

Model-based component separation exploiting sparsity

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Overview

Brief introduction to CMB component separation

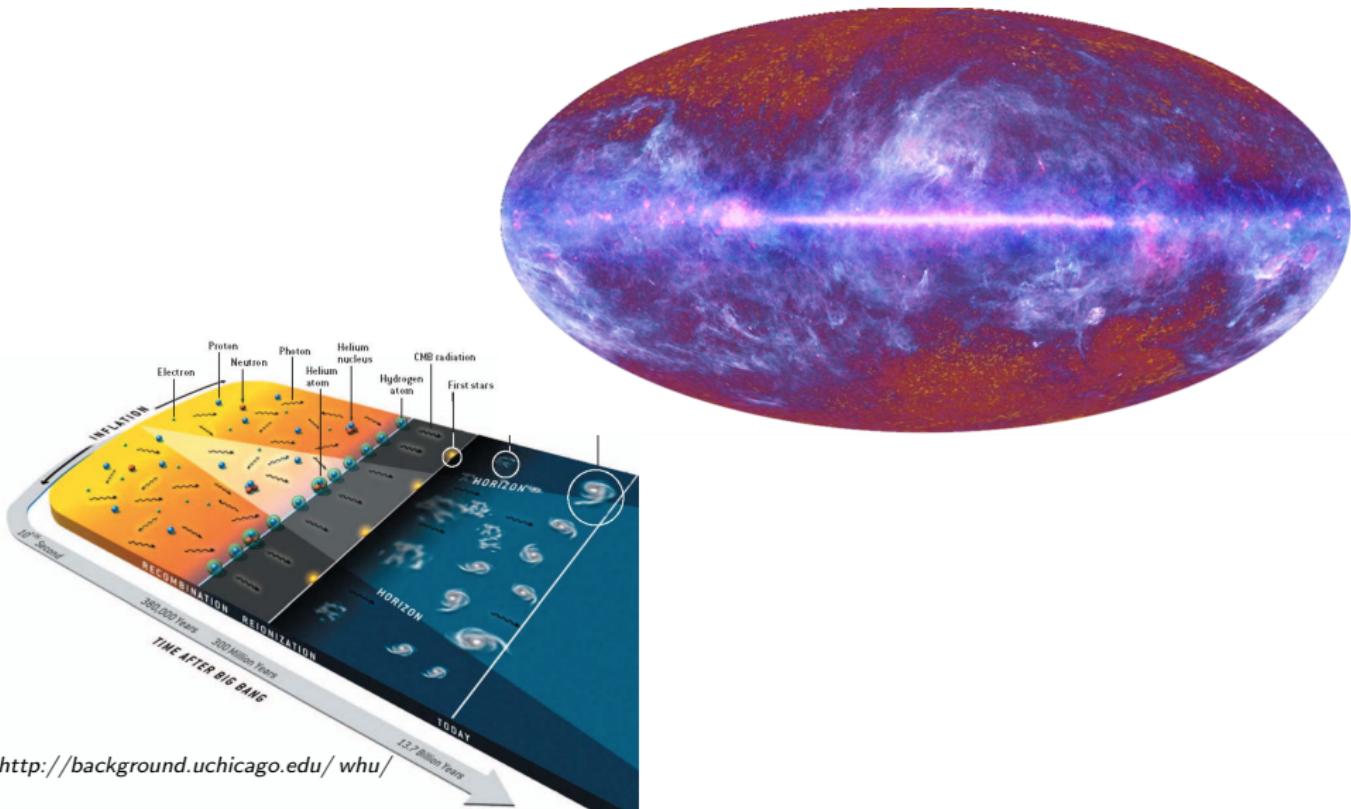
How sparsity can help

The problem at hand: thermal dust and the CIB

The new methodology

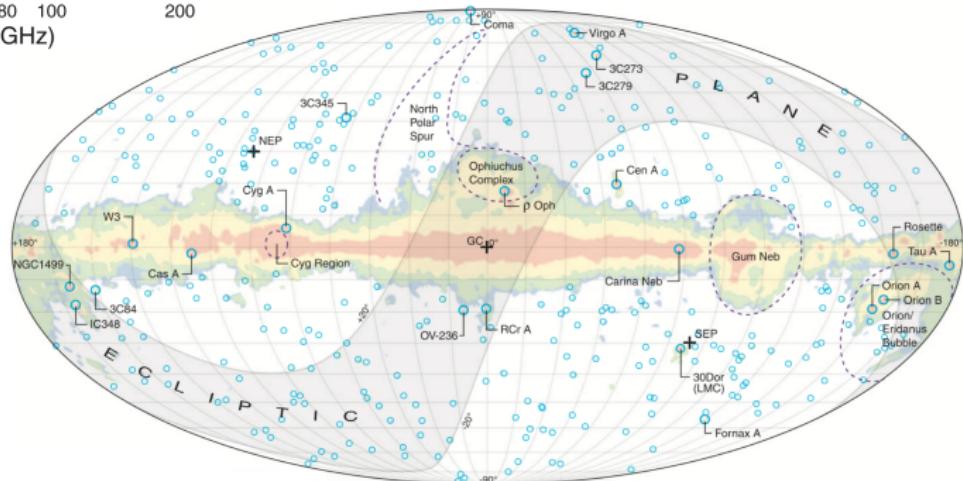
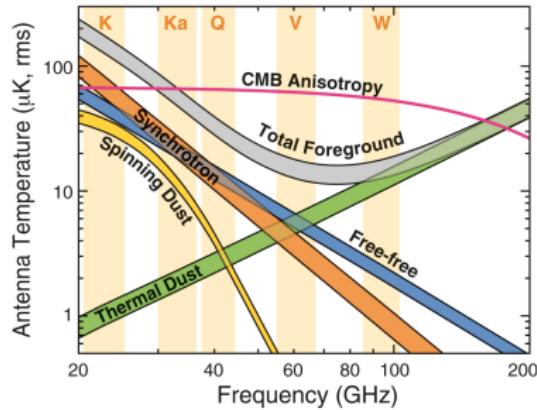
Validation on Planck simulation data

CMB component separation



<http://background.uchicago.edu/whu/>

CMB component separation

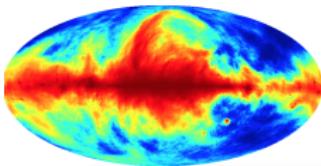


Bennett et al. 2013

CMB component separation

Commander

Pixel space, parametric, priors



Haslam 1982

ILC (internal linear combination)

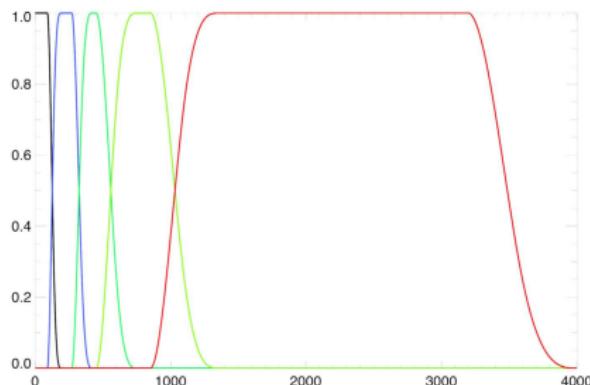
wavelet space, non-parametric, noise information - more to come

Sevem and SMICA

Recovery of just the CMB, no external data sets needed.

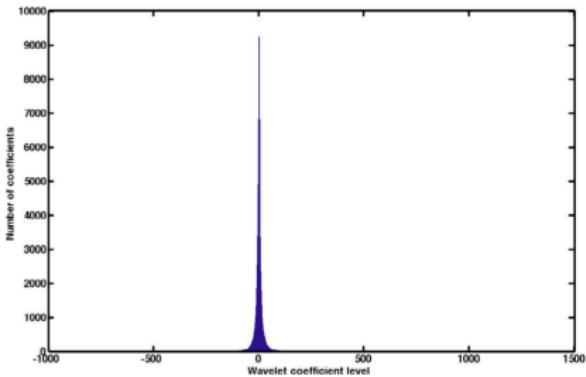
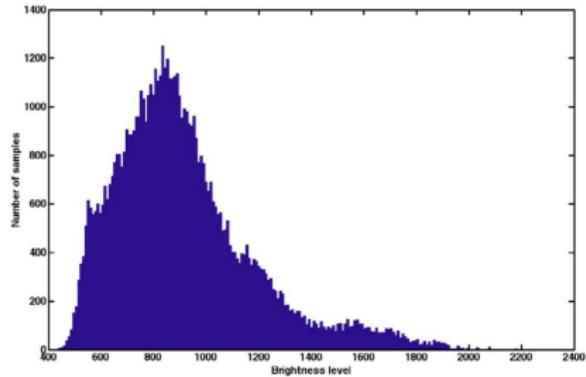
Goals for this work: provide foreground estimates as well as CMB
full sky, full resolution data
exploit sparsity in wavelet domain

Sparsity and the wavelet domain



Bobin et al. 2013

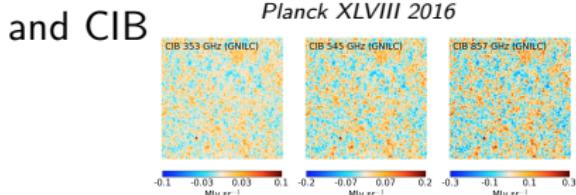
- Sparse: majority of signal is zero
- Spatially correlated source
- Wavelets filter in spherical harmonic domain (x-axis: ℓ)



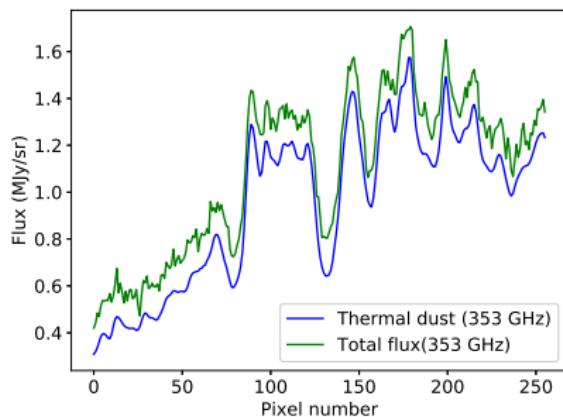
Thermal dust and the CIB

- Planck HFI: 217, 353, 545, 857 GHz
- Thermal dust

$$x_{\nu_i}^{\text{dust}} = \tau_{353} \times B(T, \nu) \times \left(\frac{\nu}{353 \text{ GHz}}\right)^{\beta}$$

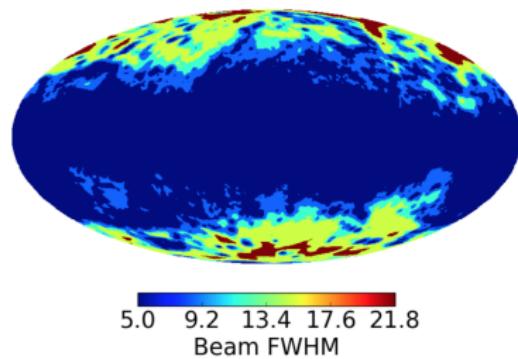


- Both BB, CIB flatter power spectrum
- Smoothing conundrum!



$$\text{total flux} = \text{dust} + \underbrace{\text{CIB} + \text{CMB} + \text{noise}}_{\text{nuisance, Gaussian approx}}$$

- Clever smoothing using nuisance estimates.



At each wavelet scale:

whitening $\mathbf{R}_{\text{nus}}^{-1/2} \mathbf{R}_{\text{tot}} \mathbf{R}_{\text{nus}}^{-1/2}$

$\mathbf{v} \sim 1 \Rightarrow$ noise dominated \rightarrow smooth

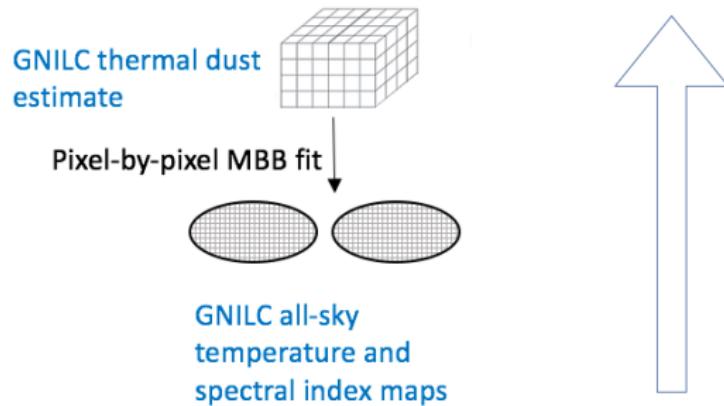
$\mathbf{v} \gg 1 \Rightarrow$ signal dominated

$$\min ||\mathbf{X} - \mathbf{AS}||^2 \text{ for thermal dust map}$$

a.k.a $||\mathbf{X} - \mathbf{A}\alpha\Phi||^2$

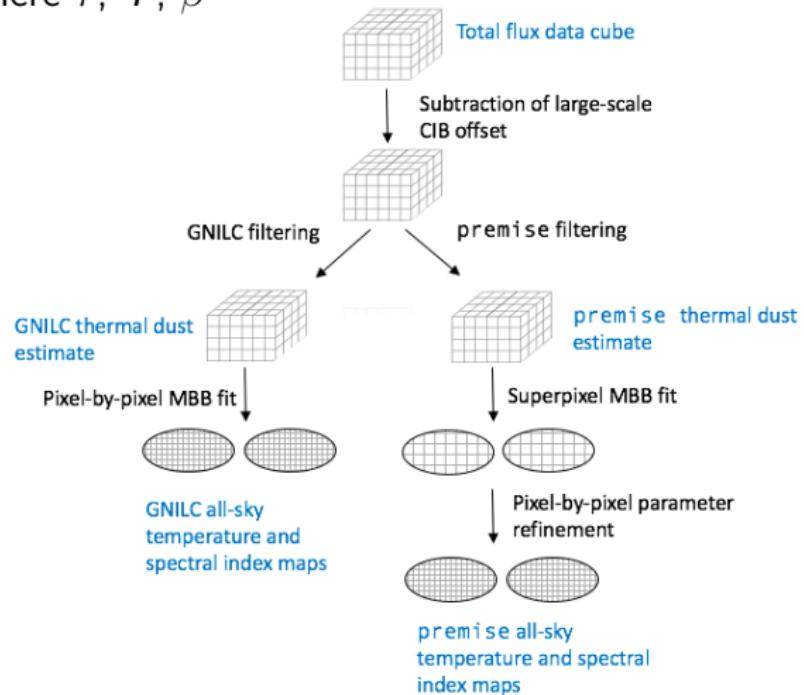
Objectives

- Don't want to smooth
- To remove sub-dominant CIB
- Don't want to complete a per pixel fit
- Parametric fit - not just dust



PREMISE

- Parameter Recovery Exploiting Model Informed Sparse Estimates
- Requires model - here τ , T , β



Filtering and Super-pixels

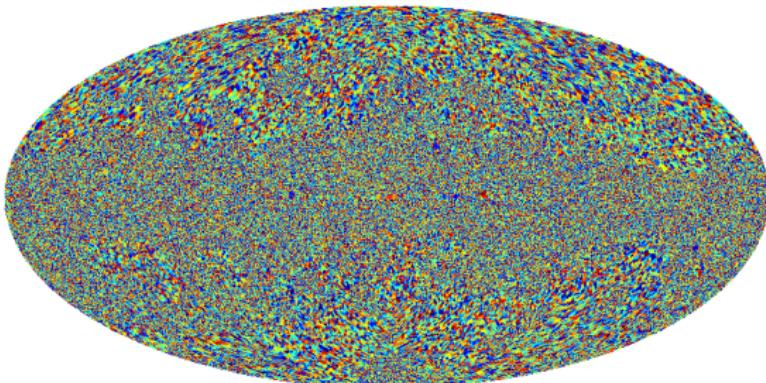
- Use GNILC filtering BUT
Marcenko-Pastur distribution
Penalise in favour of sparsity

$$\min (||X - A\alpha\Phi||^2 + \lambda ||\alpha||_1^1)$$

- Accurate and fast parameter estimates from fit - τ , T , β



χ^2_{red} in wavelet domain!



Refinement

- Low resolution informed initial guesses (64 times faster than pix-by-pix)
- T and β refinement - normalisation factor subject to degeneracies

$$x_{\nu_i}^{\text{dust}} = \tau_{353} \times B(T, \nu) \times \left(\frac{\nu}{353 \text{ GHz}} \right)^{\beta}$$

- Gradient descent at each pixel (until convergence)

$$\beta_n / T_n = \beta_0 / T_0 + \rho \times \Delta((\text{Data} - \text{model}) \text{ w.r.t } \beta \text{ and } T)$$

- Threshold all-sky β and T estimates in wavelet domain
- Template for normalisation

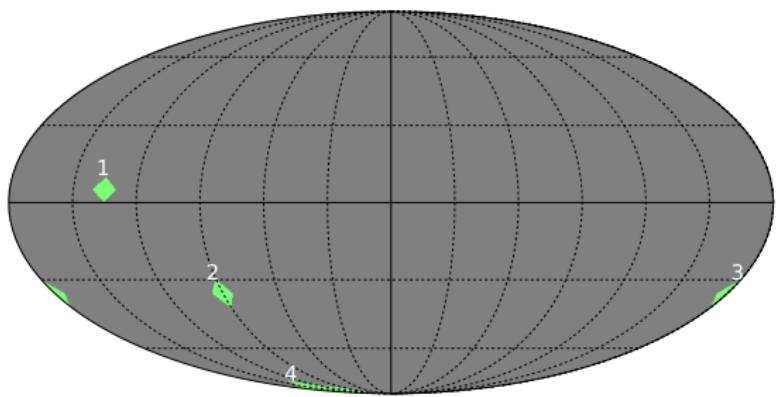
$$\tau_{353} = \frac{X_{857}}{B(T, 857 \text{ GHz}) \times \left(\frac{\nu}{353 \text{ GHz}} \right)^{\beta}}$$

Validation

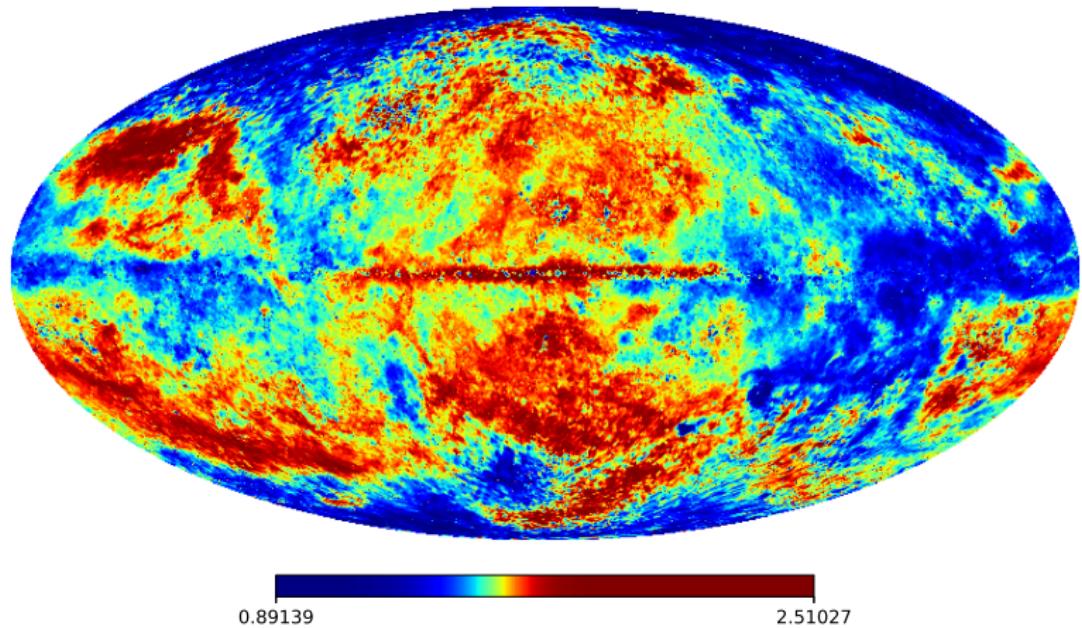
- Simulated data - known parameters

$$x_{\nu_i}^{\text{dust}} = x_{353 \text{ GHz}}^{\text{ffp8}} \times \frac{B(T, \nu)}{B(T, 353 \text{ GHz})} \times \left(\frac{\nu}{353 \text{ GHz}} \right)^\beta$$

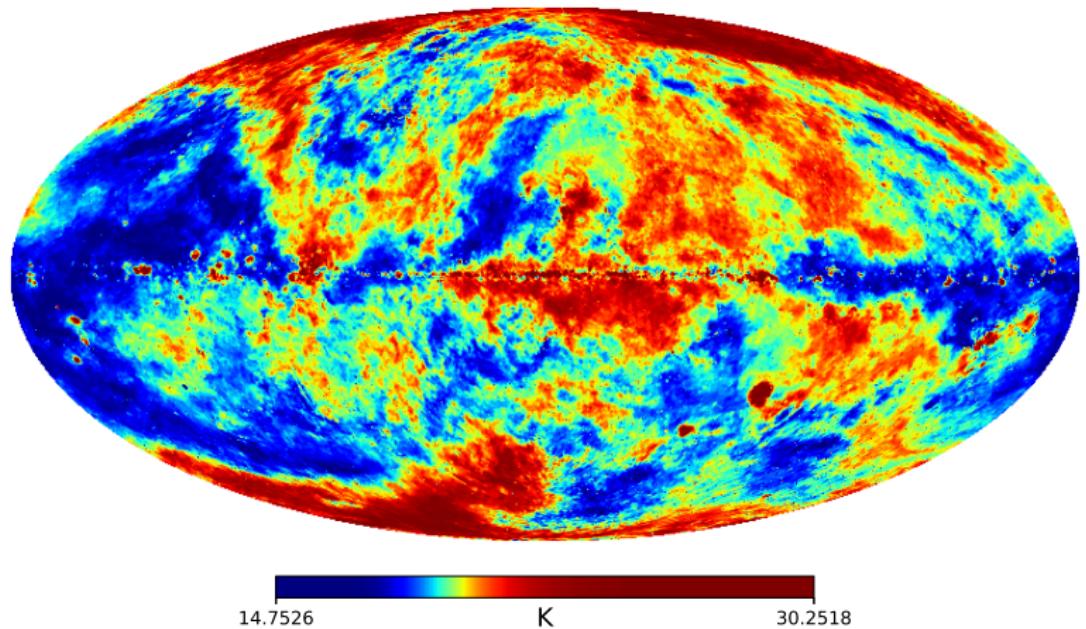
- Comparison with GNILC



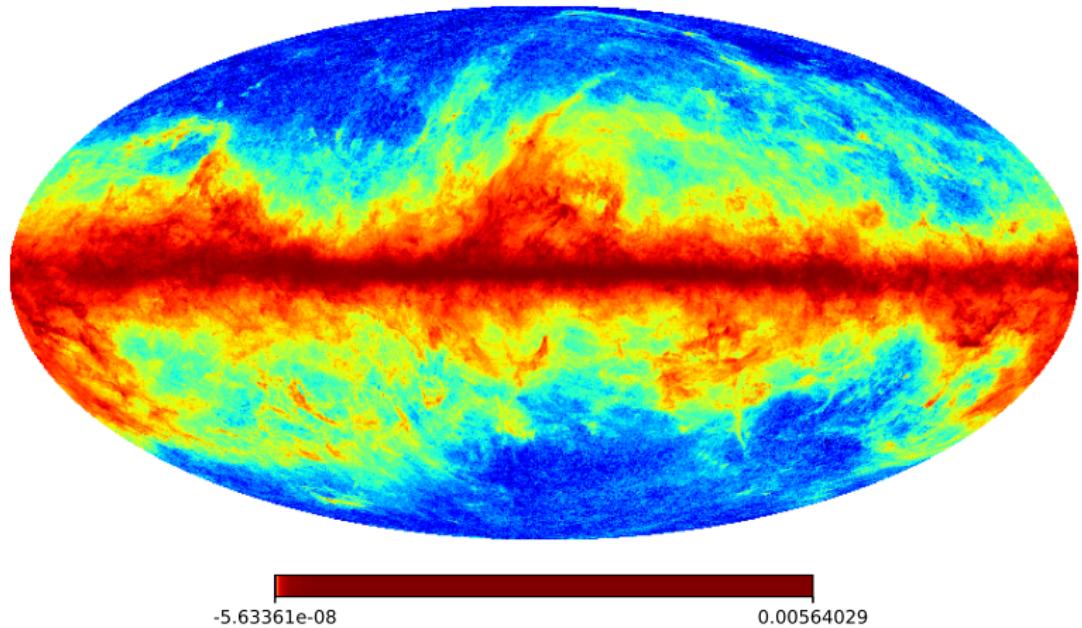
Full-sky β estimate - 5 arcmin



Full-sky T estimate - 5 arcmin

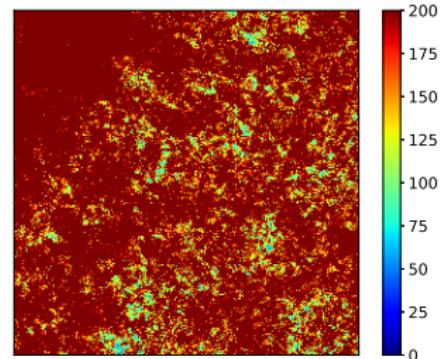
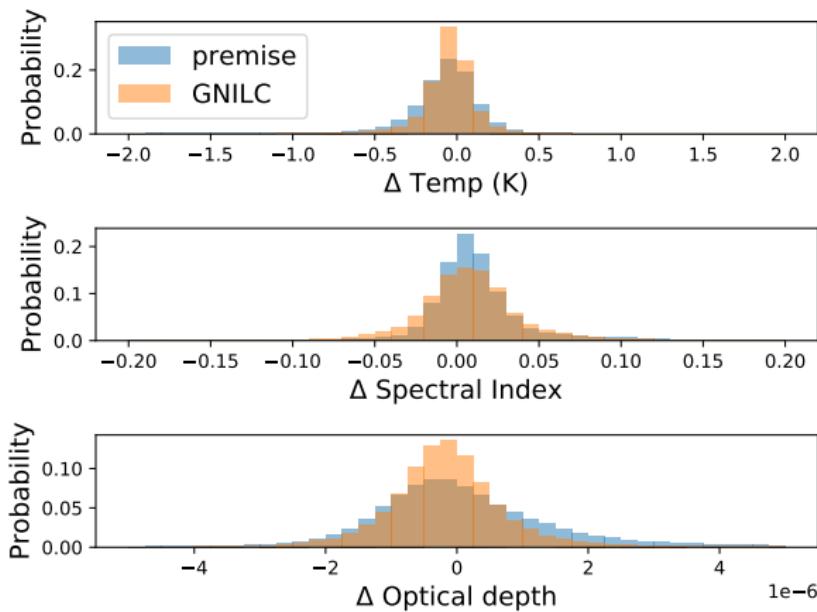


Full-sky τ_{353} estimate - 5 arcmin

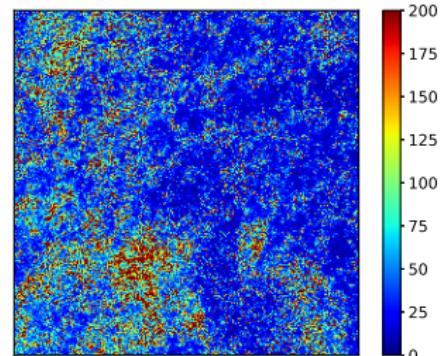
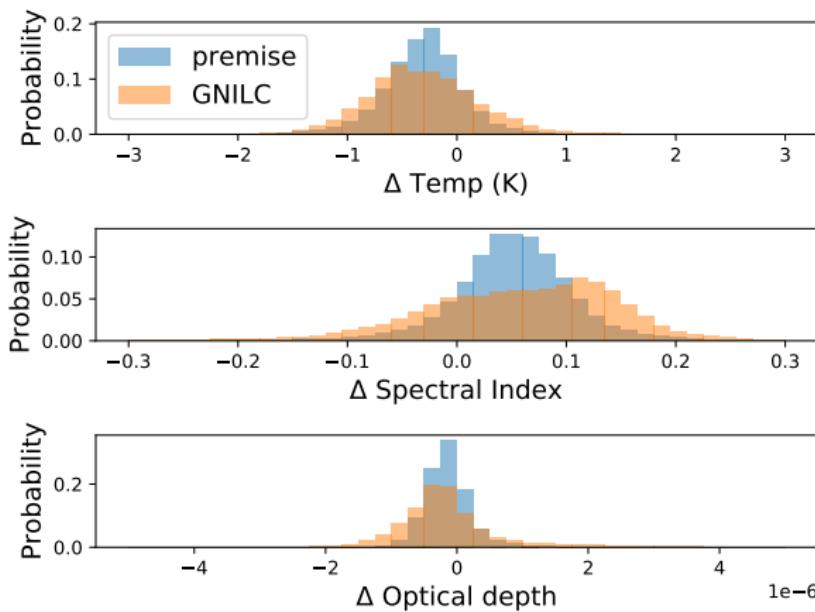


Value	Medium %Δ	1σ %Δ	2σ %Δ	3σ %Δ
Temperature	1.7	2.8	8.0	16.5
Spectral index	3.4	5.7	15.4	25.6
Optical depth (353 GHz)	3.7	7.2	31.2	77.0

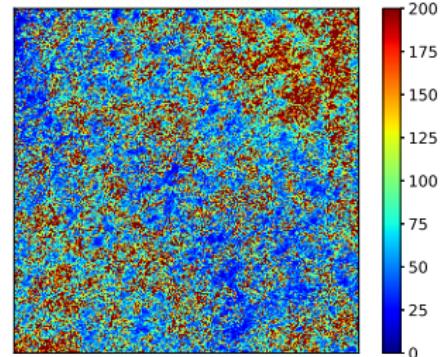
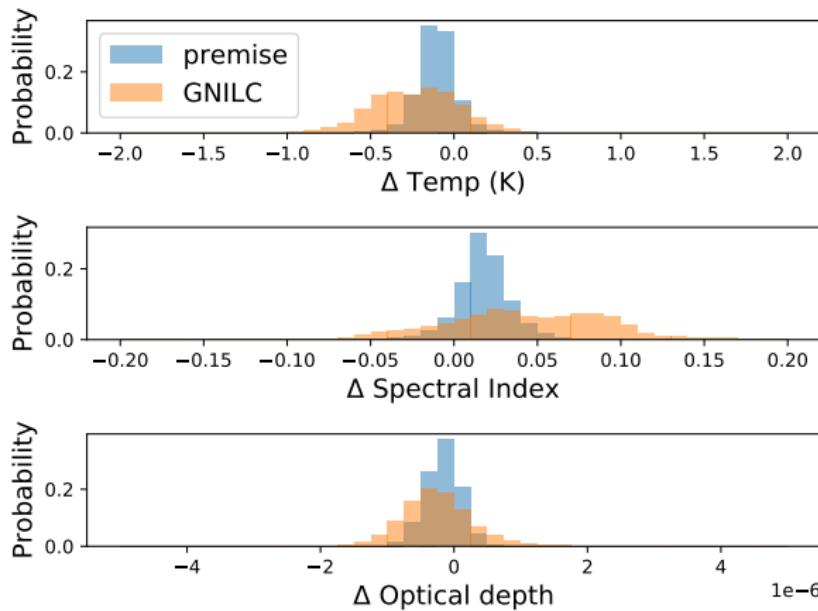
Region 1 - High SNR



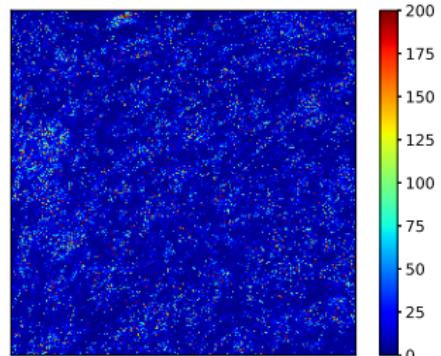
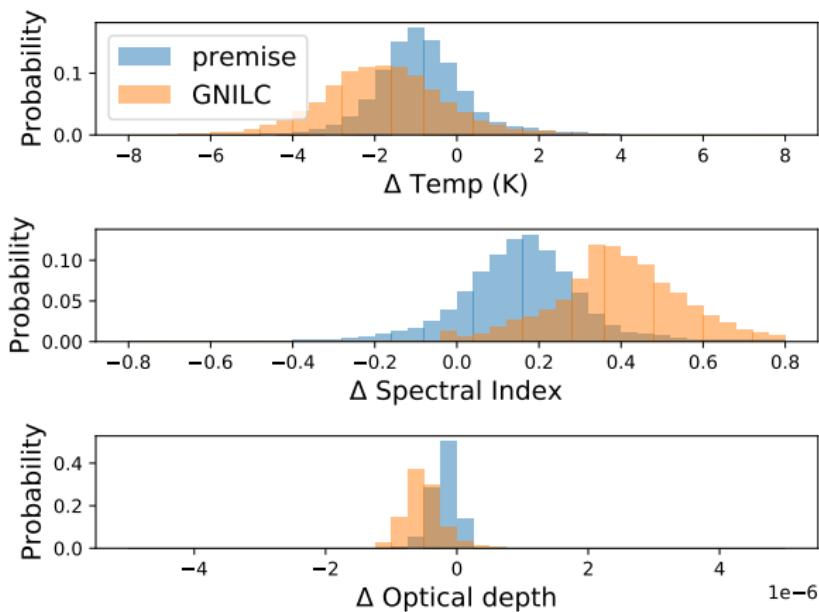
Region 2 - Medium SNR



Region 3 - Medium SNR



Region 4 - Low SNR



Conclusion

- Recovery of model parameters: full sky (varying signal to noise) at full resolution
- Sparsity in place of smoothing
- Fast (~ 2 days)
- Improvement for all but the largest signal to noise regions