

In a third stage of our work we have been interested in theoretical models for mathematical instruction (Godino, Contreras and Font, 2006). We defined six dimensions in a mathematical instruction process, each of them modelled as a stochastic process with its respective state space and trajectory: epistemic (relating to institutional knowledge), educational (teachers' roles), student (students' roles), mediational (use of technological resources and time), cognitive (genesis of personal meanings) and emotional (students' attitudes, emotions, etc. when studying mathematics) trajectories.

The theoretical constructs elaborated during these three periods constitute the *onto-semiotic approach* that we synthesize in the next section.

3. Basic theoretical tools

The starting point for the *onto-semiotic approach* was an ontology of mathematical objects that takes into account the triple aspect of mathematics as a socially shared problem solving activity, a symbolic language and a logically organized conceptual system. Taking the problem-situation as the primitive notion, we defined the theoretical concepts of practice, (personal and institutional) object and meaning, with the purpose of making visible and operative, both the mentioned triple character of mathematics and the personal and institutional genesis of mathematical knowledge, as well as their mutual interdependence.

3.1. Systems of operative and discursive practices linked to types of problems

We consider *mathematical practice* any action or manifestation (linguistic or otherwise) carried out by somebody to solve mathematical problems, to communicate the solution to other people, so as to validate and generalize that solution to other contexts and problems (Godino and Batanero, 1998, p. 182). The practices can be idiosyncratic of a person or shared within an institution. An institution is constituted by the people involved in the same class of problem-situations, whose solution implies the carrying out of certain shared social practices and the common use of particular instruments and tools.

In the study of mathematics, more than a

specific practice to solve a particular problem, we are interested in the systems of (operative and discursive) practices carried out by the people involved in certain types of problem-situations. For example, regarding the questions, What is the mathematical object⁴ "arithmetic mean"?, What does it mean or does it represent the expression "arithmetic mean"?, we propose the following pragmatist answer: "The system of practices that a person carries out (personal meaning), or are shared within an institution (institutional meaning), to solve a type of problem-situations in which finding a representative of a set of data is required."

The socio-epistemic and cognitive relativity of meanings, when they are understood as systems of practices, and their use in the didactical analysis lead to introducing a basic typology of meanings. Regarding institutional meanings we distinguish the following types:

- *Implemented*: the system of practices that a teacher effectively implements in a specific teaching experience.
- *Assessed*: the system of practices that a teacher uses to assess his/her students' learning.
- *Intended*: the system of practices included in the planning of the study process.
- *Referential*: the system of practices used as reference to elaborate the intended meaning; for example that included in curricular documents. In a particular teaching experience the reference meaning will be part of a more global or *holistic meaning*, whose determination requires carrying out a historical and epistemological study to find the origin and evolution of the object

Regarding the personal meaning we introduce the following types:

- *Global*: set of personal practices that the subject is potentially able to carry out related to a specific mathematical object.
- *Declared*: the personal practices effectively shown in solving assessment tasks and questionnaires, independently if they are

⁴ Initially we use the expression "mathematical object" as synonymous of "mathematical concept". Later we extend the use indicating any entity or thing to which we refer, or talk about it, be it real or imaginary and that intervenes in some way in mathematical activity.

correct or incorrect from the institutional point of view.

- *Achieved*: personal practices that fit the institutional meaning fixed by the teacher. The analysis of changes and evolution of personal meanings, as a result of the study process, will also serve to distinguish between *initial* and *final* personal achieved meanings.

In the *onto-semiotic* framework, teaching involves the participation of students in the community of practices sharing the institutional meaning, and learning is conceived as the students' appropriation of these meanings.

3.2. Objects involved and emerging from systems of practices

In mathematical practices ostensive (symbols, graphs etc.) and non-ostensive objects (brought to mind when doing mathematics), which are textually, orally, graphically or even gesturally represented intervene. New objects that come from the system of practices and explain their organization and structure (types of problems, procedures, definitions, properties, arguments), emerge⁵. If the system of practices is shared within an institution, the emerging objects are considered to be "institutional objects", whilst if these systems correspond to a person they are considered as "personal objects"⁶. The following types of primary mathematical objects are proposed:

- Language (terms, expressions, notations, graphics);
- Situations (problems, extra or intra-mathematical applications, exercises, etc.);
- Concepts, given by their definitions or descriptions (number, point, straight line, mean, function, etc.);
- Propositions, properties or attributes,
- Procedures (operations, algorithms, techniques);
- Arguments used to validate and explain the propositions and procedures (deductive, inductive, etc.).

⁵ "... mathematical discourse and its objects are *mutually constitutive*" (Sfard, 2000, p. 47)

⁶ "Personal objects" include cognitive constructs such as conceptions, internal representations, conceptual images, etc.

These objects are organized in more complex entities, such as conceptual systems, theories, etc. The six types of primary objects postulated widen the traditional distinction between conceptual and procedural entities that is insufficient to describe the objects intervening and emerging from mathematical activity. The problem – situations promote and contextualise the activity; language (symbols, notations, graphics, ...) represent the other entities and serve as tools for action; arguments justify the procedures and propositions that relate the concepts. These entities have to be considered as functional and relative to the language game (institutional frameworks and contexts of use) in which they participate; they have also a recursive character, in the sense that each object might be composed of other entities, depending on the analysis level, for example arguments might involve concepts, properties, operations, etc.

3.3. Relations between objects: Semiotic functions

Another component in the model is Hjelmslev's (1943) notion of *function of sign*⁷, that is the dependence between a text and its components and between these components themselves. In other words, the correspondences (relations of dependence or function) between an antecedent (expression, signifier) and a consequent (content, signified or meaning), established by a subject (person or institution) according to certain criteria or a corresponding code. These codes in mathematical activity can be rules (habits, agreements) that inform the subjects implied about the terms that should be put in correspondence in the fixed circumstances.

For us, the relations of dependence between expression and content can be representational (one object which is put in place of another for a certain purpose), instrumental (an object uses another as an instrument) and structural (two or more objects make up a system from which new objects emerge). In this way semiotic functions and the associated mathematical ontology, take into account the essentially relational nature of mathematics and radically generalize the notion of representation. The role of representation is not exclusively undertaken by language: in accordance with Peirce's semiotic, we assume the different types of objects (problem-situations,

⁷ Named by Eco (1979) as semiotic function.

procedures, definitions, propositions and arguments) can also be expression or content of the semiotic functions.

3.4. Configuration of objects and mathematical processes

The notion of “system of practices” is useful for some types of macro-didactic analysis, particularly when comparing the particular form mathematical knowledge adopts in different institutional frameworks, contexts of use or language games. A finer description of mathematical activity requires the introduction of the six types of primary entities. These objects will form “configurations”, that we define as the network of objects involved and emerging from the systems of practices and the relationships established between them. These configurations can be epistemic (networks of institutional objects) or cognitive (network of personal objects), and with the system of practices are the basic theoretical tools to describe mathematical knowledge, in its double personal and institutional facets.

These objects and relationships (configurations), emerge through time in both their personal and institutional facet, by means of mathematical processes, which we interpret as sequences of practices. The emergence of linguistic objects, problems, definitions, propositions, procedures and arguments take place throughout the respective primary mathematical processes of communication, problem posing, definition, enunciation, elaboration of procedures (algorithms, routines, ...) and argumentation. Problem solving and mathematical modelling should rather be considered as mathematical “hyper-processes”, when involving complex configurations of primary mathematical processes (establishing connections between objects and generalizing techniques, rules and justifications). The effective realization of study processes also requires sequences of planning, monitoring and assessing that might be considered as meta-cognitive processes.

3.5. Contextual attributes

The notion of *language game* (Wittgenstein, 1953) plays an important role together with that of institution in our model. Here we refer to contextual factors to which the meanings of mathematical objects are relative and which

attribute a functional nature to them. Mathematical objects intervening in mathematical practices or emerging from them, depend on the language game in which they take part, and can be considered from the following dual dimensions or facets (Godino, 2002):

Personal – institutional. Institutional objects, emerge from systems of practices shared within an institution, while personal objects emerge from specific practices from a person (Godino and Batanero, 1998, p. 185-6). “Personal cognition” is the result of individual thinking and activity when solving a given class of problems, while “institutional cognition” is the result of dialogue, agreement and regulation within the group of subjects belonging to a community of practices.

Ostensive – non ostensive. Mathematical objects (both at personal or institutional levels) are, in general, non perceptible. However, they are used in public practices through their associated *ostensives* (notations, symbols, graphs, etc.). The distinction between ostensive and non-ostensive is relative to the language game in which they take part. Ostensive objects can also be thought, imagined by a subject or be implicit in the mathematical discourse (for example, the multiplication sign in algebraic notation).

Extensive – intensive (example - type). An *extensive* object is used as a particular case (a specific example, i.e., the function $y = 2x+1$), of a more general class (i.e., the family of functions $y=mx+n$), which is an *intensive* object. The extensive / intensive duality is used to explain a basic feature of mathematical activity: the use of generic elements (Contreras and cols, 2005). This duality allows us to focus our attention on the dialectic between the particular and the general, which is a key issue in the construction and application of mathematical knowledge.

Unitary – systemic. In some circumstances mathematical objects are used as unitary entities (they are supposed to be previously known), while in other circumstances they are seen as systems that could be decomposed to be studied. For example, in teaching, addition and subtraction, algorithms, the decimal number system (tens, hundreds, ...) is considered as something known, or as unitary entities. These same objects, in first grade, should be dealt with as systemic and complex objects to be learned.

Expression – content: they are the antecedent and consequent of semiotic functions. Mathematical activity is essentially relational, since the different objects described are not isolated, but they are related in mathematical language and activity by means of semiotic functions. Each type of object can play the role of antecedent or consequent (signifier or signified) in the semiotic functions established by a subject (person or institution).

These facets are grouped in pairs that are dually and dialectically complementary. They are considered as attributes applicable to the different primary and secondary objects, giving rise to different “versions” of the said objects. In Godino, Batanero and Roa (2005) the six types of primary entities and the five types of cognitive dualities are described using examples from a research in the field of combinatory reasoning.

In Figure 1 we represent the different theoretical notions that have been concisely described as an onto-semiotic model for mathematical knowledge. Here mathematical activity plays a central role and is modelled in term of systems of operative and discursive practices. From these practices the different types of mathematical objects, which are related among them building cognitive or epistemic configurations, emerge. Lastly, the objects that take part in mathematical practices and those emerging from these practices, depend on the language game in which they participate, and might be considered from the five facets of dual dimensions.

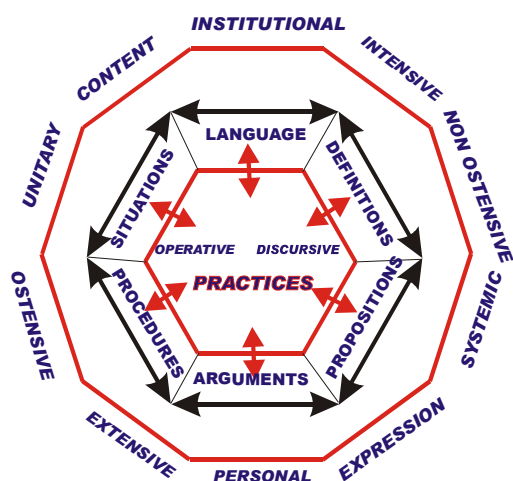


Figure 1: An onto-semiotics of mathematical knowledge

The types of objects described, summarised in figure 1 (systems of practices, emerging entities, configurations or onto-semiotic networks, the contextual attributes, together with the notion of semiotic function as the basic relational entity) make up an operative response to the ontological problem of representation and meaning of mathematical knowledge.

3.6. Understanding and knowing in the onto-semiotic approach

There are two basic ways to conceive "understanding": as a mental process or as a competence (Font 2001), which correspond to divergent or even conflicting epistemological conceptions. Cognitive approaches in Mathematics Education views understanding as a mental process, while the pragmatic position of the *onto-semiotic approach*, considers understanding as competence (a subject is said to understand a mathematical object when he/she uses it in a competent way in different practices).

However, considering the essential role played by the semiotic functions in the relational process carried out in mathematical activity (within a given language game) also lead to conceiving understanding in terms of semiotic functions (Godino, 2003). That is, we can interpret understanding of an object O by a subject X (person or institution) in terms of the semiotic functions that X can establish, in some fixed circumstances, in which O intervenes as expression or content. Each semiotic function implies a semiosis act by an interpretant agent and constitutes a knowledge. Speaking of knowledge is equivalent to speaking of the content of a (or many) semiotic function (s), and the variety of types of knowledge correspond to the diversity of semiotic functions that can be established among the diverse entities introduced in the theoretical model.

3.7. Didactical problems, practices, processes and objects

The theoretical model described for mathematical education can also be applied to other fields, particularly to pedagogical knowledge. In this case the problems from which knowledge emerge have a different nature, e.g.:

- What content should be taught in each context and circumstances?

- How should we allocate the diverse components and facets of contents through time?
- What model of the study process should be implemented in each circumstance?
- How should we plan, monitor and assess the teaching and learning processes?
- What factors condition the teaching and learning processes?

Here, the actions (didactical practices) implemented, their sequencing (didactical processes) and the emergent objects from these systems of practices (didactical objects) will be different from those arising in solving mathematical problems.

In the Theory of Didactical Configurations (Godino, Contreras y Font, 2006) that we are developing as a component of the onto-semiotic approach, we model the teaching and learning of a mathematical content as a multidimensional stochastic process composed of six sub-processes (epistemic, teacher's roles, students' roles, mediational, cognitive and emotional), and their respective trajectories and potential states. We introduce the *didactical configuration* as the primary unit for didactical analysis. This is constituted by the teacher – student interactions when studying a mathematical object or content and using some specific technological resources. Every instructional process is developed for a given time through a sequence of didactical configurations.

A didactical configuration includes an *epistemic configuration*, that is to say, a mathematical problem, the languages and actions required to solve it, rules (concepts, propositions and procedures), and argumentations, which are assumed by the teacher, students, or shared between them. There is also an *instructional configuration* made up by the teacher, students and the mediational objects (different resources) related to the mathematical content under study. The learning built throughout the process might be viewed as a set of *cognitive configurations*, that is the networks of objects emerging from or involved in the systems of personal practices that students carried out during the implementation of the epistemic configuration.

3.8. Didactical suitability criteria

We complement the theoretical notions described with the notion of *didactical suitability* of an instructional process, which is defined as the coherent and systemic articulation of the following six components (Godino, Wilhelmi and Bencomo, 2005; Godino, Contreras and Font, 2006), each of which is a matter of degree:

- *Epistemic suitability*, representativeness of institutional implemented (or intended) meaning as regards the reference meaning previously defined.
- *Cognitive suitability*, extent to which the institutional implemented (or intended) meaning is included in the students' "zone of proximal development" (Vygotski, 1934), and the closeness of personal meanings achieved to implemented (or intended) meaning.
- *Interactive suitability*, extent to which the didactical configurations and trajectories allow to identify and solve semiotic conflicts⁸ that might happen during the instructional process.
- *Media/resources suitability*, availability and adequacy of material and temporal resources needed to develop the teaching and learning process.
- *Emotional suitability*, the students' involvement (interest, motivation, ...) in the study process.
- *Ecological suitability*, extent to which the teaching and learning process fits the educational project, the school and society, and take into account the conditioning factors of the setting in which it is developed.

A higher suitability in one of these dimensions might not correspond to a high level of suitability in the other dimensions. Given preference to the different criteria will depend on the interactions among them; we then introduce *didactical suitability* as a systemic criteria of adequacy and appropriateness regarding the global educational project. This didactical suitability is relative to temporal, contextual and changing circumstances, which requires an inquiring and reflective attitude

⁸ A *semiotic conflict* is any disparity or difference of interpretation between the meanings ascribed to an expression by two subjects (persons or institutions).

from the teacher and the people sharing the responsibility of an educational project.

The theoretical tools developed in the onto-semiotic approach to mathematical knowledge and instruction can be applied to analyse the teaching and learning process implemented in a particular teaching session, the planning and development of a didactical unit, or at a more global level, in the design and implementation of a course or curricular proposal. They also can be useful to analyse partial aspects of a study process, such as the didactical resources, textbooks, students' answers to specific tasks, etc.

4. Examples of application and comparison with other frameworks

Due to the space limitation it is not possible to describe a complete example of application of the framework described, which is being used as the theoretical background for several dissertations, articles and research reports. Some of these examples are described in the authors' web sites. To follow, we have prepared a short abstract of the application of the onto-semiotic approach in Godino, Batanero and Roa' research (2005), where they describe the mathematics activity carried out by a sample of university students when solving elementary combinatoric problems.

Our theoretical tools served to identify the variety of mathematical objects involved in combinatorial problem solving, beyond classical combinatorial formulae and showed examples for the cognitive dualities from which they can be considered, so as the semiotic functions that can be established among them. The students' errors and difficulties were explained by semiotic conflicts, i.e. as disparities between the student's interpretation and the meaning in the mathematics institution. As a result of this application, we provided original and relevant information to better understand the students' combinatorial thinking. The analysis also showed some "transparency illusions" in the teaching and assessing of combinatorics and suggested some ways to improve this teaching.

We believe the *onto-semiotic approach* might help compare the theoretical frameworks used in Mathematics Education and, to the same extent, to overcome some of their limitations

for the analysis of mathematics cognition and instruction. The key role that we give to the notion of *mathematical practice*, and the features we attribute to it (any shared, situated, intentional action mediated by linguistic and material resources) might allow a coherent articulation with other theoretical frameworks, such as the social constructivism (Ernest, 1998), the socio-epistemology (Cantoral and Farfán, 2003), and the ethno-mathematical and socio-cultural approach to mathematical meaning and cognition (Radford, 2006).

In Godino, Font, Contreras and Wilhelmi (2006) we use the onto-semiotic approach to analyse and compare other theoretical frameworks, in particular, the theory of didactical situation (Brousseau, 1997), conceptual fields (Vergnaud, 1990), dialectic tool-object (Douady, 1986), anthropological theory of didactics (Chevallard, 1992), and semiotic registers (Duval, 1995).

5. Final reflections

The *onto-semiotic approach* is growing as a theoretical framework for Mathematics Education impelled by issues related to teaching and learning mathematics and the aspiration of achieving the articulation of the diverse dimensions and perspectives involved. In agreement with Steiner (1990), we are convinced that this work of articulation cannot be made through the superimposition of tools taken from different and heterogeneous theories. He conceived Mathematics Education as a scientific discipline in the centre of a complex, heterogeneous, social system – the System of Teaching Mathematics – and proposed beside Mathematics other referential sciences for our discipline, such as: Epistemology, Psychology Pedagogy Sociology and Linguistics. Each of these disciplines focuses its attention on partial aspects of the issues involved in teaching and learning mathematics, using their specific conceptual tools and methodologies. At a certain time this diversity of approaches might be inevitable, or even enriching, but we think that the progress in the discipline and the strengthening of its practical applications requires the emergence of a new global and unifying perspective.

Acknowledgement

This research work has been carried out in the frame of the project, MCYT- FEDER: SEJ2004-00789.

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Developing Authentic Assessment: Case Studies of Secondary School Mathematics Teachers' Experiences

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Abstract: Authentic assessment techniques in mathematics raise issues that merit the attention of practitioners, educators, and researchers. Teacher training in assessment, the reliability and validity of authentic assessment, the variety of methods employed in such assessment, and the ways assessment is employed are all concerns that emerge as new assessment techniques other than the expected paper-and-pencil tests are implemented. At the secondary school level, new assessment techniques are emerging in mathematics classrooms and little is known about these experiences. This article specifically addresses the issues associated with authentic assessment by describing and exploring mathematics teachers' experiences as they implement these assessment techniques in their secondary school mathematics program. It summarizes the findings of a qualitative study of five secondary school mathematics teachers in Ontario, Canada, and offers suggestions as to how to support teachers through such a change project. How teachers use authentic assessment, the problems they encounter, and the theoretical and practical issues that emerge are all questions that require exploration and understanding.

Sommaire exécutif ; Les techniques d'évaluation authentiques en mathématiques soulèvent des questions qui méritent l'attention des enseignants, des didacticiens et des chercheurs. La formation des enseignants dans le domaine de l'évaluation, la fiabilité et la validité d'une évaluation authentique, la variété des méthodes employées dans cette évaluation et la façon dont ces méthodes sont appliquées sont autant de questions qui émergent à mesure que de nouvelles techniques d'évaluation, autres que les traditionnels tests sur papier, sont adoptées dans les salles de classe. Au niveau secondaire, de nouvelles techniques d'évaluation émergent dans les cours de mathématiques, mais les résultats de ces expériences sont à ce jour très peu connus.

Cet article fait le point sur les résultats d'une étude qualitative portant sur cinq enseignants de mathématiques à l'école secondaire, qui tentent d'appliquer des stratégies d'évaluation authentique dans leur pratique de l'enseignement. Cette étude a vu le jour après qu'une analyse de la recherche sur l'utilisation de l'évaluation authentique en mathématiques à l'école secondaire eut mis en évidence la quasi-totale absence de détails dans la littérature au sujet des convictions, des pratiques et des préoccupations des enseignants qui se proposent de changer leur méthodes d'évaluation de façon à se conformer aux pratiques courantes en enseignement des mathématiques. Or, il est nécessaire de connaître ces détails si l'on veut permettre aux enseignants de comprendre la valeur, les avantages et les difficultés liés à l'utilisation de l'évaluation authentique dans le cadre d'un programme de mathématiques à l'école secondaire. Grâce à cette compréhension accrue, les enseignants pourront être en mesure de participer au développement de connaissances dans le domaine de l'évaluation.

Une description détaillée des expériences des enseignants de mathématiques au secondaire qui appliquent des méthodes d'évaluation authentique en classe permet de mieux cerner le processus d'évaluation lui-même. L'article décrit les techniques d'évaluation dont se servent les enseignants, les raisons pour lesquelles ils s'en servent et les façons dont ils les utilisent. Cinq cas ont été étudiés au moyen d'une approche qualitative, combinant interviews, comptes-rendus, évaluations types et observations de classe,