



Karlsruhe Institute of Technology

KSETA/GK Workshop

INFORMAL INTRODUCTION TO TRACKING IN HEP

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Michael Eliachevitchg | ETP – KIT

WHAT IS TRACKING AND WHY DO WE NEED IT?

- HEP accelerator: produce particles in collisions
- goal: reconstruct physically meaningful particle properties and event topology
 - energy, momentum-vector, primary and secondary vertices, dE/dX_n (\rightarrow type:)
- tracking detectors: measure ionization from charged particles (stable: e , μ , K , π , p)
- track reconstruction (tracking):
 - find tracks (pattern recognition)
 - extract parameters (fitting)

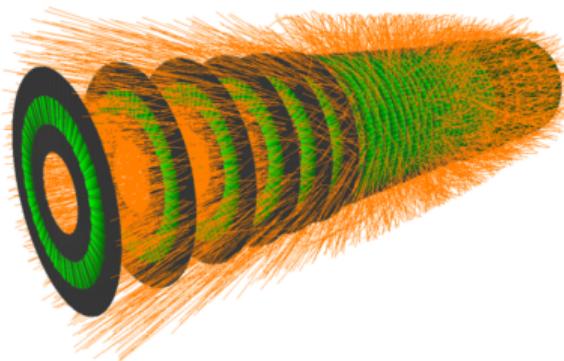
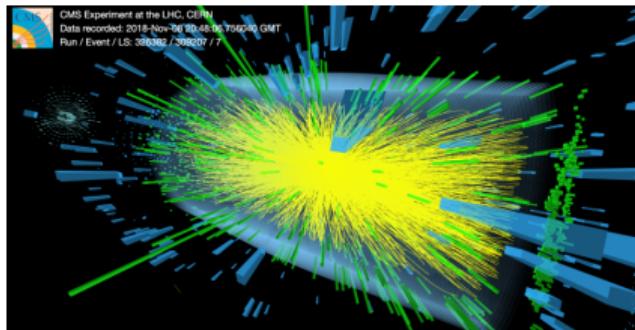


WHAT WE MEASURE

- energy depositions: "hits"
- 2D measurements: pixel detectors
- 1D measurements: strip detectors, wire chamber (measurements are times)
- binary or non-binary information (useful for dE/dX , weighting)

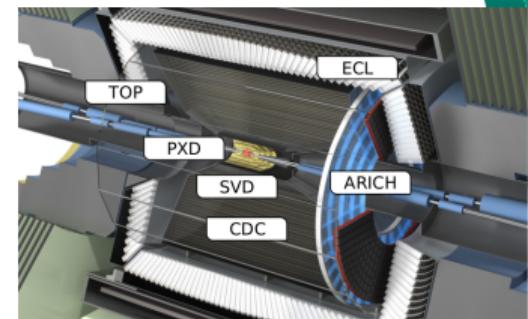
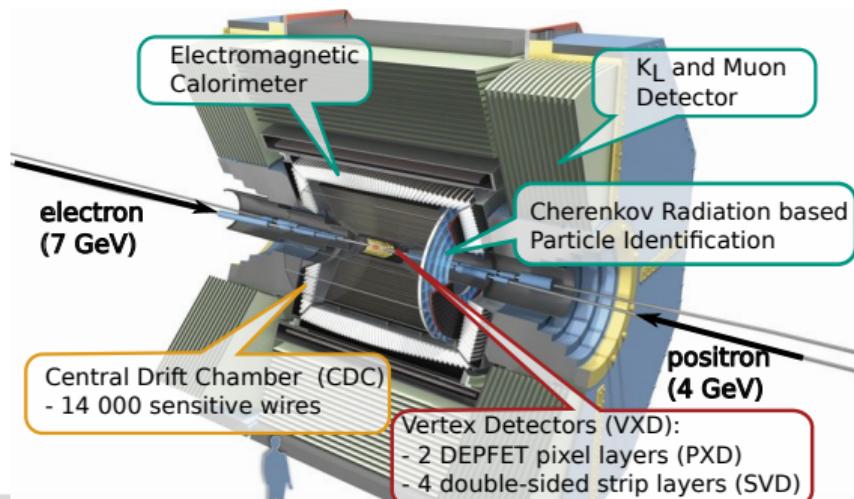
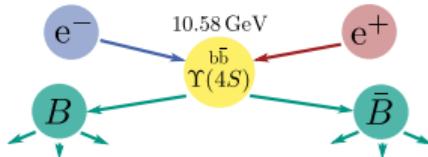
WHY IS DIFFICULT? EXAMPLE: (HL)-LHC

- pile-up and underlying event → large number of tracks from IP
 - combinatorics + ambiguities
- lumi + large cross section → high event rate → little time per event
- HLLHC: current CPU-time surpasses computing budget
 - faster algorithms required

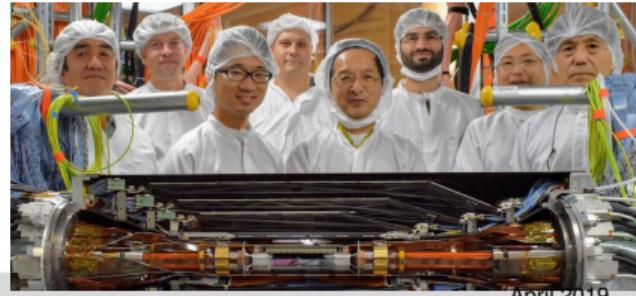
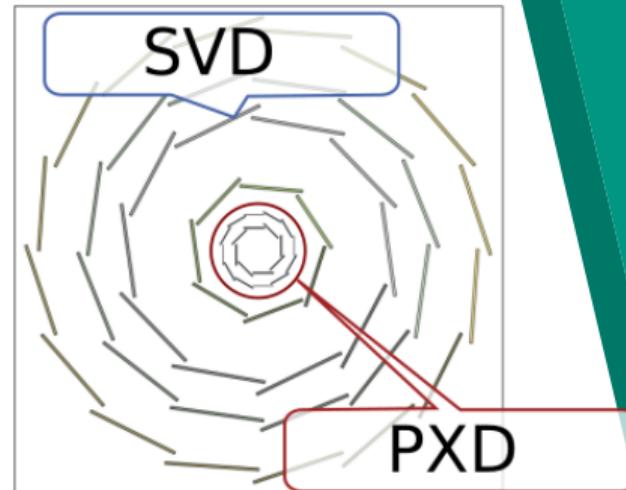
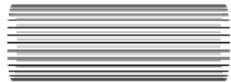
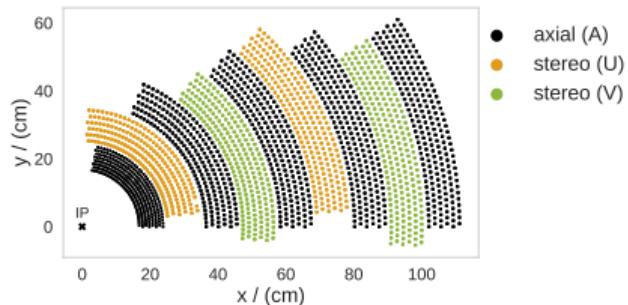


INTERLUDE: BELLE II

- e^+e^- B-factory operating on the $\Upsilon(4S)$ resonance at 10.58 GeV
- asymmetric beam energies to resolve B decay vertices



TRACKING SUBDETECTORS



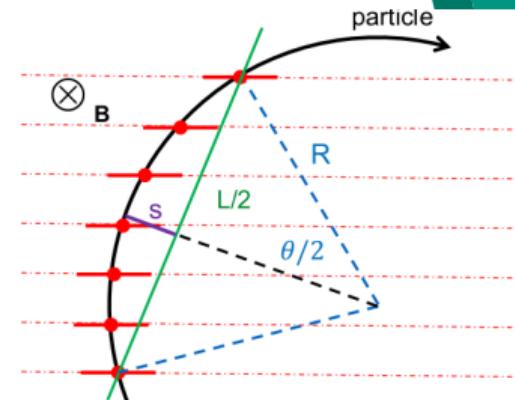
WHY IS DIFFICULT? EXAMPLE: BELLE II

- Y(4S) decays: only **11 tracks** per event
- high luminosity → large beam-induced background
 - PXD: **10^4 background hits** expected
- $\sqrt{s} = 10.58 \text{ GeV}$: **low-momentum** tracks
- curl in tracking system
- scattering significant
- physics analyzes: require reconstruction of whole event

HOW I LEARNED IT

- curvature in B-field allows momentum estimation
- $p_T = \frac{R}{qB}$, $p_T = p \cos \theta$
- estimate curvature from sagitta s

$$\frac{\sigma_{p_\perp}}{p_\perp} = \boxed{a' \frac{1}{BL^2} p_\perp} \oplus \boxed{b' \frac{1}{\sqrt{LX_0} B}}$$
$$= \mathbf{a} p_\perp \oplus \mathbf{b}$$



HOW IT'S DONE: LOCAL AND GLOBAL ALGORITHMS

- global
 - take all hits into account at the same time
 - assume helical tracks from IP
 - stable with backgrounds and gaps in hit pattern
- local
 - build track via local relations between hits
 - can handle large scattering and tracks not from IP

LEGENDRE ALGORITHM: HOUGH TRANSFORM

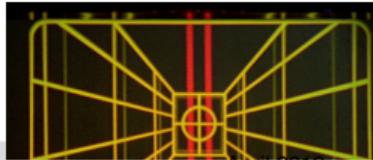
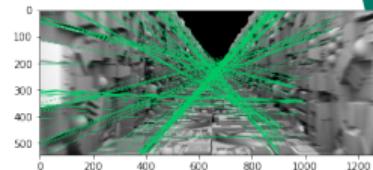
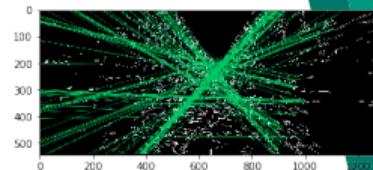
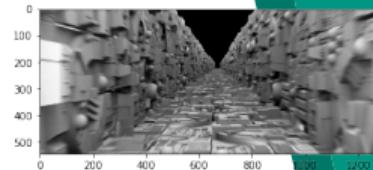
- Legendre algorithm is extension of **Hough Transform**

- transform xy-space into $\rho\theta$ -space, where each line is represented as a point
- $\rho = x \cos \theta + y \sin \theta$
- for each point in the original space, draw all points in the $\rho\theta$ -space consistent with a line through that point

;**** Algorithmus von Wikipedia :B_{ignoreheading}:

:BEAMER_{env}: ignoreheading

```
foreach pixel != 0:  
    for theta := 0 to pi:  
        rho := pixel_x * cos(theta)  
            + pixel_y * sin(theta)
```



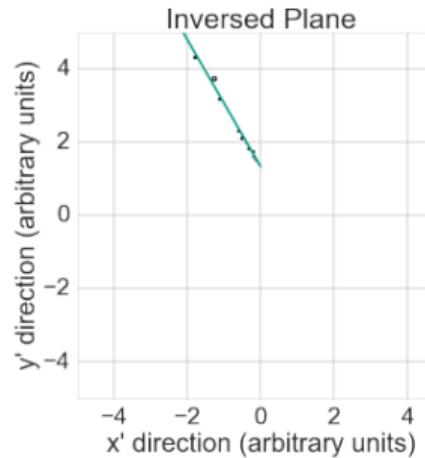
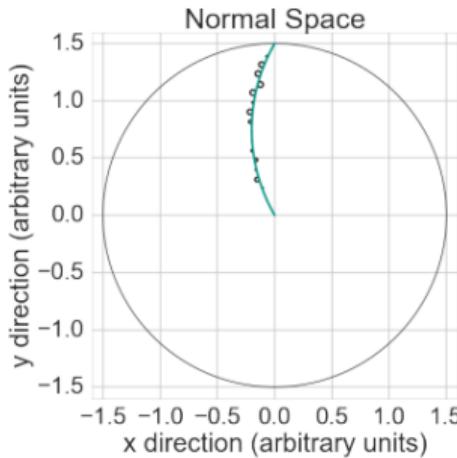
LEGENDRE: LINEARIZE CIRCULAR TRACKS

- circles through origin again described by only two parameters (in 2D)
- do the same thing again

$$x' = \frac{2x}{x^2 + y^2 - d^2}$$

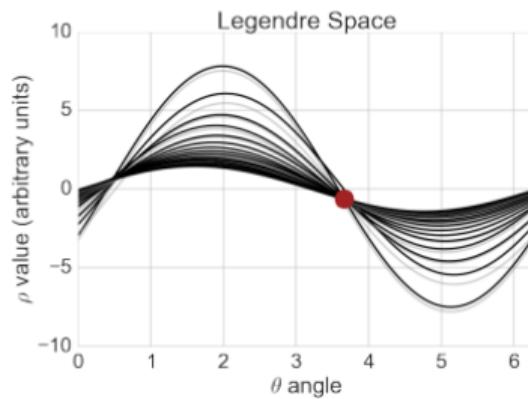
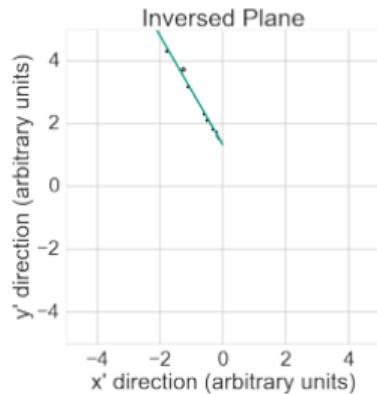
$$y' = \frac{2y}{x^2 + y^2 - d^2}$$

$$d' = \frac{2d}{x^2 + y^2 - d^2}$$



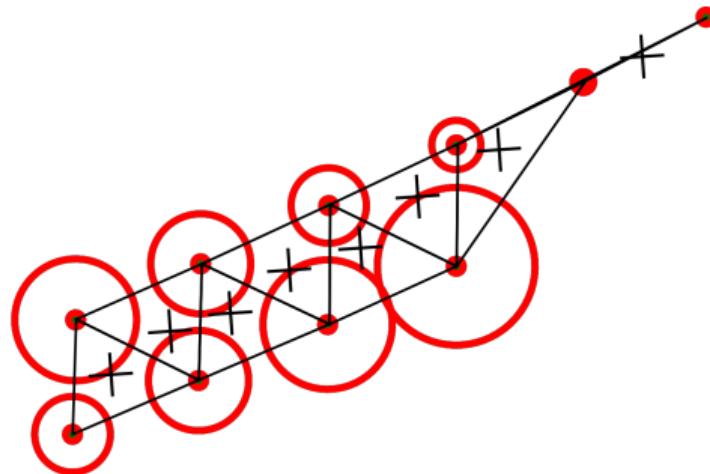
LEGENDRE

$$\rho(\theta) = x' \cos(\theta) + y' \sin(\theta) \pm d'$$



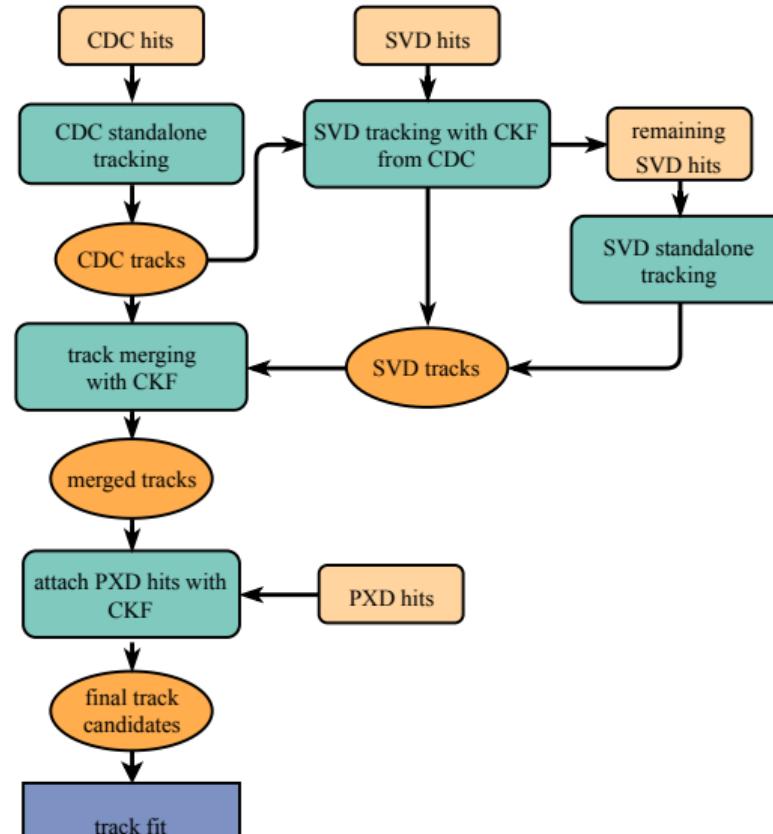
LOCAL: CELLULAR AUTOMATON

- search for longest path in graph (DAG) with nodes and edges
- length = sum of weightes edges and nodes
- e.g. CDC: nodes are hit triplets, edges from BDT

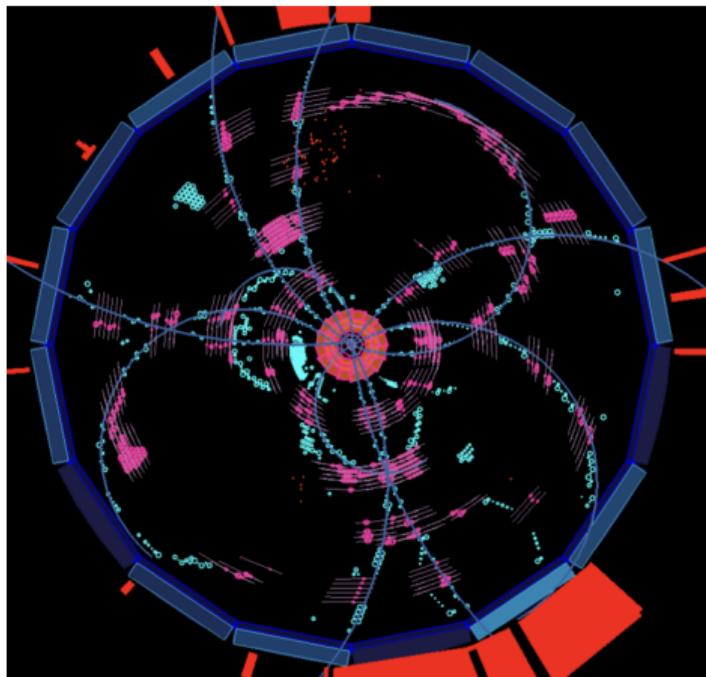


LOCAL: COMBINATORIAL KALMAN FILTER

HOW IT ALL COMES TOGETHER



WHEN IT WORKS



EXTRA: DEEP LEARNING APPROACHES TO TRACK FINDING