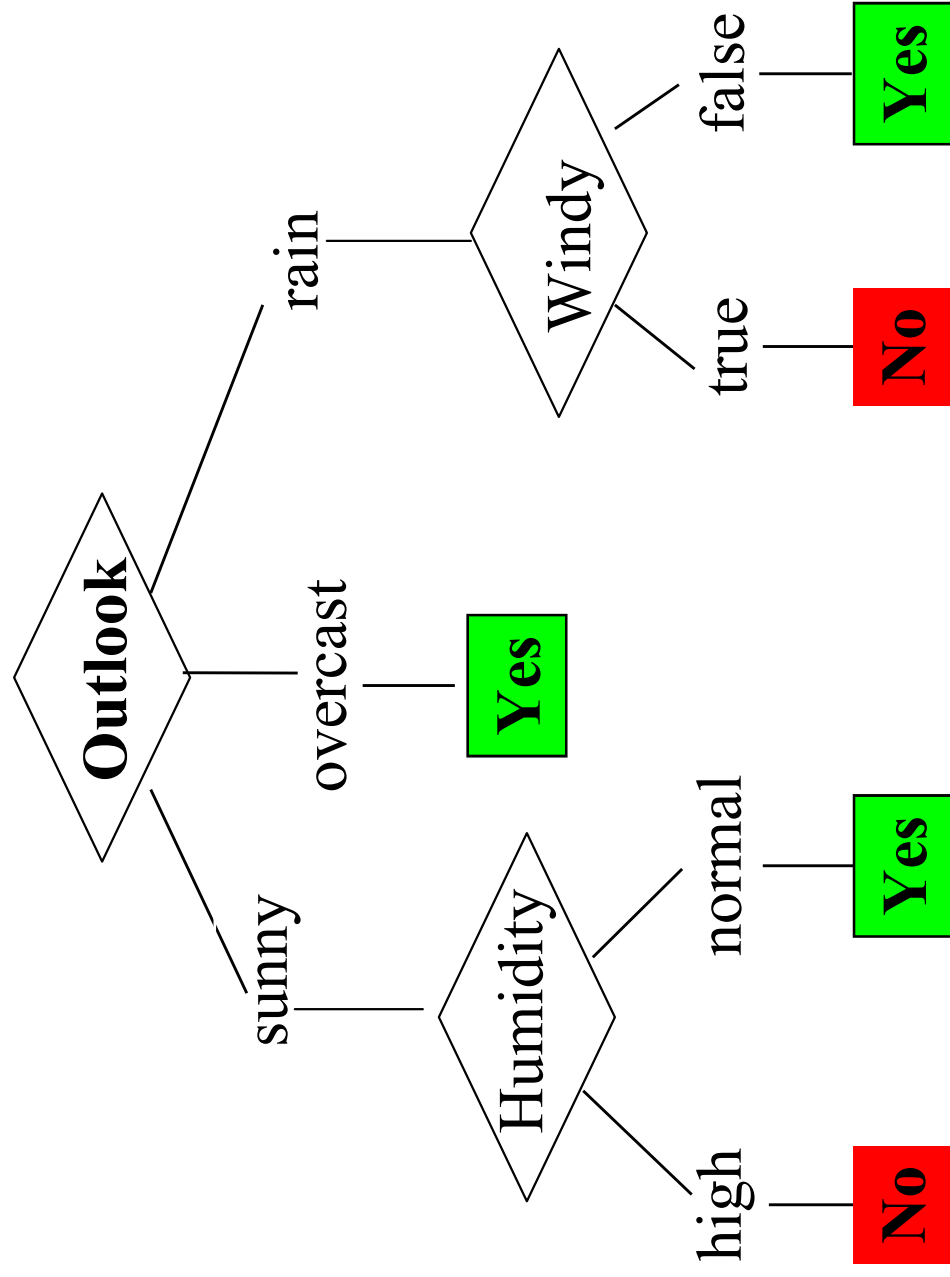


# Example Tree for "Play?"



# Building Decision Tree [Q93]

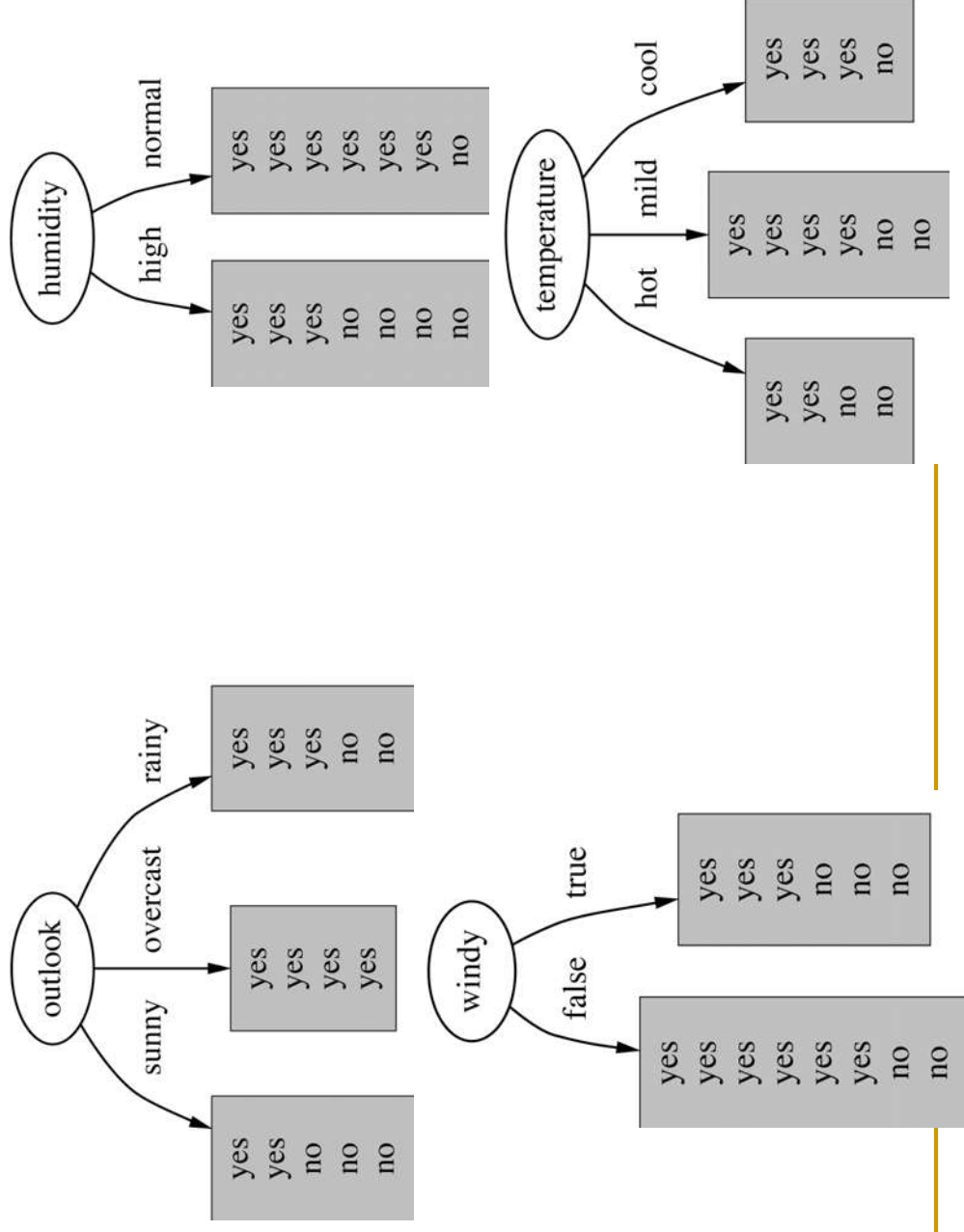
- Top-down tree construction
  - At start, all training examples are at the root.
  - Partition the examples recursively by choosing one attribute each time.
- Bottom-up tree pruning
  - Remove subtrees or branches, in a bottom-up manner, to improve the estimated accuracy on new cases.



# Choosing the Splitting Attribute

- At each node, available attributes are evaluated on the basis of separating the classes of the training examples. A Goodness function is used for this purpose.
- Typical goodness functions:
  - information gain (ID3/C4.5)
  - information gain ratio
  - gini index

# Which attribute to select?



# A criterion for attribute selection

- Which is the best attribute?
  - The one which will result in the smallest tree
  - Heuristic: choose the attribute that produces the "purest" nodes
- Popular *impurity criterion: information gain*
  - Information gain increases with the average purity of the subsets that an attribute produces
- Strategy: choose attribute that results in greatest information gain

# Computing information

- Information is measured in *bits*
  - Given a probability distribution, the info required to predict an event is the distribution's *entropy*
  - Entropy gives the information required in bits (this can involve fractions of bits!)
- Formula for computing the entropy:

$$\text{entropy}(p_1, p_2, \dots, p_n) = -p_1 \log p_1 - p_2 \log p_2 \dots - p_n \log p_n$$

# \*Claude Shannon

*Born: 30 April 1916*

*Died: 23 February 2001*

Claude Shannon, who has died aged 84, perhaps more than anyone laid the groundwork for today's digital revolution. His exposition of information theory, stating that all information could be represented mathematically as a succession of noughts and ones, facilitated the digital manipulation of data without which today's information society would be unthinkable.

Shannon's master's thesis, obtained in 1940 at MIT, demonstrated that problem solving could be achieved by manipulating the symbols 0 and 1 in a process that could be carried out automatically with electrical circuitry. That dissertation has been hailed as one of the most significant master's theses of the 20th century. Eight years later, Shannon published another landmark paper, *A Mathematical Theory of Communication*, generally taken as his most important scientific contribution.

Shannon applied the same radical approach to cryptography research, in which he later became a consultant to the US government.



Many of Shannon's pioneering insights were developed before they could be applied in practical form. He was truly a remarkable man, yet unknown to most of the world.

Education rules 12

*"Father of  
information theory"*



## Example: attribute "Outlook"

- "Outlook" = "Sunny":

$$\text{info}([2,3]) = \text{entropy}(2/5, 3/5) = -2/5 \log(2/5) - 3/5 \log(3/5) = 0.971 \text{ bits}$$

- "Outlook" = "Overcast":

$$\text{info}([4,0]) = \text{entropy}(1,0) = -1 \log(1) - 0 \log(0) = 0 \text{ bits}$$

*Note:  $\log(0)$  is not defined, but we evaluate  $0 * \log(0)$  as zero*

- "Outlook" = "Rainy":

$$\text{info}([3,2]) = \text{entropy}(3/5, 2/5) = -3/5 \log(3/5) - 2/5 \log(2/5) = 0.971 \text{ bits}$$

- Expected information for attribute:

$$\text{info}([3,2], [4,0], [3,2]) = (5/14) \times 0.971 + (4/14) \times 0 + (5/14) \times 0.971$$

$$= 0.693 \text{ bits}$$





# Computing the information gain

- Information gain:

(information before split) – (information after split)

$$\text{gain("Outlook")} = \text{info}([9,5]) - \text{info}([2,3],[4,0],[3,2]) = 0.940 - 0.693 \\ = 0.247 \text{ bits}$$

- Information gain for attributes from weather data:

$$\text{gain("Outlook")} = 0.247 \text{ bits}$$

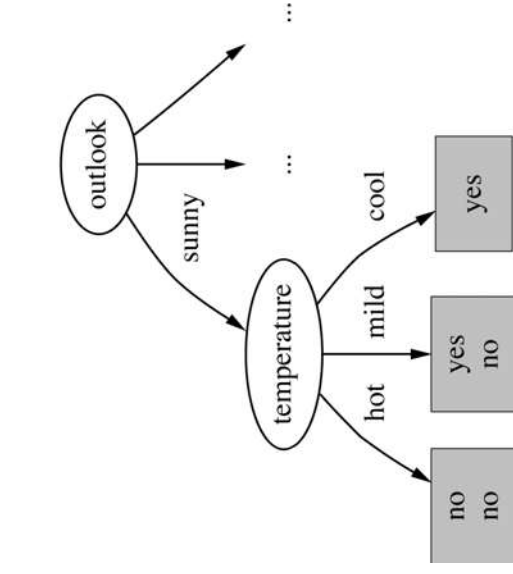
$$\text{gain("Temperature")} = 0.029 \text{ bits}$$

$$\text{gain("Humidity")} = 0.152 \text{ bits}$$

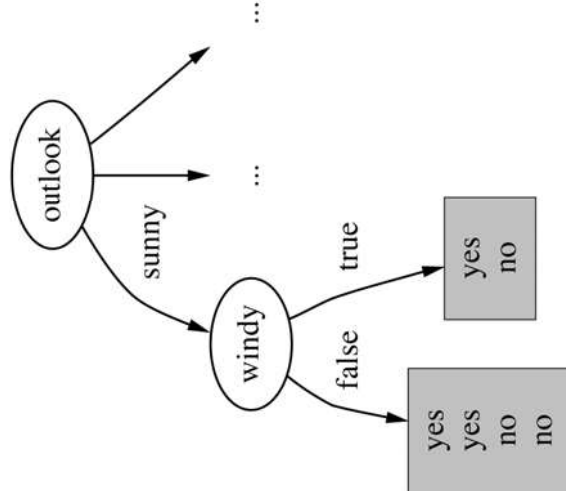
$$\text{gain("Windy")} = 0.048 \text{ bits}$$



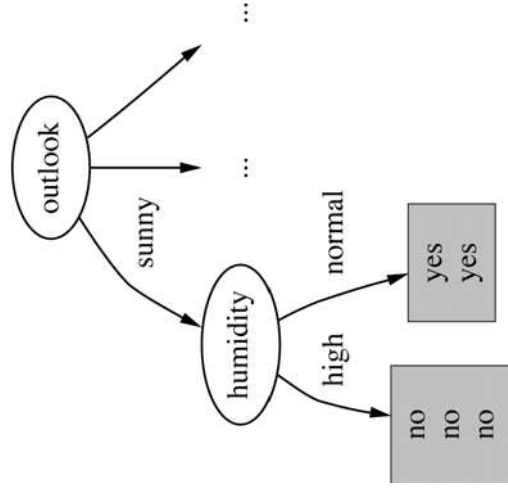
# Continuing to split



$\text{gain}(\text{"Temperature"}) = 0.571 \text{ bits}$

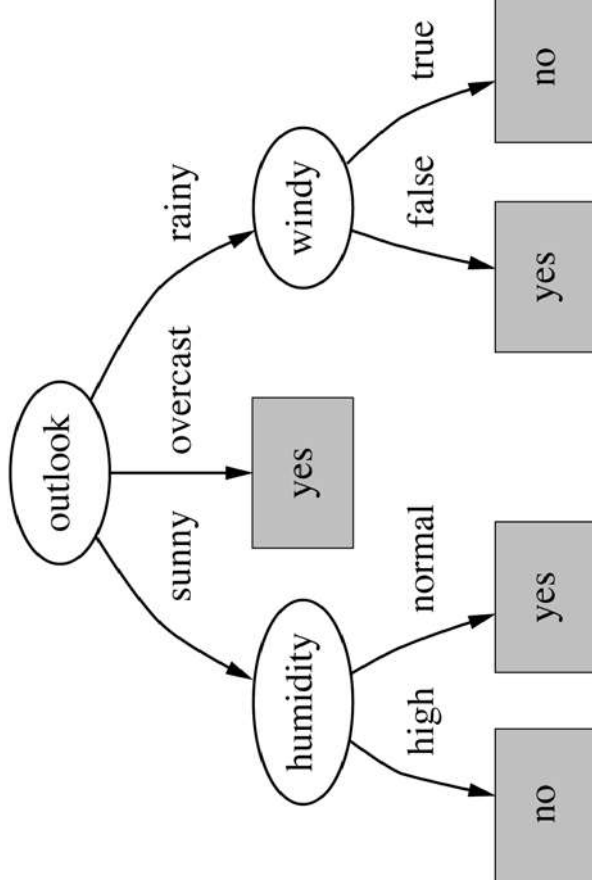


$\text{gain}(\text{"Windy"}) = 0.020 \text{ bits}$



$\text{gain}(\text{"Humidity"}) = 0.971 \text{ bits}$

# The final decision tree



- Note: not all leaves need to be pure; sometimes identical instances have different classes  
⇒ Splitting stops when data can't be split any further