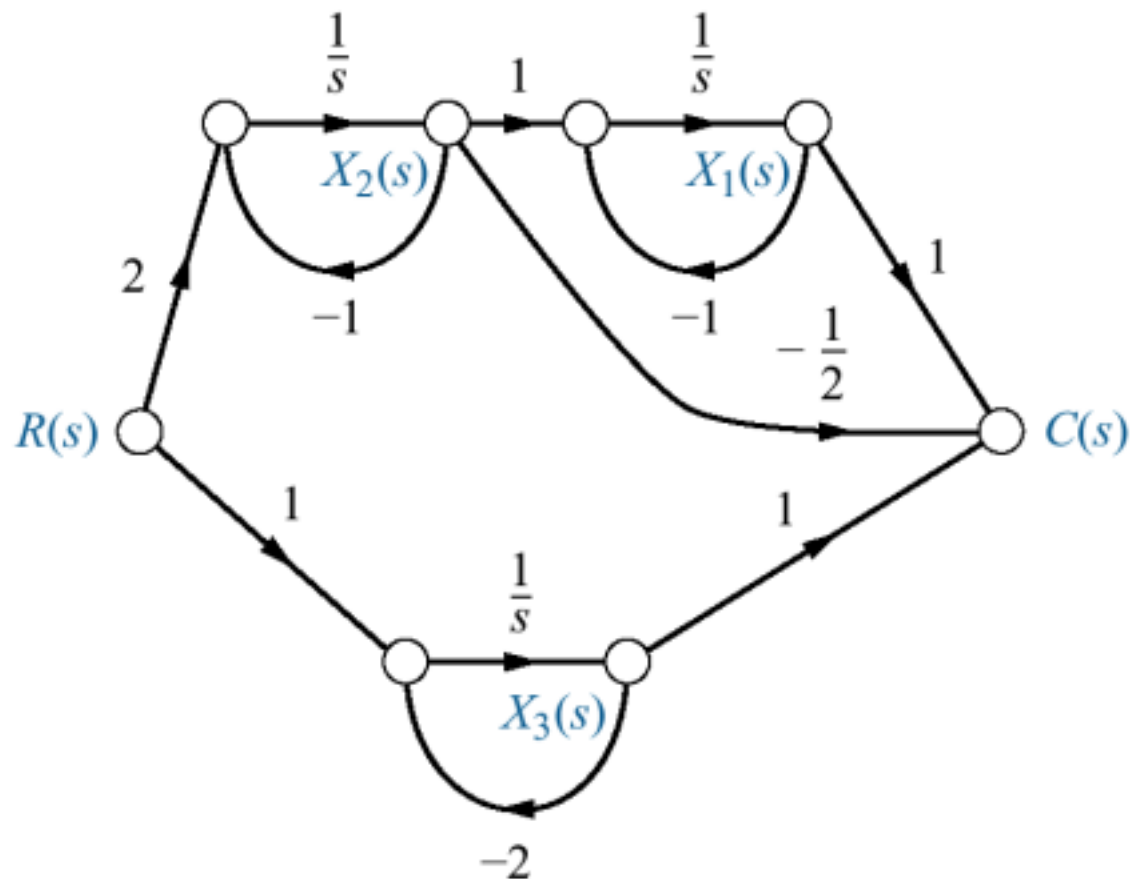


Figure 5.27

Signal-flow graphs for
obtaining forms for

$$G(s) = C(s)/R(s) = \frac{(s^2 + 7s + 2)}{(s^3 + 9s^2 + 26s + 24)}:$$

- a. phase-variable form;
- b. controller canonical form

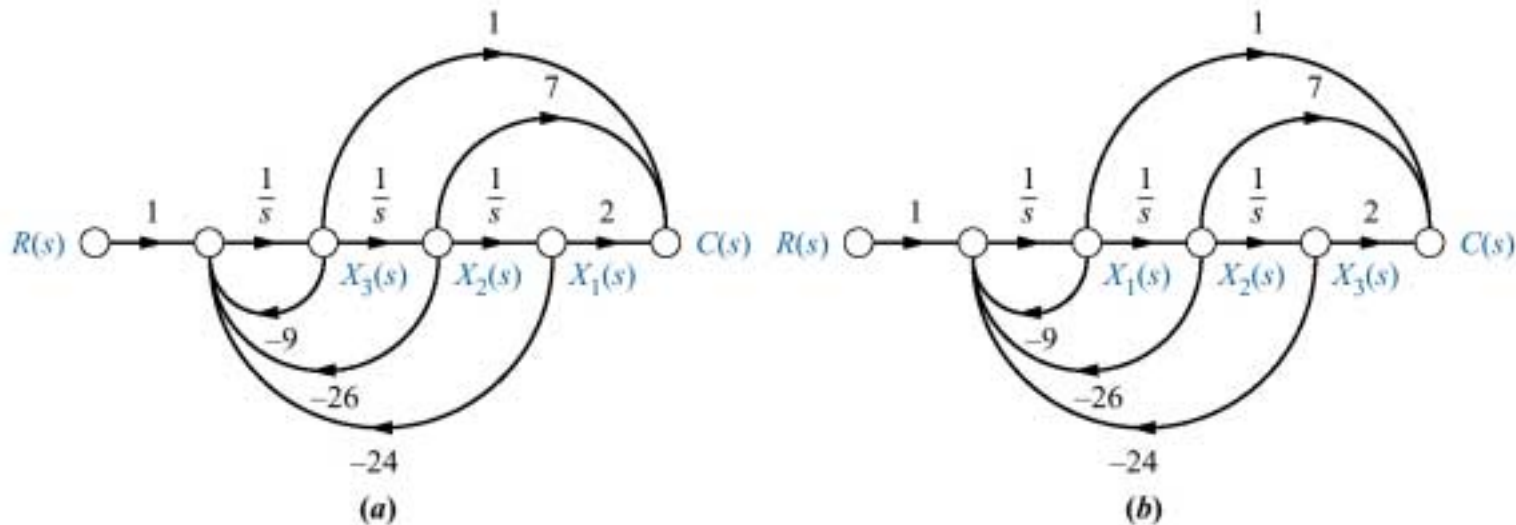


Figure 5.28

Signal-flow graph for
observer canonical
form variables:

a. planning;

b. implementation

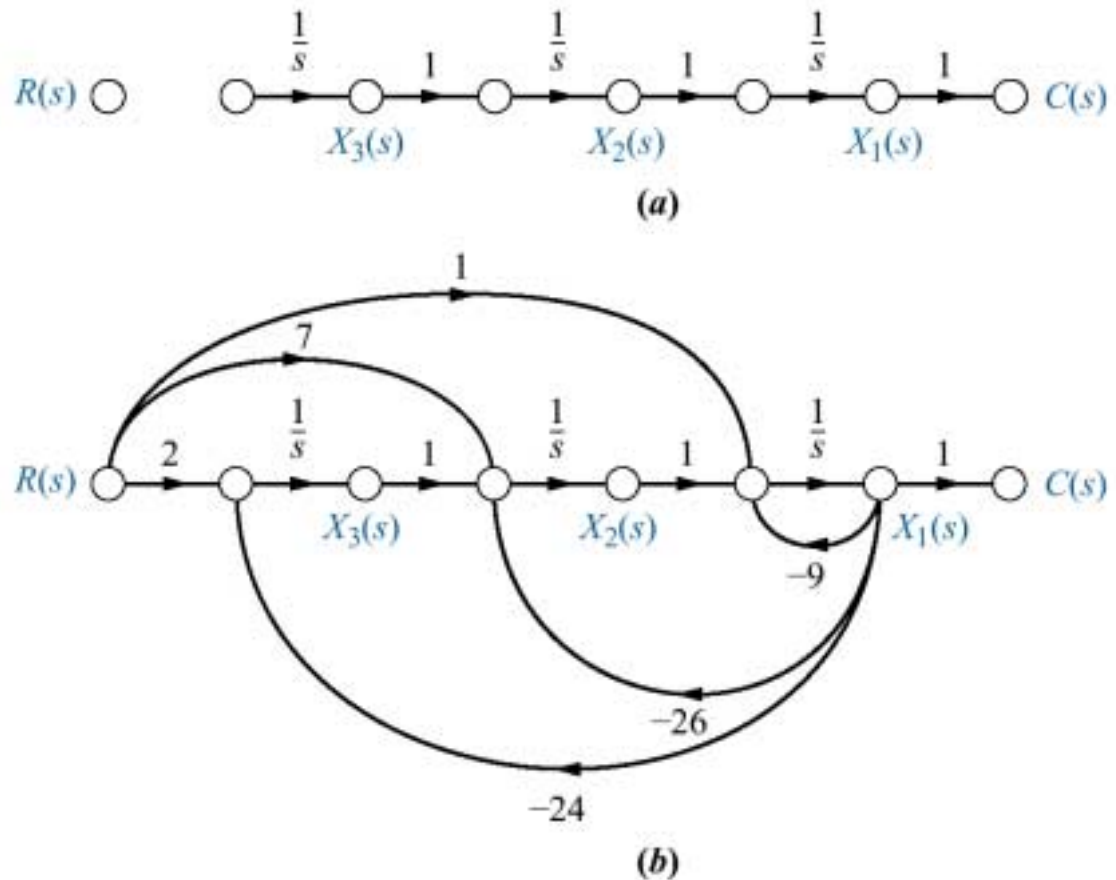


Figure 5.29
Feedback
control system
for Example 5.8

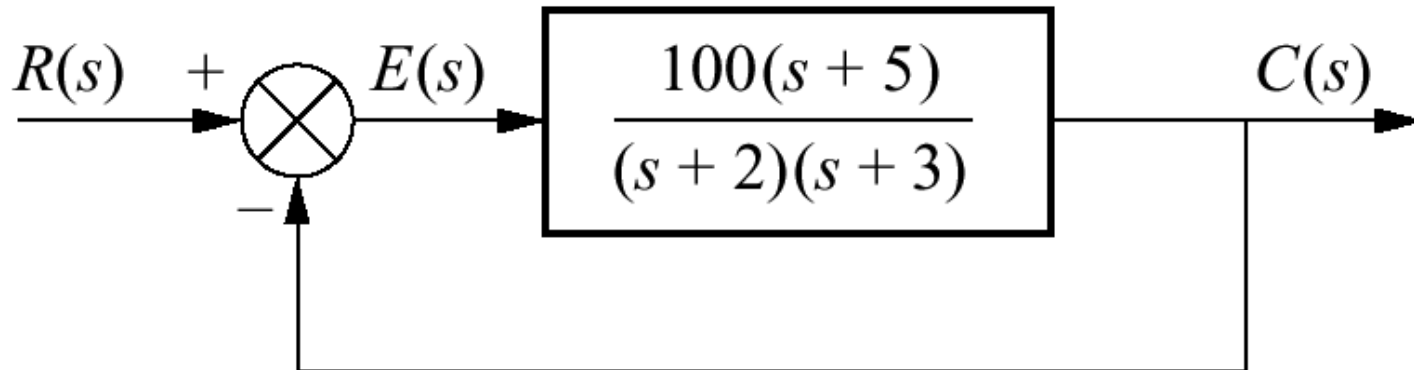


Figure 5.30

Creating a signal-flow graph for the

Figure 5.29 system:

a. forward transfer function;

b. complete system

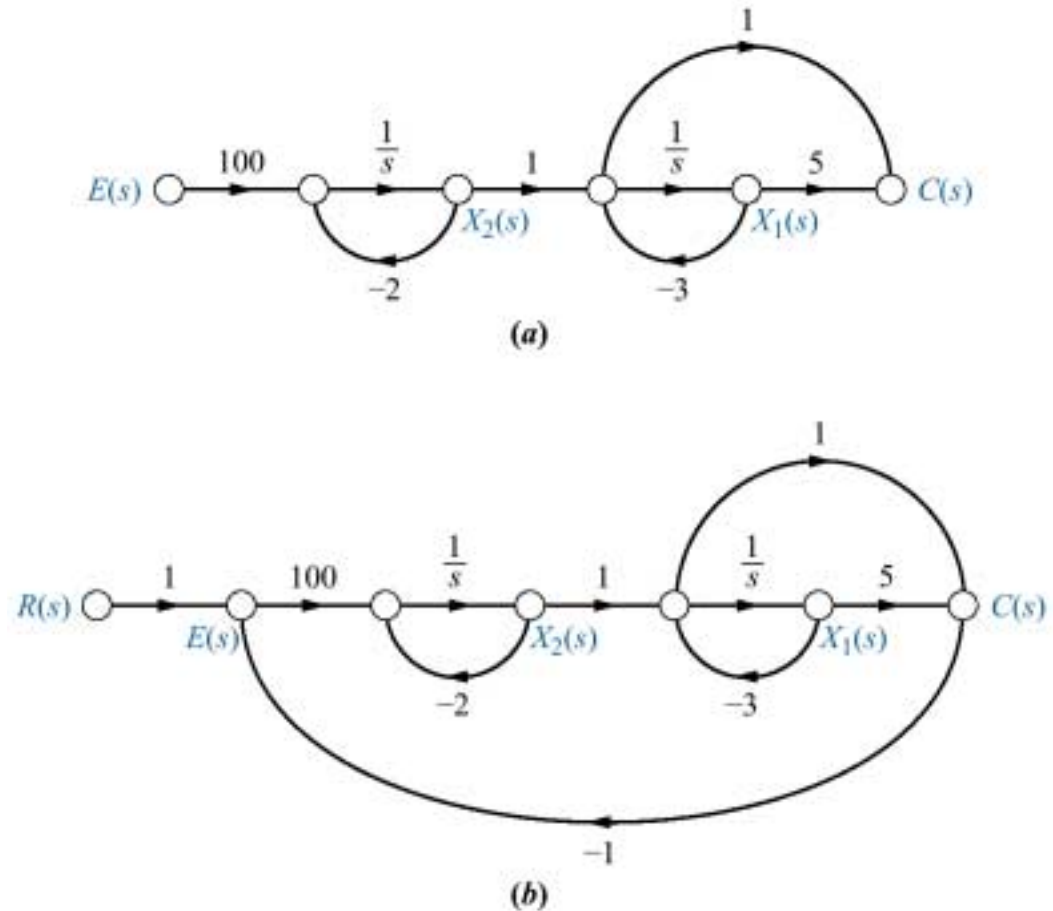


Figure 5.31
State-space forms for
 $C(s)/R(s) = (s+3)/[(s+4)(s+6)]$.
Note: $y = c(t)$

Form	Transfer Function	Signal-Flow Diagram	State Equations
Phase variable	$\frac{1}{(s^2+10s+24)}(s+3)$		$k = \begin{bmatrix} 0 & 1 \\ -24 & -10 \end{bmatrix} k + \begin{bmatrix} 0 \\ 1 \end{bmatrix} r$ $y = [1 \quad 0]x$
Parallel	$\frac{-1/2}{(s+4)} + \frac{3/2}{(s+6)}$		$k = \begin{bmatrix} -4 & 0 \\ 0 & -6 \end{bmatrix} k + \begin{bmatrix} -1/2 \\ 3/2 \end{bmatrix} r$ $y = [1 \quad 1]x$
Cascade	$\frac{1}{(s+4)} \cdot \frac{(s+3)}{(s+6)}$		$k = \begin{bmatrix} -6 & 1 \\ 0 & -4 \end{bmatrix} k + \begin{bmatrix} 0 \\ 1 \end{bmatrix} r$ $y = [-3 \quad 1]x$
Controller canonical	$\frac{1}{(s^2+10s+24)}(s+3)$		$k = \begin{bmatrix} -10 & -24 \\ 1 & 0 \end{bmatrix} k + \begin{bmatrix} 1 \\ 0 \end{bmatrix} r$ $y = [1 \quad 0]x$
Observer canonical	$\frac{1/s + 3/s^2}{1 + 10/s + 24/s^2}$		$k = \begin{bmatrix} -10 & 1 \\ -24 & 0 \end{bmatrix} k + \begin{bmatrix} 1 \\ 0 \end{bmatrix} r$ $y = [1 \quad 0]x$

Figure 5.32
State-space
transformations

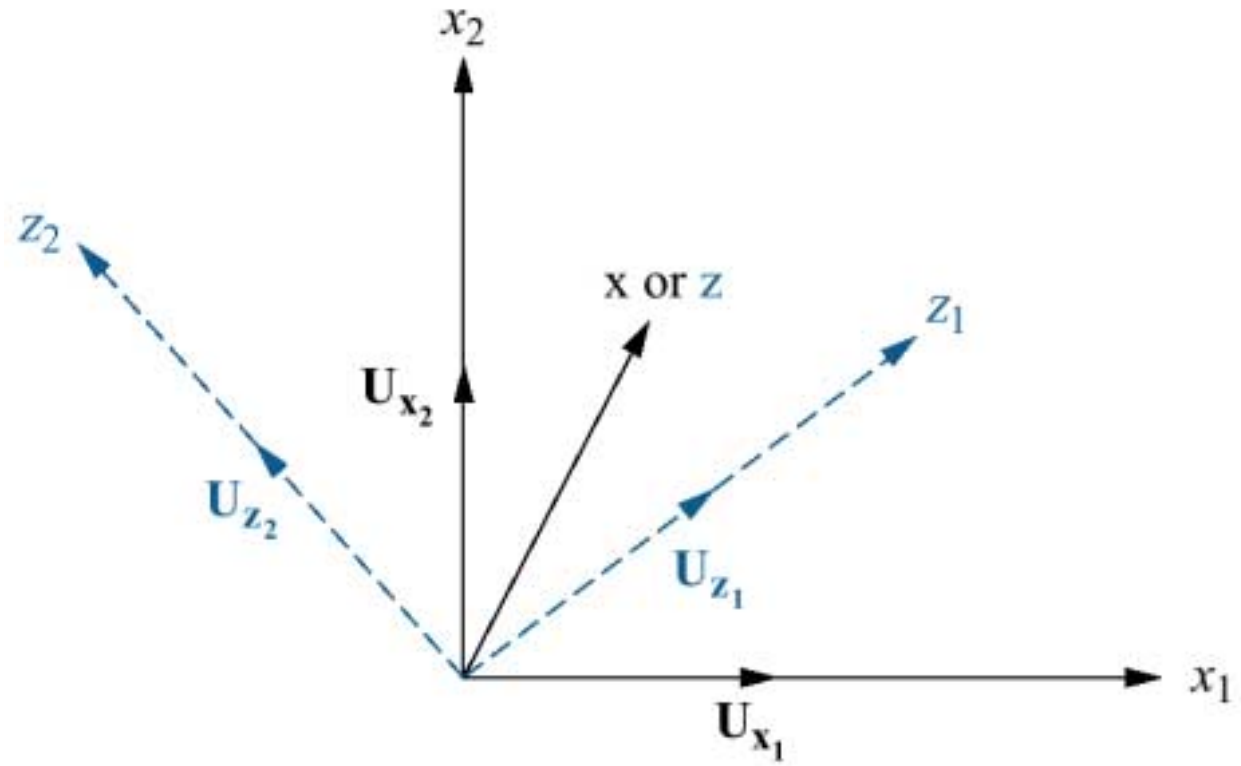


Figure 5.33

To be an eigenvector, the transformation \mathbf{Ax} must be collinear with \mathbf{x} ; thus in (a) \mathbf{x} is not an eigenvector; in (b), it is.

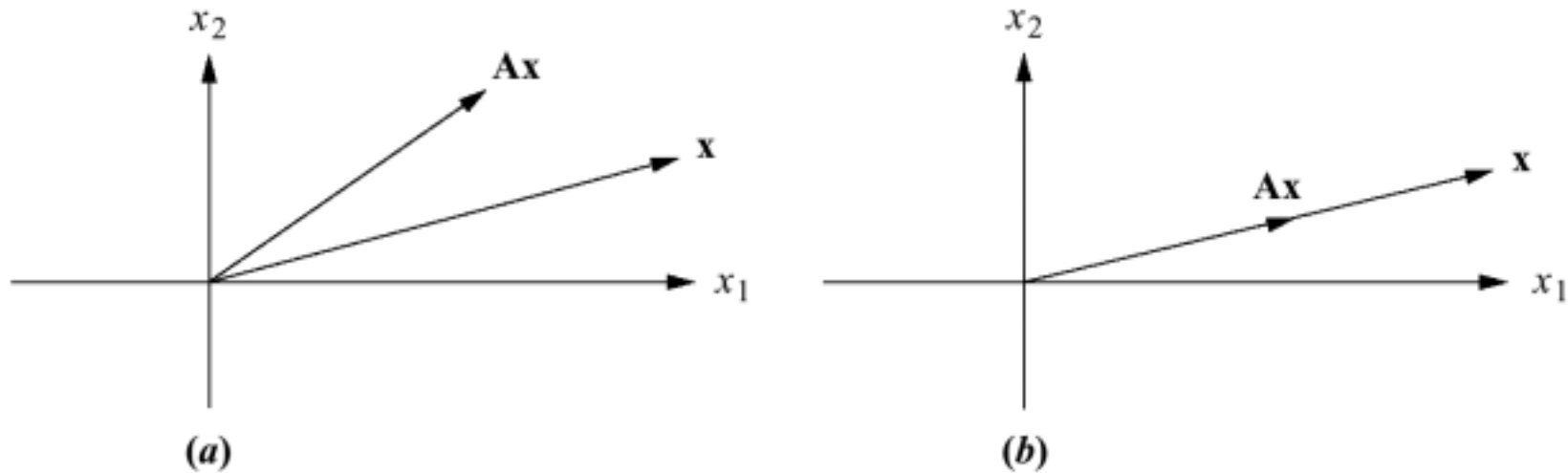


Figure 5.34

Alvin, a manned submersible, explored the wreckage of the *Titanic* with a tethered robot, *Jason Junior*.

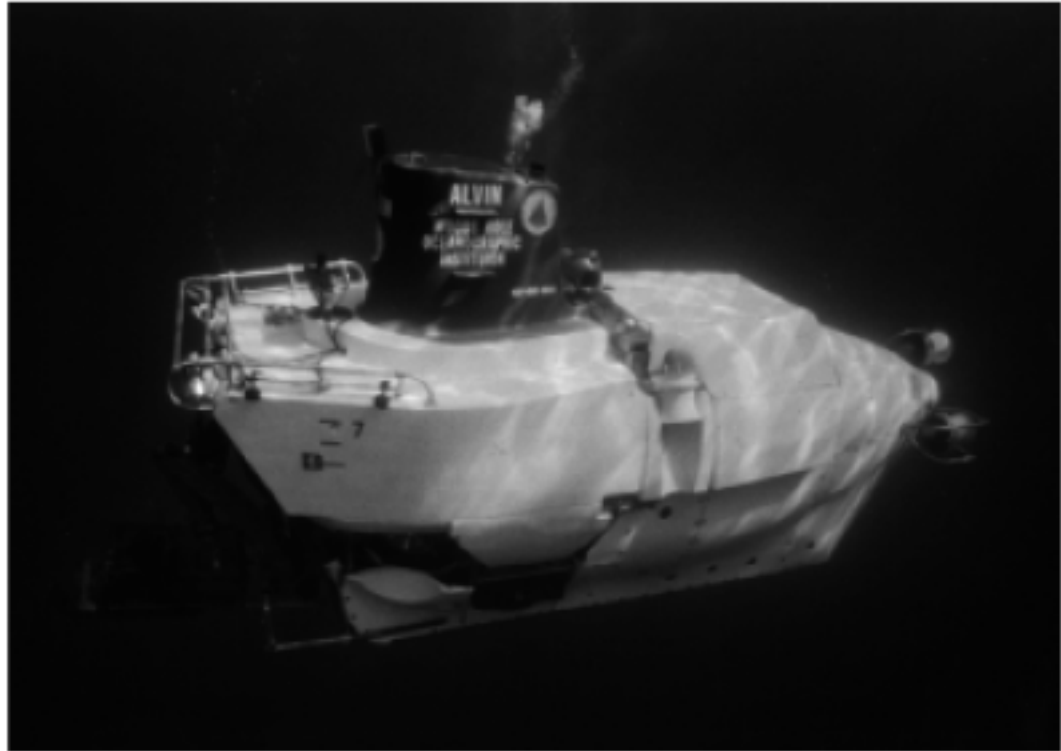


Figure 5.35

Block diagram reduction for the antenna azimuth position control system:

- a. original;
- b. pushing input potentiometer to the right past the summing junction;
- c. showing equivalent forward transfer function;
- d. final closed-loop transfer function

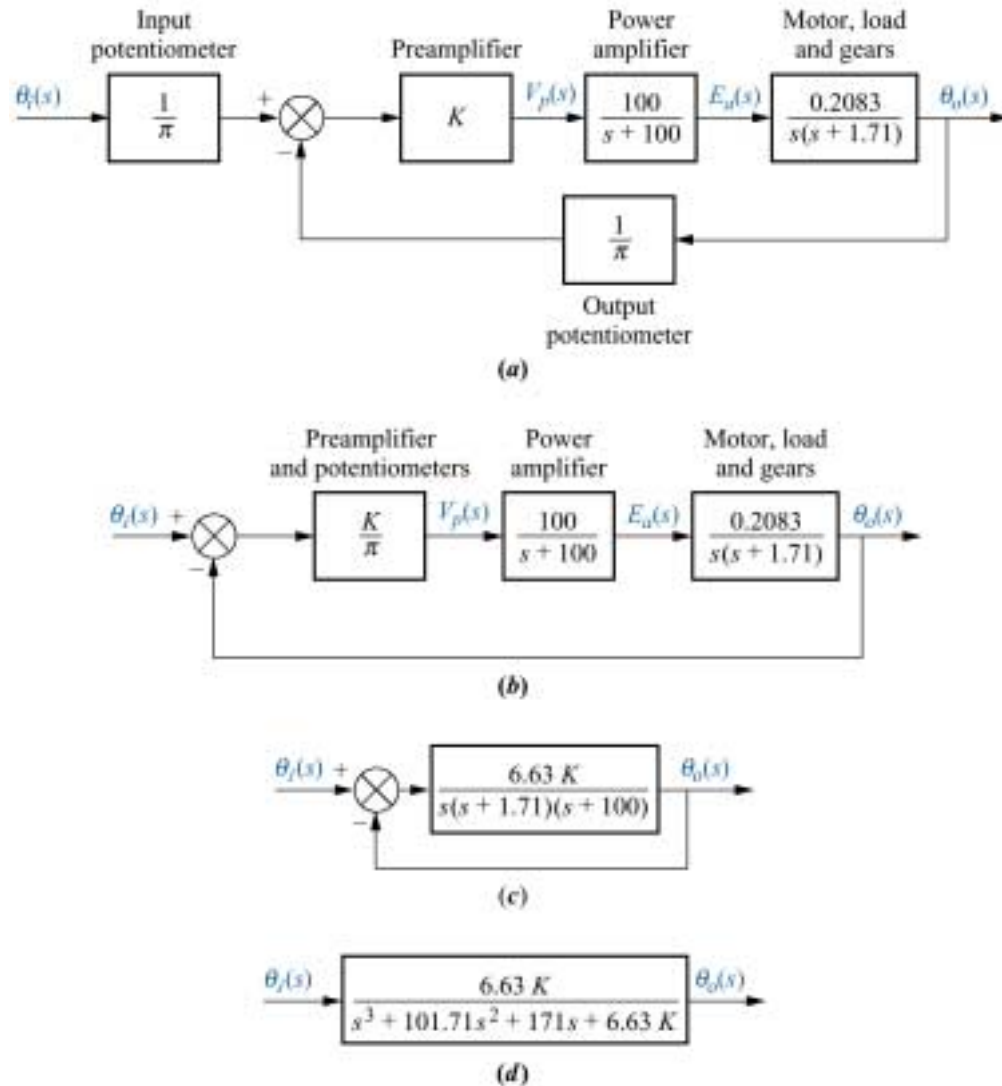


Figure 5.36

Signal-flow graph for
the antenna azimuth
position control
system

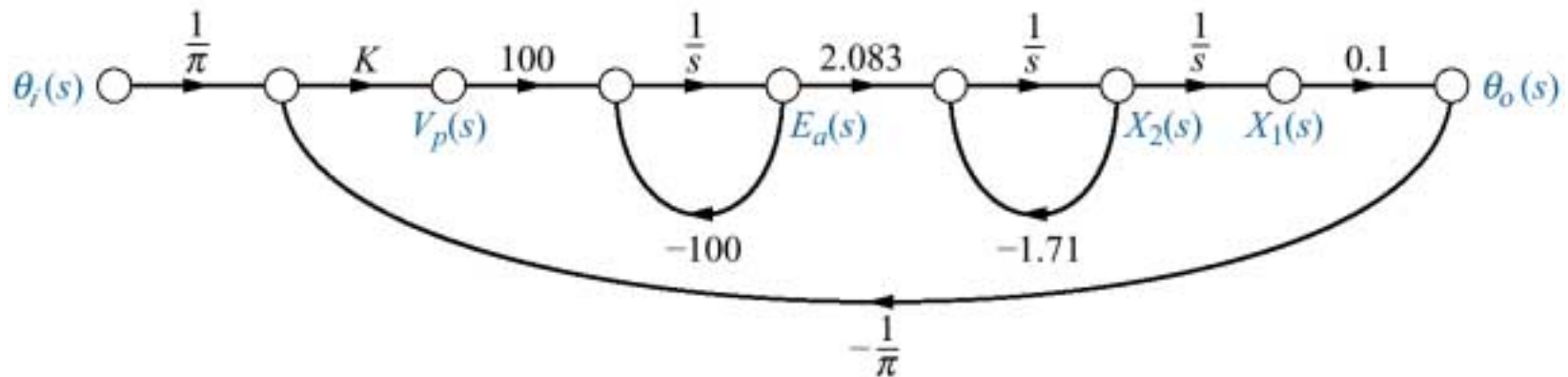


Figure 5.37

Block diagram of the UFSS vehicle's elevator and vehicle dynamics, from which a signal-flow graph can be drawn

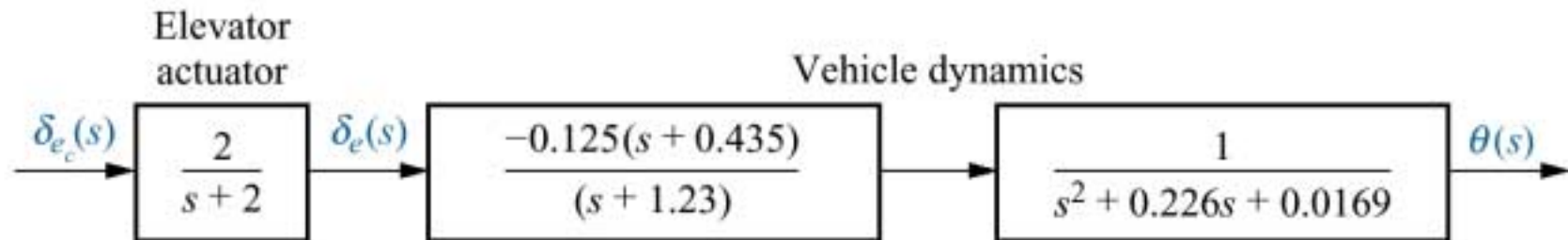


Figure 5.38

Signal-flow graph representation of the UFSS vehicle's pitch-control system:

a. without position and rate feedback;

b. with position and rate feedback

(Note: Explicitly required variables are:
 $x_1 = q$, $x_2 = dq/dt$,
 and $x_4 = d_e$)

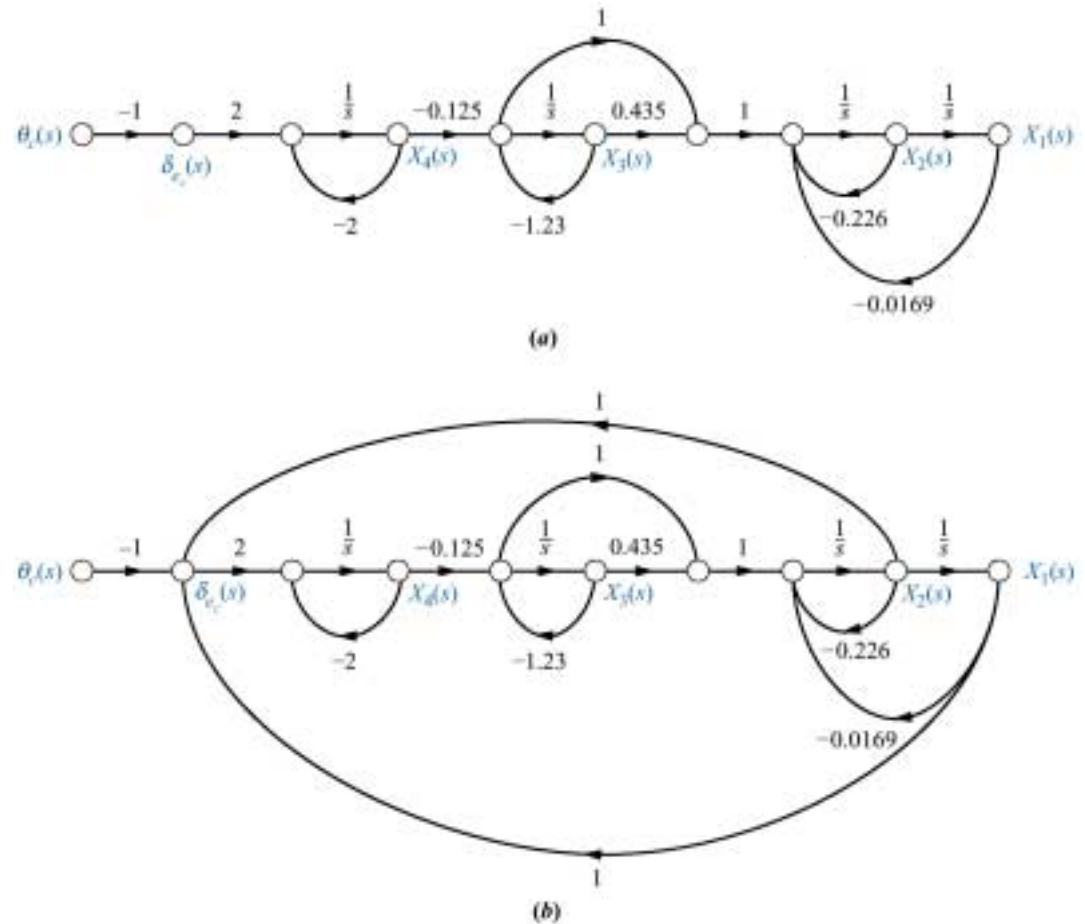


Figure 5.39

Block diagram
of the heading
control system
for the UFSS
vehicle

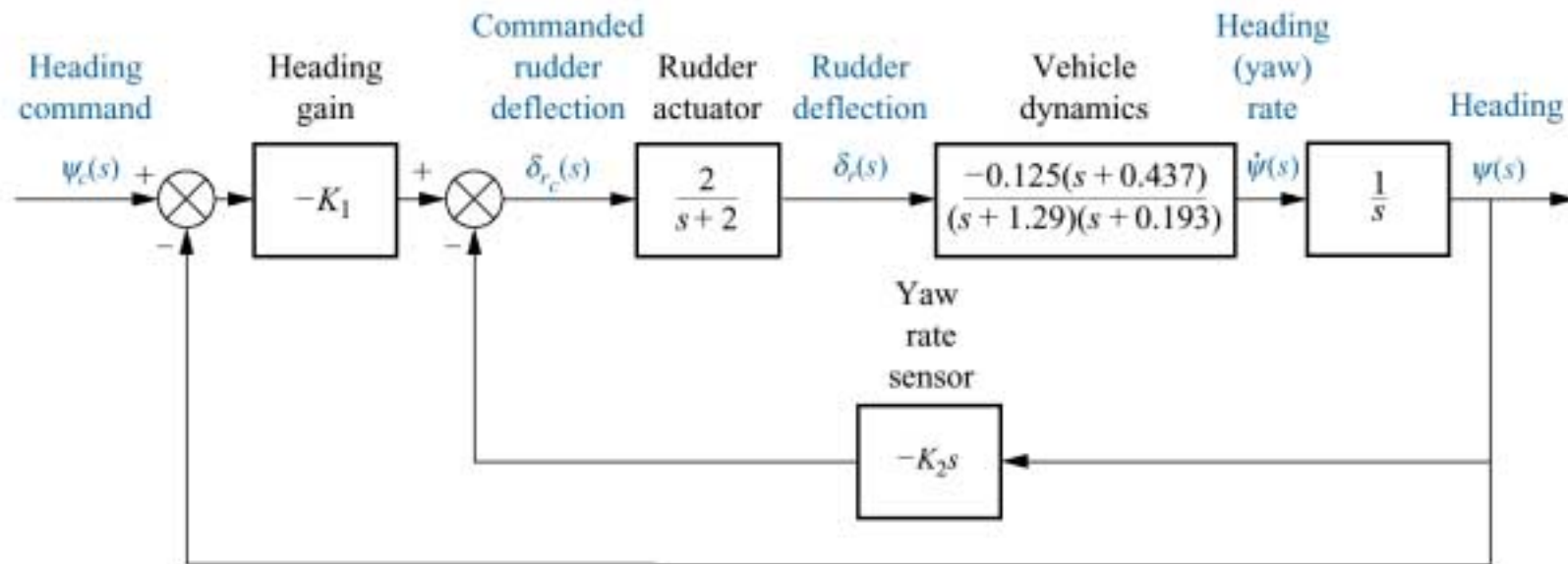


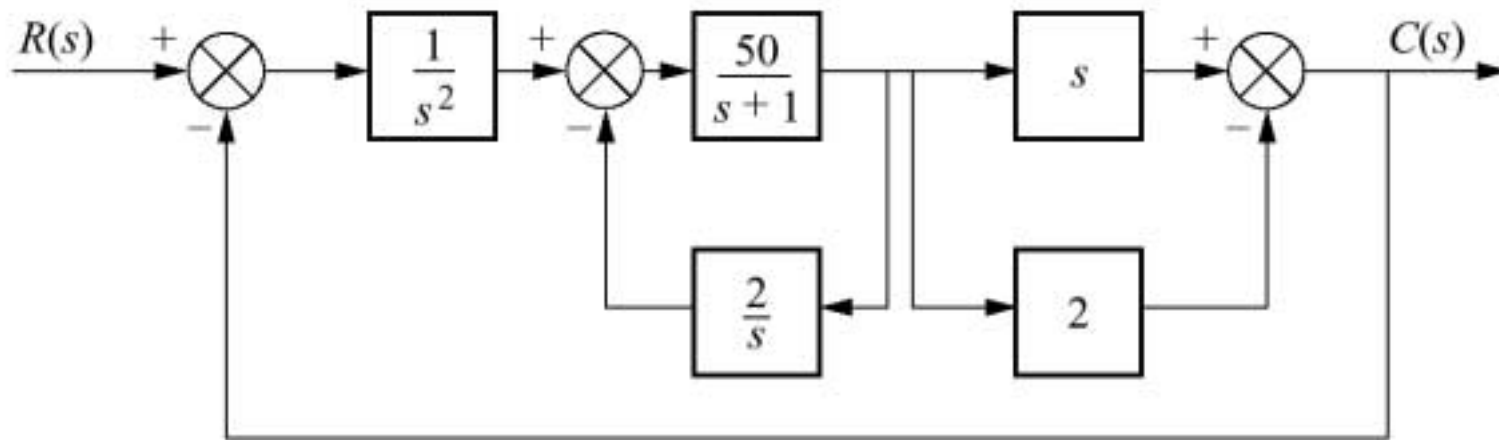
Figure P5.1

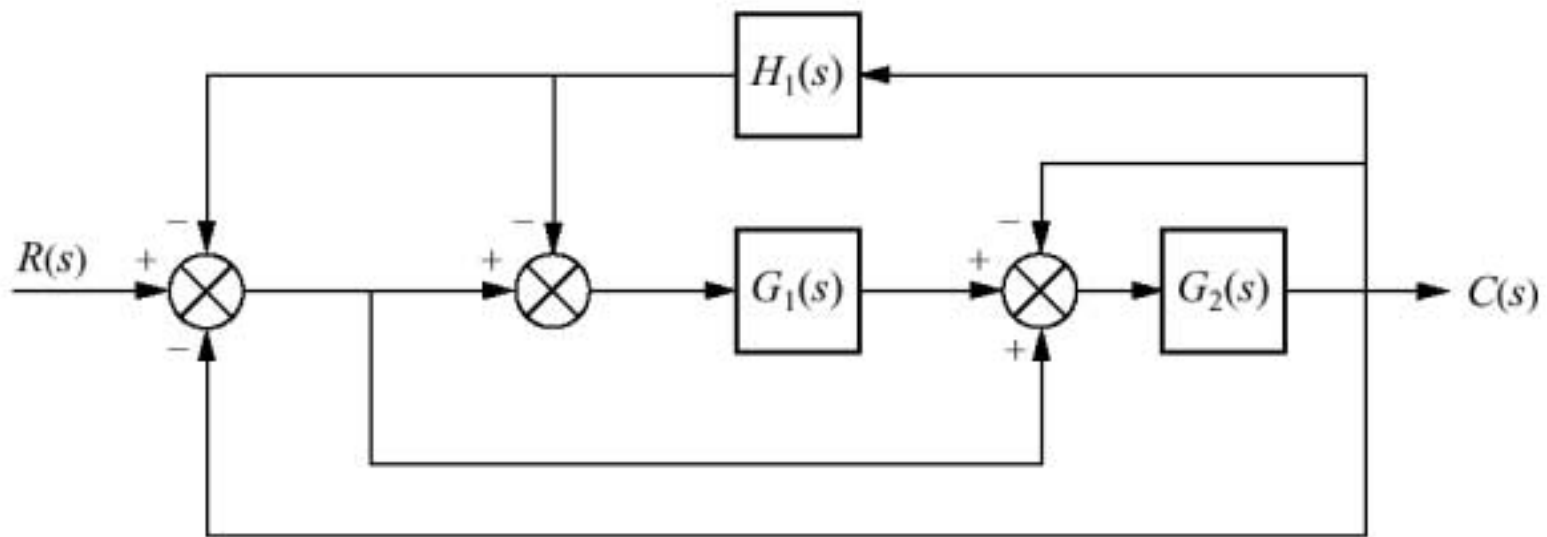
Figure P5.2

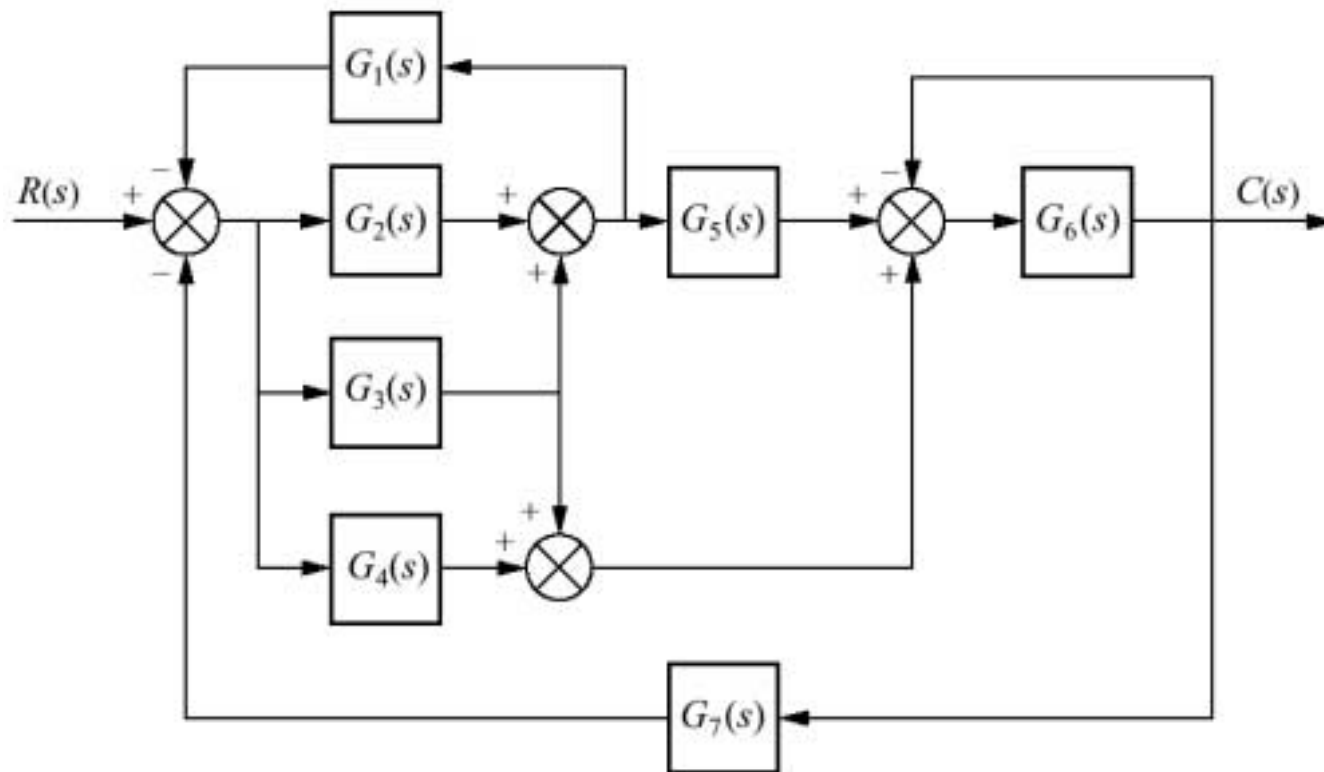
Figure P5.3

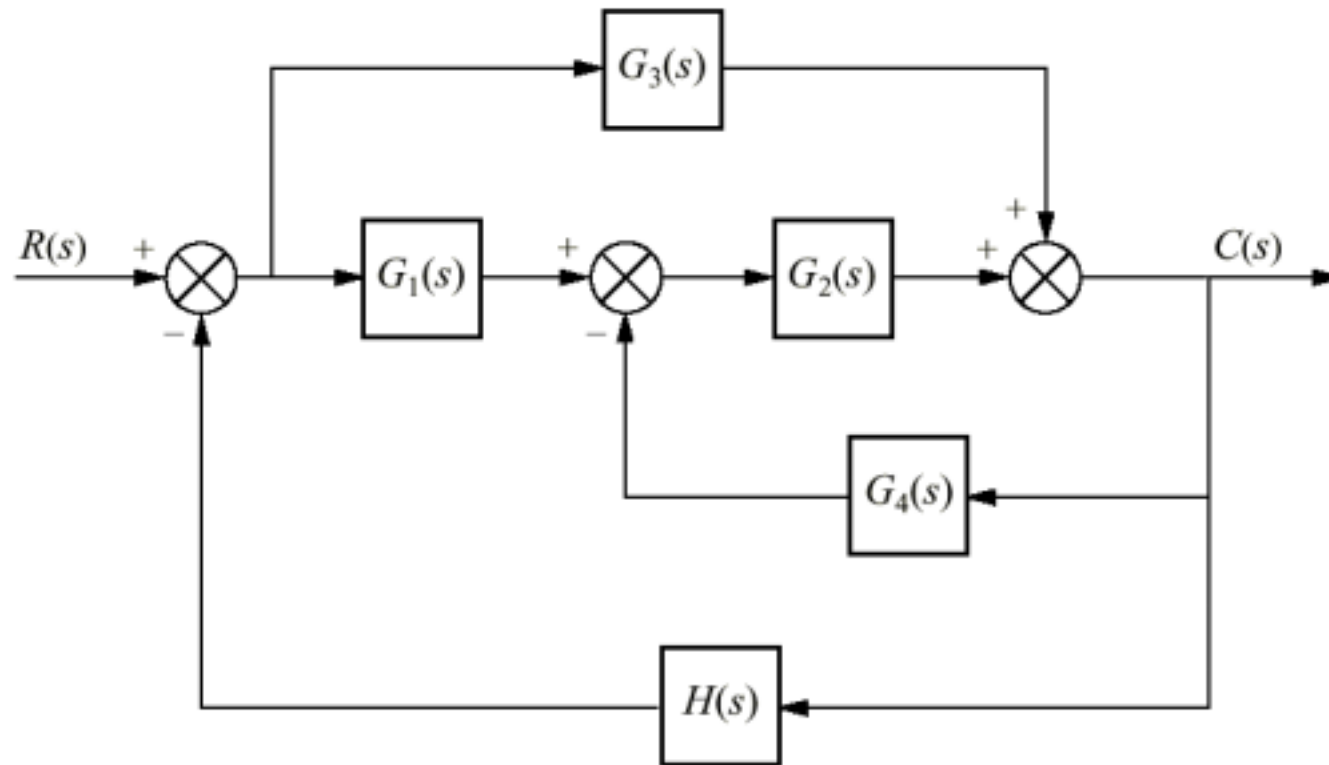
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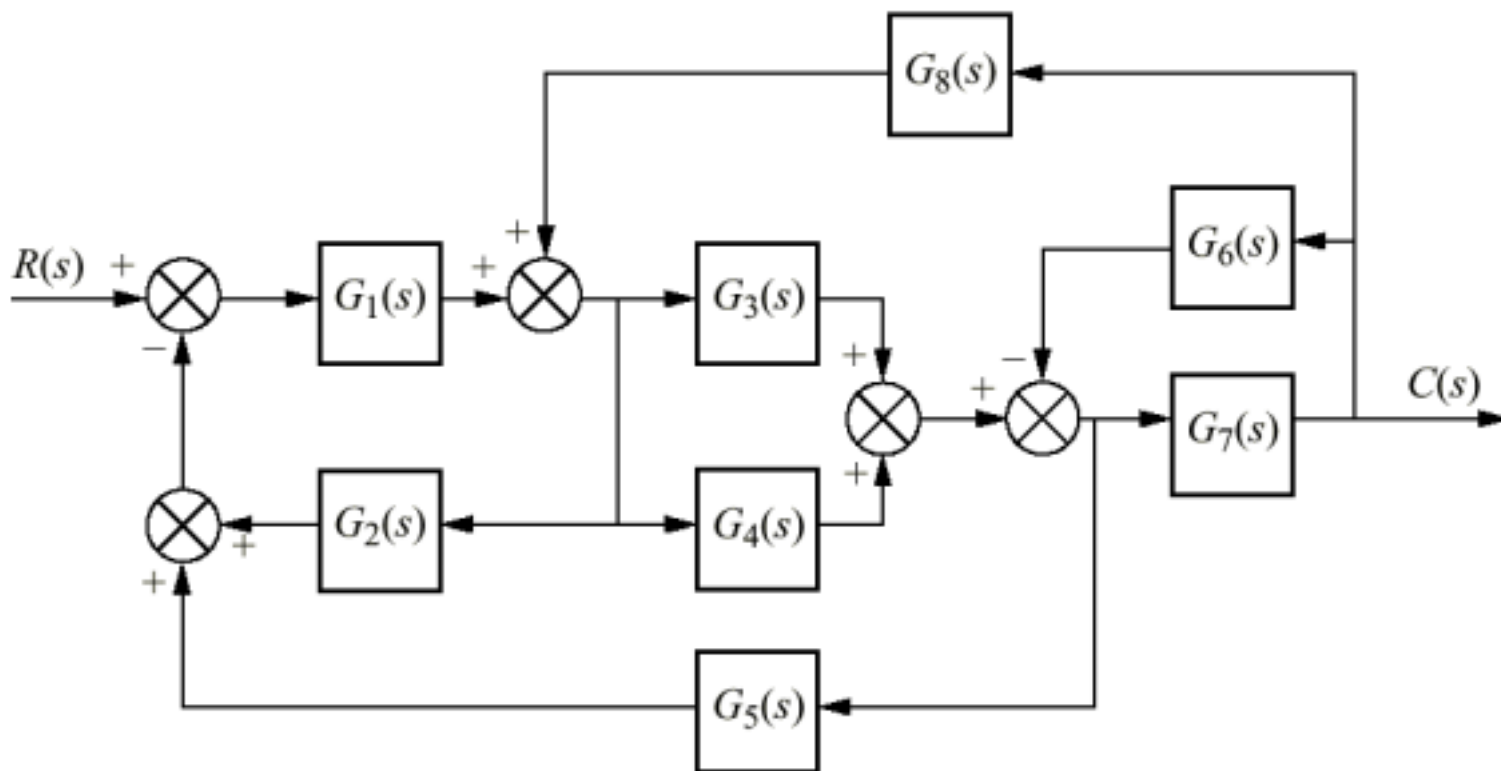
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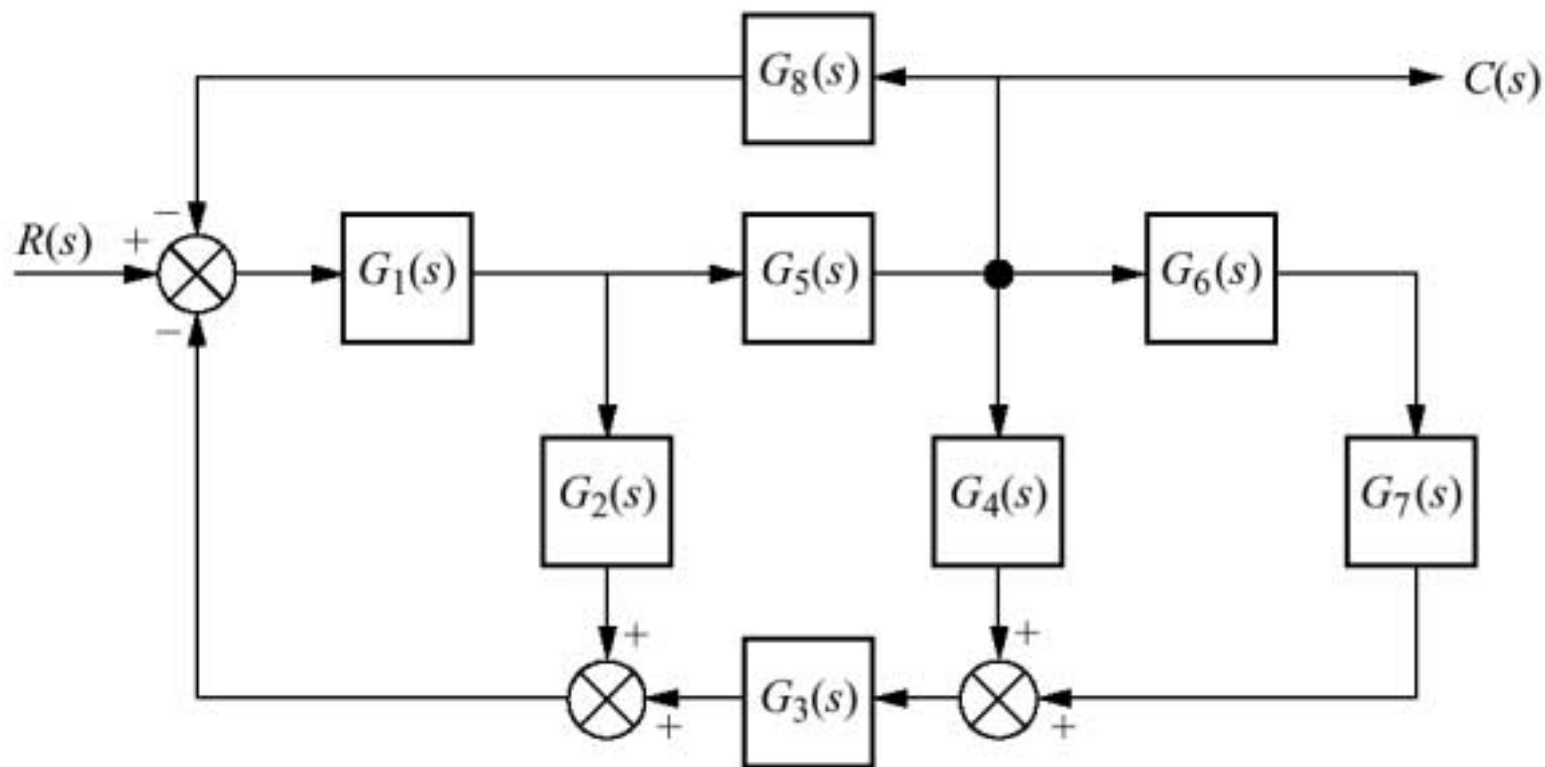
Figure P5.6

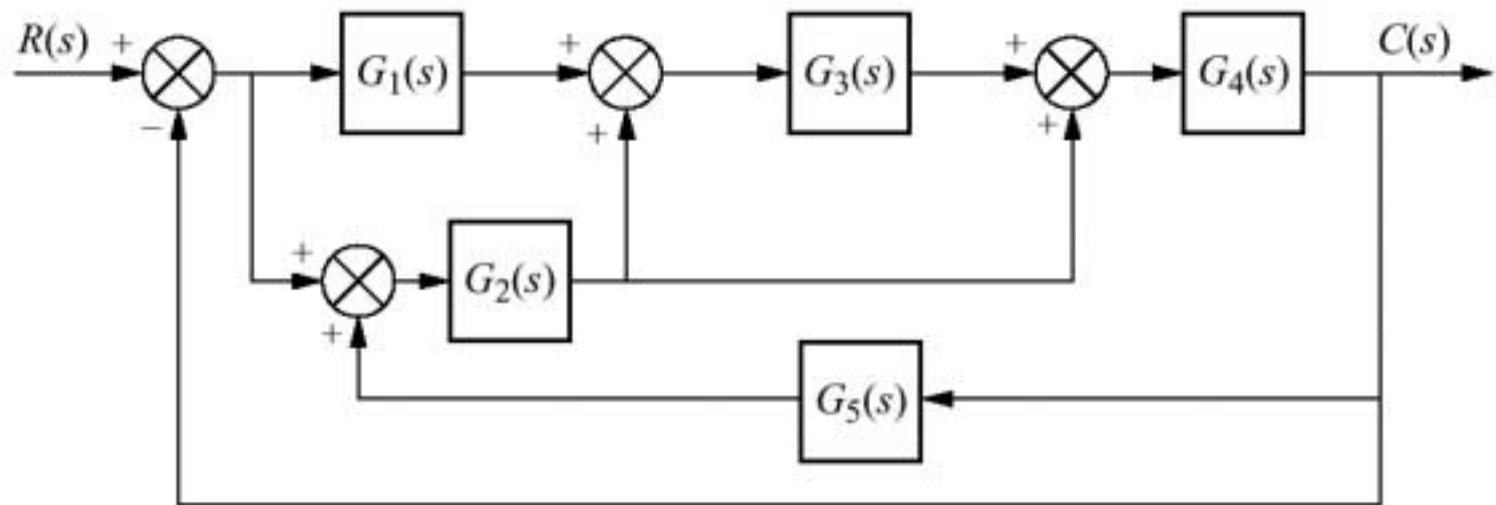
Figure P5.7

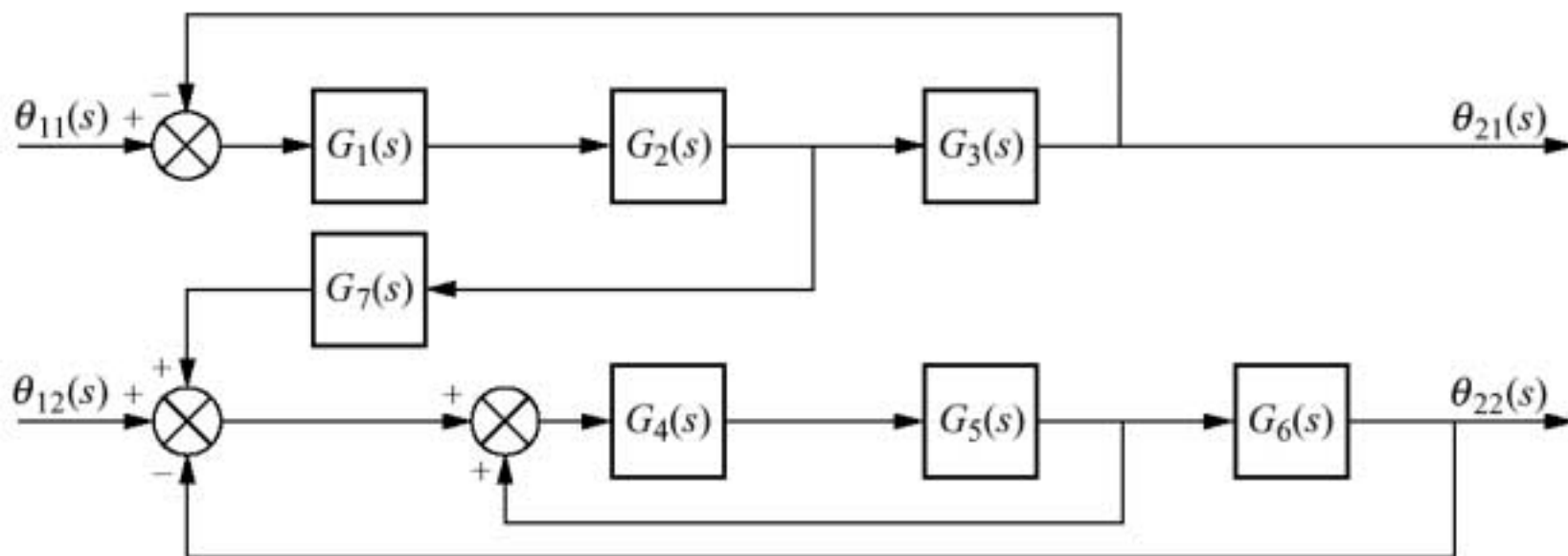
Figure P5.8

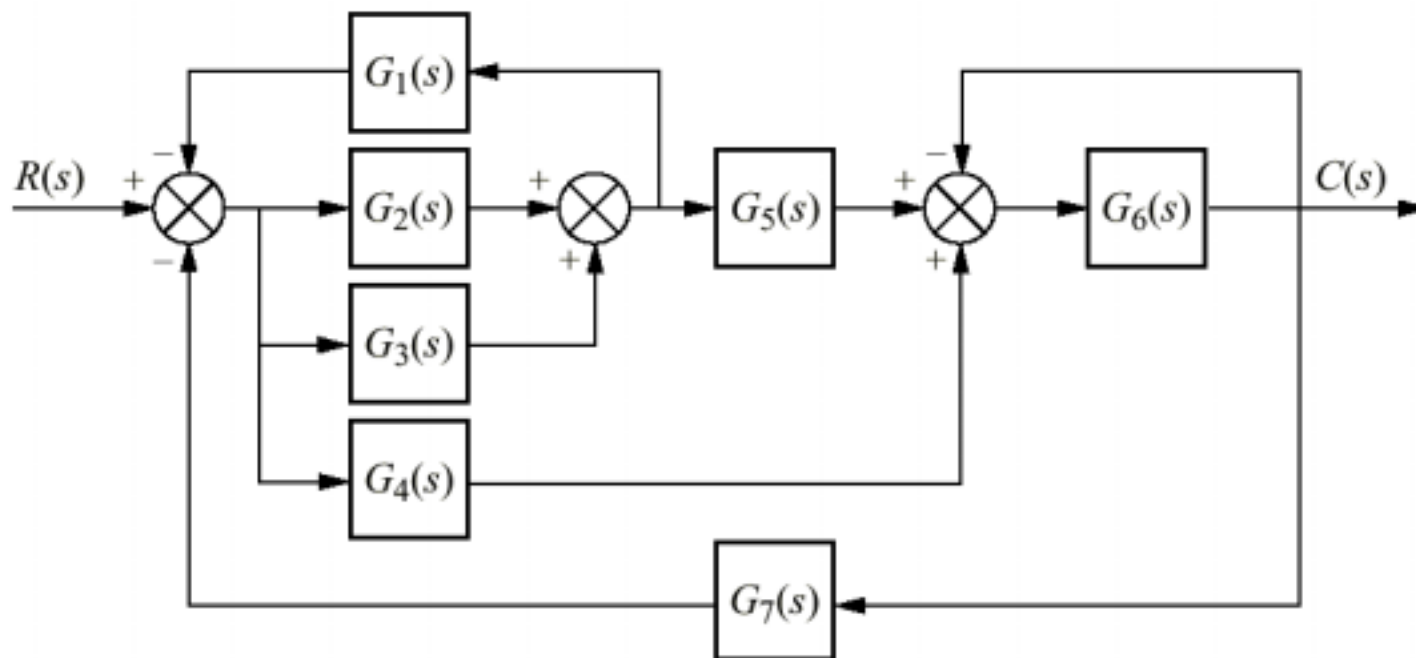
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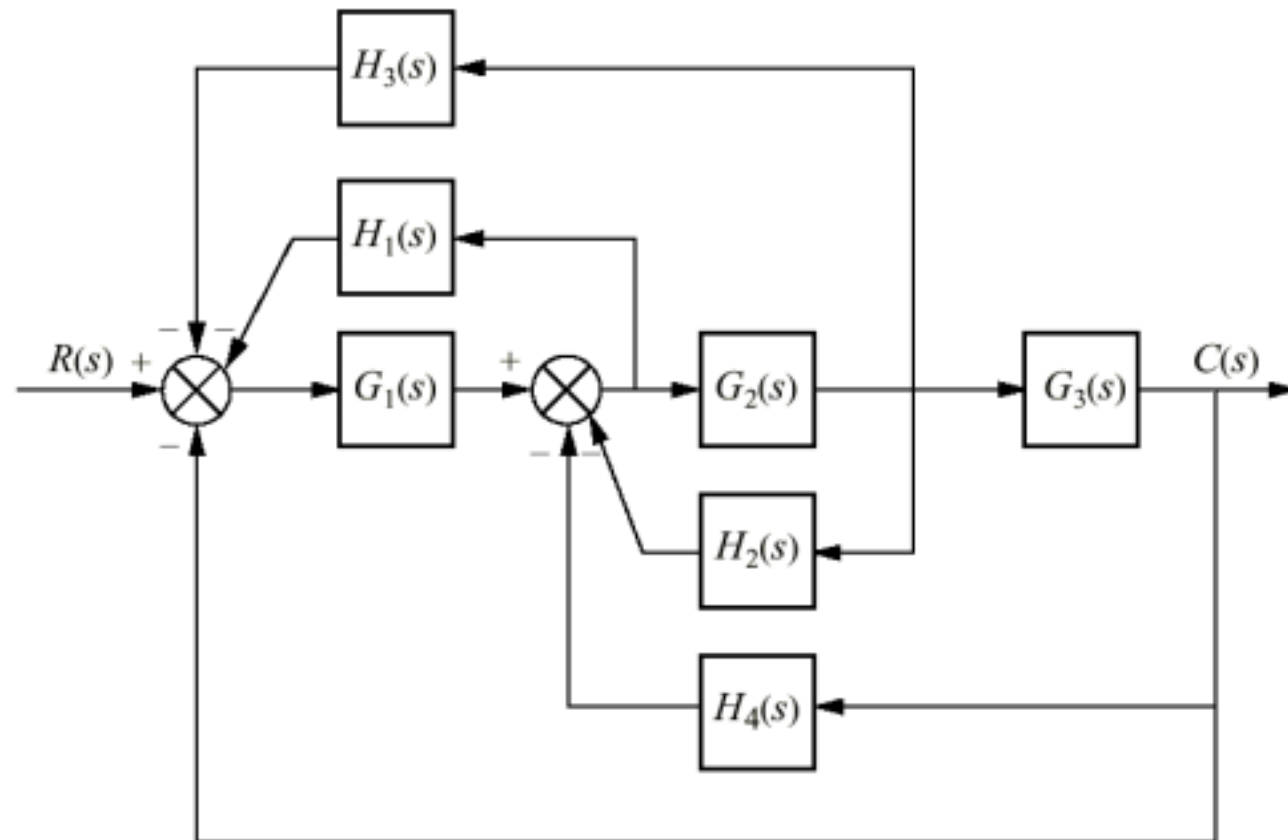
Figure P5.10

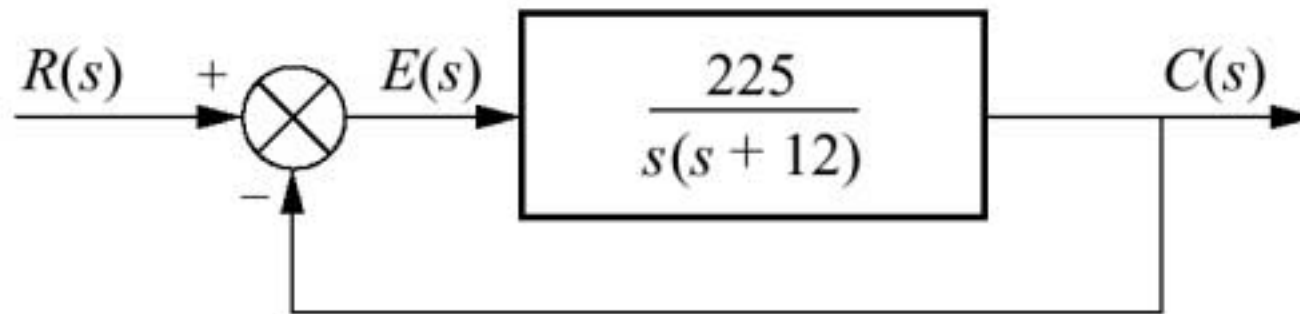
Figure P5.11

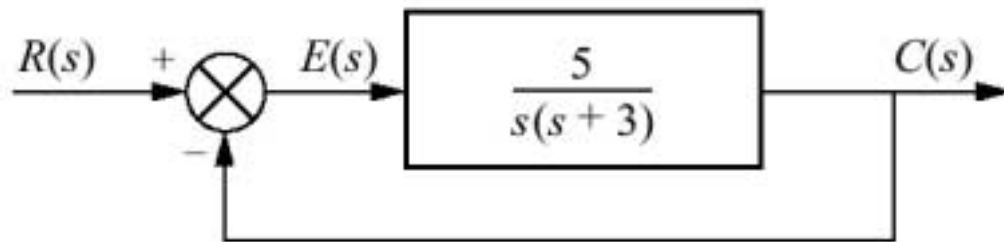
Figure P5.12

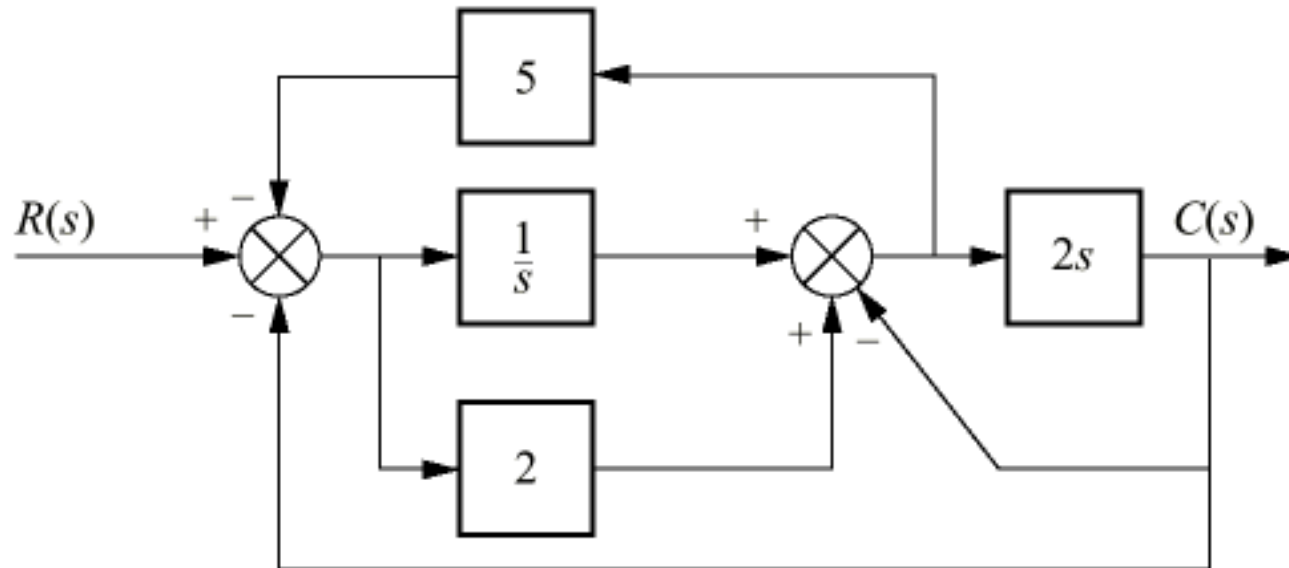
Figure P5.13

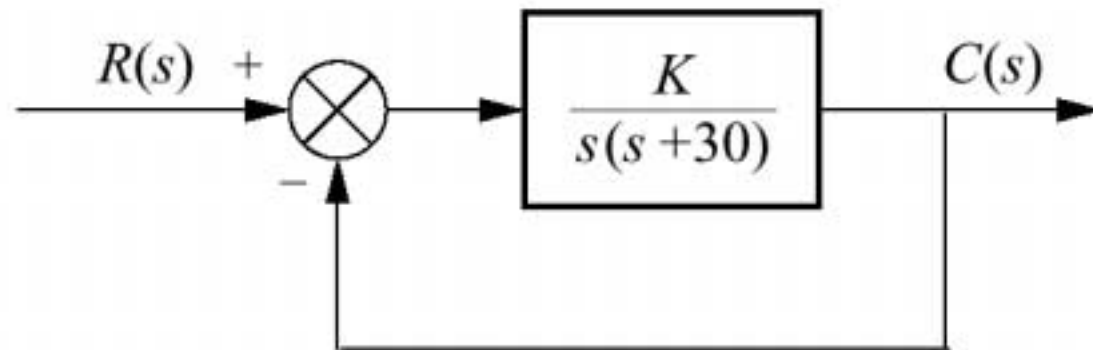
Figure P5.14

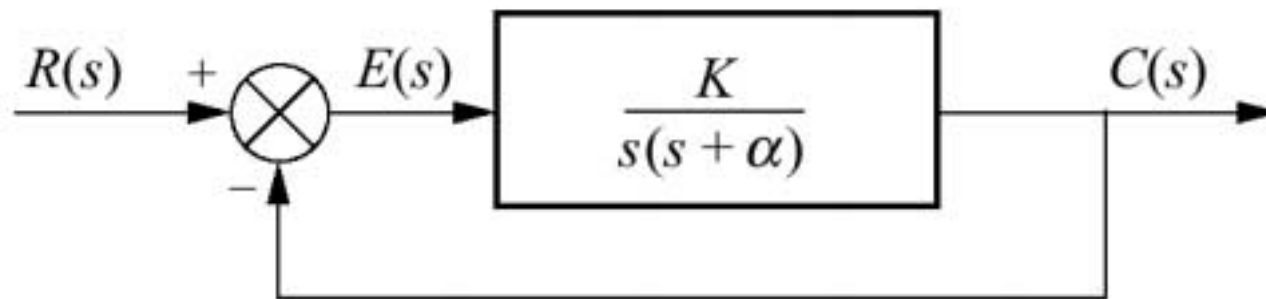
Figure P5.15

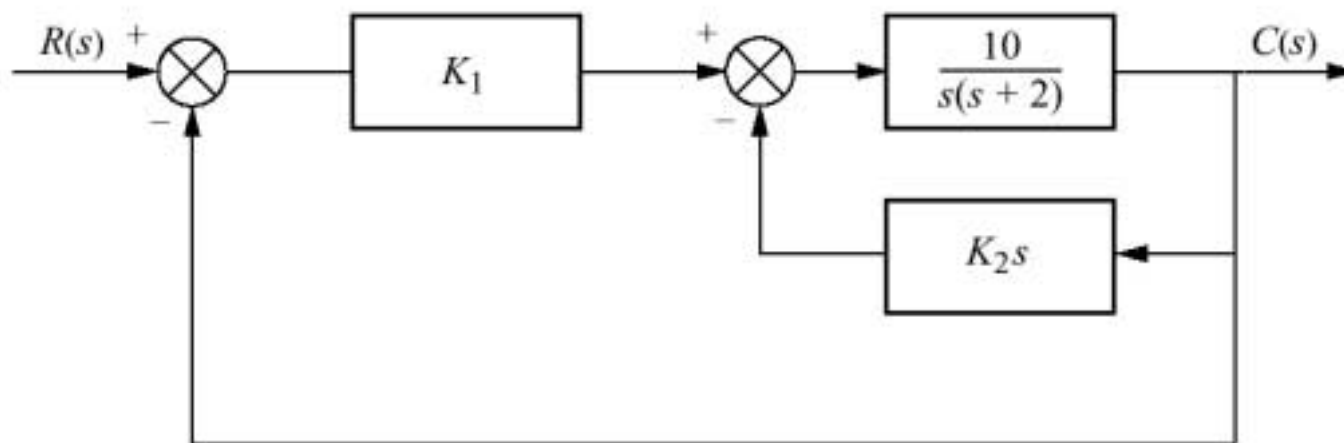
Figure P5.16

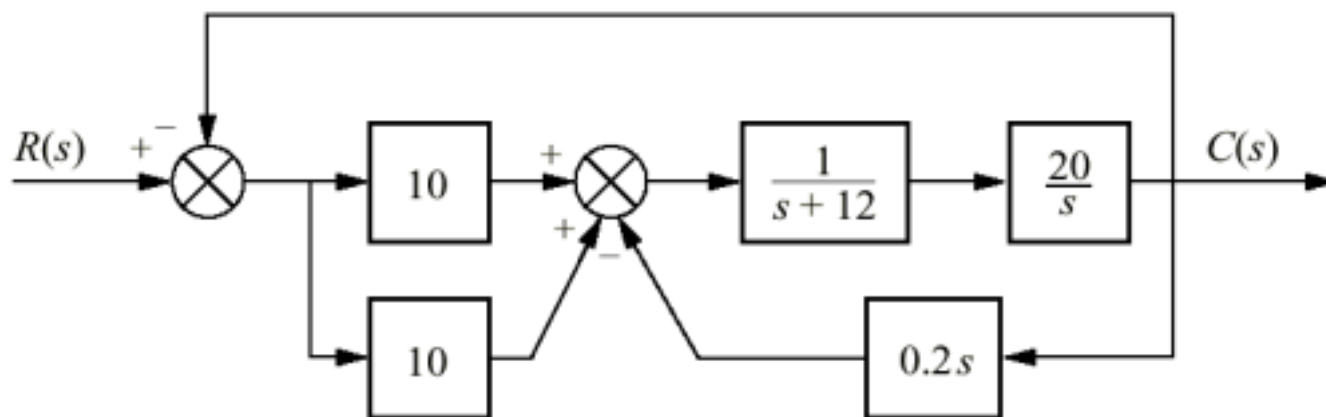
Figure P5.17

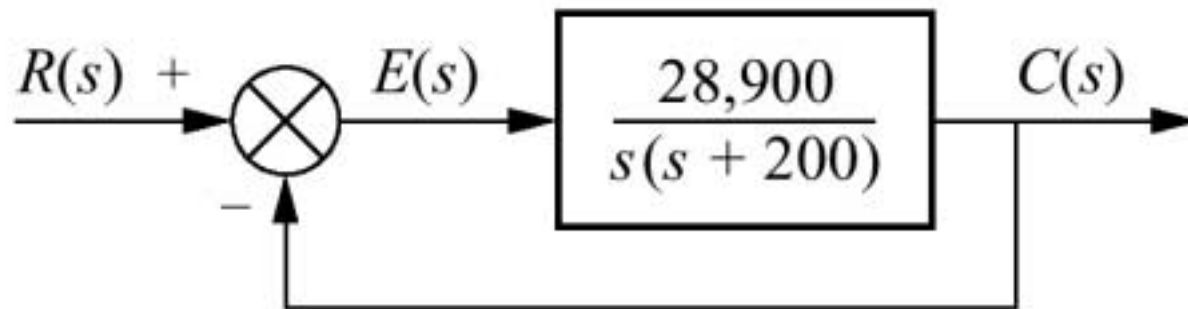
Figure P5.18

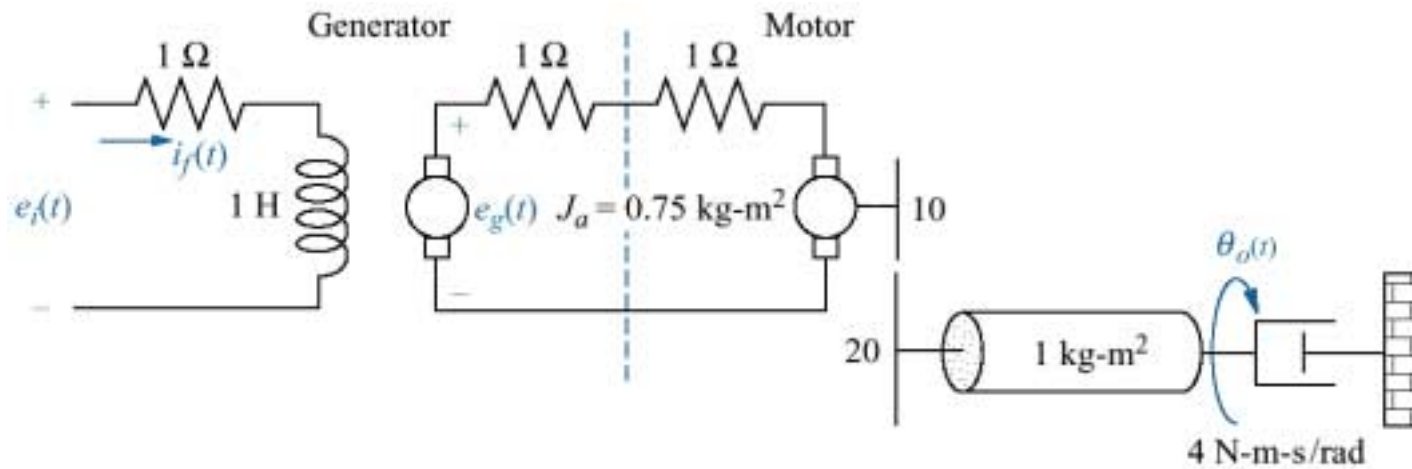
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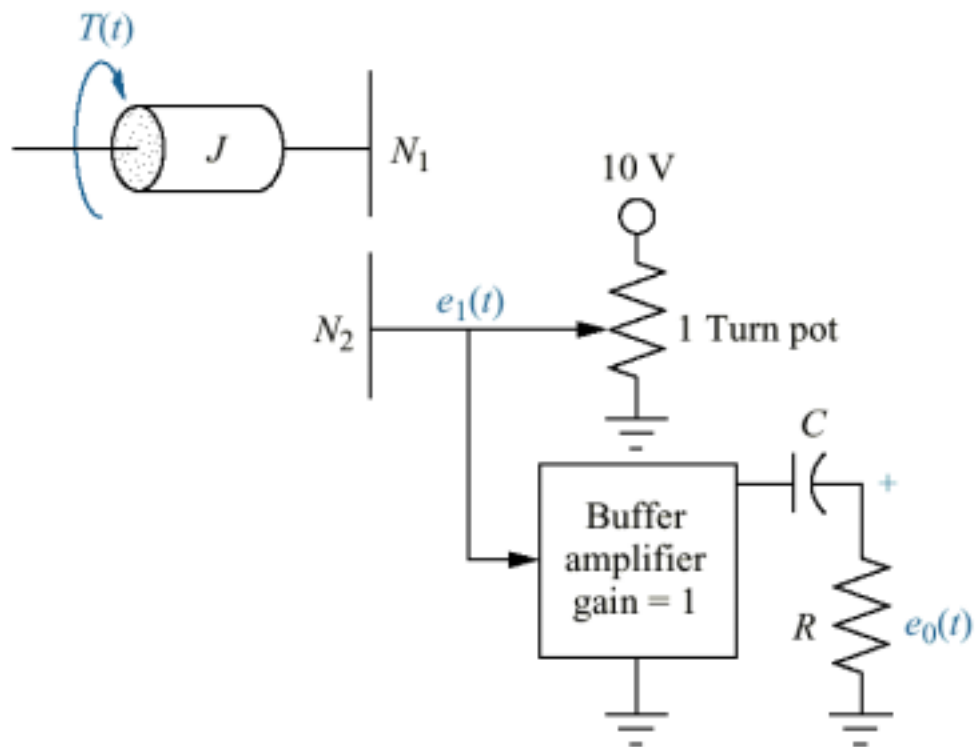
Figure P5.20

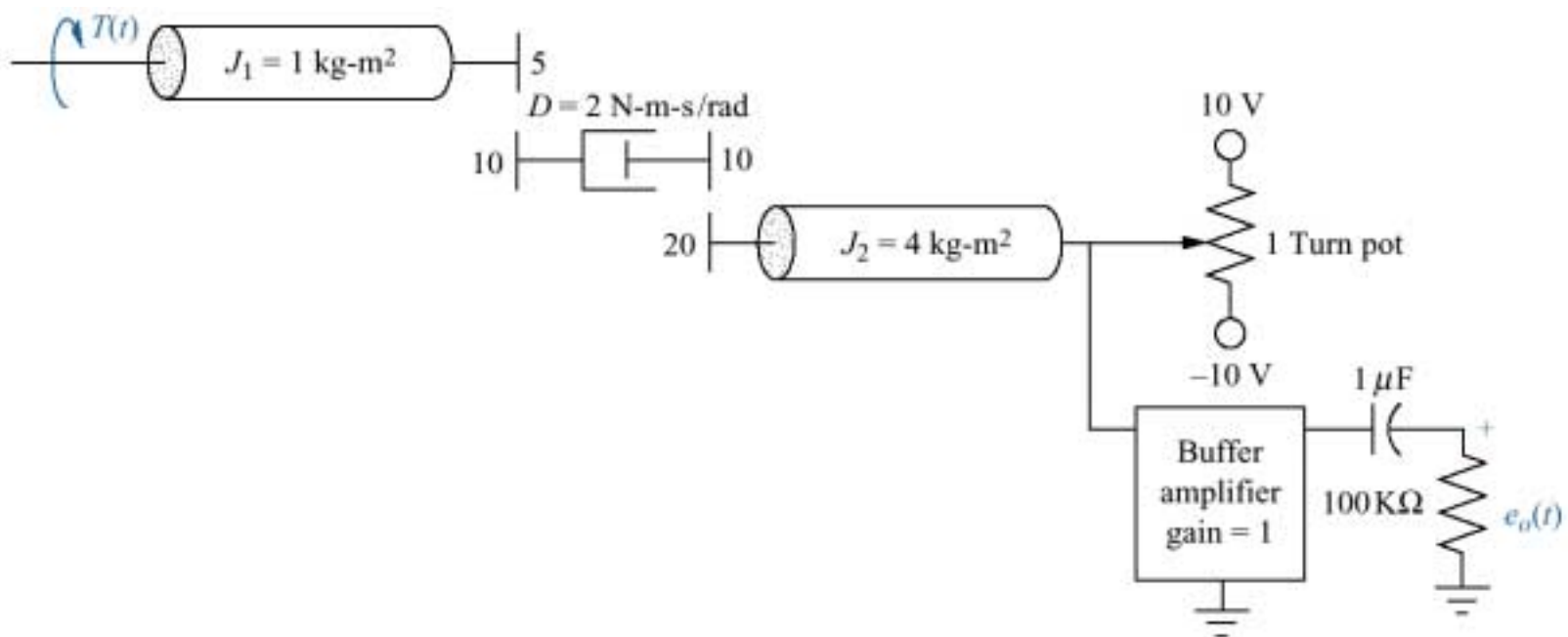
Figure P5.21

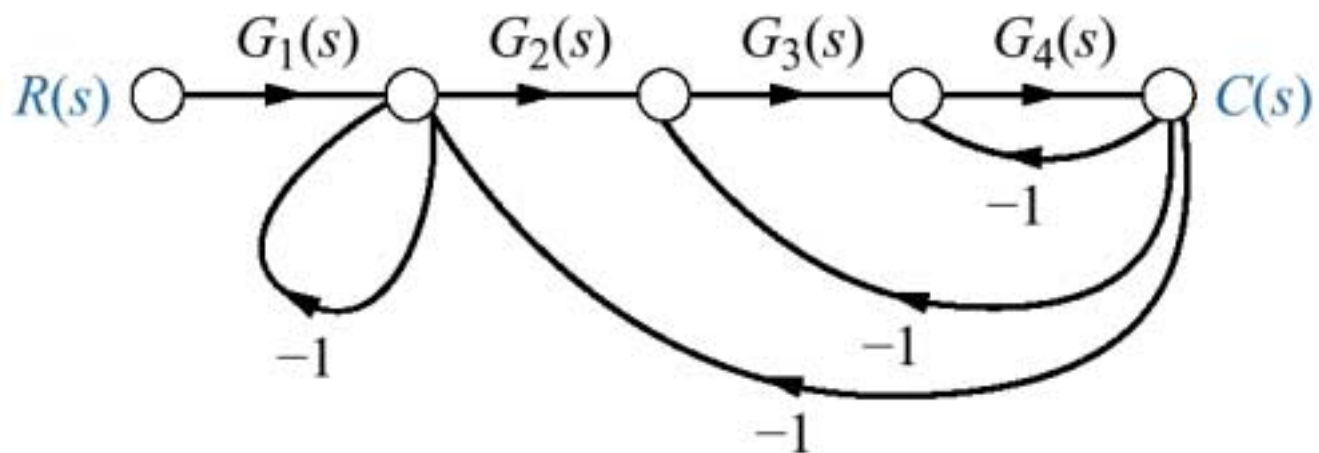
Figure P5.22

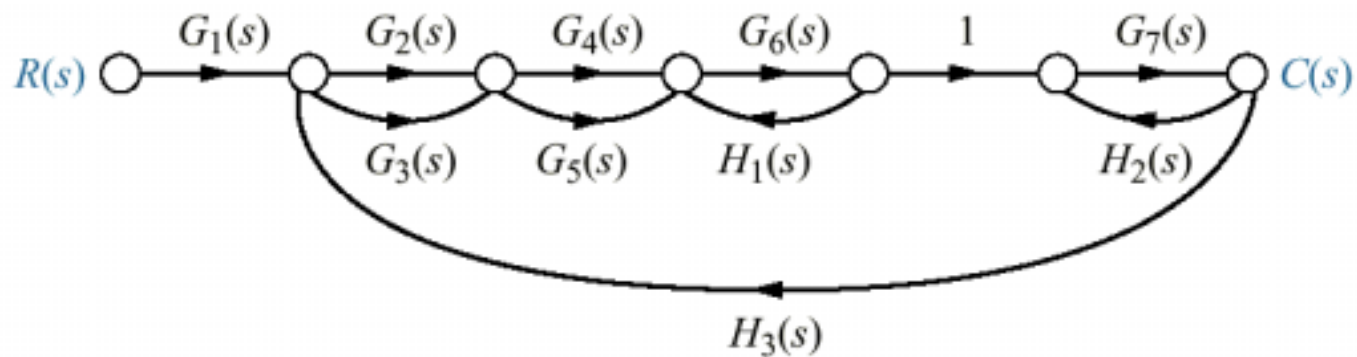
Figure P5.23

Figure P5.24
(figure continues)

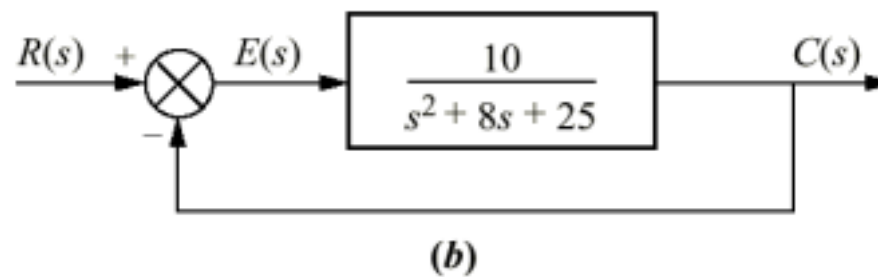
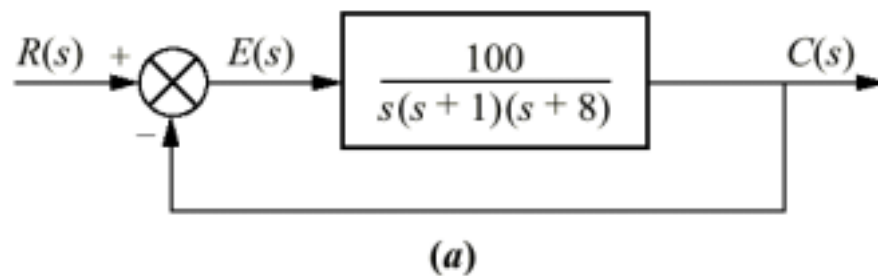
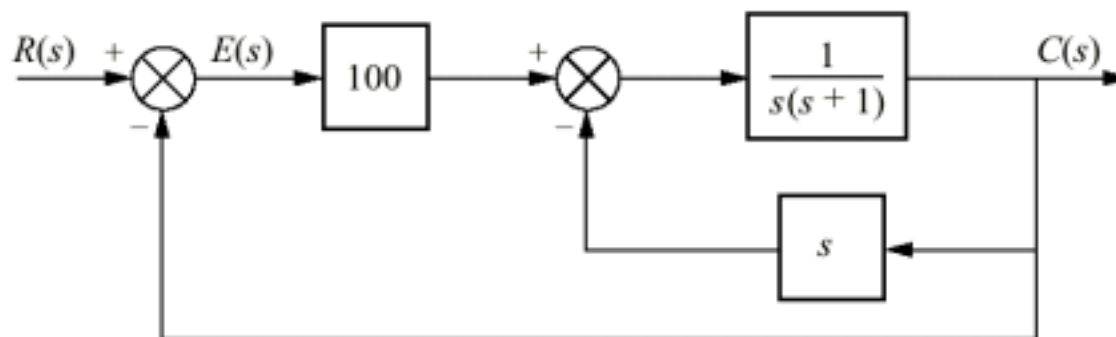
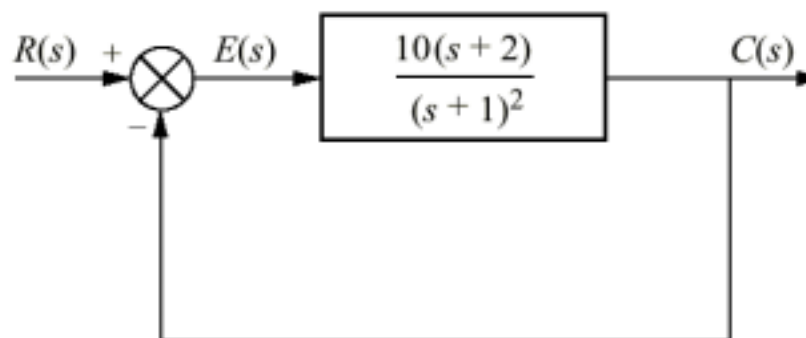


Figure P5.24
(continued)



(c)



(d)

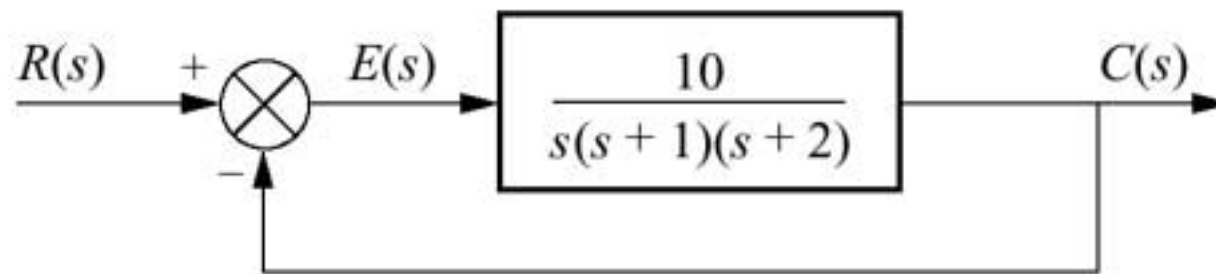
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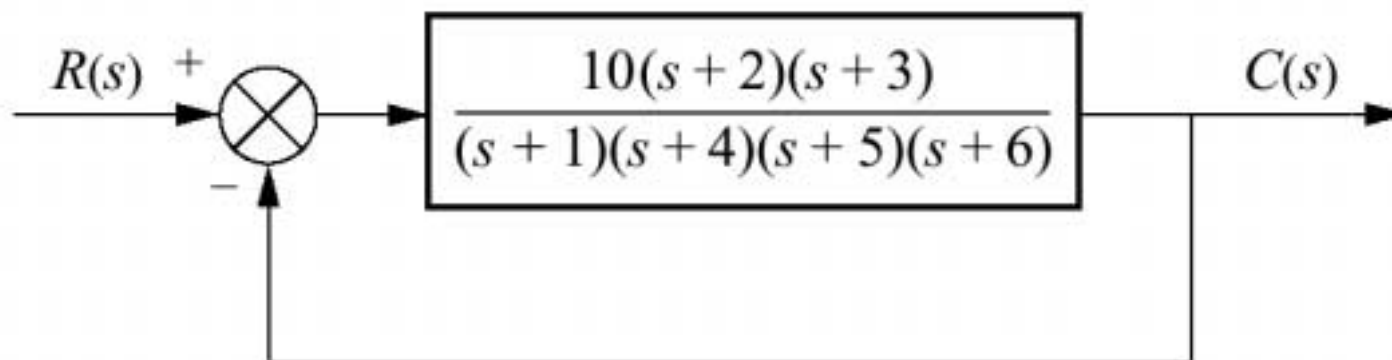
Figure P5.26

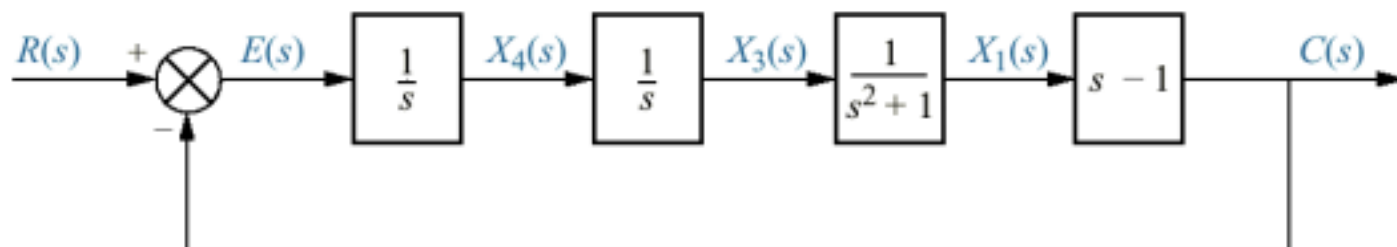
Figure P5.27

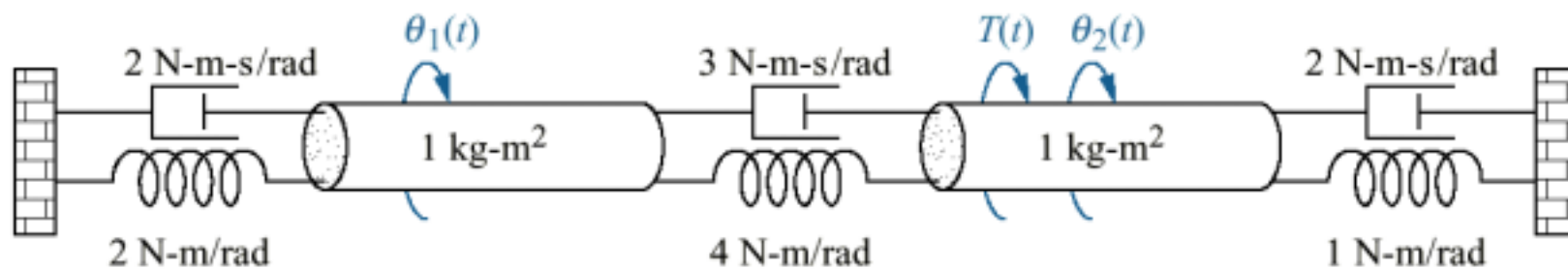
Figure P5.28

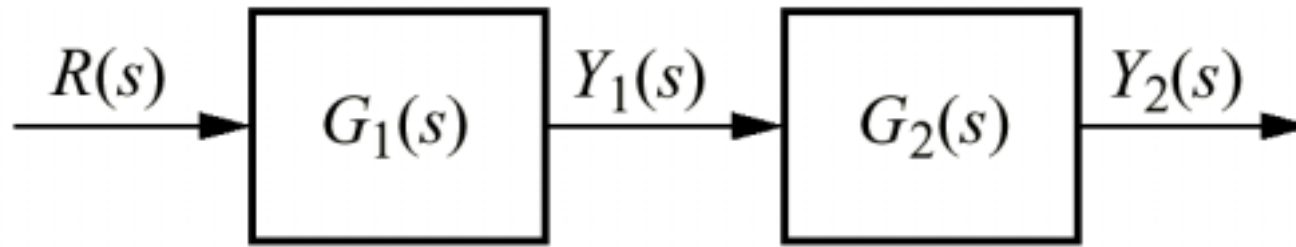
Figure P5.29

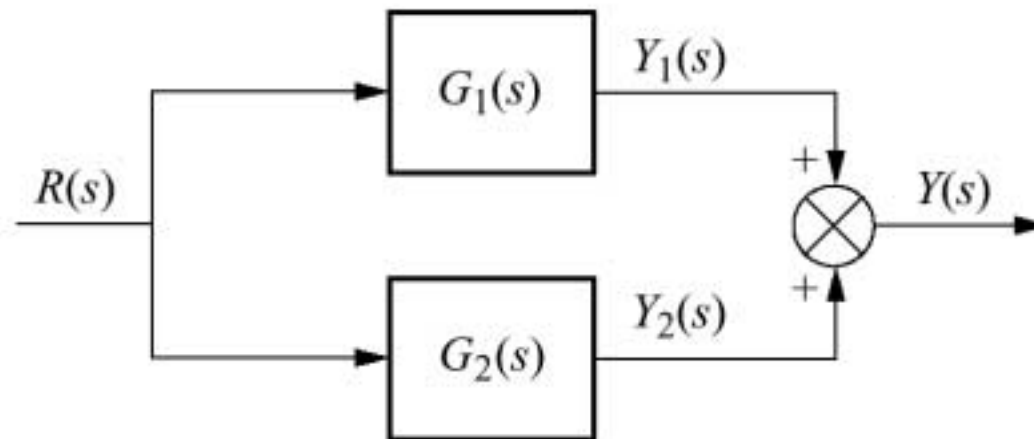
Figure P5.30

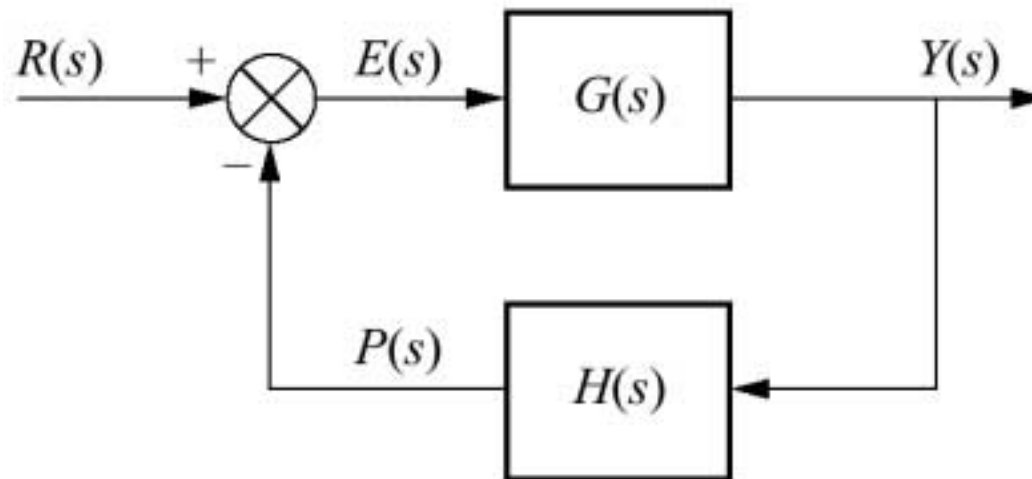
Figure P5.31

Figure P5.32
Space shuttle pitch control system (simplified)

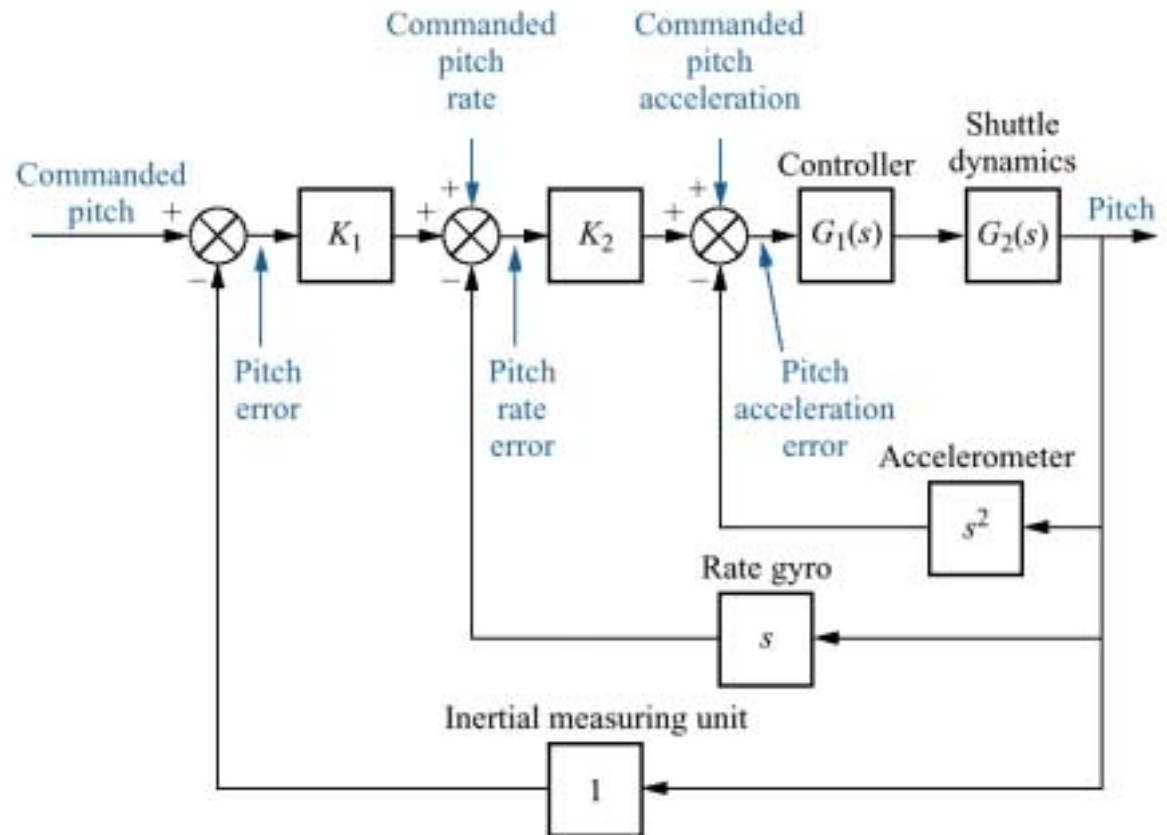


Figure P5.33
AM modulator

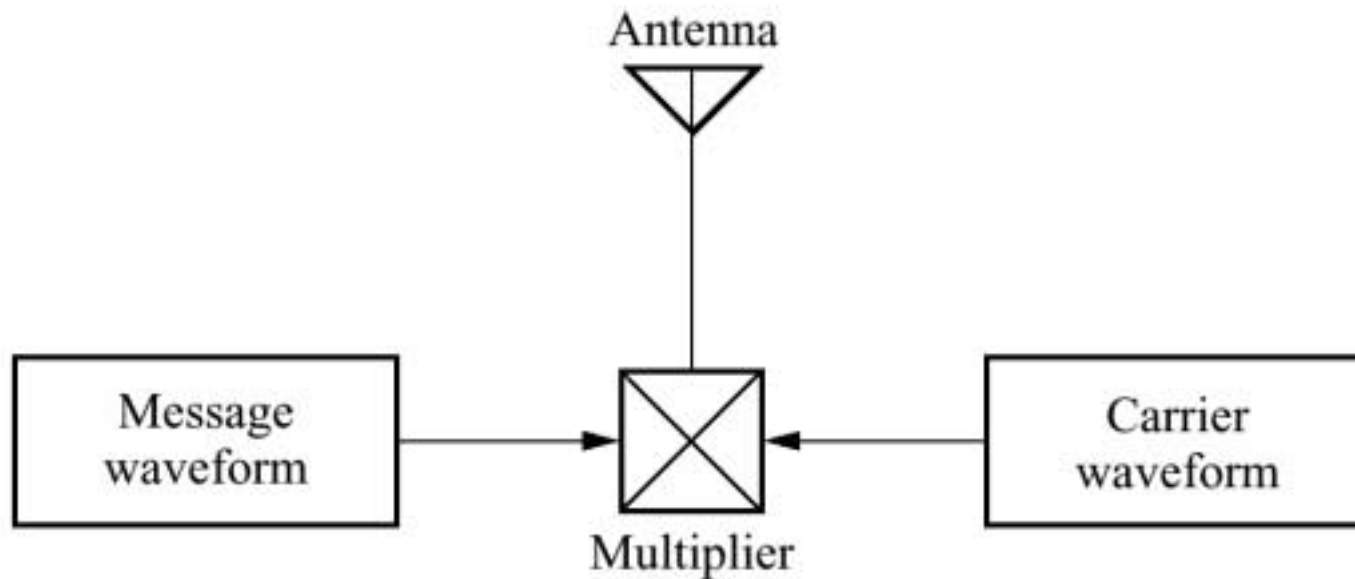


Figure P5.34
 Feedback control
 system representing
 human eye movement

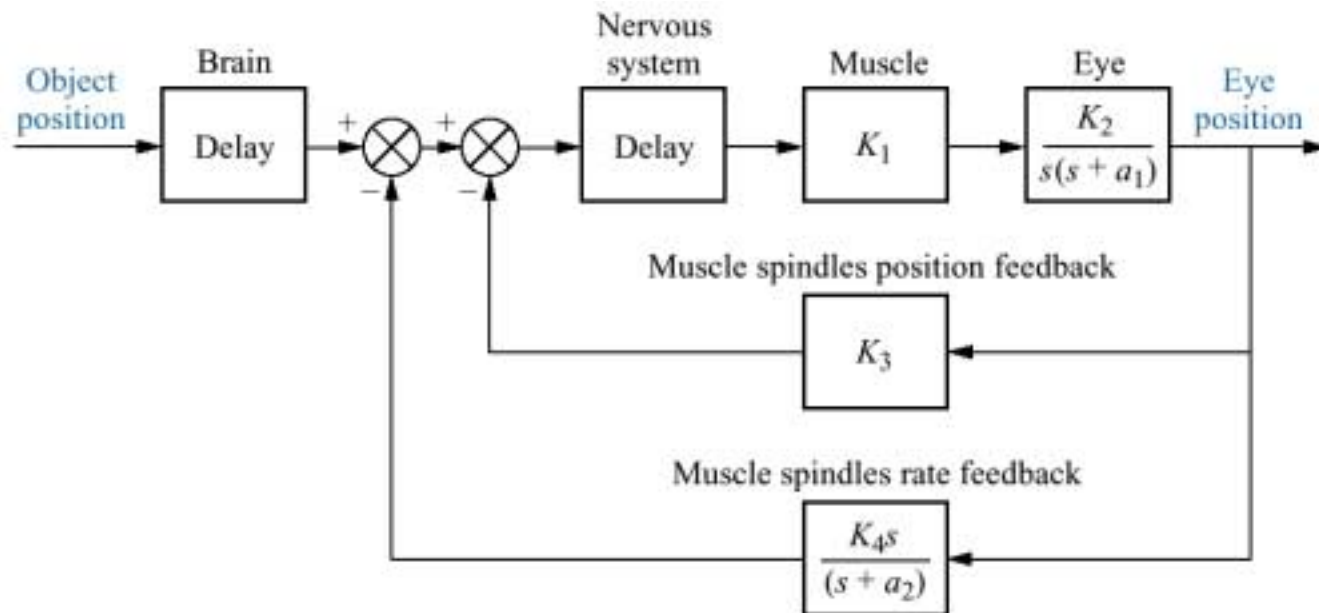


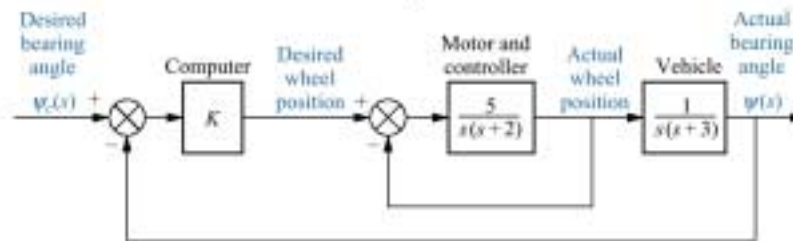
Figure P5.35

a. HelpMate robot used for in-hospital deliveries;

b. simplified block diagram for bearing angle control



(a)



(b)

Figure P5.36
a. Load tester
 (© 1992 IEEE)
b. approximate
 block diagram

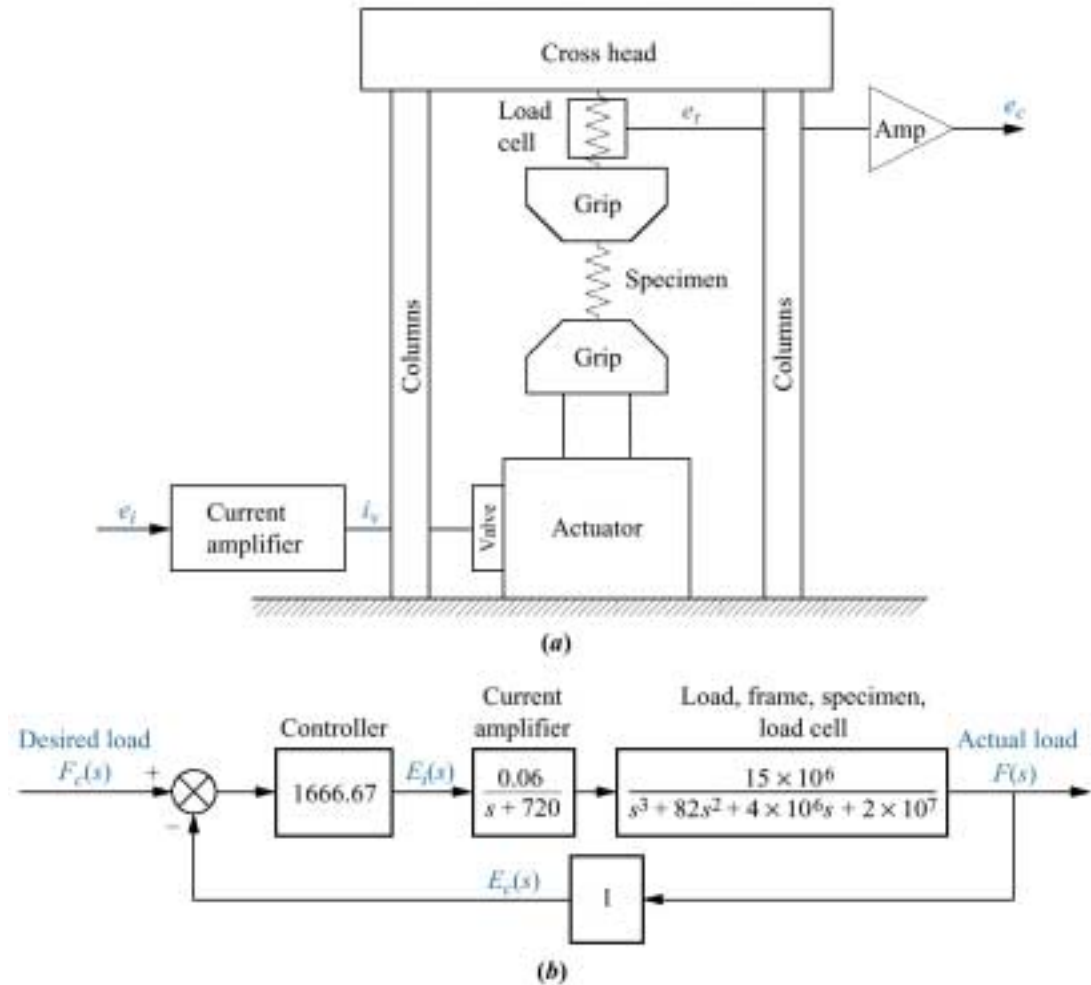


Figure P5.37
Solenoid coil circuit

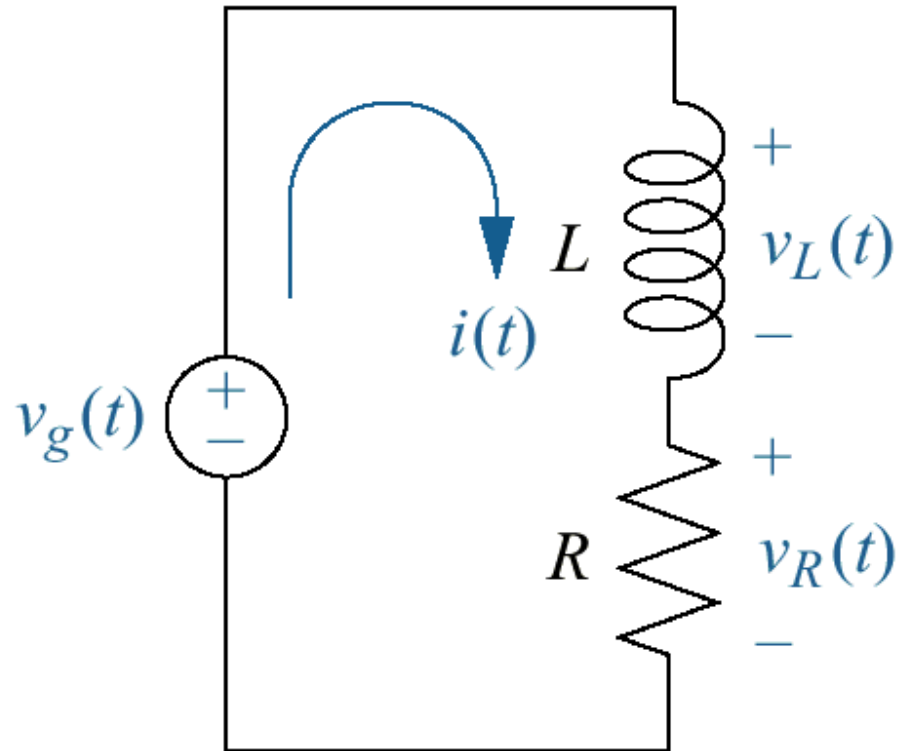


Figure P5.38

a. Position control:
motor and load;
b. block diagram

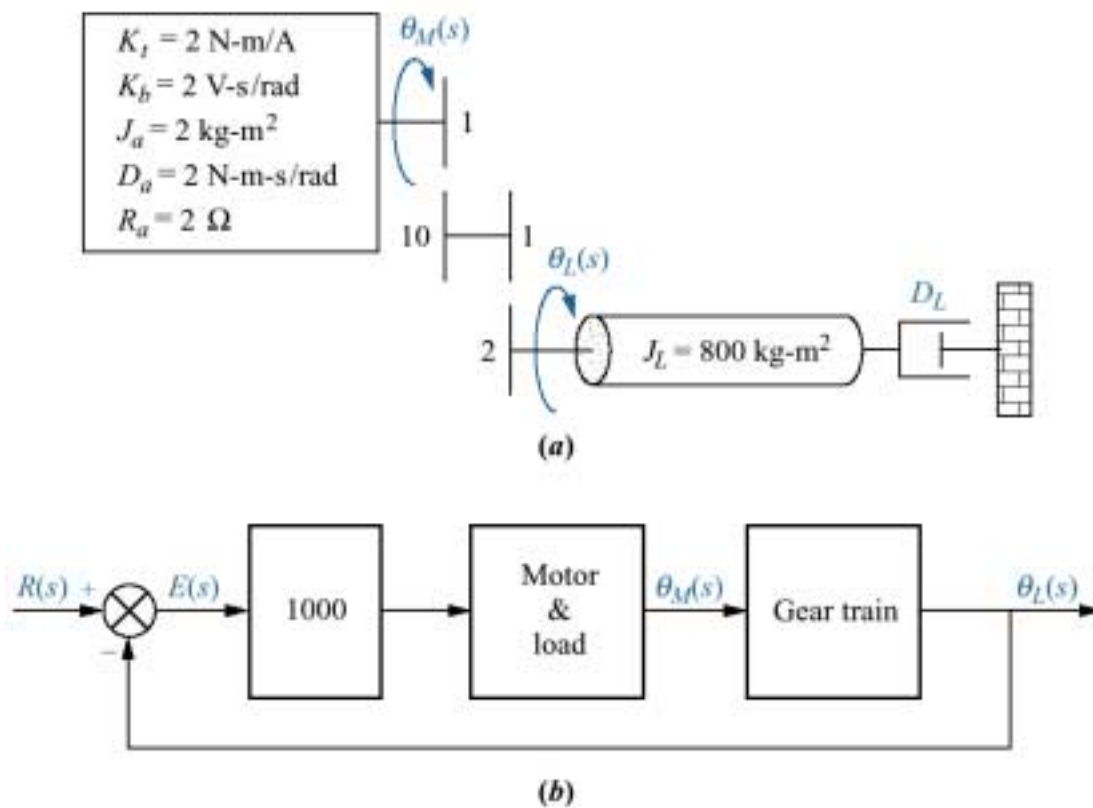


Figure P5.39

a. Position control;
b. position control
with tachometer

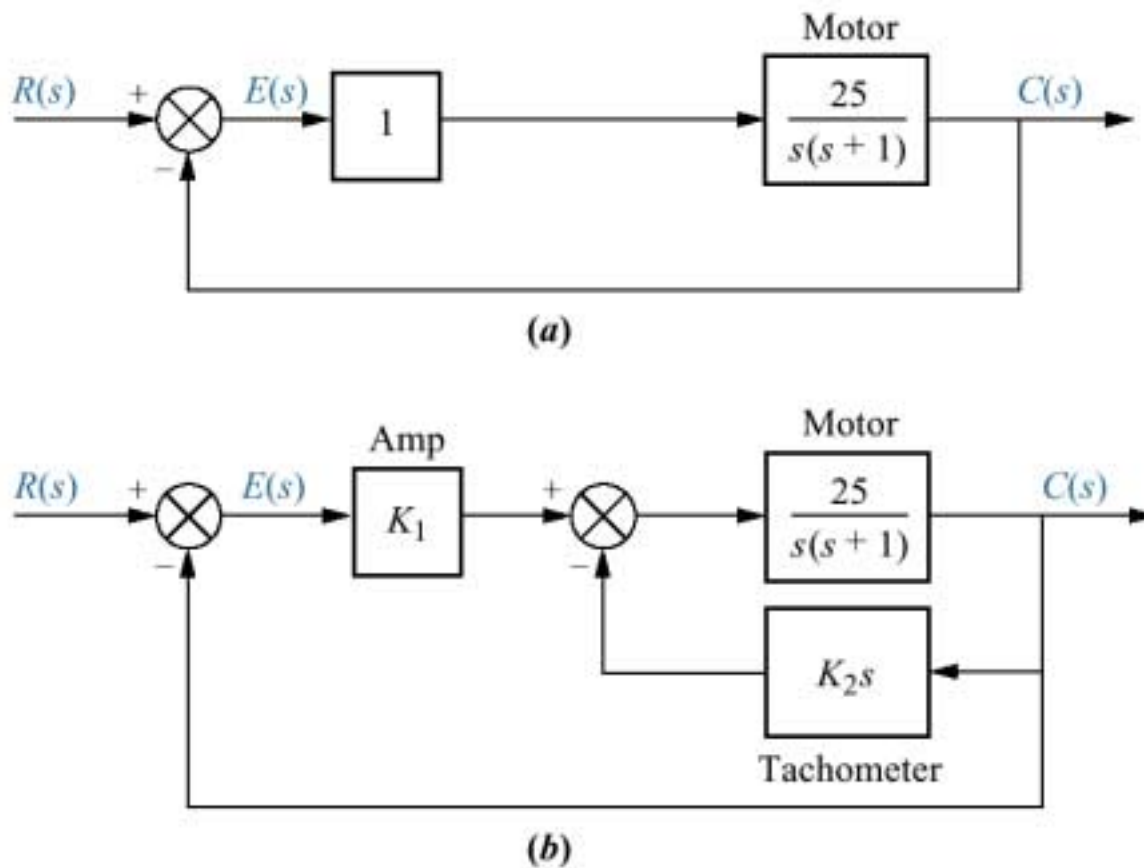


Figure P5.40
Position control

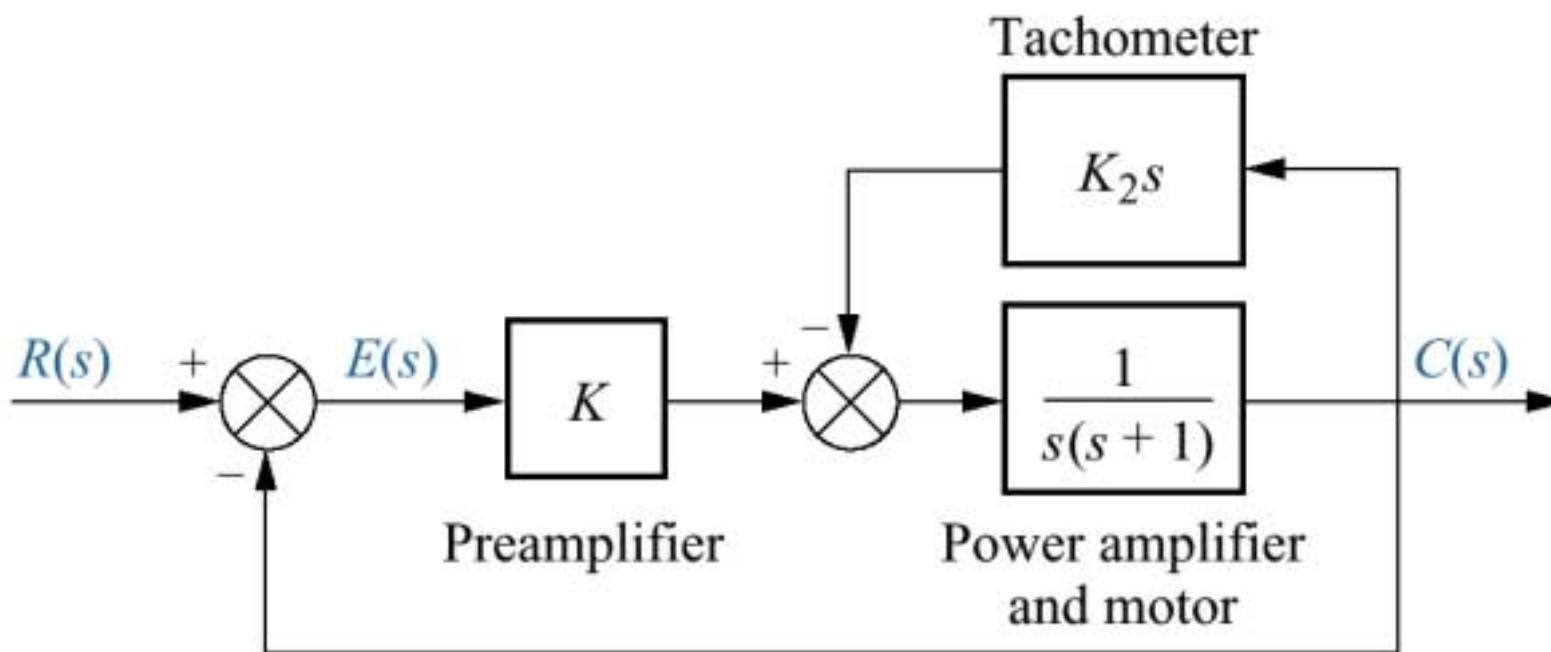


Figure P5.41

a. Motor and load;
b. Motor and load in feedback system

