

**CS 224****Section.: 2****Spring 2019****Lab No.: 6****Zeynep Cankara/ 21703381****Question 1:**

No.	Cache Size KB	N way Cache	Word Size (bits)	Block Size	No of Sets	Tag Size (bits)	Index Size (set no)	Word block offset	Byte offset size	Block replacement Needed?
1	32	1	32	4	$2^{11}$	17	11	2	2	No
2	32	2	32	4	$2^{10}$	18	10	2	2	Yes
3	32	4	32	8	$2^8$	19	8	3	2	Yes
4	32	Full	32	8	$2^0$	27	0	3	2	Yes
9	256	1	16	4	$2^{15}$	14	15	2	1	No
10	256	2	16	4	$2^{14}$	15	14	2	1	Yes
11	256	4	8	16	$2^{12}$	16	12	4	0	Yes
12	256	Full	8	16	$2^0$	28	0	4	0	Yes

**Question 2:****a.**

Instruction	Iteration No.				
	1	2	3	4	5
lw \$t1, 0x24(\$0)	Compulsory	Hit	Hit	Hit	Hit
lw \$t2, 0x2C(\$0)	Compulsory	Hit	Hit	Hit	Hit
lw \$t3, 0x28(\$0)	Hit	Hit	Hit	Hit	Hit

**b.**

Cache Representation				
V	Tag	Data		
1 (bit)	(27 bits)	(32 bits)	(32 bits)	set 3
1 (bit)	(27 bits)	(32 bits)	(32 bits)	set 2
1 (bit)	(27 bits)	(32 bits)	(32 bits)	set 1
1 (bit)	(27 bits)	(32 bits)	(32 bits)	set 0

Cache Capacity: 8 words

Block Size: 2 Words

$N = 1$  (direct associative cache)

Byte offset: 2 bit | Set: 2 bit | Block offset: 1 bit |  $\text{Tag} = 32 - (2+2+1) = 27$  bits

Total cache contains:  $(1 + 27 + 32 + 32) \times 4 = 368$  bits

**c.**

Hardware Required for the proposed cache design.

1 2:1 MULTIPLEXER for selecting the word within the block

1 EQUALITY COMPARATOR for checking tag matching

1 AND gate to determine the hit

**Question 3:****a.**

Note: Because capacity is full it in turn cause conflicts.

Instruction	Iteration No.				
	1	2	3	4	5
lw \$t1, 0x24(\$0)	Compulsory	Capacity	Capacity	Capacity	Capacity
lw \$t2, 0x2C(\$0)	Compulsory	Capacity	Capacity	Capacity	Capacity
lw \$t3, 0x28(\$0)	Capacity	Capacity	Capacity	Capacity	Capacity

**b.**

Cache Representation

V	Tag	Data	V	Tag	Data	
(1 bit)	(30 bits)	(32 bits)	(1 bit)	(30 bits)	(32 bits)	Set

Cache Capacity: 2 words

Block Size: 1 word

$N = 2$

Byte offset: 2 bit | Set: 0 bit | Block offset: 0 bit | Tag =  $32 - (2) = 30$  bits

Total cache contains:  $(1 + 30 + 32 + 1 + 30 + 32) \times 1 = 126$  bits

**c.**

Hardware Required for the proposed cache design.

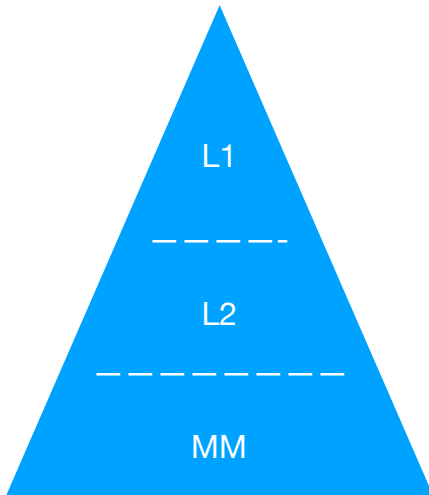
1 2:1 MULTIPLEXER for selecting the way within the block

2 EQUALITY COMPARATOR for checking tag matching

2 AND and 1 OR gates to determine the hit

**Question 4:**

Illustration of Memory Hierarchy :



Goal: Calculate AMAT in number of clock cycles

$$T_{L1} = 1 \text{ clock cycles}$$

$$T_{L2} = 4 \text{ clock cycles}$$

$$T_{MM} = 80 \text{ clock cycles}$$

$$\text{Miss}_{L1} = 5\% \text{ miss rate L1}$$

$$\text{Miss}_{L2} = 25\% \text{ miss rate L2}$$

$$\text{AMAT} = T_{L1} + \text{Miss}_{L1} \cdot (T_{L2} + \text{Miss}_{L2} \cdot T_{MM})$$

$$= 1 + 0.05 \times (4 + 80 \times 0.25)$$

$$= 2.2 \text{ clock cycles}$$

$$\text{Clock rate with } 2\text{GHz} = 0.5 \text{ ns}$$

$$10^{12} \text{ Instructions requires time} = 10^{12} \times 0.5 \times 2.2$$

$$= 1.1 \times 10^{12} \text{ ns}$$

$$= 1100 \text{ s}$$

**Question 5:**

```
# ===== TEXT SECTION ===== ###  
  
    .text  
  
    .globl    __start  
  
__start:  
    jal main # interactive menu  
    li $v0, 10 # exit the programme  
    syscall  
  
# interactive menu  
# WORKING [+]  
main:  
    # save return address to the stack  
    addi $sp, $sp, -4  
    sw $ra, 0($sp)  
    # Display intro message  
    li $v0, 4  
    la $a0, prompt # Prompt the assignment Task  
    syscall  
menu:  
    # Call display  
    jal display  
    # Ask user to enter option  
    li $v0, 4  
    la $a0, msgOption  
    syscall  
    #user option selection
```

```
li $v0, 5 # v0 read integer

syscall

# Call sub programs according to options

beq $v0, 1, opt1

beq $v0, 2, opt2

beq $v0, 3, opt3

beq $v0, 4, opt4

beq $v0, 5, opt5

beq $v0, 6, opt6

beq $v0, 7, opt7

beq $v0, 8, opt8

beq $v0, 9, optExit

opt1:

    li $v0, 4

        la $a0, msgN # Message to read N (NxN matrix)

        syscall

        li $v0, 5 # Read N

        syscall

        move $s0, $v0 # Store size in -> $s0

        mul $s2, $s0, $s0 # Elements in NxN array -> $s2

        # Now allocate the Matrix space in heap

        mul $a0, $s2, 4 # bytes to allocate

        li $v0, 9 # dynamic memory allocation

        syscall # base address -> $v0

        move $s1, $v0 # base address matrix -> $s1

        # call sub program read values from user

        jal fillCustomMatrix

        j loopBack

opt2:

    li $v0, 4
```

```
la $a0, msgN # Message to read N (NxN matrix)

syscall

li $v0, 5 # Read N

syscall

move $s0, $v0 # Store size in -> $s0

mul $s2, $s0, $s0 # Elements in NxN array -> $s2

# Now allocate the Matrix space in heap

mul $a0, $s2, 4 # bytes to allocate

li $v0, 9 # dynamic memory allocation

syscall # base address -> $v0

move $s1, $v0 # base address matrix -> $s1

# call sub program fill matrix with consecutive elements

jal fillConsecutiveMatrix

j loopBack

opt3:

# takes row and column and displays the element

li $v0, 4 # request to read row ([i], j)

la $a0, msgRow

syscall

li $v0, 5 # read row i

syscall

move $t0, $v0 # row -> $t0

li $v0, 4 # request to read col (i, [j])

la $a0, msgCol

syscall

li $v0, 5 # read col j

syscall

move $t1, $v0 # col -> $t1

# calculate the position

subi $t0, $t0, 1 # (i - 1) -> $t0
```

```
mul $t0, $t0, $s0 # (i - 1) * N -> $t0
mul $t0, $t0, 4 # (i - 1) * N * 4 -> $t0
subi $t1, $t1, 1 # (j - 1) -> $t1
mul $t1, $t1, 4 # (j - 1) * 4 -> $t1
add $t0, $t0, $t1 # (i - 1) * N * 4 + (j - 1) * 4 -> $t0
add $t2, $t0, $s1 # effective address of the position
# display result prompt
li $v0, 4
la $a0, msgOpt3Res # result
syscall
# display the item
lw $a0, 0($t2)
li $v0, 1
syscall
j loopBack
opt4:
# display the matrix row by row
jal displayMatrix
j loopBack
opt5:
# Find the trace of a matrix
jal findTrace
j loopBack
opt6:
# Find the trace like matrix
jal findTraceLike
j loopBack
opt7:
# obtain row by row summation
jal sumRowWise
```



```

        j loopBack

    opt8:
        # obtain col by col summation
        jal sumColWise
        j loopBack

    # execute main loop again
loopBack:
    j menu # go back to menu

    optExit: # exit the loop
# load back the return address
lw $ra, 0($sp)
addi $sp, $sp, 4
jr $ra # go to

# Finds the trace like summation of the matrix
findTraceLike:
    addi $sp, $sp, -16 # malloc
    sw $ra, 0($sp)
    sw $s1, 4($sp)
    sw $s2, 8($sp)
    sw $s0, 12($sp)
    # =====
    li $a0, 1
    addi $a1, $s0, 0
    li $t4, 0 # trace like summation -> $t4
traceLoop2:
    # call sub-routine to obtain trace like summation
    jal getItem
    add $t4, $t4, $v0
    addi $a0, $a0, 1

```

```
        subi $a1, $a1, 1

        ble $a0, $s0, traceLoop2

# display the result prompt
li $v0, 4

la $a0, msgOpt6Res # result

syscall

# display the trace like summation
move $a0, $t4

li $v0, 1

syscall

# =====

# calloc

lw $s0, 12($sp)

lw $s2, 8($sp)

lw $s1, 4($sp)

lw $ra, 0($sp)

addi $sp, $sp, 16

jr $ra # goto


# Get Item

# Returns item at the position

# row -> $a0

# col -> $a0

# item -> $v0

# WORKING [+]

getItem:

    addi $sp, $sp, -16 # malloc

    sw $ra, 0($sp)

    sw $s1, 4($sp)
```

```

sw $s2, 8($sp)

sw $s0, 12($sp)

# =====

move $t0, $a0 # row -> $t0
move $t1, $a1 # col -> $t1

# calculate the position
subi $t0, $t0, 1 # (i - 1) -> $t0
mul $t0, $t0, $s0 # (i - 1) * N -> $t0
mul $t0, $t0, 4 # (i - 1) * N * 4 -> $t0
subi $t1, $t1, 1 # (j - 1) -> $t1
mul $t1, $t1, 4 # (j - 1) * 4 -> $t1
add $t0, $t0, $t1 # (i - 1) * N * 4 + (j - 1) * 4 -> $t0
add $t2, $t0, $s1 # effective address of the position

# fetch the item
lw $v0, 0($t2)

# =====

# calloc
lw $s0, 12($sp)
lw $s2, 8($sp)
lw $s1, 4($sp)
lw $ra, 0($sp)
addi $sp, $sp, 16
jr $ra # goto

# Find trace of the matrix display
# WORKING [+]
findTrace:
    addi $sp, $sp, -16 # malloc
    sw $ra, 0($sp)
    sw $s1, 4($sp)

```

```
sw $s2, 8($sp)

sw $s0, 12($sp)

# =====

li $a0, 1

li $a1, 1

li $t4, 0 # trace -> $t4

traceLoop:

    jal getItem

    add $t4, $t4, $v0

    addi $a0, $a0, 1

    addi $a1, $a1, 1

    ble $a0, $s0, traceLoop

# display the result prompt

li $v0, 4

la $a0, msgOpt5Res # result

syscall

# display the trace

move $a0, $t4

li $v0, 1

syscall

# =====

# calloc

lw $s0, 12($sp)

lw $s2, 8($sp)

lw $s1, 4($sp)

lw $ra, 0($sp)

addi $sp, $sp, 16

jr $ra # goto
```

```
# Displays matrix row by row
```

```

# WORKING [+]

displayMatrix:
    addi $sp, $sp, -12 # malloc

    sw $ra, 0($sp)

    sw $s1, 4($sp)

    sw $s2, 8($sp)

    # =====

    li $v0, 4 # matrix construction

    la $a0, endl

syscall

li $t0, 2 # use to control end of line (endl)

sumRowLoop2:
    lw $a0, 0($s1) # current item -> $a0

    li $v0, 1

    syscall # print current element

    li $v0, 4 # matrix construction

    la $a0, wSpace

    syscall

    addi $s1, $s1, 4 # iterate matrix

    subi $s2, $s2, 1

    ble $t0, $s0, jEnter

    li $t0, 1 # use to control end of line (endl)

    li $v0, 4 # matrix construction

    la $a0, endl

    syscall

    jEnter:

    addi $t0, $t0, 1

    bgt $s2, $0, sumRowLoop2

# calloc

lw $s2, 8($sp)

```

```
lw $s1, 4($sp)
lw $ra, 0($sp)
addi $sp, $sp, 12
jr $ra # goto
```

```
# Obtains col by col summations of elements within the matrix
```

```
# Column-major representation
```

```
# WORKING [+]
```

```
sumColWise:
```

```
    addi $sp, $sp, -12 # malloc
```

```
    sw $ra, 0($sp)
```

```
    sw $s1, 4($sp)
```

```
    sw $s2, 8($sp)
```

```
    # =====
```

```
    mul $t3, $s0, 4 # row offset -> $t3
```

```
    li $t0, 0 # sum -> $t0
```

```
    li $t1, 0 # (col - 1) -> $t1
```

```
coLoopNextRow:
```

```
    mul $t4, $t1, 4 # col offset -> $t4
```

```
    move $t2, $0 # row - 1 -> $t2
```

```
    add $t5, $s1, $t4 # effective memory address -> $t5
```

```
    lw $t7, 0($t5) # current item -> $t7
```

```
    add $t0, $t7, $t0 # recalculate sum
```

```
cLoopNextCol:
```

```
    add $t5, $t3, $t5 # effective memory address -> $t5
```

```
    lw $t7, 0($t5) # current item -> $t7
```

```
    add $t0, $t7, $t0 # recalculate sum
```

```
    addi $t2, $t2, 1 # row++
```

```
    blt $t2, $s0, cLoopNextCol # row < N keep continue
```

```
    addi $t1, $t1, 1 # col++
```

```
        blt $t1, $s0, coLoopNextRow

# display result
li $v0, 4 # result message
la $a0, msgOpt8Res
syscall

# print the result
addi $a0, $t0, 0
li $v0, 1
syscall

# =====
# calloc
lw $s2, 8($sp)
lw $s1, 4($sp)
lw $ra, 0($sp)
addi $sp, $sp, 12
jr $ra # goto

# Obtains row by row summations of elements within the matrix
# Row-major representation
# WORKING [+]
sumRowWise:
    addi $sp, $sp, -12 # malloc
    sw $ra, 0($sp)
    sw $s1, 4($sp)
    sw $s2, 8($sp)
    li $t0, 0 # sum -> $t0
    move $t2, $s2 # Counter for items
    sumRowLoop:
        lw $t1, 0($s1) # current item -> $t1
        addi $s1, $s1, 4 #iterate over the matrix
```

```
    add $t0, $t0, $t1 # sum -> $t0

    subi $t2, $t2, 1

    bgt $t2, $0, sumRowLoop

li $v0, 4 # result message

la $a0, msgOpt7Res

syscall

# print the result

addi $a0, $t0, 0

li $v0, 1

syscall

# calloc

lw $s2, 8($sp)

lw $s1, 4($sp)

lw $ra, 0($sp)

addi $sp, $sp, 12

jr $ra # goto

# Fills the matrix with consecutive integers

# WORKING [+]

fillConsecutiveMatrix:

    addi $sp, $sp, -12 # matrix base and return address saved

    sw $ra, 0($sp)

    sw $s1, 4($sp)

    sw $s2, 8($sp)

    # start filling from 1

    li $t1, 1 # item value -> $t1

writeItems:

    sw $t1, 0($s1) # write to the array

    addi $s1, $s1, 4 # next item of the matrix

    addi $t1, $t1, 1 # increment element
```



```
sle $t3, $t1, $s2

beq $t3, 1, writeItems

lw $s2, 8($sp)
lw $s1, 4($sp)
lw $ra, 0($sp)
addi $sp, $sp, 12
jr $ra # goto

# Fills the matrix with user defined values
# WORKING [+]

fillCustomMatrix:
    addi $sp, $sp, -12 # matrix base and return address saved
    sw $ra, 0($sp)
    sw $s1, 4($sp)
    sw $s2, 8($sp)
    # start filling from 1
    li $t1, 1 # iterator -> $t1
writeItems2:
    # read items from the user
    li $v0, 5
    syscall
    move $t0, $v0 # user input -> $t0
    sw $t0, 0($s1) # write to the array
    addi $s1, $s1, 4 # next item of the matrix
    addi $t1, $t1, 1 # increment element
    ble $t1, $s2, writeItems2

lw $s2, 8($sp)
lw $s1, 4($sp)
lw $ra, 0($sp)
addi $sp, $sp, 12
```

```
jr $ra # goto

# Menu display interface
# WORKING [+]

display:
    addi $sp, $sp, -4 # allocate stack space
    sw $ra, 0($sp)
    li $v0, 4
    # print the options
    la $a0, msgMenu
    syscall
    la $a0, msgOpt1
    syscall
    la $a0, msgOpt2
    syscall
    la $a0, msgOpt3
    syscall
    la $a0, msgOpt4
    syscall
    la $a0, msgOpt5
    syscall
    la $a0, msgOpt6
    syscall
    la $a0, msgOpt7
    syscall
    la $a0, msgOpt8
    syscall
    la $a0, msgExitOpt
    syscall
    lw $ra, 0($sp) # goto return address
```

```
addi $sp, $sp, 4
```

```
jr $ra # goto
```

```
# ===== DATA SECTION ===== ###
```

```
.data
```

```
prompt: .asciiz "Interactive menu to perform operations on  
an user defined matrix \n"
```

```
msgOption: .asciiz "\n Please choose an option: "
```

```
msgMenu: .asciiz "\n ===== MENU ====="
```

```
msgOpt1: .asciiz "\n 1. Create matrix (NxN) with user values"
```

```
msgOpt2: .asciiz "\n 2. Create matrix (NxN) with consecutive values"
```

```
msgOpt3: .asciiz "\n 3. Display the target item (row, col)"
```

```
msgOpt4: .asciiz "\n 4. Display matrix (Row by row)"
```

```
msgOpt5: .asciiz "\n 5. Obtain trace of the matrix -> display"
```

```
msgOpt6: .asciiz "\n 6. Obtain trace like summation (other diagonal)  
-> display"
```

```
msgOpt7: .asciiz "\n 7. Obtain sum of matrix elements (Row by row)"
```

```
msgOpt8: .asciiz "\n 8. Obtain sum of matrix element (Column by  
column) "
```

```
msgExitOpt: .asciiz "\n 9. Exit"
```

```
msgN: .asciiz "\n Please enter N of (NxN) matrix: "
```

```
msgRow: .asciiz "\n Please enter Row number i [1:N]: "
```

```
msgCol: .asciiz "\n Please enter Column number j [1:N]: "
```

```
msgOpt3Res: .asciiz "\n Item in the given row & col: "
```

```
msgOpt7Res: .asciiz "\n Sum of elements obtained in terms of Row-Major  
iteration (row by row): "
```

```
msgOpt8Res: .asciiz "\n Sum of elements obtained in terms of Column-Major  
iteration (col by col): "
```

```
msgOpt5Res: .asciiz "\n Trace of the NxN matrix: "
```

```
msgOpt6Res: .asciiz "\n Trace like summation of the NxN matrix: "
```

```
endl: .asciiz "\n"
```

```
wSpace: .asciiz " "
```