Exploração dos dados da tese de doutorado da Vivian

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Tabela de dados

```
27 obs. of 18 variables:
'data.frame':
              7.58 7.97 8.23 7.91 7.95 7.95 8.28 8.11 8.04 8.5 ...
       : num
$ EC
              15.4 17.4 25 30 19.4 29 28.8 23.6 35.8 64.4 ...
       : num
              6.67 6.65 7.05 5.58 7.01 ...
       : num
$ TDS : num
              7.6 8.6 12.8 15 9.8 14.6 14.4 12 18 32.2 ...
              0.16 0.43 1.76 3.67 0.25 ...
$ Sol : num
$ Turb : num
              0.984 0.779 2.269 6.707 1.341 ...
              19.8 18.9 19.6 19.7 18.6 ...
$ Temp : num
$ ColF : num
              32 64 240 496 32 ...
              512 1072 3328 2368 720 ...
$ ColT : num
$ PT
              0 0 0 0.003 0 0 0.028 0.004 0.026 0.003 ...
       : num
$ Nitri: num
              0 0 0.001 0.003 0.001 0.003 0.004 0.001 0.012 0.004 ...
              0.079 0.099 0.084 0.065 0.06 0.034 0.083 0.083 0.121 0.05 ...
$ Nitra: num
$ NumP : int
              11 10 10 32 28 9 29 18 25 16 ...
              34.8 31.48 45.65 7.37 22.71 ...
$ MPS
       : num
$ ED
              1.66 1.36 1.85 3.5 3.71 ...
       : num
$ TE
              24706 20262 27498 52096 55280 ...
       : num
              2246 2026 2750 1628 1974 ...
$ MPE : num
$ MSI
       : num
              3.48 2.81 1.62 1.85 1.97 ...
                       EC
                                        OD
                                                       TDS
      Нq
                        :15.40
                                         :2.096
Min.
       :7.580
                 Min.
                                 Min.
                                                  Min.
                                                          : 7.60
                 1st Qu.:27.10
1st Qu.:7.860
                                  1st Qu.:4.929
                                                  1st Qu.:13.60
Median :8.040
                 Median :36.00
                                 Median :5.624
                                                  Median :18.00
Mean
      :8.070
                 Mean
                        :41.26
                                 Mean
                                         :5.633
                                                  Mean
                                                         :20.62
3rd Qu.:8.265
                 3rd Qu.:52.20
                                  3rd Qu.:6.648
                                                  3rd Qu.:26.00
                        :97.20
                                         :9.066
Max.
        :8.620
                 Max.
                                 Max.
                                                  Max.
                                                          :48.80
     Sol
                       Turb
                                           Temp
                                                           ColF
Min.
       : 0.160
                  Min.
                         : 0.7794
                                     Min.
                                             :17.54
                                                      Min.
                                                                  32
1st Qu.: 1.602
                  1st Qu.: 4.4532
                                     1st Qu.:18.93
                                                      1st Qu.:
Median: 3.934
                  Median: 10.1361
                                      Median :19.80
                                                      Median :
                                                                 176
      : 7.105
                         : 15.5832
                                                              : 1646
Mean
                  Mean
                                     Mean
                                             :19.91
                                                      Mean
3rd Qu.: 6.270
                  3rd Qu.: 13.9608
                                      3rd Qu.:20.87
                                                      3rd Qu.:
                                                                 344
Max.
       :78.511
                  Max.
                         :160.0335
                                      Max.
                                             :22.10
                                                      Max.
                                                              :19408
     ColT
                       PT
                                                           Nitra
                                        Nitri
       : 288
                        :0.00000
                                           :0.000000
                                                       Min.
                                                               :0.01500
Min.
                 Min.
                                   Min.
1st Qu.: 1080
                 1st Qu.:0.00000
                                   1st Qu.:0.001000
                                                       1st Qu.:0.05600
Median: 1664
                 Median :0.00600
                                   Median :0.004000
                                                       Median :0.07900
      : 5441
                        :0.01315
Mean
                 Mean
                                   Mean
                                           :0.005963
                                                       Mean
                                                               :0.08785
3rd Qu.: 3056
                 3rd Qu.:0.01700
                                   3rd Qu.:0.006000
                                                       3rd Qu.:0.09400
Max.
       :60000
                 Max.
                        :0.07800
                                   Max.
                                           :0.067000
                                                       Max.
                                                               :0.35800
     NıımP
                      MPS
                                         ED
                                                          TE
Min. : 6.00
                        : 7.014
                                         : 0.784
                                                           : 11684
                 Min.
                                  Min.
                                                    Min.
1st Qu.:12.00
                 1st Qu.:15.400
                                  1st Qu.: 1.831
                                                    1st Qu.: 27245
```

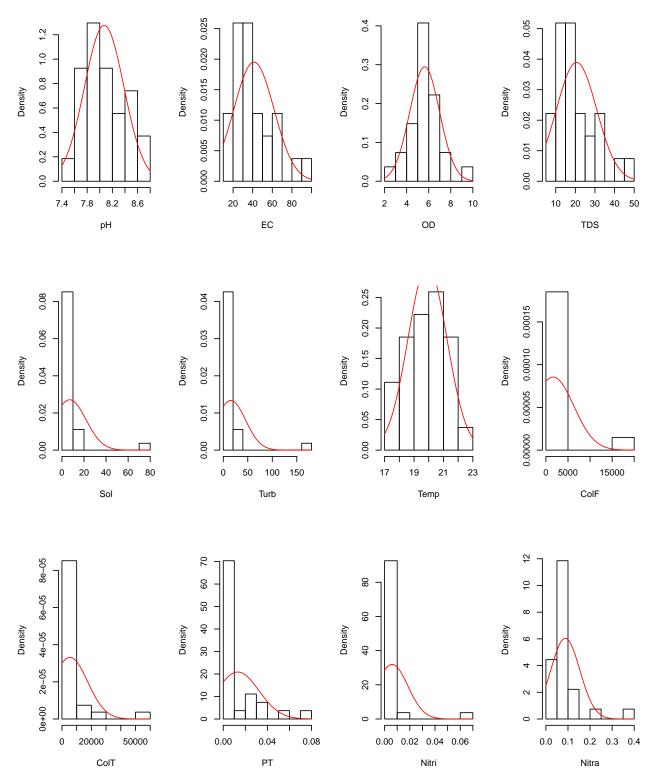
```
Median :22.00
               Median :22.237
                                Median : 2.995
                                                 Median : 44640
Mean :24.48
               Mean :23.088
                                Mean : 3.767
                                                       : 56138
                                                 Mean
3rd Qu.:29.50
                3rd Qu.:29.258
                                3rd Qu.: 3.769
                                                 3rd Qu.: 56180
Max.
      :92.00
               Max.
                      :45.650
                                Max.
                                       :15.889
                                                 Max.
                                                        :236808
    MPE
                   MSI
Min.
      :1488
                     :1.595
               Min.
1st Qu.:1881
               1st Qu.:1.734
Median:2294
              Median :1.937
Mean
       :2254
              Mean
                     :2.436
3rd Qu.:2593
               3rd Qu.:2.667
Max.
       :3026
               Max.
                     :5.598
```

Separando as variáveis de água e de paisagem para facilitar análises.

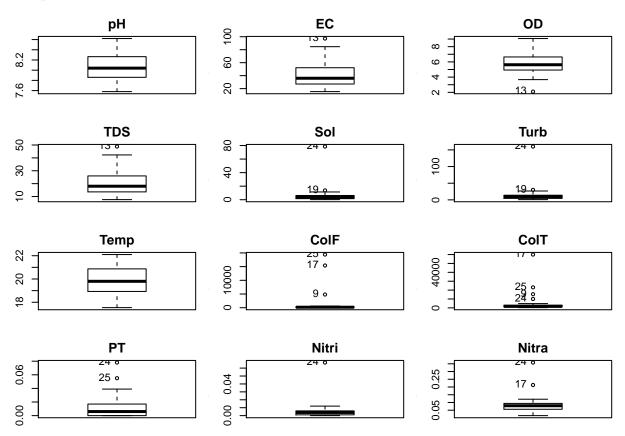
Gráficos exploratórios das variáveis brutas

variáveis da água

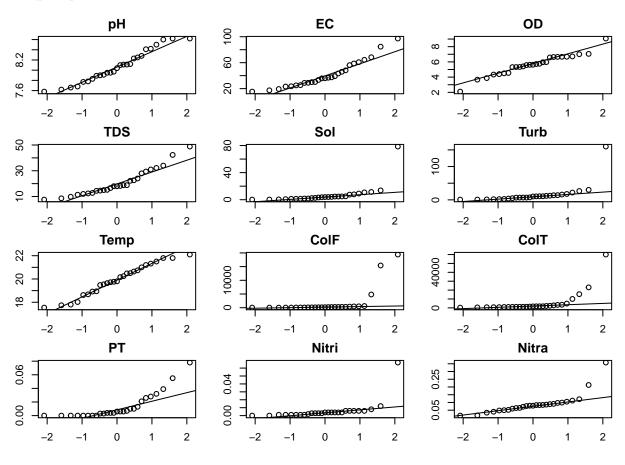
Histograma + density (como se fosse normal)



Boxplot identificando os outliers



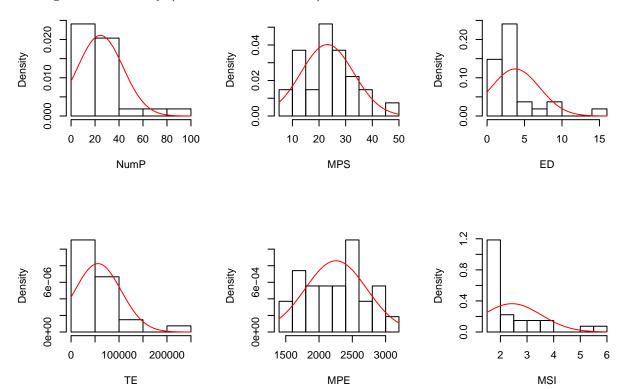
QQplot para ver normalidade



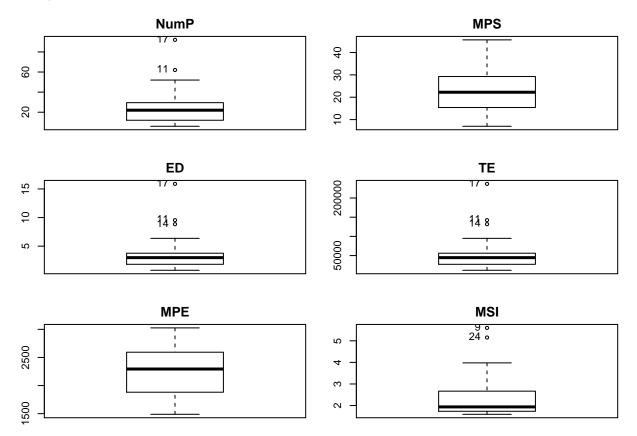
null device

variáveis da paisagem

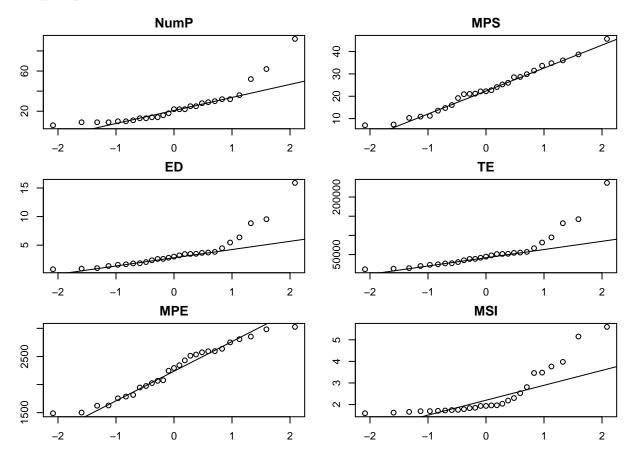
Histograma + density (como se fosse normal)



Boxplot identificando os outliers



QQplot para ver normalidade



Testes de premissas SEM

Valores de skewness e kurtosis

	skew	Pskew	kurt	Pkurt
pН	0.306	0.447	2.092	0.241
EC	1.090	0.015	3.639	0.215
OD	-0.185	0.644	4.062	0.110
TDS	1.099	0.014	3.661	0.208
Sol	4.449	0.000	22.133	0.000
Turb	4.419	0.000	21.950	0.000
Temp	-0.181	0.651	2.073	0.220
ColF	3.154	0.000	11.441	0.000
ColT	3.773	0.000	17.130	0.000
PT	1.982	0.000	6.520	0.004
Nitri	4.546	0.000	22.759	0.000
Nitra	2.793	0.000	11.890	0.000
NumP	2.035	0.000	7.425	0.002
MPS	0.243	0.545	2.473	0.764
ED	2.292	0.000	8.577	0.001
TE	2.292	0.000	8.576	0.001
MPE	-0.076	0.848	1.839	0.047
MSI	1.641	0.001	4.703	0.042

Dados com muitas variáveis com skewness e kurtosis significativos. Isso deve estar ocorrendo principalmente devido aos outliers.

Normalidade de cada variável separadamente

\$`	Shap	iro-	Wilk'	s	Normality	Test`
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Variable	Statistic	p-value	Normality
pН	0.9528	0.2508	YES
EC	0.9036	0.0162	NO
OD	0.9562	0.3021	YES
TDS	0.9018	0.0147	NO
Sol	0.3948	0.0000	NO
Turb	0.4057	0.0000	NO
Temp	0.9652	0.4816	YES
ColF	0.3795	0.0000	NO
ColT	0.4308	0.0000	NO
PT	0.7154	0.0000	NO
Nitri	0.3699	0.0000	NO
Nitra	0.6853	0.0000	NO
NumP	0.7776	0.0001	NO
MPS	0.9776	0.8053	YES
ED	0.7379	0.0000	NO
TE	0.7379	0.0000	NO
MPE	0.9559	0.2966	YES
MSI	0.7335	0.0000	NO
	pH EC OD TDS Sol Turb Temp ColF ColT PT Nitri Nitra NumP MPS ED TE MPE	EC 0.9036 OD 0.9562 TDS 0.9018 Sol 0.3948 Turb 0.4057 Temp 0.9652 ColF 0.3795 ColT 0.4308 PT 0.7154 Nitri 0.3699 Nitra 0.6853 NumP 0.7776 MPS 0.9776 ED 0.7379 TE 0.7379 MPE 0.9559	pH 0.9528 0.2508 EC 0.9036 0.0162 OD 0.9562 0.3021 TDS 0.9018 0.0147 Sol 0.3948 0.0000 Turb 0.4057 0.0000 Temp 0.9652 0.4816 ColF 0.3795 0.0000 ColT 0.4308 0.0000 PT 0.7154 0.0000 Nitri 0.3699 0.0000 Nitra 0.6853 0.0000 NumP 0.7776 0.0001 MPS 0.9776 0.8053 ED 0.7379 0.0000 TE 0.7379 0.0000 MPE 0.9559 0.2966

null device

1

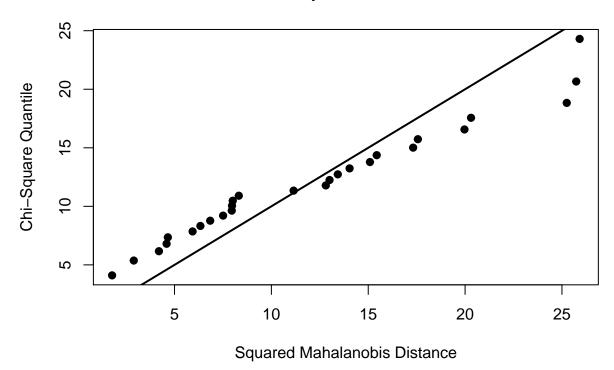
Como era de se esperar pela visualização dos gráficos.

Teste de distribuição normal multivariada

Teste de Mardia recomendado no Shipley (2004) usando pacote MVN. Como o teste só roda com até 15 variáveis, separei as de água e de paisagem:

água

Chi-Square Q-Q Plot



Mardia's Multivariate Normality Test

data : da[1:12]

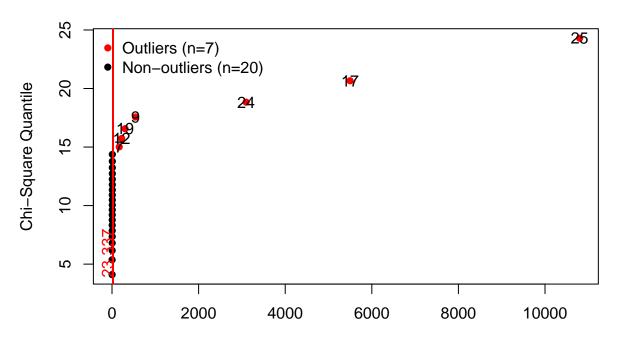
g1p : 132.1651 chi.skew : 594.7431 p.value.skew : 2.299536e-13

g2p : 192.6751
z.kurtosis : 3.497368
p.value.kurt : 0.000469873

chi.small.skew : 671.9009 p.value.small : 1.338575e-20

Result : Data are not multivariate normal.

Chi-Square Q-Q Plot



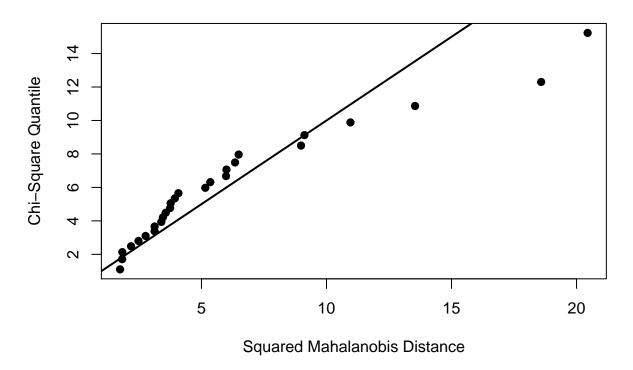
Robust Squared Mahalanobis Distance

<pre>\$outlier</pre>	
Observation	Mal

ΨΟι	101101		
	Observation	Mahalanobis Distance	Outlier
25	25	10799.844	TRUE
17	17	5498.571	TRUE
24	24	3097.240	TRUE
9	9	542.016	TRUE
19	19	302.117	TRUE
12	12	222.875	TRUE
7	7	166.787	TRUE
21	21	7.596	FALSE
11	11	7.371	FALSE
13	13	7.096	FALSE
15	15	6.994	FALSE
27	27	6.686	FALSE
20	20	6.636	FALSE
22	22	6.464	FALSE
26	26	6.432	FALSE
3	3	6.428	FALSE
14	14	6.281	FALSE
18	18	5.638	FALSE
6	6	5.273	FALSE
8	8	4.792	FALSE
16	16	4.375	FALSE
4	4	4.311	FALSE
10	10	4.296	FALSE
2	2	4.125	FALSE
1	1	3.529	FALSE
23	23	2.196	FALSE
5	5	1.882	FALSE

paisagem

Chi-Square Q-Q Plot



Mardia's Multivariate Normality Test

data : da[13:18]

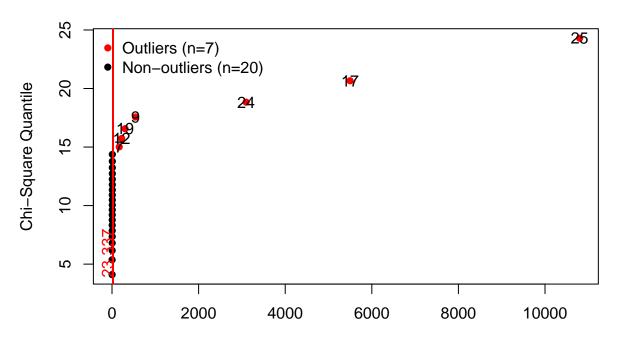
g1p : 33.31189 chi.skew : 149.9035 p.value.skew : 1.660335e-10

g2p : 58.68711 z.kurtosis : 2.833847 p.value.kurt : 0.004599136

chi.small.skew : 171.8192 p.value.small : 1.078246e-13

Result : Data are not multivariate normal.

Chi-Square Q-Q Plot



Robust Squared Mahalanobis Distance

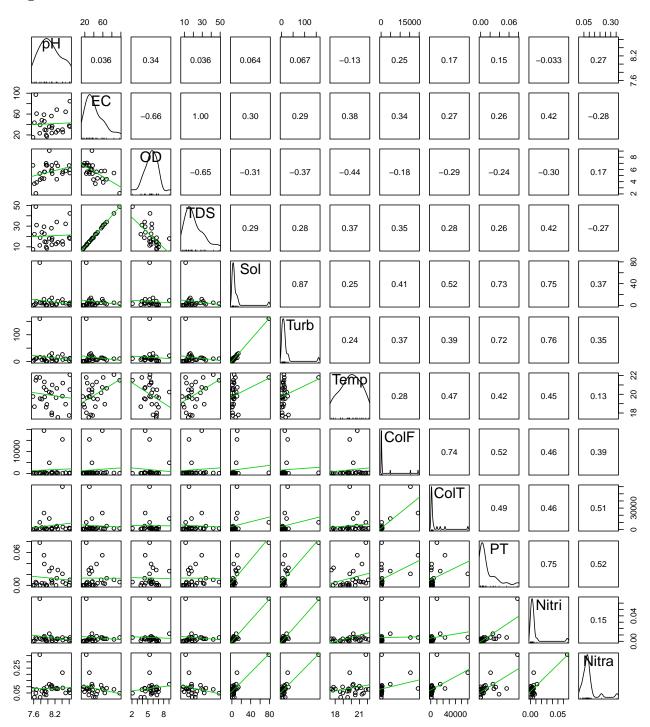
-

	Observation	Mahalanobis Distance	Outlier
25	25	10799.844	TRUE
17	17	5498.571	TRUE
24	24	3097.240	TRUE
9	9	542.016	TRUE
19	19	302.117	TRUE
12	12	222.875	TRUE
7	7	166.787	TRUE
21	21	7.596	FALSE
11	11	7.371	FALSE
13	13	7.096	FALSE
15	15	6.994	FALSE
27	27	6.686	FALSE
20	20	6.636	FALSE
22	22	6.464	FALSE
26	26	6.432	FALSE
3	3	6.428	FALSE
14	14	6.281	FALSE
18	18	5.638	FALSE
6	6	5.273	FALSE
8	8	4.792	FALSE
16	16	4.375	FALSE
4	4	4.311	FALSE
10	10	4.296	FALSE
2	2	4.125	FALSE
1	1	3.529	FALSE
23	23	2.196	FALSE
5	5	1.882	FALSE

Correlação entre as variáveis

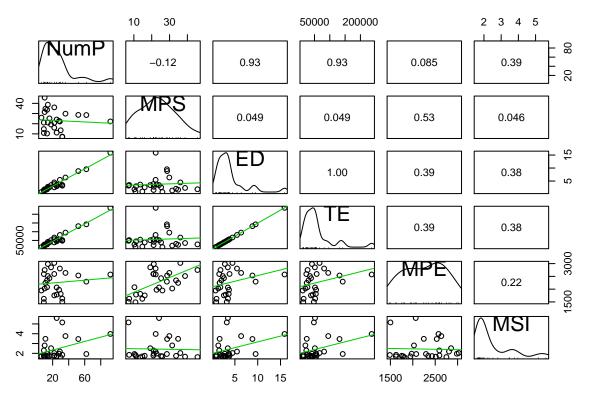
Lembrando que os valores destas correlações levam em consideração os outliers. e vendo as linhas verdes, eles estão puxando muito os valores das correlações.

Água



Comentários: correlação igual a 1 entre EC e TDS.

Paisagem



Comentários: correlação igual a 1 entre ED e TE.